

Light-induced coherent interlayer transport in stripe-ordered $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$

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We have investigated the photoexcited transient responses of stripe-ordered phase in a cuprate superconductor, $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ ($x = 0.12$), using optical-pump terahertz (THz)-probe spectroscopy. Upon the near-infrared photoexcitation with the electric field polarized along the c axis, a clear plasma edge appears in the THz reflection spectrum along the c axis with its position nearly coinciding with the Josephson plasma resonance of similarly doped $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ ($x = 0.125$) in the low-temperature superconducting phase. The appearance of a light-induced plasma edge sustains up to the onset temperature of the charge-stripe order, indicating the inherent interplay between the light-induced phase and the charge-stripe order. The optical conductivity spectrum of the light-induced state is mostly reproduced by the Drude model with a scattering rate as small as a few meV, and its imaginary part does not exhibit $\frac{1}{\omega}$ -divergence behavior in any temporal region after the photoexcitation. We discuss the possible origin of the observed coherent interlayer transport behavior as manifested by the narrow Drude response in the THz reflectivity along the c axis.

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I. INTRODUCTION

A common characteristic of high- T_c cuprates is that the superconductivity emerges by doping carriers into parent compounds of antiferromagnetic Mott insulators. In the proximity of the superconductivity, various phases appear including the original antiferromagnetic phase, the pseudogap region, the charge- and spin-ordered phase, and the pair density wave order [1–5]. Elucidation of their interplay with the superconductivity has been one of the central issues in the study of high- T_c superconducting cuprates. Recently, various experimental studies have revealed that the charge order is present in a wide range of high- T_c cuprates and thus the relevance of the charge order to the superconductivity and other proximity phases has been intensively investigated [5–7]. One of the most concrete forms of the charge order is perhaps the stripe order [8–11], in which both charges and spins are spontaneously segregated in a form of stripes in the CuO_2 plane, as found in 214 families of La-based cuprates including $\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$ (LBCO), $\text{La}_{2-x-y}\text{Eu}_y\text{Sr}_x\text{CuO}_4$ (LESCO), and $\text{La}_{2-x-y}\text{Nd}_y\text{Sr}_x\text{CuO}_4$ [11,12]. Near the hole doping level of $x = \frac{1}{8}$, the static charge- and spin-stripe orders (CO and SO, respectively) are stabilized by pinning to the low-temperature tetragonal (LTT) lattice deformation [9,11–14], associated with a substantial suppression of the three-dimensional (3D)-superconducting critical temperature T_c [Fig. 1(a)]. This phenomenon, dubbed the $\frac{1}{8}$ anomaly, primarily indicates the strong competition between the stripe orders and bulk superconductivity. This competition was further supported by the

absence of the $\frac{1}{8}$ anomaly in thin-film samples [15,16] and by the recovery of T_c under pressure which suppresses the LTT deformation and thus destabilizes the stripes [17]. On the other hand, neutron scattering measurements have revealed the coexistence of bulk superconductivity and stripe orders [18]. Furthermore, far-infrared spectroscopy [19] and resistivity measurements [20,21] have elucidated the signature of two-dimensional superconductivity coexisting with the stripe order above T_c . These experiments indicate the intimate interplay between the stripe orders and superconductivity.

Recent developments in ultrafast pump-probe spectroscopy techniques have provided further insights into the relationship between the stripe orders and superconductivity. Remarkably, the emergence of the plasma edge in the terahertz (THz) reflectivity spectrum was observed in $\frac{1}{8}$ -doped LESCO above T_c up to the onset temperature of CO (T_{CO}) after the midinfrared pulse excitation and interpreted as a light-induced superconducting Josephson plasma edge [22,23]. Similar behavior was identified in the stripe phase of the LBCO system by midinfrared and also by visible wavelength optical pumping [24,25]. As the photoexcitation melts stripe orders [26–28], these phenomena were interpreted as a recovery of c axis Josephson coupling caused by the photoinduced destruction of the stripe order, indicating the development of two-dimensional (2D) superconducting pairings in the charge-ordered state in equilibrium. The presence of equilibrium in-plane superconductivity above T_c was also indicated from the observation of THz third-harmonic generation along the c axis [29,30].

In this paper, to have a deeper insight into the intertwining of the charge- and spin-stripe order and the superconductivity, we applied the ultrafast spectroscopy technique to another stripe-ordered system of the La-214 family, $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ (LNSCO), where the static charge and

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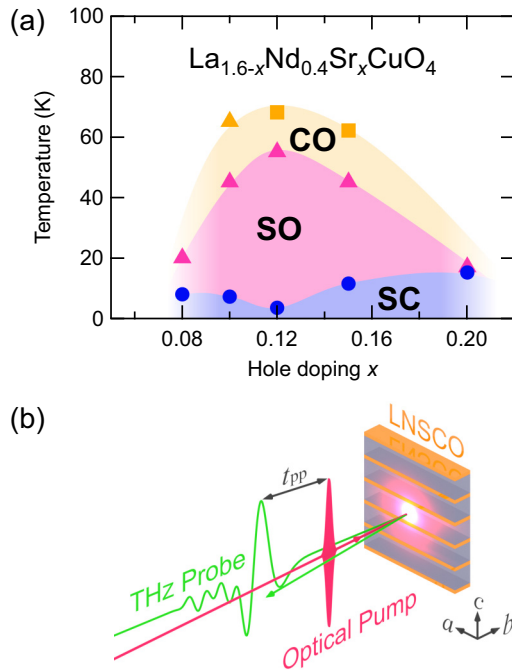


FIG. 1. (a) Phase diagram of $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ (LNSCO). CO: charge-stripe order observed by x-ray (orange squares, [32,33]) and neutron (orange triangle, [34]) diffraction; SO: spin-stripe order by neutron scattering (magenta triangles, [18,31,34]); SC: superconducting state by magnetic susceptibility (blue circles, [18,34]). (b) Schematic of the optical-pump THz probe measurement along the c axis of LNSCO.

spin stripes are stabilized by Nd^{3+} substitution [12,18,31–34]. An x-ray scattering study has revealed a shorter correlation length in LNSCO than in LBCO [35]. The study of how such a short-range character of charge stripes influences the light-induced superconductinglike state is imperative for the understanding of the interplay between those competing or coexisting orders.

II. METHOD

We used a $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ single crystal with the doping level of $x = 0.12$ grown by the floating-zone method, where $T_{\text{CO}} = 67$ K and $T_{\text{SO}} = 55$ K [31]. T_c was determined as 3.2 K from the onset temperature of diamagnetism. All the pump-probe experiments were performed above T_c . The mirror-polished ac surface of the sample was mounted on a copper sample holder with a tapered hole ($\phi 3$ mm). In Fig. 1(b) we show a schematic of near-infrared optical-pump THz-probe spectroscopy. As a light source, we used a Ti:sapphire-based regenerative amplifier with a pulse energy of 7 mJ, a repetition rate of 1 kHz, a pulse duration of 100 fs, and a center wavelength of 800 nm (1.55 eV in photon energy). The output of the laser was divided into three beams: one each for the optical pump, probe THz generation, and the gate pulse for the THz time-domain spectroscopy. The optical-pump beam has a Gaussian profile with a $1/e^2$ diameter of 6 mm, which ensures spatially uniform excitation on the probed region. The THz probe pulse was generated by optical rectification in a large-aperture ZnTe crystal. Both the optical

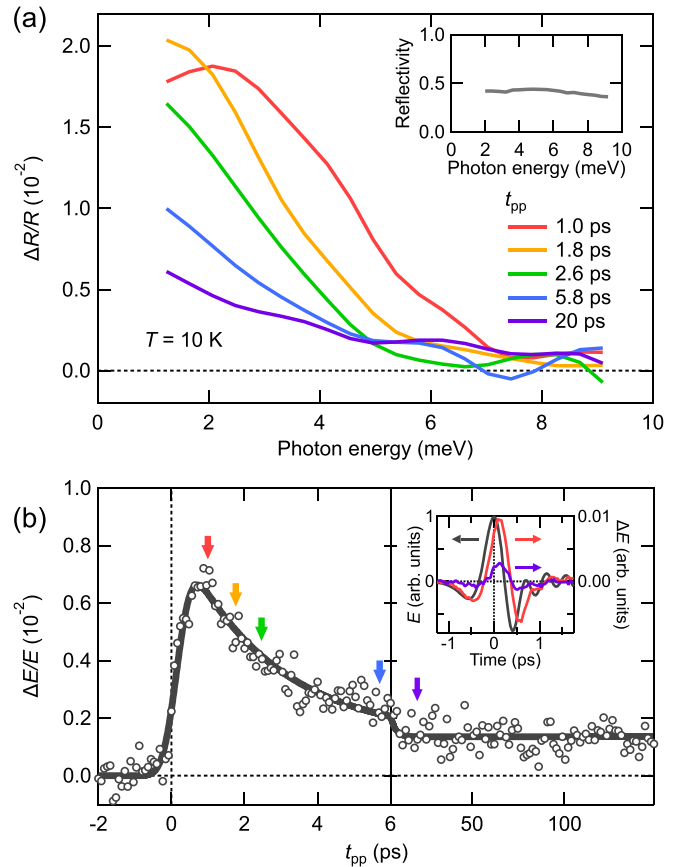


FIG. 2. Dynamics of reflectivity change after the photoexcitation at 10 K. (a) Transient reflectivity change spectra. Inset shows equilibrium reflectivity spectrum at 10 K. (b) Dynamics of THz electric field change $\Delta E/E$. Colored arrows indicate the pump-probe delays corresponding to the traces in (a). Bold line represents the fitting result by Eq. (1). Inset: reflected THz waveform without pump, E (gray line), and pump-induced electric field change ΔE for $t_{\text{pp}} = 1.0$ ps (red line) and 20 ps (purple line). $\Delta E/E$ in the main figure was measured at the peak position of the probe THz E field.

pump and THz probe pulse were linearly polarized along the c axis of LNSCO. The reflected THz pulse was detected by the electro-optic sampling in a ZnTe crystal with the gate pulse. To obtain the pump-induced reflection spectrum change, the delay time between the pump pulse and the gate pulse (t_{pp}) was fixed and the probe THz pulse was swept relative to the gate pulse, and then Fourier transformed.

III. RESULTS

Figure 2(a) shows the light-induced c axis reflectivity change for each pump-probe delay t_{pp} with a pump fluence of 1 mJ/cm^2 at 10 K. While the reflection spectrum is featureless in equilibrium in the measured photon energy range as shown in the inset, a sharp reflectivity edge emerges, and then redshifts within a few picoseconds after the photoexcitation. To capture the dynamics of the photoinduced state in a longer timescale, we plotted the reflected THz electric field change $\Delta E/E$ as a function of t_{pp} in Fig. 2(b). After the photoexcitation, $\Delta E/E$ first rises with a slight delay (~ 1 ps) relative to the pump pulse, followed by exponential decaying behavior

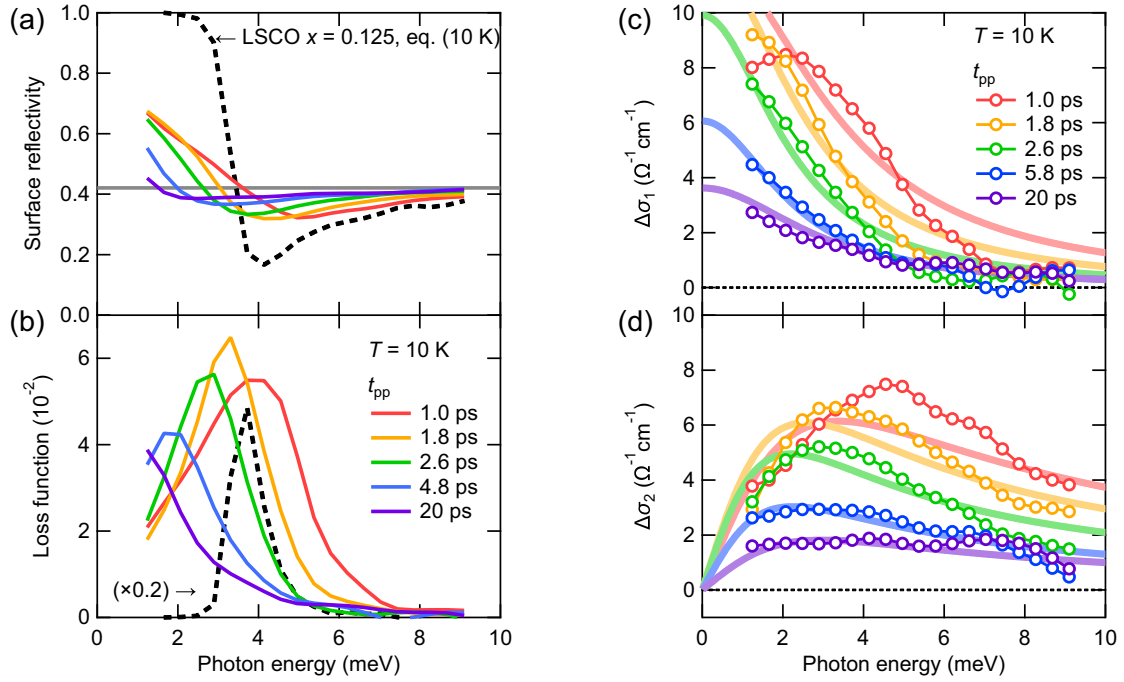


FIG. 3. Optical spectra at the sample surface extracted by the multilayer model. (a) Surface reflectivity, defined as the reflectivity of the boundary between air and photoexcited sample surface. Gray horizontal line represents the equilibrium reflectivity calculated from $n_{\text{eq}} = 4.7$. (b) Loss function spectra, $-\text{Im}[1/\varepsilon(\omega)]$. The peak corresponds to the longitudinal plasma resonance. The black dashed lines in (a,b) indicate the equilibrium reflectivity and loss function spectrum of superconducting LSCO with a doping level of $x = 0.125$ at 10 K. (c,d) Real and imaginary part of the conductivity change. Bold lines are fitting results by the Drude model.

with two characteristic timescales. The data were fitted by the following function:

$$f(t_{\text{pp}}) = \frac{1 + \text{erf}[(t_{\text{pp}} - t_0)/\sigma]}{2} \left[A_1 \exp\left(-\frac{t_{\text{pp}} - t_0}{\tau}\right) + A_2 \right], \quad (1)$$

where the fast-decaying component is described by the amplitude A_1 and lifetime $\tau \sim 2$ ps, and the long-lived component much longer than 100 ps is approximated by a constant term A_2 .

To take into account the effect of penetration depth mismatch between the optical pump and THz probe pulses, we adopted a multilayer model [36,37] and extracted the optical response functions at the sample surface, where the pump-induced reflectivity change is the largest. In this model, the induced refractive index change is assumed to decay exponentially along the sample's depth direction, as given by $n(z) = (n_{\text{surf}} - n_{\text{eq}}) \exp(-z/d) + n_{\text{eq}}$. Here, z is the depth from the surface, $d = 0.31 \mu\text{m}$ is the penetration depth for the optical-pump pulse determined by ellipsometry measurements, n_{surf} is the refractive index at the surface region under the photoexcitation, and $n_{\text{eq}} = 4.7$ is the refractive index in equilibrium without the pump which was extracted from the reflection spectrum shown in the inset of Fig. 2(a), by approximating that it is constant in the measured photon energy range. We note here that the spectral analysis using the above exponential decay model can result in artificial spectral structures in particular below T_c unless the effect of heating is correctly taken into account [38], but such an artifact is not significant in

the present LNSCO system above T_c because the equilibrium reflection spectrum is featureless.

Figure 3(a) presents surface reflection spectra obtained from n_{surf} using Fresnel's formula for the reflectivity, $R = |(1 - n_{\text{surf}})/(1 + n_{\text{surf}})|^2$. A sharp edge structure arises with its position almost identical to that of the raw transient reflection spectrum shown in Fig. 2(a). The induced surface reflectivity approaches unity toward the low-energy limit, which is in accordance with the behavior expected for the plasma edge.

Corresponding to the edge structure observed in the reflection spectra, a sharp peak is identified in the loss function spectra defined by $-\text{Im}[1/\varepsilon(\omega)]$ where $\varepsilon(\omega) = n_{\text{surf}}^2(\omega)$ is the dielectric function, as represented in Fig. 3(b), which corresponds to the longitudinal plasma resonance. This peak also shows a redshift after the photoexcitation and moves away from the measured spectral range after 20 ps. As a reference, the c axis reflectivity and loss function spectrum of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ (LSCO) with $x = 0.125$ sample ($T_c = 33$ K) in its equilibrium superconducting state at 10 K are shown by the black dashed lines.

From the complex transient reflection spectrum obtained by THz time-domain spectroscopy, the photoinduced changes of the real and imaginary part of the optical conductivity, $\Delta\sigma_1(\omega)$ and $\Delta\sigma_2(\omega)$, are extracted without using the Kramers-Kronig analysis as shown in Figs. 3(c) and 3(d), respectively, at the indicated pump-probe delay. The spectral features of the induced optical conductivity for later delays at $t_{\text{pp}} = 5.8$ and 20 ps are reasonably well described by the Drude model, $\Delta\sigma_1(\omega) + i\Delta\sigma_2(\omega) = i\varepsilon_0\omega_p^2/(\omega + i\gamma)$, as represented by the bold lines in Figs. 3(c) and 3(d), where ε_0

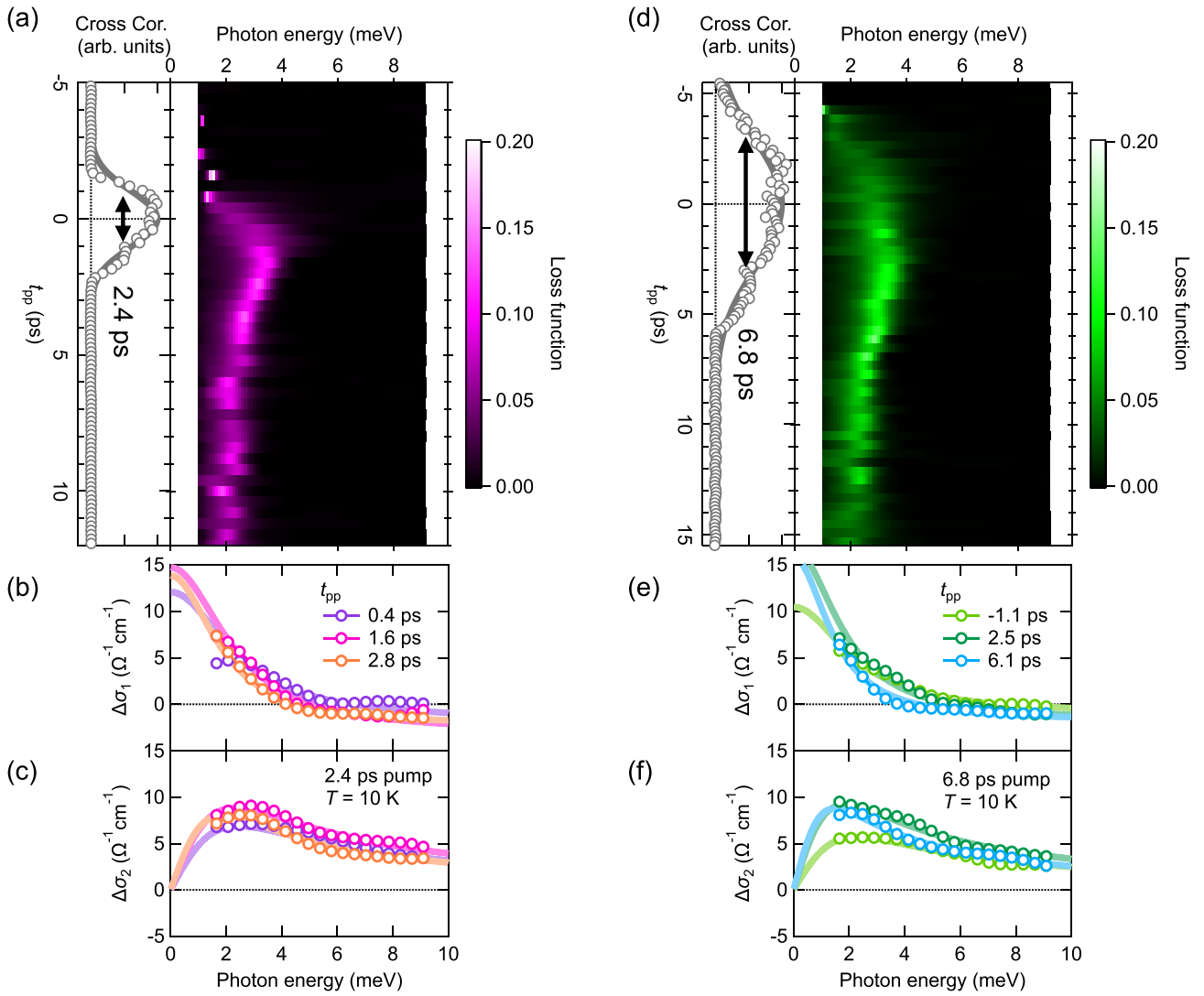


FIG. 4. Results of chirped-pulse excitation measurements at 10 K with the pump pulse widths of (a–c) 2.4 ps and (d–f) 6.8 ps. Gray circles in (a,d) are cross-correlation signals between the chirped pump pulse and the unchirped 35-fs gate pulse, and gray solid lines represent Gaussian fitting to them. The pump pulse widths are estimated without performing the deconvolution of the gate pulse width. The color plots represent the transient evolution of the loss function spectra. (d,e) The real and (c,f) imaginary part of the optical conductivity change at representative t_{pp} shown in legends. Bold lines are fitting results by the Drude model with constant offset (see Appendix A).

is the vacuum permittivity, ω_p is the plasma frequency, and γ is the scattering rate. A deviation from the Drude model is discerned for earlier delays at $t_{pp} = 1.0$ – 2.6 ps, as represented by the peak structure at ~ 2 meV in $\Delta\sigma_1(\omega)$ at $t_{pp} = 1.0$ ps, but the $\frac{1}{\omega}$ -divergent behavior is not observed in the $\Delta\sigma_2(\omega)$ spectra at any t_{pp} unlike the case of LBCO and LESCO [22–25]. This behavior is possibly related to the short-range character of charge stripes in LNSCO [35], as we discuss later in the Discussion section.

One may also consider the artifact of the ultrafast pump-probe signal that appears when the signal decays faster than the period of probe THz field [39]. To examine this possibility, we performed the optical-pump THz-probe spectroscopy with a longer pump pulse duration ranging from 2.4 to 6.8 ps using a grating pair (see Appendix A for the experimental details). As displayed in Figs. 4(a) and 4(d), the loss function peak corresponding to the longitudinal plasma resonance evolves

after the pump pulse irradiation accompanied by a slight delay (~ 1 ps) as in the case of short-pulse (100-fs) excitation, which may reflect the buildup timescale of the plasmon, or the melting dynamics of charge stripes [27] as we discuss later. Importantly, the loss function peak reaches around 4 meV at the largest and then shows a redshift, as also observed in the short-pulse excitation experiments. These results indicate that the emergence of the plasmon peak reflects the intrinsic nature of the light-induced nonequilibrium state, and its lifetime can be prolonged by using a longer pump pulse. The prolongation of the light-induced state is also reported in the $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ system recently [40], although the microscopic mechanism for realizing the light-induced state may differ from that of the stripe-ordered system. The real and imaginary parts of the conductivity spectrum are shown in Figs. 4(b) and 4(c) for the 2.4-ps pump, and Figs. 4(e) and 4(f) for the 6.8-ps pump. The bold lines represent fitting results by the Drude model

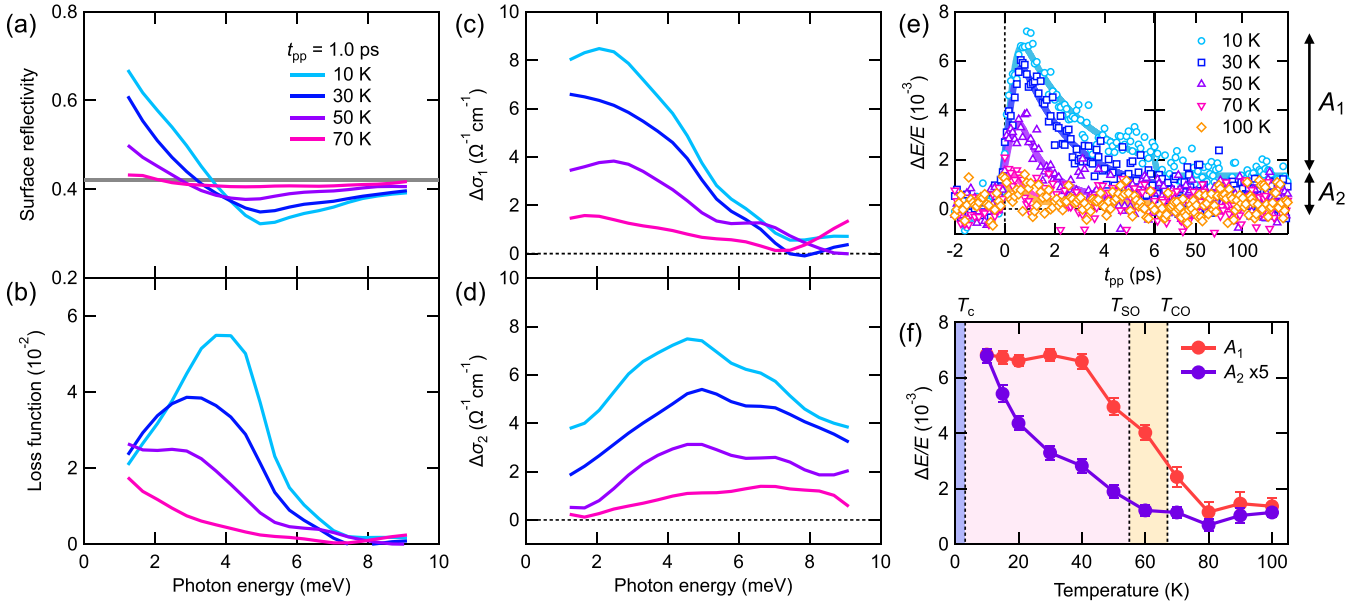


FIG. 5. Temperature dependence of the photoinduced reflectivity change taken at $t_{pp} = 1$ ps. (a) Surface reflection spectra, (b) loss function spectra $-\text{Im}[1/\epsilon(\omega)]$, and (c,d) real and imaginary parts of the conductivity change. Gray horizontal line in (a) represents the equilibrium reflectivity calculated from $n_{eq} = 4.7$. (e) Dynamics of THz electric field change for each temperature. Solid lines are fitting results by Eq. (1). (f) Temperature dependence of the fitting parameters A_1 and A_2 in Eq. (1).

with a negative offset, the latter of which needs to be included to account for the heat accumulation effect due to the higher pump fluence used in these long-pulse experiments compared to the case of the short-pulse (100-fs) pump (see Appendix A for the details). The spectra are reasonably well reproduced with a finite scattering rate of 2–3 meV, indicating that the finite peak observed in $\Delta\sigma_2(\omega)$ in short-pulse excitation is not attributed to the artifact of the measurement.

Next, we show the temperature dependences of the light-induced reflectivity change and the loss function spectrum at $t_{pp} = 1.0$ ps in Figs. 5(a) and 5(b), respectively. With increasing temperature, the plasma edge and the correspondent loss function peak show a redshift and disappear above T_{CO} . Also shown in Figs. 5(c) and 5(d) are $\Delta\sigma_1(\omega)$ and $\Delta\sigma_2(\omega)$ spectra, respectively, for each temperature at $t_{pp} = 1.0$ ps. $\Delta\sigma$ gradually decreases as temperature increases but sustains up to T_{CO} with its spectral shape nearly unchanged. The dynamics of the reflected THz electric field change $\Delta E/E(t_{pp})$ is displayed in Fig. 5(e) for each temperature with the fitting result by Eq. (1). The extracted temperature dependences of the parameters A_1 and A_2 are summarized in Fig. 5(f). We can clearly see that the fast-decaying component A_1 develops below T_{CO} , while A_2 develops at a lower temperature.

IV. DISCUSSION

Now we discuss the possible origin of the observed photoinduced plasma edge and the coherent interlayer transport behavior as indicated by the narrow Drude response in the THz reflectivity along the c axis. Because the reflection spectrum in equilibrium is nearly featureless in the THz frequency range due to the insulating character along the c axis in LNSCO above T_c , the emergence of such a distinct plasma edge structure by the photoexcitation cannot be attributed to

the heating effect. In the present case of the 1.55-eV pump polarized along the c axis, the initial process of the photoexcitation should be primarily the charge redistribution, most likely the transfer of holes from the CuO_2 planes to apical oxygens as reported in Ref. [41]. However, the photodoped carriers themselves cannot be directly attributed to the origin of the observed Drude weight because the observed weight decreases with increasing temperature and disappears above T_{CO} .

Combined with the previous observation in LESCO and LBCO systems, the light-induced reflectivity edge is interpreted as a general character of the charge-stripe phase in cuprates. As suggested from recent time-resolved resonant x-ray scattering measurements in the LBCO system in which the CO melting is shown to occur within 1 ps after the photoexcitation with a recovery time of about 5 ps [27], it is likely that the melting of CO also occurs in the present case of LNSCO. In fact, the pump fluence of 1 mJ/cm^2 (corresponding to 1×10^{-2} photon/Cu) in our experiments is higher than the previously investigated pump fluence region for the CO melting to occur [27].

Unlike the case of LBCO and LESCO [22–25], however, the $\frac{1}{\omega}$ divergence is not observed in $\Delta\sigma_2$ in the present case of LNSCO and, instead, a narrow Drude-like response appears in the earlier time (~ 1 ps) after the photoexcitation. One may consider that the observed narrow Drude response is ascribed to quasiparticles that appear when the CO is destroyed. In fact, the appearance of the narrow Drude response itself has been reported as an in-plane response in the normal state of the underdoped $\text{HgBa}_2\text{CuO}_{4+\delta}$ with exhibition of the Fermi liquid behavior [42]. Therefore, one can attribute in principle the origin of the light-induced Drude weight along the c axis to quasiparticles in the normal state. Although we do not rule out this possibility, it is highly nontrivial that such coherent

quasiparticles along the c axis with a scattering rate as small as 3 meV appear below 70 K associated with the destruction of the CO.

Taking into account that the static CO is a competing order with the superconductivity, it is still tempting to relate the observed coherent c axis interlayer transport behavior to the c axis pair tunneling that is activated by quenching the CO. As we have seen in Fig. 3, the coincidence of the energy of the light-induced plasma edge in LNSCO and that of LSCO in the equilibrium superconducting phase in similar doping ($x = 0.125$) is indicative. Along with this picture, the recent theoretical investigation using variational Monte Carlo calculation has shown the transient appearance of the superconductivity after the photoexcitation with suppressing the charge order which dominates the superconductivity in equilibrium as a consequence of a subtle free energy competition between the CO and the superconductivity [43]. In light of this picture, we then infer that the unusually narrow Drude response that appeared after the photoexcitation is still related to the superconductivity even though the $\frac{1}{\omega}$ -like divergence is not observed in $\Delta\sigma_2$.

Significantly, a recent theoretical study has shown that the d -wave superconducting order is enhanced by an optical pump while its superconducting correlation is limited to a short-range one, associated with the suppression of antiferromagnetic spin order [44]. Such short-range nonequilibrium superconductivity may explain the suppression of $\frac{1}{\omega}$ divergence in $\Delta\sigma_2(\omega)$ in the low-energy (-frequency) range [45], while maintaining the Josephson plasma edge structure in the THz frequencies. It is also indicative that a recent theoretical calculation based on Ginzburg-Landau theory explains that a subdominant order appears associated with a large fluctuation when the other competing order is rapidly quenched off [46].

One complication is that a finite spectral weight in $\Delta\sigma_1$ appears instead of exhibiting the spectral weight missing as normally expected for the superconductivity. However, this behavior is also compatible with the short-range superconductivity associated with spatial inhomogeneity. For example, in the Bi2212 system, a growth of finite spectral weight in the sub-THz frequency range toward the low-temperature limit has been reported, exhibiting a correlation with the growth of superfluid density [47,48]. This result was theoretically described by taking into account the inhomogeneous distribution of superfluid density that reproduces the spectral weight transfer from the δ -function peak at $\omega = 0$ to finite frequencies [49,50]. It is also noteworthy that the residual Drude weight of the in-plane THz response with a relatively small scattering rate of ~ 3 meV has been observed in thin-film samples of an overdoped LSCO system below T_c in equilibrium and attributed to phase fluctuating Cooper pairs [51]. Although it is not clear that the same argument can be applied to the c axis response of LNSCO, the observed narrow Drude response in the photoinduced state may indicate the fluctuating nature of the light-induced superconductivity, regardless of its classical or quantum origin [52,53].

One may also recall the relatively sharp peak near the Josephson plasma frequency in $\sigma_1(\omega)$ along the c axis in the equilibrium superconducting phase of LSCO near the $\frac{1}{8}$ doping [54,55] as another candidate for the finite spectral weight in $\Delta\sigma_1$. A plausible explanation of this conductivity

peak has been made by van der Marel and Tsvetkov by taking into account the transverse Josephson plasmon with the introduction of the spatial variation of Josephson coupling strength [56]. In the light-induced state of LNSCO, the induced superconducting state is likely more inhomogeneous than that in equilibrium LSCO; thus a broadened form of such a peak is expected to appear in $\sigma_1(\omega)$. This can be also responsible for the finite spectral weight in the light-induced state of LNSCO.

In whichever cases, the emergence of Josephson plasma resonance without the $\frac{1}{\omega}$ divergence in $\Delta\sigma_2(\omega)$ and with the increase of spectral weight in $\Delta\sigma_1(\omega)$ in the THz frequency range can be reconciled by considering the inhomogeneously distributed superconducting order parameter, even without possessing long-range superconducting order, which has been also discussed in the context of vortex phase [57]. This behavior in LNSCO distinct from LBCO may share a common origin with the short correlation length of charge stripes observed in LNSCO [35].

In this regard, we note another important difference between LNSCO and LBCO: the light-induced plasma edge is clearly observed in LNSCO at nearly the $\frac{1}{8}$ doping ($x = 0.12$), whereas none was observed in LBCO with similarly doped $x = 0.125$. Considering that the stripe order is more robustly developed in LBCO than in LNSCO [24], this difference suggests that the moderate competition between the stripe order and the superconductivity, including pair density wave, plays an important role in the enhancement of the photosusceptibility of the induced superconductivity.

It is highly nontrivial that the plasma frequency of the equilibrium LSCO and that of the induced state in LNSCO far above T_c coincide with each other. This coincidence implies that the induced state reflects the nonequilibrium nature which appears only during or right after the pump pulse irradiation. It is also noteworthy that the transient redshift of the light-induced plasma frequency is observed after the optical pumping, which may indicate the thermalization of the electron, spin, and lattice system that leads to the thermal destruction of Cooper pairs and the interlayer coherence. The coincidence of plasmon frequency also implies that the Cooper pair density is determined by the doping irrespective of the Nd substitution, and the nonthermal melting of the stripes in LNSCO triggers the appearance of interlayer coherence with the plasma frequency limited by the preexisting Cooper pair density.

We would like to remark on the peak structure that appeared in $\Delta\sigma_1$ in the early delays. Note that the energy scale of this spectral feature is smaller than the energy scale of charge stripes as reported in LBCO [58] and $\text{La}_{2-x}\text{Sr}_x\text{NiO}_4$ [59] where the spectral weight transfer to the higher-energy side has been identified in much larger energy scales. Although such a prominent spectral weight transfer was not identified in LNSCO [60,61], the same energy scale of charge stripes with that of LBCO would apply to LNSCO as the onset temperatures of the charge stripes are nearly the same. Then, the origin of the finite spectral weight in $\Delta\sigma_1$ in the THz frequency range is likely attributed to the coherent charge carrier responses. One possible origin of this is again ascribed to the inhomogeneously distributed superconducting order parameter, which calls for further experimental and theoretical investigation including the possibility of collective modes [50,62,63].

Finally, we comment on the possible origin of the long-lived component described by the A_2 term in Eq. (1). As shown in Fig. 3(a), even in such a longer delay limit, the edgelike behavior is also discerned at the low-energy region to which the high-energy plasma edge structure asymptotically approaches. Presumably, such a long-lived signal is attributed to the heating effect caused by photoexcitation. Using the heat capacity of LNSCO [64], the temperature increase by the pump pulse with the fluence of 1 mJ/cm^2 is estimated to be about 60 K. Therefore, the charge stripes are considered to be melted thermally in a longer time delay, which may explain the increase of the conductivity in such a long-lived component. This long-lived behavior also deserves further investigation to clarify the slow dynamics of charge-stripe order.

V. CONCLUSION

We have investigated the photoexcitation effect of the stripe-ordered phase in $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ ($x = 0.12$) above T_c by optical-pump THz probe spectroscopy along the c axis. The transient reflection spectrum shows a clear plasma edge in the THz frequency range and its maximum position nearly coincides with that of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ ($x = 0.125$) in its equilibrium superconducting phase. This photoinduced plasma edge was identified only below T_{CO} , indicating that the suppression of the charge stripes is crucial for the emergence of the photoinduced plasma edge.

The extracted transient complex optical conductivity exhibits a Drude-like spectrum with a small scattering rate of $\gamma \sim 3 \text{ meV}$. This coherent charge carrier response along the c axis is discussed in view of fluctuating superconductivity with a short-range correlation length.

Having seen the crucial role of stripe order for the emergence of the light-induced plasma edge, possibly the short-range superconducting state, it will be promising to study how the nature of stripes will affect the photosuscep-

tibility of the induced superconductivity, e.g., by changing the doping and also by comparing the behavior of Nd-free LSCO, for the further elucidation of the interplay between the superconductivity and the stripe orders.

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APPENDIX A: LONG-PULSE EXCITATION WITH A CHIRPED PULSE

To confirm that the observed plasma edge and the loss function peak are not sensitive to the pump pulse duration, we performed optical-pump THz-probe spectroscopy with a prolonged pump pulse. For this purpose, we used a Ti:sapphire-based regenerative amplifier with a pulse energy of 2 mJ and pulse duration of 35 fs. As schematically illustrated in Fig. 6, the beam output was divided into optical pump, THz generation, and gate pulse. The optical-pump pulse was down-chirped by a grating pair. The pulse width is tuned between 2.4 and 6.8 ps by changing the grating separation. The pump fluence is 3 and 4 mJ/cm^2 for 2.4 and 6.8 ps pumping, respectively. These fluences were determined as the value at which the pump-induced signal begins to saturate, by the same procedure as the short-pulse excitation. The other parameters are the same as the 100-fs pumping setup.

In such high pump fluence region the conductivity change becomes negative in particular for higher frequencies. This negative component is long-lived and attributed to the heat accumulation caused by higher pump fluence than in the

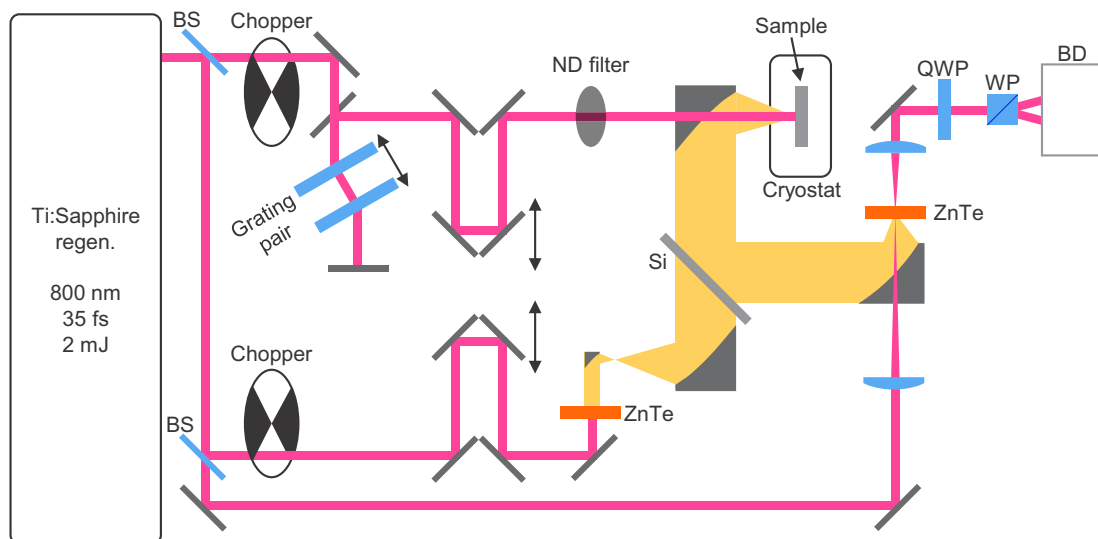


FIG. 6. Schematic image of the long-pulse excitation measurement. The optical-pump pulse was down-chirped with a grating pair. BS: beam splitter; QWP: quarter wave plate; WP: Wollaston prism, BD: balanced detector.

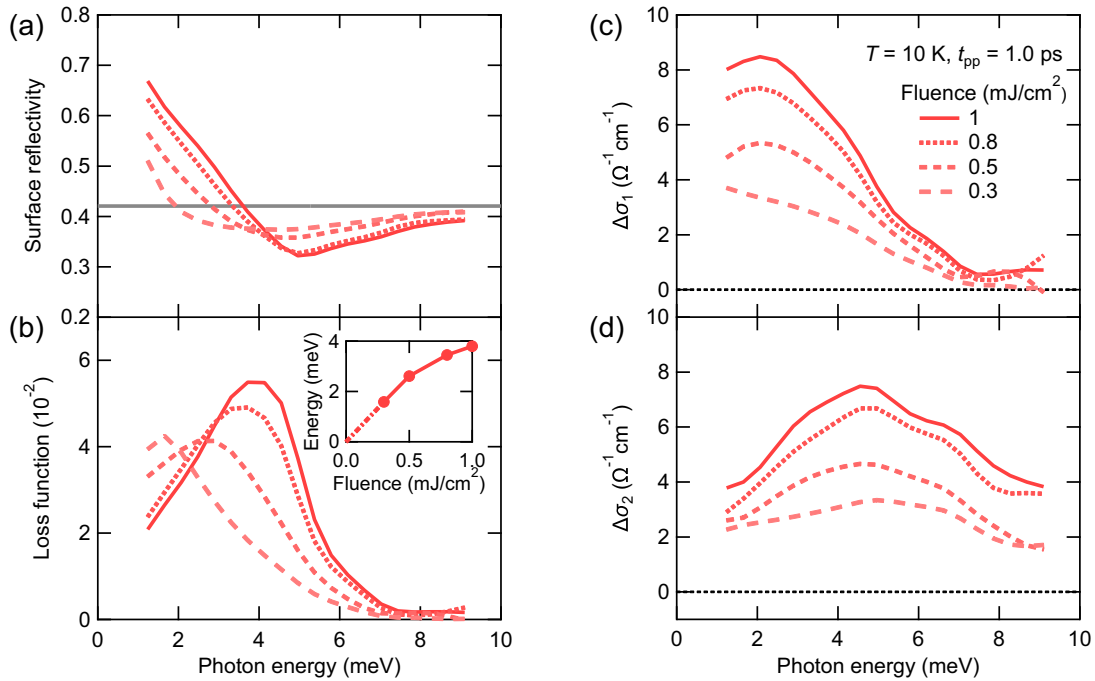


FIG. 7. (a) Surface reflection spectra, (b) loss function spectra $-\text{Im}[1/\epsilon(\omega)]$, and (c,d) real and imaginary parts of the conductivity change at 10 K for several fluences. Gray line in (a) represents equilibrium reflectivity calculated from $n_{\text{eq}} = 4.7$. The inset of (b) shows the pump fluence dependence of the loss function peak energy at $t_{\text{pp}} = 1.0$ ps.

100-fs pumping case which becomes unavoidable in our pump probe measurements even for the low repetition rate of 1 kHz. In the fitting, we represent this average heating by introducing a negative offset value σ_{ofs} in the conductivity change from the equilibrium spectrum. The fitted spectrum is thus obtained by using the Drude model with negative offset, $\Delta\sigma_1(\omega) + i\Delta\sigma_2(\omega) = i\epsilon_0\omega_p^2/(\omega + i\gamma) - |\sigma_{\text{ofs}}|$.

APPENDIX B: PUMP-FLUENCE DEPENDENCE

To study further the behavior of the photoinduced state, we have measured the pump-fluence dependence of the reflectivity change and the loss function spectra as represented in Figs. 7(a) and 7(b), respectively, at $t_{\text{pp}} = 1.0$ ps. With increasing the pump fluence, the plasma edge in the reflection spectrum blueshifts and asymptotically approaches the maximum value of ~ 4 meV. Concomitantly the loss function peak shows a blueshift with increasing pump fluence, whose energy is plotted in the inset of Fig. 7(b) against the pump fluence. These behaviors are consistent with the long-pulse excitation experiments described in the main text, where the increase of the loss function peak energy was observed following the rising of the pump pulse envelope.

The fluence dependences of the photoinduced complex optical conductivity at $t_{\text{pp}} = 1.0$ ps are also displayed in Figs. 7(c) and 7(d). While the amplitude of $\Delta\sigma_1(\omega)$ and $\Delta\sigma_2(\omega)$ increases as the pump fluence rises, their spectral shapes are almost identical without showing the $\frac{1}{\omega}$ divergence in the imaginary part irrespective of the pump fluence, and show a saturation behavior above 0.5 mJ/cm².

In our analysis of the surface layer model, the saturation effect of the pump-induced refractive index change discussed in Ref. [65] is not taken into account, because the loss function peak energy grows linearly up to ~ 3 meV with the pump fluence as shown in the inset of Fig. 7(b). Above the fluence of 0.5 mJ/cm², we can discern the saturation behavior in the extracted optical responses. If the saturation of the refractive index change is taken into account, the effective pump penetration depth should become longer (but yet sufficiently shorter than the THz probe penetration depth). This correction of the penetration depth should cause the more pronounced saturation of the plasma edge energy in such a high-fluence region, and thus we can conclude that the asymptotic value of the plasma resonance should rest between 3 and 4 meV.

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