

Large anomalous Hall effect in single crystals of the kagome Weyl ferromagnet Fe₃Sn

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The material class of kagome metals has rapidly grown and has been established as a field to explore the interplay between electronic topology and magnetism. In this work, we report a combined theoretical and experimental study of the anomalous Hall effect of the ferromagnetic kagome metal Fe₃Sn. The compound orders magnetically at 725 K and presents an easy-plane anisotropy. Hall measurements in single crystals below room temperature yield an anomalous Hall conductivity $\sigma_{xy} \sim 500 (\Omega \text{ cm})^{-1}$, which is found to depend weakly on temperature. This value is in good agreement with the band-intrinsic contribution obtained by density-functional calculations. Our calculations also yield the correct magnetic anisotropy energy and predict the existence of Weyl nodes near the Fermi energy.

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I. INTRODUCTION

In recent years, a number of materials with kagome layers as structural building blocks have been investigated. Their electronic structures have been found to host unconventional fermions, such as the Weyl fermions in Mn₃(Ge,Si) [1,2] and Co₃Sn₂S₂ [3,4], quasi-two-dimensional (quasi-2D) Dirac fermions in Fe₃Sn₂ [5], and quasi-2D Dirac fermions together with flat bands in FeSn [6].

The variety of kagome metals is being intensively studied including compounds based on different transition metals, e.g., FeSn and CoSn [7–9], but also different composition variants for a given transition metal, e.g., FeSn and Fe₃Sn₂. The two-dimensional limit has been also addressed, e.g., in thin films of Mn₃Sn [10], FeSn [11], or Co₃Sn₂S₂ [12] and in monolayers of Cu₂Ge, Fe₂Ge, and Fe₂Sn [13]. The latter are isostructural monolayers combining the honeycomb lattice structure of Cu or Fe with the triangular lattice of Ge or Sn. Interesting electronic properties have been reported, such as massive Weyl points in the ferromagnetic (FM) state of Fe₂Ge and massless Weyl points in the FM state of Fe₂Sn [13].

Large efforts have been made to correlate the geometrical aspects of the electronic structure with the electronic response to external fields. In particular, large anomalous Hall and Nernst conductivities have been reported in several kagome metals, both in cases in which the ground state is ferromagnetic [4,14–17] or antiferromagnetic [1,2,10,18].

In this work, we study the compound Fe₃Sn, one natural structural derivative of FeSn and Fe₃Sn₂ [6,19]. This mate-

rial has recently attracted attention as a possible permanent magnet due to its large ordering temperature (725 K) and the possibility of changing its magnetic ground state from easy plane to easy axis through alloying [20,21]. Recently, large anomalous Nernst data in polycrystals of Fe₃Sn have been reported [22]. Here, we report the growth of single crystals along with magnetic properties and measurements of the anomalous Hall resistivity. In addition, we calculate the electronic structure by means of density-functional theory (DFT) calculations. Our main result is the experimental finding of a large anomalous Hall conductivity (AHC) of about $500 (\Omega \text{ cm})^{-1}$, a value which is found to agree well with the band-intrinsic contribution computed from DFT. The measured AHC is weakly temperature dependent below room temperature. Further, our calculations indicate the existence of Weyl nodes near the Fermi surface and suggest that moderate hole doping could further increase the AHC up to values of $\sim 1250 (\Omega \text{ cm})^{-1}$.

This work is organized as follows. Section II describes the experimental and computational methods used in our investigation. Section III presents experimental results with focus on the anomalous transport properties. Section IV contains our theoretical results, which include a characterization of the bulk electronic and magnetic properties, as well as a characterization of the Weyl nodes structure in the ferromagnetic phase. Lastly, Sec. V contains our concluding remarks.

II. METHODS

A. Experimental methods

The bulk crystal structure of Fe₃Sn shown in Figs. 1(a) and 1(b) consists of layers of iron and tin piled in an A-B stacking. The Fe atoms form a kagome lattice with Sn atoms sitting

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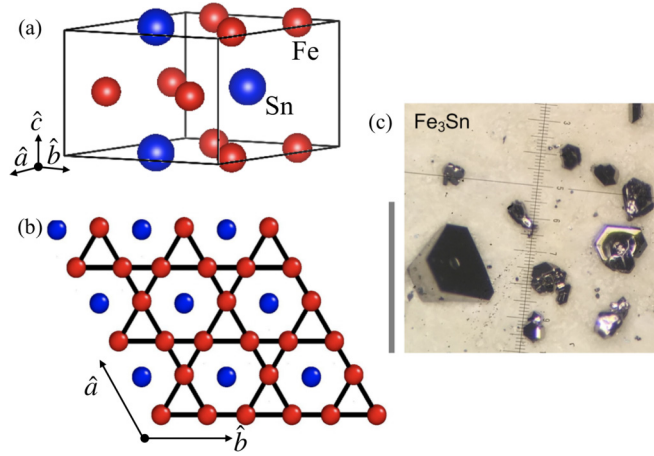


FIG. 1. (a) Crystal structure of Fe_3Sn . (b) Kagome lattice in the ab plane along the a axis. (c) Photo of Fe_3Sn single crystals where the hexagonal facets are (001) planes. The vertical scale bar stands for 1 mm.

at the center of the hexagon. This structure belongs to space group (SG) $P6_3/mmc$ (SG 194) with the experimental lattice constants $a = b = 5.487 \text{ \AA}$ and $c = 4.31 \text{ \AA}$, respectively [23,24].

In view of the narrow stability regime of Fe_3Sn in the iron-tin binary phase diagram [25], we grew single crystals of Fe_3Sn via a solid state reaction. Iron powder (Alfa Aesar; 99.998%) and tin powder (Alfa Aesar; 99.995%) were mixed in a ratio of $3.5 \sim 3:1$ and loaded into an evacuated quartz tube. After being heated up to 850°C , kept for 120 h and slowly cooled to 800°C over the course of 400 h, the quartz tube was quenched to cold water and we found crystals of Fe_3Sn up to the lateral size of $500 \mu\text{m}$ as we show in Fig. 1(c). We note that a small number of Fe_5Sn_3 crystals can also be found in the quartz tubes. We confirmed with x-ray diffraction (XRD) that during the growth process Fe_3Sn and Fe_5Sn_3 tend to crystallize in distinct morphologies: Fe_3Sn forms hexagonal prisms [see crystals in Fig. 1(c)] and Fe_5Sn_3 tends to form elongated hexagonal bipyramids. Phase purity of the sample under study is confirmed by powder XRD (see Supplemental Material, Fig. S1) [26]. Electrical transport measurements were performed using the standard five-probe methods in a commercial superconducting magnet. The magnetic field is applied along the c axis and the current within the ab plane.

B. Computational details

DFT calculations were performed using the full potential local orbital (FPLO) code version 18.00-52 [27,28]. The generalized gradient approximation (GGA) with the parametrization of Perdew, Burke, and Ernzerhof was used [29]. Relativistic effects were treated in the four-component formalism as implemented in FPLO. Brillouin zone (BZ) integrals were performed with the tetrahedron method based on a k mesh formed of $24 \times 24 \times 24$ subdivisions. The experimental structure was used as detailed above. To ensure an accurate band structure close to the Fermi level, an enhanced basis set as defined in the Appendix to Ref. [30] was used.

FM configurations were considered with different quantization axes. In particular, the magnetic anisotropy energy

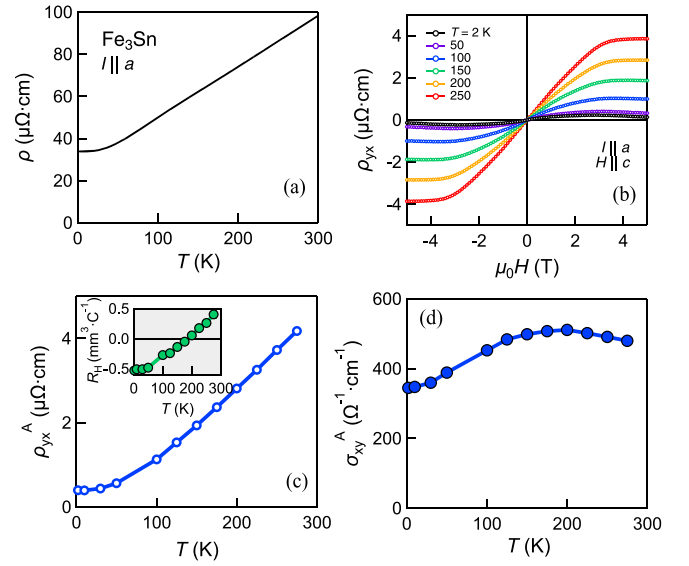


FIG. 2. (a) Resistivity ρ of Fe_3Sn as a function of T with current I in the kagome lattice plane. (b) Hall resistivity ρ_{yx} as a function of H at selected T . Here the magnetic field H is applied along the c axis. (c) Anomalous Hall resistivity ρ_{yx}^A and ordinary Hall coefficient R_H (inset) vs T in Fe_3Sn extracted from ρ_{yx} . (d) T evolution of the anomalous Hall conductivity σ_{xy}^A in Fe_3Sn .

(MAE) was computed based on calculations with the magnetic moments oriented within the kagome planes ([100] direction) or perpendicular to these layers ([001] direction).

The study of Weyl nodes, of the surface spectral properties and of the anomalous Hall conductivities, are based on a tight-binding model obtained by constructing maximally projected Wannier functions. For this aim, we used the PYFPLO [28] module of the FPLO code. The local Wannier basis set is formed of Fe $3d$, Fe $4s$, Sn $5s$, and Sn $5p$ orbitals. The search for Weyl nodes was done with a bisection method that detects sources of the Berry curvature field. After a set of candidate nodes is found, the corresponding Chern number associated to each point is computed by integrating the Berry curvature flux through a small sphere centered at the node, as done in Ref. [31].

Finally, the band-intrinsic contribution to the anomalous Hall conductivity is calculated using the formula

$$\sigma_{\alpha\beta}^A = -\frac{\epsilon_{\alpha\beta\gamma} e^2}{\hbar} \sum_n \int_{\text{BZ}} \frac{dk}{(2\pi)^3} f_n(k) \Omega_{n,\gamma}(k), \quad (1)$$

where n is a band index, $\Omega_{n,\gamma}$ is the γ component of the Berry curvature, $f_n(k)$ is the occupation number of the Bloch state, and $\epsilon_{\alpha\beta\gamma}$ is the Levi-Civita tensor [32]. A $300 \times 300 \times 300 k$ mesh was used for this calculation.

III. EXPERIMENTAL RESULTS

Fe_3Sn is known to order ferromagnetically at $T_C = 725 \text{ K}$ [20,21]. The resistivity ρ of Fe_3Sn as a function of temperature T within the kagome lattice plane is shown in Fig. 2(a), exhibiting a residual resistivity ratio (RRR) of 2.9. We assume that the diffusive nature of the solid state reaction process facilitates disorder formation throughout the synthesis process,

TABLE I. Total energy referred to the ground state energy and total magnetic moments (including spin and orbital contributions) for the two considered magnetic states. The reported data are calculated considering the extended basis set.

| State | Energy (meV/f.u.) | Total moment (μ_B /f.u.) |
|----------|-------------------|-------------------------------|
| FM [100] | 0 | 7.22 |
| FM [001] | 0.64 | 7.20 |

resulting in the high residual resistivity $\sim 35 \mu\Omega \text{ cm}$ and low RRR in Fe_3Sn as compared with its cousin compounds Fe_3Sn_2 [19] and FeSn [6].

As expected in prototypical ferromagnetic metals, we observe in the Hall traces of Fe_3Sn a prominent anomalous component as shown in Fig. 2(b). Saturation is observed at about 3 T external field, which we relate to the complete reorientation of the magnetization from its easy-plane ground state to the c axis. The Hall resistivity ρ_{yx} can be decomposed into the ordinary and anomalous contributions via $\rho_{yx} = R_H B_z + R_S M_z$, where R_H is the ordinary Hall coefficient, B_z the magnetic induction in the z direction, R_S the anomalous Hall coefficient, and M_z the magnetization in the z direction. $R_S M_z$ gives the anomalous Hall resistivity ρ_{yx}^A . We infer ρ_{yx}^A and R_H from the high field intercept and slope (above 3 T) of ρ_{yx} , respectively. This means, the extracted ρ_{yx}^A data refers to saturated M_z . The results are shown in Fig. 2(c). ρ_{yx}^A grows monotonically with T while R_H exhibits a sign reversal; R_H at $T = 2$ K corresponds to a carrier density of $1.2 \times 10^{22}/\text{cm}^3$. The observed R_H suggests the coexistence of both large electron and hole pockets in the system. The anomalous Hall conductivity σ_{xy}^A estimated from ρ_{yx}^A via $\sigma_{xy}^A \sim \rho_{yx}^A / \rho^2$ is displayed in Fig. 2(d). σ_{xy}^A is found to depend weakly on T and the maximum is around $500 \Omega^{-1} \text{ cm}^{-1}$. We note that the system is characterized by longitudinal conductivity $\sigma_{xx} \approx 1/\rho$ between $1 \sim 3 \times 10^4 \Omega^{-1} \text{ cm}^{-1}$, and falls rather in the moderately dirty regime, such that the observed σ_{xy}^A is expected to reflect an underlying intrinsic Berry curvature contribution [33,34].

IV. COMPUTATIONAL RESULTS

In this section, we first analyze the magnetic properties and electronic structure of Fe_3Sn , we report the existence of several Weyl nodes near the Fermi surface, and we present calculations of the band-structure-intrinsic contribution to the anomalous Hall conductivity.

Table I shows the total energies and magnetic moments obtained for different quantization axes. The FM state with a quantization axis along the [100] direction is found to be the ground state with a total magnetic moment of $7.22 \mu_B$ per Fe_3Sn .

The magnetic moment is slightly reduced if the magnetization is oriented along the c axis. The MAE calculated from the energy difference between these two states amounts to ~ 0.64 meV per Fe_3Sn . Note that we refrain from an analysis of in-plane magnetic anisotropy, which is very small in hexagonal systems and not expected to affect the transport properties considered here. Under the assumption of negligible higher-order terms, this translates into an anisotropy

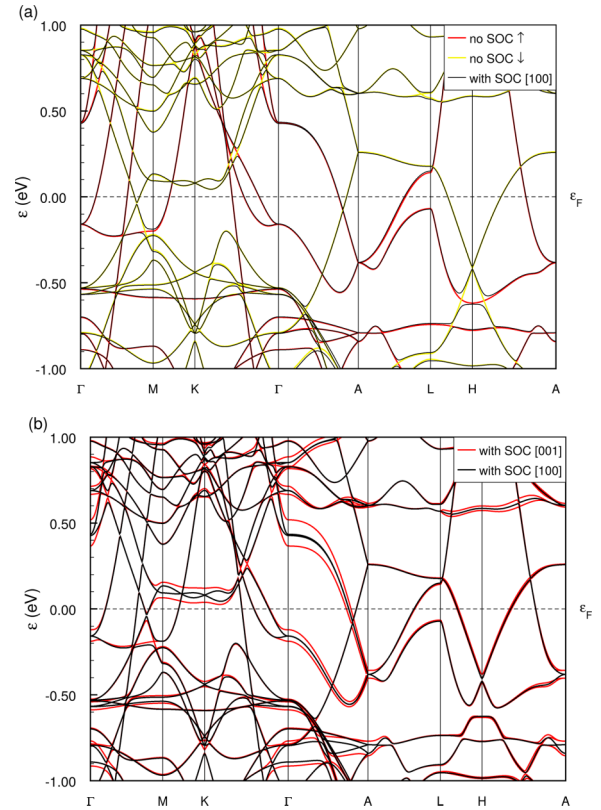


FIG. 3. (a) Band structures in the scalar relativistic and fully relativistic approximations with the magnetic quantization axis along [100]. (b) Fully relativistic band structures with the quantization axis along [100] and [001].

constant $K_1 = -1.8 \text{ MJ/m}^3$ and an anisotropy field of 3.1 T. The former value agrees with earlier theoretical results of $|K_1| = 1.59 \text{ MJ/m}^3$ [20] (the authors of this reference use a sign convention opposite to the usual one) and of -1.5 MJ/m^3 [35]. The calculated anisotropy field agrees with the experimentally observed saturation around 3 T [see Fig. 2(b)], and with the same result of 3 T obtained from earlier magnetization data [20]. We tried the application of so-called orbital polarization corrections (OPCs) [36] which, however, yield a twofold enhanced anisotropy field. Thus, we conclude that Fe_3Sn is better described by conventional GGA than by GGA-OPC and use only GGA data for the further investigation.

Figure 3(a) presents the energy dispersion obtained in the scalar and in the fully relativistic calculations with [100] orientation of the magnetization. Several bands, which mainly present Fe $3d$ character, cross the Fermi energy. Bands with relatively flat energy dispersion as a fingerprint of the kagome lattice are present in the Γ - M - K plane around -0.5 eV as well as in the A - L - H plane around $+0.6$ eV and around -0.8 eV. Without spin-orbit coupling (SOC), apparent low-energy band crossings along the paths Γ - M and M - K - Γ can be observed, which appear to be robust to the SOC for this direction of the magnetic moments. Figure 3(b) compares the bands with SOC for the FM [001] and FM [100] configurations and shows that these crossings become gapped when the magnetization points along [001].

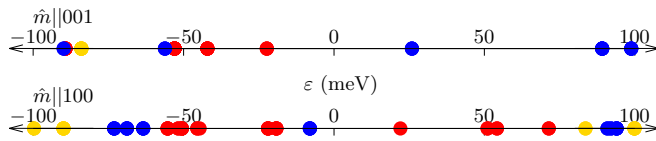


FIG. 4. Energy of Weyl nodes near the Fermi surface for the magnetization along the [001] and [100] directions. Red, blue, and orange dots correspond to Weyl nodes in which the lower band has index $N - 1$, N , and $N + 1$, respectively, with N the number of valence electrons.

A search of Weyl nodes for the FM [100] ground state yields the existence of several Weyl nodes; the closest to Fermi surface are found 8 meV below the Fermi energy. Notice that in SG 194, for this magnetic configuration, there can be up to eight symmetry-related Weyl nodes generated by the inversion symmetry I : the twofold rotations $C_2(y) \times \Theta$, $C_2(2x + y)$, $C_2(z) \times \Theta$ and the reflection symmetries $m(y) \times \Theta$, $m(2x + y)$ and $m(z) \times \Theta$, where Θ is the time-reversal operator.

When the magnetization is rotated towards the hard axis, a situation experimentally relevant in view of the MAE found above and the observed saturation of ρ_{yx} , one can expect the Weyl nodes to move in momentum and energy space as theoretically found in other magnetic compounds [37,38]. A search of Weyl nodes for the FM [001] indeed leads to sizable changes in the number and energy of the Weyl nodes near the Fermi energy, as illustrated in Fig. 4, which shows the found Weyl nodes ordered according to their energy, relative to the Fermi energy, for both magnetic configurations. We also present the distribution of these Weyl nodes in the Brillouin zone in the Supplemental Material (see Figs. S2 and S3) [26]. Figure 5 presents the band-intrinsic contribution to the anomalous Hall conductivity as a function of the chemical potential. For the quantization axis along [001] ([100]) only σ_{xy} (σ_{yz}) is different from zero. At the charge neutrality point ($\mu = 0$), the related values are $\sigma_{xy}^A = 702 (\Omega \text{ cm})^{-1}$ and $\sigma_{yz}^A = 482 (\Omega \text{ cm})^{-1}$. The former value is in fairly good agreement with the experimental result. In the Supplemental Material

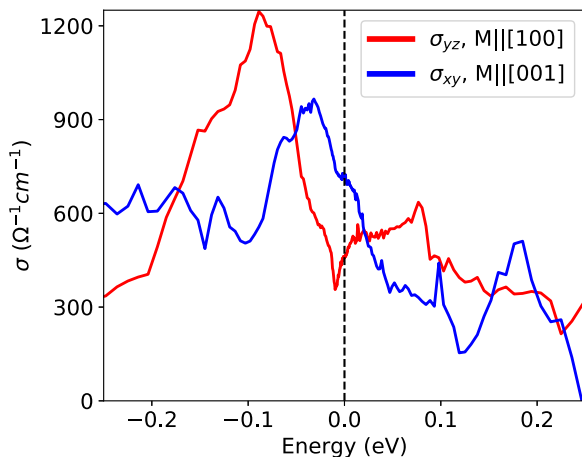


FIG. 5. Anomalous Hall conductivity as a function of the chemical potential.

[26], we analyze the contribution to the AHC from states at different parts of the Brillouin zone and show that the most prominent hot spots acquire a loop structure which reflects the importance of structures other than isolated Weyl nodes for the AHC. The AHC obtained for Fe_3Sn is significantly larger than Fe_3Sn_2 with a value of $200 (\Omega \text{ cm})^{-1}$ [19], and is comparable to Fe_5Sn_3 with a value of $507 (\Omega \text{ cm})^{-1}$ [39]. Interestingly, according to the calculations a moderate amount of hole doping could increase σ_{xy}^A and σ_{yz}^A up to maximum values of $\sim 950 (\Omega \text{ cm})^{-1}$ and $\sim 1250 (\Omega \text{ cm})^{-1}$, respectively. However, this increase is contingent upon maintaining the stability of the ground state property during the doping process [40,41]. Recent values of AHC at E_F [42] is found to be larger than our reported value obtained from the enhanced basis calculations, but is well supported with our earlier work [43].

V. CONCLUSIONS

We have studied single-crystalline kagome metal Fe_3Sn by means of transport experiments and on the basis of density-functional calculations. The system is found to be ferromagnetic, with an easy-plane magnetic anisotropy. A moderate magnetic field of about 3 T is sufficient to reorientate the magnetization along the hexagonal axis. From transport measurements we have inferred the anomalous Hall conductivity to be $\sim 500 (\Omega \text{ cm})^{-1}$. Our DFT results reproduce the preference of the easy-plane anisotropy and our calculation of the band-intrinsic contribution to the AHC agrees well with the experimental results. Interestingly, our calculations indicate that moderate hole doping could largely increase the AHC. Altogether, our experimental and theoretical results establish Fe_3Sn as a kagome Weyl metal with large AHC.

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