# Microscopic characterization of the magnetic properties of the itinerant antiferromagnet  $\text{La}_2\text{Ni}_7$  by **139La NMR***/***NQR measurements**

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(Received 4 April 2023; revised 19 June 2023; accepted 31 July 2023; published 10 August 2023)

<sup>139</sup>La nuclear magnetic resonance (NMR) and nuclear quadrupole resonance (NQR) measurements have been performed to investigate the magnetic properties of the itinerant magnet  $La_2Ni_7$ , which shows a series of antiferromagnetic (AFM) phase transitions at  $T_{\text{N1}} = 61 \text{ K}$ ,  $T_{\text{N2}} = 56 \text{ K}$ , and  $T_{\text{N3}} = 42 \text{ K}$  under zero magnetic field. Two distinct La NMR signals were observed due to the two crystallographically inequivalent La sites in La<sub>2</sub>Ni<sub>7</sub> (La1 and La2 in the La<sub>2</sub>Ni<sub>4</sub> and the LaNi<sub>5</sub> subunits of the La<sub>2</sub>Ni<sub>7</sub> unit cell, respectively). From the  $139$ La NQR spectrum in the AFM state below  $T_{N3}$ , the AFM state was revealed to be a commensurate state where Ni-ordered moments align along the crystalline *c* axis. Owing to the two different La sites, we were able to estimate the average values of the Ni-ordered moments (0.09–0.10  $\mu_B/Ni$  and 0.17  $\mu_B/Ni$  around La1 and La2, respectively) from  $139$ La NMR spectrum measurements in the AFM state below  $T_{\text{N3}}$ , suggesting a nonuniform distribution of the Ni-ordered moments in the AFM state. In contrast, a more uniform distribution of the Ni-ordered moments in the saturated paramagnetic state induced by the application of high magnetic fields is observed. The temperature dependence of the sublattice magnetization measured by the internal magnetic induction at the La2 site in the AFM state was reproduced by a local-moment model better than the self-consistent renormalization (SCR) theory for weak itinerant antiferromagnets. Given the small Ni-ordered moments in the magnetically ordered state, our results suggest that  $\text{La}_2\text{Ni}_7$  has characteristics of both itinerant nature and localized nature in its magnetism. With this in mind, it is noteworthy that the temperature dependence of nuclear spin-relaxation rates  $(1/T_1)$  in the paramagnetic state above  $T_{\text{N1}}$  measured at zero magnetic field can be explained qualitatively by both the SCR theory and the local-moment model.

DOI: [10.1103/PhysRevB.108.064413](https://doi.org/10.1103/PhysRevB.108.064413)

## **I. INTRODUCTION**

Fragile magnets with small ordered moments, such as weak itinerant ferromagnets and antiferromagnets, have attracted much interest in studying quantum phase transitions since the magnetic states of those compounds can be tuned by perturbations such as magnetic field, pressure, and doping  $[1,2]$ . As part of our research on fragile magnets, we have been studying several fragile magnets such as the itinerant ferromagnets LaCrGe<sub>3</sub> [\[3](#page-8-0)[–7\]](#page-9-0) and La<sub>5</sub>Co<sub>2</sub>Ge<sub>3</sub> [\[8\]](#page-9-0), which were found to exhibit avoided quantum critical points. It is now generally believed that the ferromagnetic quantum critical points in clean itinerant ferromagnets are avoided with some exceptions with noncentrosymmetric metals having strong spin-orbit interaction [\[9\]](#page-9-0). Unconventional properties near quantum critical points for weak itinerant antiferromagnets have also been of particular interest and have been studied in many compounds such as Fe-based superconductors, heavy fermions, and so on.

Recently, single crystals of the fragile itinerant antiferromagnet  $La<sub>2</sub>Ni<sub>7</sub>$  with a small ordered moment were successfully synthesized [\[10\]](#page-9-0), which makes it possible to study the physical properties of the material in detail [\[10–12\]](#page-9-0).  $La<sub>2</sub>Ni<sub>7</sub>$  crystallizes in a Ce<sub>2</sub>Ni<sub>7</sub>-type hexagonal structure (space group  $P6_3/mmc$ ) [\[13,14\]](#page-9-0), and the lattice parameters are  $a = b = 5.06235(11)$  Å and  $c = 24.6908(8)$  Å at room temperature  $[10]$ . As shown in Fig.  $1(a)$   $[15]$ , the structure consists of  $La<sub>2</sub>Ni<sub>4</sub>$  and  $LaNi<sub>5</sub>$  subunits, and the unit cell contains two blocks of  $(La_2Ni_4 + 2 LaNi_5)$ , where two different La sites (La1 and La2 in the  $La_2Ni_4$  and the LaNi<sub>5</sub> subunits of the  $La<sub>2</sub>Ni<sub>7</sub>$  unit cell, respectively) and five different sites for Ni atoms exist  $[16,17]$ . The magnetic properties of the compound  $La<sub>2</sub>Ni<sub>7</sub>$  have been investigated since the 1980s, but only in polycrystalline form. Magnetic susceptibility  $\chi(T)$ measurements on  $La<sub>2</sub>Ni<sub>7</sub>$  in polycrystalline samples show a maximum around 51–54 K corresponding to an antiferromagnetic (AFM) phase transition  $[18–20]$ . The effective moment and Curie-Weiss temperature estimated from the  $\chi(T)$  measurement in the paramagnetic state were reported to be 0.80  $\mu_B/Ni$  and 67 K, respectively [\[21\]](#page-9-0). The saturation moment of Ni ions in the magnetically ordered state was reported to be ∼0.08  $\mu_B/Ni$  from magnetization curves [\[22\]](#page-9-0), evidencing the small ordered moments in  $La<sub>2</sub>Ni<sub>7</sub>$ . The magnetization curves show complex temperature-dependent metamagnetic behaviors, suggesting the existence of several magnetic phases [\[21,23\]](#page-9-0).

In fact, from the recent detailed specific heat, magnetization, and electrical resistivity measurements on single crystals, Ribeiro *et al.* [\[10\]](#page-9-0) reported the complete, anisotropic magnetic-field–temperature (*H*-*T* ) phase diagrams for magnetic fields applied parallel and perpendicular to the crystallographic  $c$  axis shown in Fig.  $1(c)$ . In zero applied magnetic field, there are a series of AFM phase transitions at  $T_{\rm N1} \sim$ 

<span id="page-1-0"></span>

FIG. 1. (a) Crystal structure of La<sub>2</sub>N<sub>17</sub> (space group  $P6_3/mmc$ ), which consists of La<sub>2</sub>N<sub>14</sub> and LaN<sub>15</sub> subunits with two different La sites (La1 and La2 in the La<sub>2</sub>Ni<sub>4</sub> and the LaNi<sub>5</sub> subunits, respectively). (b) Schematic view of spin distribution in the antiferromagnetic state (A phase) proposed by DFT calculations [\[17\]](#page-9-0) and ND measurements [\[11\]](#page-9-0). (c) *H*-*T* phase diagrams for *H*  $\parallel$  *c* (bottom) and *H* ⊥ *c* (top) reported by Ribeiro *et al.* based on the *H* and *T* dependences of magnetization  $[M(H)]$  and  $M(T)]$  and resistivity  $[R(H)]$  and  $R(T)]$  measurements [\[10\]](#page-9-0).

61 K,  $T_{N2} \sim 56.5$  K, and  $T_{N3} \sim 42$  K, making three different magnetically ordered phases named the C, B, and A phases for  $T_{N2} < T < T_{N1}$ ,  $T_{N3} < T < T_{N2}$ , and  $T < T_{N3}$ , respectively. It is noted that in the case of the C phase, a small ferromagnetic (FM) component was reported in its AFM ordering [\[10\]](#page-9-0).

Recent neutron diffraction (ND) measurements on single crystals indicate that the B and C phases are incommensurate AFM states, while the A phase is a commensurate AFM state [\[11\]](#page-9-0). In the A and C phases, the ordered moments are parallel to the *c* axis, while in the B phase, there is an additional component of the ordered moments perpendicular to the *c* axis. The commensurate AFM state in the lowest-temperature A phase reported by the ND measurements is consistent with the theoretical predictions [\[17\]](#page-9-0) which suggest that two ferromagnetic unit blocks with opposite Ni spin directions are separated by the nonmagnetic Ni layers in the  $La<sub>2</sub>Ni<sub>4</sub>$  units [see Fig.  $1(b)$ ]. The theoretical studies [\[17\]](#page-9-0) also proposed that the Ni-ordered moments point along the *c* axis and their magnitude depends on the Ni positions. As shown in Fig.  $1(b)$ , the magnitude is the minimum in the  $La<sub>2</sub>Ni<sub>4</sub>$  subunits and is the maximum at the middle of the two LaNi<sub>5</sub> subunits  $[17]$ .

Although detailed studies of the thermodynamic, transport, and structural measurements on the itinerant antiferromagnet  $La<sub>2</sub>Ni<sub>7</sub>$  using a single crystal have been performed, it is important to investigate the static and dynamic magnetic properties of the fragile antiferromagnet  $La_2Ni_7$  with the small ordered moment from a microscopic point of view. Nuclear magnetic resonance (NMR) and nuclear quadrupole resonance (NQR) are powerful techniques to investigate the magnetic properties of materials from a microscopic point of view [\[24\]](#page-9-0). In particular, one can obtain the direct and local information regarding the magnetic state at nuclear sites, providing important information about the magnetic structure of magnetic systems. In addition, the nuclear spin-lattice relaxation time,  $T_1$ , provides important information about magnetic fluctuations.

Here we report the results of <sup>139</sup>La NMR and NQR measurements on  $La<sub>2</sub>Ni<sub>7</sub>$  single crystals and oriented powder samples. Two distinct La signals with two different values of quadrupolar frequencies of  $v<sub>O</sub> = 0.70(2)$  and 3.60(3) MHz are observed. Those are assigned to La1 and La2, respectively, based on density functional theory (DFT) calculations. In the antiferromagnetic state of the lowest-temperature A phase, the internal magnetic induction  $B<sub>int</sub>$  at La2 was determined to be −0.79 T at 4.3 K by the observation of the splitting of NQR lines. In addition, using a single crystal, the direction of  $B<sub>int</sub>$  is determined to be parallel to the  $c$  axis from further splittings of NQR lines under small magnetic fields. From NMR measurements using an oriented powder sample, we found that the  $B<sub>int</sub>$  values at La1 and La2 are close to  $-0.32$  to  $-0.39$  T and  $-0.74$  to  $-0.76$  T, respectively, at 4.3 K in the antiferromagnetic A phase. This result indicates that the Ni-ordered moments are not uniform and the average magnitude of the Ni-ordered moment around La2 is greater than that around La1, which is consistent with the ND results and the DFT calculations. In further measurements, in the saturated paramagnetic state under a high magnetic field of 8 T parallel to the *c* axis at 4.3 K,  $B<sub>int</sub>$  at La1 is found to increase to  $-0.52$  T while  $B<sub>int</sub>$  at La2 decreases to −0.40 T. These results suggest that the Ni-ordered moments are more uniformly distributed at Ni positions in the saturated paramagnetic state. The temperature dependence of  $B<sub>int</sub>$  at the La2 site was well reproduced by the localized-moment model rather than the self-consistent renormalization (SCR) theory for weak itinerant antiferromagnets. The temperature <span id="page-2-0"></span>dependence of  $1/T_1$  measured at zero magnetic field in the paramagnetic state above  $T_{\text{N1}}$  can be reproduced by both the SCR theory and the localized-moment model. These results suggest that the itinerant antiferromagnet  $La<sub>2</sub>Ni<sub>7</sub>$  has magnetic properties characterized by a localized-moment nature, as well as the nature of weak itinerant antiferromagnets as seen by the small Ni-ordered moments in  $La<sub>2</sub>Ni<sub>7</sub>$ .

## **II. EXPERIMENT**

Hexagonal-shaped platelike  $La<sub>2</sub>Ni<sub>7</sub>$  single crystals were grown from high-temperature solutions as detailed in Ref. [\[10\]](#page-9-0). The crystalline *c* axis is perpendicular to the plane. NMR and NQR measurements of  $^{139}$ La nuclei ( $I = 7/2$ ,  $\gamma_{\rm N}/2\pi = 6.0146 \text{ MHz/T}, Q = 0.21 \text{ b}$  were carried out using a laboratory-built phase-coherent spin-echo pulse spectrometer. The 139La NMR spectra were obtained by recording the integrated spin-echo intensity with changing  $H$  at a fixed frequency or changing resonance frequency at a constant magnetic field. The <sup>139</sup>La NQR spectra in zero magnetic field were obtained either by measuring the intensity of the Hahn spin echo in steps of the frequency or by performing a Fourier transform (FT) of the spin-echo signals. For most of the NMR and NQR measurements, we performed the measurements using a powdered sample crushed from the single crystals, as the intensities of NMR and NQR signals for the single crystals are very weak, making the measurements difficult at higher temperatures. For NMR measurements, we used a loosely packed powder sample and found that the grains of the loosely packed sample were oriented under magnetic fields and the orientation direction depends on temperature and magnetic field as shown below. Only for NQR measurements at the lowest temperature of  $T = 1.6$  K under small magnetic fields was a single crystal used to determine the internal field direction.

The <sup>139</sup>La spin-lattice relaxation rates  $(1/T_1)$  were measured using a saturation recovery method. The  $1/T_1$  at each temperature for an NQR line (corresponding to a transition line for  $m = \pm 5/2 \leftrightarrow \pm 7/2$ ) was determined by fitting the nuclear magnetization *M* versus time *t* using the exponential function  $1 - M(t)/M(\infty) = 0.214e^{-3t/T_1} +$ 0.649 $e^{-10t/T_1}$  + 0.136 $e^{-21t/T_1}$ , where *M*(*t*) and *M*(∞) are the nuclear magnetization at time *t* after the saturation and the equilibrium nuclear magnetization at  $t \to \infty$ , respectively [\[25\]](#page-9-0).

#### **III. RESULTS AND DISCUSSION**

## **A. 139La NMR in the paramagnetic state**

Figure  $2(a)$  shows the temperature *T* dependence of frequency-swept 139La NMR spectra for the loosely packed powder sample under a magnetic field  $H = 7.4089$  T. The typical spectrum for a nucleus with spin  $I = 7/2$  with Zeeman and quadrupolar interactions can be described by a nuclear spin Hamiltonian [\[26\]](#page-9-0)

$$
\mathcal{H} = -\gamma_{\rm N} \hbar (1 + K) \mathbf{H} \cdot \mathbf{I} + \frac{h v_{\rm Q}}{6} \left( 3I_{\rm Z}^2 - I^2 + \frac{1}{2} \eta (I_{+}^2 + I_{-}^2) \right),\tag{1}
$$



FIG. 2. (a) Frequency-swept <sup>139</sup>La NMR spectra under  $H =$ 7.4089 T at various temperatures. The green and blue lines are the position of 139La NMR spectra calculated with the temperatureindependent  $v_0 = 0.70(2)$  MHz for La1 and  $v_0 = 3.60(3)$  MHz for La2, respectively. The vertical dashed red line corresponds to the Larmor-frequency position. (b) Temperature dependence of *M*/*H* measured at  $H = 7$  T parallel to the *c* axis  $[(M/H)_c$  in black] and parallel to the *ab* plane  $[(M/H)_{ab}$  in red]. The inset shows the temperature dependence of  $\Delta M/H = (M/H)_{ab} - (M/H)_{c}$ .

where  $H$  is the external field,  $\hbar$  is Planck's constant  $h$  divided by  $2\pi$ , and *K* represents the NMR shift. The first and second terms represent Zeeman and quadrupolar interactions, respectively [\[27\]](#page-9-0). The nuclear quadrupole frequency for  $I = 7/2$  nuclei is given by  $v_{Q} = eQV_{ZZ}/14h$ , where Q is the nuclear quadrupole moment and  $V_{ZZ}$  is the maximum electric field gradient (EFG) at the La sites.  $\eta$  is the asymmetry parameter of EFG defined by  $\frac{V_{XX}-V_{YY}}{V_{ZZ}}$  with  $|V_{ZZ}|\geqslant$  $|V_{YY}| \ge |V_{XX}|$ . The local symmetries at La1 and La2 are 3*m* in La<sub>2</sub>Ni<sub>7</sub> [\[13,14\]](#page-9-0). This means that there is a threefold rotational symmetry around the *c* axis for both La sites. Therefore  $\eta = 0$  and  $V_{ZZ}$  is parallel to the *c* axis for both La sites in  $La<sub>2</sub>Ni<sub>7</sub>$ . Our DFT calculations also confirm this, as described below.

In first-order perturbation theory, when the Zeeman interaction is much greater than the quadrupole interaction, one has the nuclear energy levels for  $I = 7/2$ 

$$
E_m = -\gamma_N \hbar (1 + K) Hm - \frac{h\nu_Q}{12} (3 \cos^2 \theta - 1) \left( 3m^2 - \frac{63}{4} \right),\tag{2}
$$

<span id="page-3-0"></span>where  $\theta$  is the angle between the quantization axis of the La nuclear spin due to the Zeeman interaction and the principal axis of the EFG. Thus the  $139$ La NMR spectrum is composed of a central transition line and three pairs of satellite lines shifted from the central transition line by  $\pm \frac{1}{2}v_Q(3\cos^2\theta - 1)$ (for the transitions of  $m = 3/2 \leftrightarrow 1/2$  and  $-3/2 \leftrightarrow -1/2$ ),  $\pm v_0(3\cos^2\theta - 1)$  (for  $m = 5/2 \leftrightarrow 3/2$  and  $-5/2 \leftrightarrow -3/2$ ), and  $\pm \frac{3}{2}v_Q(3\cos^2\theta - 1)$  (for  $m = 7/2 \leftrightarrow 5/2$  and  $-7/2 \leftrightarrow$  $-5/2$ ). It is noted that the spacing between the lines of the spectrum for  $\theta = 0$  is twice that for  $\theta = 90^{\circ}$ , producing a spectrum for  $\theta = 0$  that is almost two times wider than that for  $\theta = 90^\circ$ .

As shown in Fig.  $1(a)$ ,  $La<sub>2</sub>Ni<sub>7</sub>$  has two inequivalent La sites: La1 and La2 belonging to the  $La<sub>2</sub>Ni<sub>4</sub>$  and the LaNi<sub>5</sub> subunits, respectively. The observed spectra were well reproduced by the simulated spectra [green and blue lines in Fig.  $2(a)$ ] from the simple nuclear spin Hamiltonian with  $v<sub>O</sub> = 0.70(2)$  MHz for green lines and  $v<sub>O</sub> = 3.60(3)$  MHz for blue lines. Here we calculated the spectrum by fully diagonalizing the nuclear spin Hamiltonian [Eq.  $(1)$ ] to ensure that the effects of quadrupolar interaction were fully accounted for in the determination of the NMR shifts.

In order to assign the La sites, we have calculated the electric field gradient at each La site by a full-potential linear augmented plane wave (FLAPW) method [\[28\]](#page-9-0) with a generalized gradient approximation [\[29\]](#page-9-0) using the lattice parameters described in the Introduction. The  $v<sub>O</sub>$  values were calculated to be 0.50 and 4.1 MHz for La1 and La2, respectively. We also found from the calculations that  $V_{ZZ}$  is parallel to the  $c$ axis and the  $\eta$  is zero for both sites, as expected from the local symmetries of the La sites. The relatively large difference in the  $v<sub>O</sub>$  values for those two La sites is consistent with the experimental results. Therefore we assigned the signals with  $v<sub>O</sub> = 3.6$  MHz to La2 and those with  $v<sub>O</sub> = 0.7$  MHz to La1.

As shown in the bottom panel of Fig.  $2(a)$ , the observed spectrum at  $T = 297$  K is relatively sharp and is not a socalled powder pattern. Here we found that the small grains of the loosely packed powder sample were oriented due to *H*. The spectrum was reproduced by the simulated spectrum with  $\theta = 90^\circ$ . A similar but slightly broader spectrum with  $\theta = 90^\circ$  was observed at  $T = 100$  K. Since  $V_{ZZ}$  is parallel to the *c* axis,  $\theta = 90^\circ$  indicates that the *c* axis of the small grains in the loosely packed sample is aligned perpendicular to the external magnetic field. To orient this direction, the magnetization parallel to the *ab* plane (*Mab*) must be greater than *M* parallel to the *c* axis  $(M_c)$  under  $H = 7.4089$  T above 100 K.

To check this, we measured the temperature dependences of  $(M/H)_{ab}$  and  $(M/H)_{c}$  under a magnetic field  $H = 7.0$  T, the results of which are shown in Fig.  $2(b)$  [\[30\]](#page-9-0). Although the  $(M/H)_{ab}$  and  $(M/H)_{c}$  are nearly the same in the paramagnetic state in the scale of the figure, one can see a small difference between  $(M/H)_{ab}$  and  $(M/H)_{c}$  as shown in the inset of Fig. [2\(b\),](#page-2-0) where  $\Delta M/H = (M/H)_{ab} - (M/H)_{c}$  is plotted as a function of temperature.  $\Delta M/H$  changes sign around 90 K:  $(M/H)_{ab}$  is greater than  $(M/H)_{c}$  above 90 K, while  $(M/H)_{ab}$  is less than  $(M/H)_{c}$  below that temperature. The positive value of  $\Delta M/H$  above 100 K is consistent with the NMR results. Therefore our NMR data show that  $\Delta M/H$ is enough to orient the grains of the powder sample even



FIG. 3. Temperature dependences of the 139La NMR shifts: <sup>139</sup>*K<sub>ab</sub>* (green triangles) and <sup>139</sup>*K<sub>c</sub>* (red squares) at *H* = 7.4089 T. <sup>139</sup>*K<sub>c</sub>* measured at *H* = 4 T are also plotted (black circles) [\[31\]](#page-9-0). Open and filled symbols correspond to La1 and La2, respectively. The inset shows the *K* vs  $M/H$  plots for the corresponding *H*. Here we used  $M/H$  measured at  $H = 7.0$  T for the *K*-*M*/*H* plot since no *M*/*H* data at 7.4089 T are available [\[30\]](#page-9-0). The  $M/H$  data at  $H = 4.0$  T are from Ref.  $[31]$ . The blue dashed and solid lines are linear fits for the  $K_c$ data of La1 and La2, respectively. The green dashed and solid lines are linear fits for the *Kab* data of La1 and La2, respectively.

though it is relatively small. The rotation of the grains of the powder sample is due to a torque acting on each grain, and the conditions for getting an oriented powder sample depend on the size of each grain,  $\Delta M/H$ , and so on. Therefore we do not discuss the grain orientation quantitatively here.

With decreasing temperature, each line becomes broader, and the spacings of lines in each NMR spectrum below  $~\sim$ 100 K become twice as large as those in the spectra above that temperature as shown in the upper two panels of Fig. [2\(a\).](#page-2-0) Those spectra measured at 85 and 70 K are well reproduced with  $\theta = 0^\circ$  with the same  $v_Q$  values for the two La sites (the  $T$ -independent  $v_Q$  is confirmed by NQR measurements shown below). This means that the *c* axis of the small grains of the powder sample is rotated by 90◦ and now is oriented along the external magnetic field in that temperature range where  $M_c$  must be greater than  $M_{ab}$ . Again this is consistent with the negative values of  $\Delta M/H$  below 90 K, where  $(M/H)_c$  is greater than  $(M/H)_{ab}$  as seen in the inset of Fig. [2\(b\).](#page-2-0)

Figure 3 shows the temperature dependence of NMR shifts determined by fitting the observed spectra. The open and filled symbols correspond to La1 and La2, respectively. The NMR shift data above 100 K correspond to the case for  $H \parallel ab$  plane  $(K_{ab})$  while *H*  $\parallel$  *c* axis  $(K_c)$  below 100 K at *H* = 7.4089 T. With decreasing temperature, the values of *K* for La1 and La2 decrease similarly. It is noted that the change in the slopes around 100 K is mainly due to the different values of the hyperfine coupling constants for the different magnetic field directions as described below. To see the effect of *H* on NMR shifts (or the magnetization), we also measured NMR spectra at a different magnetic field,  $H = 4.0$  T, the results <span id="page-4-0"></span>of which are shown by the black circles in Fig. [3.](#page-3-0) As can be seen, the NMR shifts under 4.0 T are greater than those at 7.4089 T in magnitude. These observations are consistent with the  $T$  dependence of  $M/H$  under the different magnetic field, where  $M/H$  is suppressed with increasing  $H$  in the  $T$  range  $T = 50-80$  K [\[10\]](#page-9-0). It is noted that we were able to measure  $K_c$  at 100 K under  $H = 4.0$  T because  $(M/H)_c$  is greater than  $(M/H)_{ab}$  at 100 K at  $H = 4.0$  T [\[31\]](#page-9-0).

The NMR shift consists of a temperature-dependent spin shift  $K_s(T)$  and a *T*-independent shift  $K_0$ ;  $K(T) = K_s(T) +$  $K_0$ , where  $K_s(T)$  is proportional to the magnetization  $M(T)$ divided by  $H$ ,  $M(T)/H$ , via the hyperfine coupling constant *A*, i.e.,  $K_s(T) = \frac{A'}{\mu_B N_A} \frac{M(T)}{H}$ . Here  $N_A$  is Avogadro's number. Utilizing the *T* dependence of *M*/*H* under the corresponding magnetic fields for the NMR measurements, we plot all  $K_c$ data as a function of  $M/H$  in the inset of Fig. [3.](#page-3-0) Here, for  $K_c$ at  $H = 7.4089$  T, we used  $M/H$  data measured at 7.0 T since no *M*/*H* data at 7.4089 T are available [\[30\]](#page-9-0). The blue dashed and solid lines are linear fits for La1 and La2, respectively. From the slopes of the blue lines, the hyperfine coupling constants for *H*  $\parallel$  *c* are estimated to be  $A_c = -4.1(6)$  and  $-4.5(5)$  T/ $\mu$ <sub>B</sub> for La1 and La2, respectively. It is noted that the coupling constants estimated here are considered to be the total hyperfine coupling constant produced by the nearest-neighboring (NN) Ni ions, as both La1 and La2 are surrounded by six NN Ni ions [\[32\]](#page-9-0). The values of  $K_0$  for  $H \parallel c$ are estimated to be  $0.5(2)$ % for La1 and  $0.5(2)$ % for La2.

We also plotted the  $K_{ab}$  data (green symbols) as a function of  $(M/H)_{ab}$  at  $H = 7.0$  T in the inset of Fig. [3.](#page-3-0) The green dashed and solid lines are linear fits for La1 and La2, respectively. From the slopes of the linear fits, we obtained  $A_{ab} = -2.2(4)$  T/ $\mu_B$  for La1 and  $-2.5(2)$  T/ $\mu_B$  for La2 under *H*  $\parallel$  *ab*. The  $K_0$  values are also estimated to be 0.7(1) and 1.0(1)% for La1 and La2, respectively.

# **B. 139La NMR spectrum in magnetically ordered states**

Figures  $4(a)$ –4(c) show the frequency-swept  $^{139}$ La NMR spectra in magnetically ordered states at  $T = 4.3$  K for the loosely packed powder sample under magnetic fields of 2.0 T [Fig. 4(a)],  $3.5$  T [Fig. 4(b)], and  $8.0$  T [Fig. 4(c)]. As observed in the paramagnetic state, the spectra are the sum of the two sets of La NMR lines originating from La1 and La2 with  $v<sub>O</sub> =$ 0.7 and 3.6 MHz, respectively. Since the observed spectra are relatively sharp and not so-called powder patterns, the small grains of the powder sample are also found to orient due to *H*, similar to the case of the NMR spectra in the paramagnetic state discussed in Sec. [III A.](#page-2-0)

At  $H = 2$  T, the observed spectrum was reproduced by a sum of the two spectra from La1 (green area) and La2 (blue areas) with the  $H \perp c$  configuration. This indicates that the  $c$ axis of the small grains is oriented perpendicular to *H*. This is due to the fact that  $M_{ab}$  is greater than  $M_c$  in the AFM state (A phase) at 2.0 T, as shown in the inset of Fig.  $4(a)$ , where the *H* dependences of  $M_c$  and  $M_{ab}$  at  $T = 5$  K are shown (the data are from Ref.  $[10]$ ). In the simulations of the spectra, we introduced the internal magnetic inductions  $B<sub>int</sub>$  at the La sites which are produced by the Ni-ordered moments. This is reasonable since the Ni moments are ordered in the AFM state.



FIG. 4. Frequency-swept <sup>139</sup>La NMR spectra at  $T = 4.3$  K on the loosely packed powder sample under magnetic fields of (a) 2.0 T, (b) 3.5 T, and (c) 8.0 T. The green and blue areas are simulated spectra with  $v_0 = 0.7$  MHz for La1 and  $v_0 = 3.6$  MHz for La2, respectively, and different internal magnetic inductions  $B<sub>int</sub>$  discussed in the text. The magenta curves are the sum of the two simulated spectra. The down arrows  $(f_0)$  correspond to the Larmor frequencies for each magnetic field. The peak around  $f_0$  clearly observed in the spectrum at  $H = 8$  T probably comes from impurities [\[33\]](#page-9-0). The inset of (a) shows the external magnetic field dependence of *M* for *H ab*  $(M_{ab}$  in red) and  $H \parallel c$  ( $M_c$  in black) measured at 5 K from Ref. [\[10\]](#page-9-0). The inset of (b) shows the schematic view of the configuration for the canting angles  $\theta'$  for *M* and  $\theta''$  for  $B_{int}$  from the *c* axis, respectively.  $\theta$  is the angle between the quantization axis of La nuclear spin ( $B_{\text{eff}}$ ) and the *c* axis.

For La2, we used  $B_{\text{int}}^{c} = -0.76(1)$  T parallel to the *c* axis and  $B_{\text{int}}^{ab} = -0.03(1)$  T perpendicular to the *c* axis. At zero magnetic field, as described in Sec. [III C,](#page-5-0) the direction of  $B<sub>int</sub>$ at La2 is determined to be parallel to the *c* axis (that is, parallel to the Ni-ordered moments) in the A phase. Under a magnetic field perpendicular to the *c* axis, however, *B*int is no longer parallel to the *c* axis because of spin canting as shown in the inset of Fig.  $4(b)$ . This is the reason why we needed to introduce  $B_{int}^{ab}$  in the simulation. The canting angle  $\theta'$  of the Ni-ordered moment from the *c* axis can be calculated from magnetization data since  $\theta'$  is given by  $\sin^{-1}(M_{ab}/M_s)$ , where *M*<sup>s</sup> is the saturation of magnetization. Taking the saturated value of  $M_c$  at 7.0 T as  $M_s$  [see the inset of Fig. 4(a)],  $\theta'$  is estimated to be 8.9° at  $H = 2.0$  T. It is noted that the angle  $\theta'$ is not the same as  $\theta''$  because of the anisotropy in the hyperfine <span id="page-5-0"></span>coupling constants. Here  $\theta''$  is the angle between  $B_{int}$  and the *c* axis. From  $B_{\text{int}}^c = -0.76(1)$  T and  $B_{\text{int}}^{ab} = -0.03(1)$  T,  $\theta''$  is estimated to be 2.3(5)°. This value is smaller than the  $\theta'' = 4.9(9)°$  which is estimated from the  $M_{ab}/M_s$  at 2 T by using  $A_c = -4.5(5) \text{ T}/\mu_B$  and  $A_{ab} = -2.5(2) \text{ T}/\mu_B$ . As shown in the inset, the effective magnetic induction at the La site  $(\mathbf{B}_{\text{eff}})$  given by the vector sum of  $\mathbf{B}_{\text{int}}$  and **H** is not perpendicular to the  $c$  axis due to the  $B<sub>int</sub>$ . We also estimated the angle  $\theta$  between the quantization axis of the La nucleus and the *c* axis. Using the experimentally obtained  $B_{\text{int}}$ ,  $\theta$  is estimated to be  $68(2)^\circ$ .

For the simulation of the spectrum for La1,  $B_{int}^c =$  $-0.39(1)$  T and  $B_{\text{int}}^{ab} = -0.015(5)$  T were used.  $\theta''$  and  $\theta$ are estimated to be 2.2(4)° and 79(2)°, respectively.  $\theta''$  is estimated to be  $4.8(5)°$  from the *M* data utilizing the hyperfine coupling constants.

The observed spectrum at  $H = 3.5$  T is also reproduced with the  $H \perp c$  configuration and a similar set of the parameters of  $B_{\text{int}}^{c} = -0.32(2)$  [-0.74(1)] T and  $B_{\text{int}}^{ab} = -0.05$  T [-0.03(1)] T for La1 (La2), respectively, with the same  $v<sub>Q</sub>$ values. Again  $H \perp c$  is consistent with the *M* data, where  $M_{ab}$ is greater than  $M_c$  at  $H = 3.5$  T [see the inset of Fig. [4\(a\)\]](#page-4-0). At  $H = 3.5$  T, we estimate  $\theta' = 15.5^{\circ}$  from the *M* data.  $\theta'' =$ 5.4(5)° [3.9(4)°] and  $\theta = 78(1)$ ° [83.8(6)°] for La1 (La2) are evaluated from the NMR data.

When we simulated the spectra at  $H = 2$  and 3.5 T, it turned out that the changes in  $B<sub>int</sub><sup>c</sup>$  alter the spacings between lines. On the other hand,  $B_{\text{int}}^{ab}$  mainly shifts the whole spectrum without changing the spacing between the lines much. This is because the direction of the external magnetic field is perpendicular to the *c* axis. Therefore we can determine the relatively accurate value of  $B<sub>int</sub><sup>c</sup>$  by simulations. In contrast, we were not able to determine  $\ddot{B}_{int}^{ab}$  precisely since one needs to take the contribution of the Knight shift *K* into consideration. Since  $La<sub>2</sub>Ni<sub>7</sub>$  is in a metallic state, we should have a finite value of *K* along the *H* direction. This *K* shifts the whole spectrum as  $B_{\text{int}}^{ab}$  does. Thus the estimates of the  $B_{\text{int}}^{ab}$  values depend on the value of *K*. In our simulations, we used  $K = 0.5\%$ , which is estimated from the value of  $1/T_1T$  in the AFM state using the Korringa relation [\[34\]](#page-9-0). Although we consider that  $K = 0.5\%$ is reasonable because this value is close to the values of  $K_0$ estimated from the  $K-\chi$  analysis, there must be relatively large uncertainty in the estimation of  $B_{int}^{ab}$ . Therefore the estimated directions of  $B<sub>int</sub>$  and  $B<sub>eff</sub>$  discussed above should be considered as tentative ones.

When the system is in the saturated paramagnetic state under  $H = 8$  T, the spectra become wider due to the change from the  $H \perp c$  configuration to the  $H \parallel c$  configuration. This corresponds to the *c* axis of the small grains of the powder sample being oriented along *H*, which is again consistent with the *M* data, where  $M_c$  is now greater than  $M_{ab}$  above  $H = 6.2$  T as can be seen in the inset of Fig.  $4(a)$ . By fitting the spectra while keeping the same  $v<sub>O</sub>$  values for the La sites, we found that  $B_{int}^{c} = -0.52(1)$  T and  $-0.40(1)$  T for La1 and La2, respectively.

Utilizing the hyperfine coupling constants and the internal magnetic inductions, the average values of Ni-ordered moments around La1 and La2 from  $\mu = \sqrt{\left(\frac{B_{\text{int}}^c}{A_c}\right)^2 + \left(\frac{B_{\text{int}}^{abc}}{A_{\text{dp}}}\right)^2}$  are estimated to be 0.10(1)  $\mu_B$  for La1 and 0.17(1)  $\mu_B$  for La2 at  $H = 2$  T in the AFM state (A phase). Although we have uncertainty in  $B_{\text{int}}^{ab}$ , the estimated  $\mu$  values should be relatively reliable because the values of  $\mu$  are mainly determined by the  $(\frac{B_{\text{int}}^c}{A_c})^2$  term in the formula due to  $(\frac{B_{\text{int}}^c}{A_c})^2 \gg (\frac{B_{\text{int}}^{ab}}{A_{ab}})^2$ . At  $H = 3.5$  T, the values of  $\mu$  were estimated to be 0.09(1)  $\mu_B$  and 0.17(1)  $\mu_B$  for La1 and La2, respectively. The average values of Ni-ordered moments around La1 is 56% of that around La2, suggesting a nonuniform distribution of the Ni-ordered moments in the AFM state. This is qualitatively consistent with the AFM state predicted by the theory and the ND measurement, where the maximum amplitude of the Ni-ordered moments is expected at the middle of two LaNi<sub>5</sub> subunits close to La2 while the minimum amplitude of the Ni-ordered moments is proposed at Ni ions in the  $La<sub>2</sub>Ni<sub>4</sub>$ subunit close to La1.

We also estimate the average values of Ni-ordered moments to be 0.12(1)  $\mu_B$  and 0.09(1)  $\mu_B$  around La1 and La2, respectively, in the saturated paramagnetic state. According to the theoretical calculations, in the ferromagnetic state, the ferromagnetic units are stacked ferromagnetically while keeping the nonuniform distribution of the moments as in the AFM state [\[17\]](#page-9-0). In this case, we expect almost no change in the average values of Ni-ordered moments around both La sites in the saturated paramagnetic state as compared with the AFM state. This is inconsistent with the NMR results showing that the distribution of the average values of Ni-ordered moments in the saturated paramagnetic state is different from the case of the AFM state.

It is noted that the NMR spectrum for La2 at  $H = 2$  T shows six lines instead of the expected seven lines. This is because one of the NMR lines overlaps with another line due to the relatively large  $B<sub>int</sub><sup>c</sup> = -0.75$  T along the *c* axis, which is perpendicular to the external magnetic field of 2 T. Qualitatively, this could be understood by taking two effects into consideration: (1) the change in the angle  $\theta$  between the quantization axis of the nuclear spin and  $V_{ZZ}$  and  $(2)$ the increase in the effective magnetic induction due to  $B_{\text{int}}$ . Since the position of the satellite lines changes following  $3\cos^2\theta - 1$ , each satellite line will shift toward the central transition line with increasing  $B_{int}$ . At the same time, the effective magnetic induction increases, making the NMR lines shift to a higher frequency. By combining the two effects, one could qualitatively understand the spectrum at  $H = 2$  T. As shown, we were able to reproduce the observed spectrum by the simulation where the nuclear spin Hamiltonian including the internal magnetic induction was fully diagonalized.

# **C. 139La NQR spectrum**

At zero magnetic field, the electric quadrupole Hamilto-nian [the second term of Eq. [\(1\)](#page-2-0)] for the case of  $I = 7/2$ produces three equally spaced NQR lines at resonance frequencies of  $v<sub>0</sub>$ ,  $2v<sub>0</sub>$ , and  $3v<sub>0</sub>$  corresponding to the transitions of  $m = \pm 1/2 \leftrightarrow \pm 3/2, \pm 3/2 \leftrightarrow \pm 5/2$ , and  $\pm 7/2 \leftrightarrow \pm 5/2$ , respectively. From NMR measurements, the values of  $v<sub>O</sub>$  are estimated to be 3.60(3) MHz for La2, so one expects three NQR lines at 3.6, 7.2, and 10.8 MHz, named the  $v_1$ ,  $v_2$ , and  $v_3$ lines, respectively. In fact, we observed such NQR lines in the paramagnetic state as shown in Fig.  $5(a)$ , where the  $v_1$  line was not measured due to the limitation of the resonance frequency

FIG. 5. (a) <sup>139</sup>La NQR spectra for La2 at zero magnetic field at various temperatures in both the paramagnetic and magnetically ordered states. The magenta curves are simulated spectra. (b) Temperature dependence of the resonance frequency for each peak. The symbols in black, red, and blue represent the  $v_3$ ,  $v_2$ , and  $v_1$  lines, respectively. (c) Temperature dependence of the magnitude of the internal magnetic induction  $|B_{int}|$  at La2. The values of  $B_{int}$  are estimated by fitting the the spectra, and the simulated spectra are shown by the magenta curves in (a). The expected temperature dependences of  $B_{\text{int}}$  based on the ND data [\[11\]](#page-9-0) are also plotted in (c) with the green open triangles (the *c* components of the ordered moments in the commensurate antiferromagnetic A phase), the blue open triangles (the *ab*-plane components of the ordered moments in the incommensurate antiferromagnetic B phase), and the magenta open triangles (the *c* components of the ordered moments in the incommensurate antiferromagnetic B and C phases). The ND data sets shown by the green, blue, and magenta symbols were normalized to scale the NMR data at 40, 45, and 50 K, respectively. The black and red curves show the expected temperature dependences of  $B<sub>int</sub>$  based on the SCR theory and the localized-moment picture, respectively (see text).

of our spectrometer (we also could not measure the NQR lines for the La1 site due to the small value of  $v<sub>O</sub> = 0.7$  MHz). The observed NQR spectra, that is, the peak frequencies for the  $v_2$ and  $v_3$  lines, for the La2 site are well reproduced with  $v_0 =$ 3.63(1) MHz as shown by the calculated spectra in magenta, and those peak frequencies are independent of temperature in the paramagnetic state [see Fig.  $5(b)$ ], indicating no change in  $v<sub>Q</sub>$  with temperature.

In the AFM state, we found that each line splits into two lines, as shown in Fig.  $5(a)$ . This is due to the appearance of *B*int at La2 produced by Ni-ordered moments in the AFM state. The  $B_{\text{int}}$  lifts the degenerate nuclear spin levels of  $\pm m$ states. To estimate  $B_{\text{int}}$ , we calculated NQR spectra using a Hamiltonian where a Zeeman term due to  $B_{\text{int}}$ , similar to the first term of Eq.  $(1)$ , was added to the electric quadrupole Hamiltonian. We found that the observed spectra were well reproduced by taking  $B_{int}$  parallel to the  $c$  axis, as shown by the calculated spectra in magenta in the magnetically ordered state. The value of  $|B_{int}|$  is estimated to be 0.79 T at 4.3 K. It is noted that we also observed the small signals around 6 and 9 MHz at low temperatures below 30 K which were not reproduced by the simulation. The origin of the lines is not clear at present. It might be related to the impurity signals observed at the Larmor frequency in the NMR spectrum measured at 8 T described in Sec. [III B.](#page-4-0) The temperature dependence of  $B_{int}$  at the La2 site is shown in Fig.  $5(c)$ , which corresponds to the temperature dependence of sublattice magnetization  $M_{sub}$ . Here we also plotted the expected temperature dependence of  $M_{sub}$  ( $\propto B_{int}$ ) based on the ND data [\[11\]](#page-9-0) by the green open triangles (the *c* components of the ordered moments in the commensurate antiferromagnetic A phase), the blue open triangles (the *ab*-plane components of the ordered moments in the incommensurate antiferromagnetic B phase), and the magenta open triangles (the *c* components of the ordered moments in the incommensurate antiferromagnetic B and C phases). The ND data sets shown by the green, blue, and magenta symbols were normalized to scale the NMR data at 40, 45, and 50 K, respectively. It is noted that the phase transitions at  $T_{N2}$  and  $T_{N1}$  are of second order while the first-order phase transition was observed at  $T_{N3}$  [\[11\]](#page-9-0). It is also noted that the temperature dependences of *M*sub from the ND measurements in the magnetically ordered states are overlapped with that of  $B<sub>int</sub>$  determined by the NMR measurements although the overlapped temperature range  $(T = 35-50 \text{ K})$  is not wide.

According to self-consistent renormalization (SCR) theory, the temperature dependence of  $M_{sub}$  for the case of weak itinerant antiferromagnets is given by [\[35\]](#page-9-0)

$$
M_{sub}(T) \propto \sqrt{1 - (T/T_N)^{3/2}}.
$$
 (3)

The black curve is the calculated temperature dependence of  $|B_{\text{int}}|$   $[= B_{\text{int},0} \sqrt{1 - (T/T_{\text{N}})^{3/2}}]$  based on the above formula with  $B_{\text{int},0} = 0.79$  T and  $T_N = 62$  K, which does not reproduce the experimental data well. Since the phase transition at  $T_{\text{N3}}$ is of first order, we also tried to fit only for the data above *T*N3 using the formula. However, we could not fit the data well with a reasonable value of  $B_{\text{int},0}$ . In addition, it is clear that the observed temperature dependence of  $B<sub>int</sub>$  cannot be explained by the formula using the different values of  $T_N$ . Thus we conclude that the temperature dependence of  $M_{sub}$ in  $La<sub>2</sub>Ni<sub>7</sub>$  cannot be explained by the model of weak itinerant antiferromagnets. Instead, the temperature dependence of  $B<sub>int</sub>$ was found to be reasonably well reproduced by a Brillouin function which was calculated based on the Weiss molecular field model shown by the red curve, where we tentatively assumed  $S = 1$  and used  $T<sub>N</sub> = 62$  K. Here we normalized the calculated temperature dependence to scale with  $|B_{int}|$ at the lowest temperature. These results may indicate that the magnetic state of the Ni ions is more likely described by the local-moment picture, contrary to the anticipation from the small Ni-ordered moments in the itinerant antiferromagnet  $La<sub>2</sub>Ni<sub>7</sub>$ . Interestingly, a similar discrepancy between  $M<sub>sub</sub>$  and the SCR theory has been reported in weak itinerant antiferromagnets such as  $V_5Se_8$  [\[36\]](#page-9-0),  $V_5S_8$  [\[37\]](#page-9-0),  $CrB_2$  [\[38\]](#page-9-0), and  $YM_{12}$  [\[39\]](#page-9-0). Further theoretical and experimental studies are called for to understand the local-moment nature in those weak itinerant systems.

The direction of  $B<sub>int</sub>$  in the AFM state is also directly confirmed by  $^{139}$ La NQR spectrum measurements on the single crystal in nonzero *H*. Figure [6](#page-7-0) shows the *H* dependence

<span id="page-6-0"></span>

<span id="page-7-0"></span>

FIG. 6. 139La NQR spectra for La2 under small magnetic fields at 1.6 K. The inset shows the external magnetic field dependence of peak frequencies of the split lines for the  $v_2$  and  $v_3$  lines. The solid lines are the expected *H* dependence of peak frequencies when  $B_{\text{int}}$ is parallel or antiparallel to the *c* axis.

of the NQR spectrum at 1.6 K under small magnetic fields applied parallel to the *c* axis using a single crystal. With the application of small  $H$  less than 0.2 T, we found that one of the split  $v_2$  lines that is shifted to the higher-frequency side (around 12 MHz) further splits into two lines as shown in Fig. 6. Similar splitting is also observed for the  $v_3$  line around 15.6 MHz under small magnetic fields. These results clearly indicate the existence of two La2 sites with  $B<sub>int</sub>$  parallel or antiparallel to the *c* axis. As discussed above, the effective field at the La site is given by the vector sum of  $\mathbf{B}_{\text{int}}$  and  $\mathbf{H}$ , i.e.,  $|\mathbf{B}_{\text{eff}}| = |\mathbf{B}_{\text{int}} + \mathbf{H}|$ ; the resonance frequency is expressed for *H*  $\parallel$  *B*<sub>int</sub> as  $f = \frac{y_N}{2\pi} |B_{\text{eff}}| = \frac{y_N}{2\pi} |B_{\text{int}} \pm \hat{H}|$ . As shown in the inset of Fig. 6, the *H* dependence of the split peak frequencies is well reproduced by the relation using  $\frac{\dot{Y}_N}{2\pi} = 6.0146 \text{ MHz/T}$ for the La nucleus, evidencing that  $B_{int}$  is parallel or antiparallel to the *c* axis without any obvious deviation. This result also clearly shows the appearance of two sublattices, a direct confirmation of the antiferromagnetic state.

To see how the NQR spectra change around magnetic phase transition temperatures for the investigation of the AFM states of the B and C phases, we measured the NQR spectra around 11 MHz at zero magnetic field for the three phases. Figure 7 shows the measured NQR spectra for the powder samples in the three magnetic phases together with the one in the paramagnetic (PM) state. The line around 10.9 MHz in the PM state corresponds to the  $v_3$  line. When the sample is in the AFM state at  $T = 58$  K (C phase), we found that the position of the NQR line does not change, although the line becomes slightly broad. According to the ND measurements, the C phase is proposed as an incommensurate AFM state with the Ni-ordered moment parallel to the *c* axis. Therefore the small broadening could be due to a small  $B<sub>int</sub>$  in the phase. With further decrease in temperature, the signal around 10.9 MHz disappeared when the system entered the B phase as shown by the spectrum at  $T = 50$  K. Instead, we observed the slightly broader NQR line centered at 10.5 MHz, lower than the peak



FIG. 7. 139La NQR spectra for La2 at zero magnetic field at various temperatures in both the paramagnetic and the magnetically ordered states. The spectra shown by black solid and red open circles are the  $v_3$  and  $v_2$  lines, respectively.

frequency of 10.9 MHz in the paramagnetic state and the C phase. We assigned the line to be one of the split  $v_2$  lines due to  $B_{\text{int}}$  being along the *c* axis because the position of the line smoothly connects to that of the line in the A phase [see Fig.  $5(c)$ ]. This suggests that the dominant component of *B*int at La2 is parallel or antiparallel to the *c* axis in the B phase, similar to the case in the A phase. According to the ND data, the propagation vectors parallel and perpendicular to the *c* axis are incommensurate in the B phase. This indicates that the Ni-ordered moments are no longer ferromagnetic blocks [\[11\]](#page-9-0). In this case, one expects the large distribution of  $B_{int}$  at the La sites. Therefore the NMR data would be inconsistent with the ND results. The slightly broader lines are due to small distributions of  $B<sub>int</sub>$ . This suggests that the slight distributions of the Ni-ordered moments in the B phase might be related to the in-plane component of the incommensurate AFM state reported from the ND data. In contrast, as we discussed in Sec. [III B,](#page-4-0) the commensurate AFM state (phase A) reported from the ND measurements is consistent with the NMR results.

# **D.**  $^{139}$ La spin-lattice relaxation time  $T_1$

Figure [8](#page-8-0) shows the *T* dependence of  $1/T_1T$  measured at the  $v_3$  line of the <sup>139</sup>La NQR spectrum under zero magnetic field. In the paramagnetic state,  $1/T_1T$  is nearly constant above 150 K, starts to increase below that temperature with

<span id="page-8-0"></span>

FIG. 8. Temperature dependence of  $1/T_1T$  measured at the 3 $v<sub>O</sub>$ line in the paramagnetic and magnetic states. The red and green curves are the calculated results based on the SCR theory and the localized-moment picture, respectively (see text).

decreasing  $T$ , and shows a peak around  $T_{\rm N1}$  due to critical slowing down of the spin fluctuation, characteristics of a second-order phase transition. In the AFM state (A phase), the  $1/T_1T$  = const behavior expected for metals is observed [\[34\]](#page-9-0). This is consistent with the itinerant nature of  $La<sub>2</sub>Ni<sub>7</sub>$ .

Since the system has small ordered moments, we first fit the data based on the SCR theory. For the case of weak itinerant antiferromagnets, the SCR theory predicts the temperature dependence of  $1/T_1T$  in paramagnetic states given by [\[40,41\]](#page-9-0)

$$
1/T_1T = \frac{a}{\sqrt{T - T_N}} + b,\tag{4}
$$

where the first term originates from AFM fluctuations around a wave vector  $q = Q$  (Q being an antiferromagnetic wave vector) and the second term is due to Korringa-type relaxation, a characteristic feature of metallic materials. The red curve in the paramagnetic state shows the calculated results based on the SCR theory with a set of parameters of  $a = 8 \text{ s}^{-1} \text{ K}^{-0.5}$ ,  $b = 1.6$  s<sup>-1</sup> K<sup>-1</sup>, and  $T_N = 62$  K, which reproduces the experimental data in contrast to the case of the *T* dependence of  $B_{\text{int}}$ .

On the other hand, as the  $T$  dependence of  $B<sub>int</sub>$  suggests a localized-moment nature rather than a weak itinerant antiferromagnet nature, we also analyzed the  $T_1$  data with the localized-moment model described by

$$
1/T_1T = \frac{a'}{T - \Theta} + b',\tag{5}
$$

where the first term originates from the paramagnetic uniform spin fluctuations of localized spins described by Curie-Weiss behavior of the magnetic susceptibility, i.e.,  $1/T_1 \propto \chi T$ , and the second term is Korringa-type relaxation, a characteristic feature of metallic materials as in Eq. (4). With  $a' = 20 s^{-1}$ ,  $b$ <sup>'</sup> = 2.2 s<sup>-1</sup> K<sup>-1</sup>, and  $\Theta$  = 62 K, the experimental data are also reproduced reasonably well as shown by the green curve in Fig. 8. Therefore both the SCR theory and the localizedmoment picture can explain the observed *T* dependence of  $1/T_1$ , although these are different in terms of the character of the spin fluctuations. Thus, given the small Ni-ordered moments evidenced by the magnetization and present NMR spectrum measurements, our experimental results may suggest that  $La<sub>2</sub>Ni<sub>7</sub>$  has both the characteristic nature of weak itinerant antiferromagnets and the characteristic nature of localized-moment antiferromagnets.

#### **IV. SUMMARY**

In summary, we have performed a microscopic characterization of the itinerant antiferromagnet  $La_2Ni_7$  using  $139La$ NMR and NQR measurements. Our results show the presence of a commensurate antiferromagnetic A phase with Ni-ordered moments aligned along the crystalline *c* axis. Furthermore, a nonuniform distribution of the Ni-ordered moments was found with the comparative analysis of inequivalent La1 and La2 sites. In the saturated paramagnetic state under a magnetic field of 8 T at 4.3 K, the Ni-ordered moments were found to become more uniform. The temperature dependence of the sublattice magnetization measured by the internal magnetic induction  $B<sub>int</sub>$  at the La2 site is reproduced by the local-moment model. The temperature dependence of  $139$ La spin-lattice relaxation time  $(T_1)$  suggests that the paramagnetic-to-antiferromagnetic phase transition at *T*<sub>N3</sub> is second order in nature and that its temperature dependence in the paramagnetic state can be produced by both the localmoment model and the self-consistent renormalization model for weak itinerant antiferromagnets. Our NMR results suggest a peculiar magnetism in the itinerant antiferromagnet  $La<sub>2</sub>Ni<sub>7</sub>$ that exhibits properties of both localized and itinerant nature.

#### **ACKNOWLEDGMENTS**

The authors would like to thank J. Wilde and A. Sapkota for providing the neutron diffraction data and also for fruitful discussions. The research was supported by the U.S. Department of Energy, Office of Basic Energy Sciences, Division of Materials Sciences and Engineering. Ames National Laboratory is operated for the U.S. Department of Energy by Iowa State University under Contract No. DE-AC02-07CH11358.

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