




## Steering skyrmions with microwave and terahertz electric pulses

Xi-guang Wang <sup>1</sup>, Guang-hua Guo,<sup>1</sup> V. K. Dugaev <sup>2</sup>, J. Barnaś <sup>3,4</sup>, J. Berakdar,<sup>5</sup>  
S. S. P. Parkin,<sup>6</sup> A. Ernst,<sup>6,7</sup> and L. Chotorlishvili<sup>2</sup>

<sup>1</sup>*School of Physics and Electronics, Central South University, Changsha 410083, China*

<sup>2</sup>*Department of Physics and Medical Engineering, Rzeszow University of Technology, 35-959 Rzeszow, Poland*

<sup>3</sup>*Faculty of Physics, Adam Mickiewicz University, ulica Uniwersytetu Poznańskiego 2, 61-614 Poznań, Poland*

<sup>4</sup>*Institute of Molecular Physics, Polish Academy of Sciences, ulica M. Smoluchowskiego 17, 60-179 Poznań, Poland*

<sup>5</sup>*Institut für Physik, Martin-Luther Universität Halle-Wittenberg, D-06120 Halle/Saale, Germany*

<sup>6</sup>*Max Planck Institute of Microstructure Physics, Weinberg 2, D-06120 Halle, Germany*

<sup>7</sup>*Institute for Theoretical Physics, Johannes Kepler University, Altenberger Straße 69, 4040 Linz, Austria*



(Received 13 November 2022; accepted 22 February 2023; published 7 March 2023)

Tools for controlling electrically the motion of magnetic skyrmions are important elements towards their use in spintronic devices. Here, we propose and demonstrate the transport of skyrmions via gigahertz and terahertz electric pulses. The method relies on using polarization-textured pulses such that the skyrmion experiences (via its inherent magnetoelectricity) the out-of-plane and in-plane components of the pulse electric field. It is shown how the electric field efficiently drags the skyrmion. The control of the skyrmion motion depends solely on the amplitude of electric fields, frequency, polarization, or phase in case two pulses are applied. Micromagnetic calculations supported by analytic modeling and analysis indicate the experimental feasibility of the control scheme.

DOI: [10.1103/PhysRevB.107.094404](https://doi.org/10.1103/PhysRevB.107.094404)

### I. INTRODUCTION

Magnetic skyrmions are topological textures formed in thin magnetic films with no inversion symmetry. Their unique physical features, such as nanoscale size, high stability, and high mobility, make them ideal for diverse applications in future spintronic devices [1–10]. The high mobility of skyrmions reduces the energy costs of skyrmion-based transfer of information and manipulation of skyrmion-based memory elements. Recent studies showed that skyrmion displacement can be effectively driven by electric or magnonic spin transfer torques [4,11–18], a magnetic field gradient [19–21], voltage [22], a microwave magnetic field [23,24], or a thermal gradient [21,25,26]. Recently, it has been reported that an electric field gradient can be used for manipulating skyrmions [27–29]. The inherent spin noncollinearity renders skyrmions magnetoelectric. Exploiting magnetoelectric coupling enables an optical tweezing of skyrmions and vortices [30–32], even though near intense focused fields are necessary.

In this paper we propose a protocol to move skyrmions with propagating electric field pulses. The fields are polarized such that they possess a component in the plane and a component orthogonal to the plane of the skyrmion. The speed and direction of the skyrmion motion are determined by the amplitudes, frequencies, and phases of the electric pulses. This mechanism is different from the skyrmion motion driven by the microwave magnetic field, where an asymmetric skyrmion distortion induced by an in-plane static magnetic field is necessary [24]. Our mechanism is operational when using harmonic pulses as well as for two broadband terahertz time-asymmetric pulses with perpendicular components. The

pulses are applied uniformly to the sample, and field focusing at the nanoscale is not necessary. Our results point to opportunities for the optical control of skyrmions.

### II. THEORETICAL MODEL

To study the skyrmion motion governed by an electric field, we consider a magnetic system with the free energy containing the exchange, Zeeman, and magnetoelectric (ME) interaction terms

$$F[\mathbf{m}] = \int [A_{\text{ex}}(\nabla\mathbf{m})^2 - \mu_0 M_s m_z H_z + E_{\text{me}}] d\mathbf{r}. \quad (1)$$

Here,  $\mathbf{M} = M_s \mathbf{m}$ ,  $M_s$  is the saturation magnetization,  $A_{\text{ex}}$  is the exchange constant, and  $H_z$  is the external magnetic field applied along the  $\mathbf{z}$  direction. The ME interaction allows a coupling to an electric field  $\mathbf{E}$  via the effective electric polarization  $\mathbf{P} = c_E[(\mathbf{m} \cdot \nabla)\mathbf{m} - \mathbf{m}(\nabla \cdot \mathbf{m})]$ , which is associated with the nonuniform magnetic distribution within the skyrmion. The ME coupling parameter  $c_E$  plays the role of an effective Dzyaloshinskii-Moriya (DM) constant  $D = c_E|\mathbf{E}|$  [33,34]. The skyrmion dynamics is governed by the Landau-Lifshitz-Gilbert (LLG) equation,

$$\frac{\partial \mathbf{m}}{\partial t} = -\gamma \mathbf{m} \times \mathbf{H}_{\text{eff}} + \alpha \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t}, \quad (2)$$

where  $\gamma$  is the gyromagnetic ratio and  $\alpha$  is the phenomenological Gilbert damping constant. The effective field  $\mathbf{H}_{\text{eff}} = -\frac{1}{\mu_0 M_s} \frac{\delta F}{\delta \mathbf{m}}$  consists of the exchange field, the applied external magnetic field, and the effective DM field. The total electric field  $\mathbf{E} = \mathbf{E}_s + \mathbf{E}(t)$  includes a perpendicular static electric field  $\mathbf{E}_s$  and a time-varying electric field  $\mathbf{E}(t)$ . Due to the

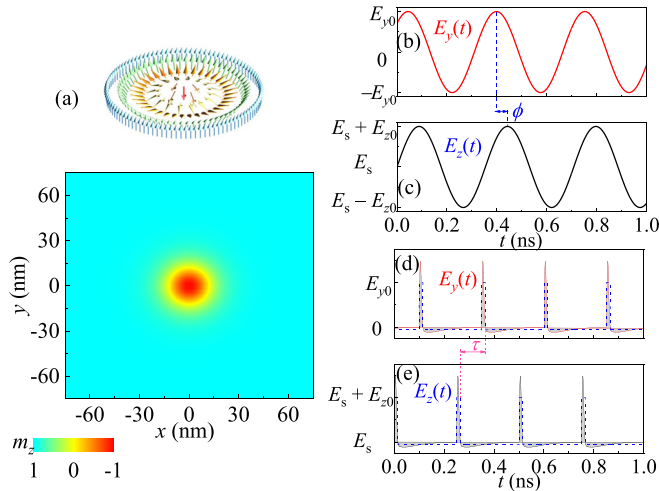


FIG. 1. (a) Magnetization configuration of skyrmion structure and its  $z$  component  $m_z$  profile. (b) and (c)  $E_y$  and  $E_z$  components of gigahertz microwave electric fields. (d) and (e) Two periodic time-asymmetric pulses  $E_y(t)$  and  $E_z(t)$ ; the red (d) and black (e) envelopes show the time profile of an experimentally feasible asymmetric pulse, and the blue dashed line describes the shape of the field adopted in numerical simulations.

ME term  $c_E$ ,  $\mathbf{E}_s = (0, 0, E_s)$  acting on the electric polarization  $\mathbf{P}$  changes the energy by  $-\mathbf{E}_s \cdot \mathbf{P}$ . This coupling can be viewed as an effective DM interaction with the constant  $D_0 = c_E E_s$ . The effective DM term stabilizes a skyrmion magnetic structure of Néel type [Fig. 1(a)]. The impact of the static field  $\mathbf{E}_s$  is similar to a breaking of inversion symmetry of the lattice structures such as B20 and ferromagnet/heavy metal bilayers [1,2,35,36]. The time-dependent field  $\mathbf{E}(t)$  is applied to the whole sample to trigger the skyrmion dynamics. Here, we consider two types of  $\mathbf{E}(t)$ : (i) a harmonic pulse  $\mathbf{E}(t) = E_{z0} \sin(2\pi ft)\mathbf{e}_z + E_{y0} \sin(2\pi ft + \phi)\mathbf{e}_y$  with a frequency  $f$  [Figs. 1(b) and 1(c)] and (ii) periodic time-asymmetric broadband terahertz pulses [i.e., half-cycle laser pulses; see Figs. 1(d) and 1(e)] with period  $T$  and delay time  $\tau$ . In the following analysis, the frequencies  $f$  and  $1/T$  are in the gigahertz range, and the length of the laser pulse head is 15 ps. Such terahertz pulses have been used to control the vortex dynamics even in metallic samples [37], but here we consider insulating samples.

In numerical calculations we assume the following parameters: the saturation magnetization  $M_s = 1.4 \times 10^5$  A/m, the exchange constant  $A_{\text{ex}} = 3 \times 10^{-12}$  J/m, the ME coupling strength  $c_E = 0.9$  pC/m, and the Gilbert damping constant  $\alpha = 0.01$ . The Néel skyrmion is stabilized by the constant electric field  $E_s = 2.5$  MV/cm and  $H_z = 1 \times 10^5$  A/m. The finite difference simulations based on Eq. (2) are done for a magnetic film with size  $600 \times 600 \times 10$  nm, and a  $3 \times 3 \times 10$  nm cell size is adopted. From the simulated profile  $\mathbf{m}(x, y)$ , we extract the topological charge density  $c(x, y) = (1/4\pi)\mathbf{m} \cdot (\partial_x \mathbf{m} \times \partial_y \mathbf{m})$ , and the total topological charge of a single skyrmion is  $Q = \int c dx dy = -1$ . In the following simulations, the single skyrmion starts to move under the effect of the time-varying electric field, and by defining the skyrmion

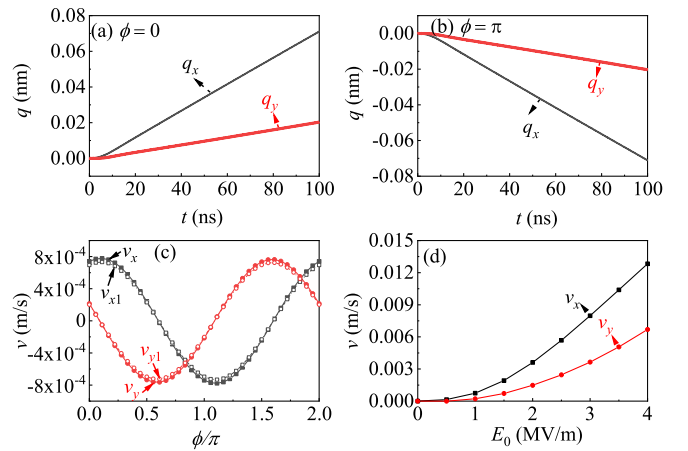


FIG. 2. (a) and (b) Center of the skyrmion  $(q_x, q_y)$  steered through the applied microwave electric fields [ $E_{z0} = E_{y0} = E_0 = 1$  MV/m,  $f = 2.825$  GHz, and  $\phi = 0$  (a) or  $\phi = \pi$  (b)]. (c) and (d) The velocity  $(v_x, v_y)$  as a function of the phase difference  $\phi$  (c) and amplitude  $E_0$  (d). The curves with solid symbols are obtained from micromagnetic simulations, while the curves with open symbols are estimated from Eq. (5).

position  $\mathbf{q} = (q_x, q_y)$  weighed by the topological charge  $\mathbf{q} = \int d^2\mathbf{r} (c\mathbf{r})/Q$ , we characterize the skyrmion motion by  $\mathbf{q}(t)$ .

### III. SKYRMION MOTION DRIVEN BY A MICROWAVE ELECTRIC FIELD

Considering the skyrmion motion driven by gigahertz electric fields with two  $y$  and  $z$  components, when only one component  $y$  (or  $z$ ) is applied, the motion of the skyrmion is not continuous. Figure 2 shows the displacement of a single skyrmion for  $E_{z0} = E_{y0} = E_0 = 1$  MV/m,  $f = 2.825$  GHz, and  $\phi = 0$ . As is evident, both  $x$  and  $y$  components of  $\mathbf{q} = (q_x, q_y)$  change in time, and the speed  $v_x = 7.4 \times 10^{-4}$  m/s along  $x$  is higher than  $v_y = 2.1 \times 10^{-4}$  m/s along  $y$ . The velocity of the skyrmion depends on the phase difference  $\phi$ . In Fig. 2(b), the directions of  $v_x$  and  $v_y$  are reversed by changing the phase to  $\phi = \pi$ . The relation between the skyrmion velocity  $\mathbf{v}$  and the phase difference  $\phi$  is shown in Fig. 2(c). Apparently, the magnitude of  $|\mathbf{v}| = \sqrt{v_x^2 + v_y^2}$  is a constant and does not depend on  $\phi$ . One component of the velocity approaches its maximum when the second component tends to zero. The velocities can be enhanced by increasing the field amplitude  $E_0$ . As follows from Fig. 2(d),  $|\mathbf{v}|$  increases quadratically with the microwave field amplitude, indicating a linear dependence on the combination of  $E_{y0} \times E_{z0}$ . We conclude that a gigahertz microwave electric field with a certain frequency moves the skyrmion effectively. The direction of the skyrmion motion can be controlled through the differences in the phase between  $y$  and  $z$  components, and the microwave field amplitude enhances the speed.

By steering the frequency  $f$  of microwave electric field  $\mathbf{E}(t)$  (Fig. 3), we find that the skyrmion speed  $|\mathbf{v}|$  is frequency dependent and several peaks appear on the  $|\mathbf{v}|$  versus  $f$  curve. These peaks originate from the excitation of internal modes of the skyrmion texture. To study the excitation mode of the skyrmion, we calculate the oscillation spectrum. Applying

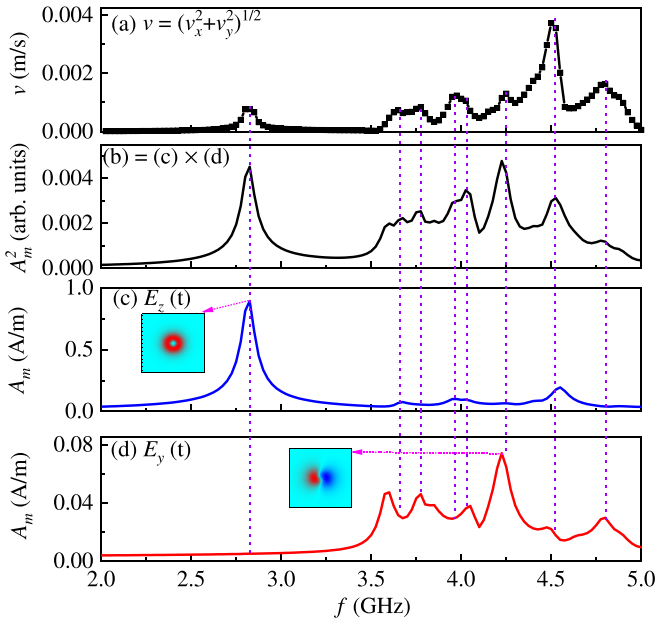


FIG. 3. (a) The skyrmion speed  $v = (v_x^2 + v_y^2)^{1/2}$  as a function of the electric field frequency  $f$ . (b)–(d) The frequency spectra obtained from the Fourier analysis of the magnetization component  $m_z$ . Oscillations are excited by applying a periodic electric field (c)  $E_z(t) = E_0 \sin(2\pi f_c t)$  and (d)  $E_y(t) = E_0 \sin(2\pi f_c t)$  with  $E_0 = 5$  MV/m and  $f_c = 20$  GHz. The curve in (b) is the product of the results shown in (c) and (d). The insets show the spatial distributions of the excited oscillation amplitudes.

a periodic pulse  $E_{z(y)}(t) = E_{z0(y0)} \sin(\omega_s t) / (\omega_s t)$  along the  $z$  (or  $y$ ) axis, we compute the Fourier transform of the magnetization oscillations, depicted in Figs. 3(c) and 3(d). The oscillation excited by  $E_z(t)$  [inset of Fig. 3(c)] is located in the skyrmion outer boundary and is synchronized in phase with the external field, i.e., the typical feature of a breathing mode [27,38–40]. The lowest-order breathing mode with 2.825 GHz frequency cannot propagate outside the skyrmion texture. At higher frequencies, 3.68 or 4.55 GHz, the propagating higher-order breathing modes are reflected from the geometric boundary and generate standing wave modes. As for the mode excited by  $E_y(t)$ , the oscillation in the boundary of a skyrmion is divided into two parts with opposite phases, corresponding to an asymmetric mode [inset of Fig. 3(d)]. Propagating asymmetric modes generate standing waves in the finite magnetic film, leading to higher-order peaks in the spectrum [27,38–40].

Several peaks in the velocity versus frequency curve can be found in the spectrum excited by  $E_z(t)$ , and other peaks correspond to the  $E_y(t)$  component. To clarify the connection between the skyrmion velocity and skyrmion modes, we multiplied the spectrum excited by  $E_z(t)$  and the spectrum excited by  $E_y(t)$  [see Fig. 3(b)] and achieved a better agreement between the spectrum and the  $|\mathbf{v}|(f)$  curve. From this feature we infer that combining two types of oscillation modes drives the skyrmion motion. For the analytic description of the skyrmion motion driven by the microwave electric field, we use a slowly varying magnetization vector  $\mathbf{m}_s$  corresponding to the moving skyrmion profile and a fast vector  $\mathbf{n}$  for the gigahertz

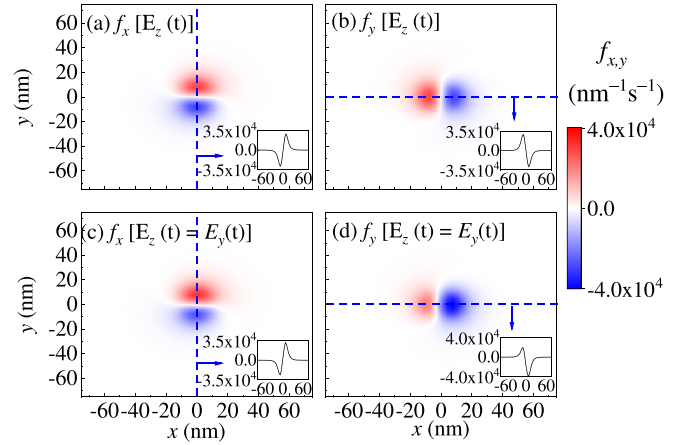


FIG. 4. Spatial profiles of the force density  $f_i = \gamma \mathbf{m}_s \cdot [\partial_i \mathbf{m}_s \times \langle \mathbf{m} \times \mathbf{H}_{\text{eff}} \rangle]$  for (a) and (b)  $E_z(t)$  without  $E_y(t)$  and (c) and (d)  $E_z(t) = E_y(t)$  (i.e.,  $\phi = 0$ ). Here, the microwave electric fields have the amplitude 1 MV/m and the frequency  $f = 2.825$  GHz. The insets show the force density  $f_{x,y}$  profiles along the blue dashed lines.

magnetization oscillation. Exploiting the ansatz  $\mathbf{m} = \mathbf{m}_s + \mathbf{n}$  for the total magnetization vector in the LLG equation (2) and following the procedure from Ref. [24], we deduce the Thiele's equation for the skyrmion motion,

$$\mathbf{G} \times \mathbf{v} + \hat{D}\mathbf{v} = \mathbf{F}, \quad (3)$$

where we used the following notations:  $\mathbf{v} = (v_x, v_y)$ ,  $\mathbf{G} = 4\pi Q \mathbf{e}_z$ , and the tensor  $\hat{D}_{ij} = \alpha \int (\partial_i \mathbf{m}_s \cdot \partial_j \mathbf{m}_s) dx dy = \delta_{ij} 4\pi \alpha$ , where  $i, j = x, y$ . We note that several terms such as  $\langle \mathbf{n} \times \hat{\mathbf{n}} \rangle$  and  $\langle \mathbf{n} \times \mathbf{m}_s \rangle$  do not contribute to the Thiele's equation because their time average over the fast oscillations vanishes. The driving force  $\mathbf{F}$  explicitly reads

$$F_i = \gamma \int \mathbf{m}_s \cdot [\partial_i \mathbf{m}_s \times \langle \mathbf{m} \times \mathbf{H}_{\text{eff}} \rangle] dx dy. \quad (4)$$

The skyrmion velocity is defined as follows:

$$v_{x1} = \frac{-\alpha F_x + F_y}{4\pi Q}, \quad v_{y1} = \frac{F_x + \alpha F_y}{4\pi Q}. \quad (5)$$

Extracting the force density from the simulation results, we draw their spatial profiles in Fig. 4. If one applies  $E_z(t)$  [without  $E_y(t)$ ], the force density is symmetric, and the total force is zero. Therefore the skyrmion does not move. Simultaneous application of the two components of the electric field,  $E_z(t)$  and  $E_y(t)$ , leads to asymmetric force distribution and a nonzero net force. Substituting the net force into Eq. (5), we obtain the velocity  $(v_{x1}, v_{y1})$  in a good agreement with the simulation results [Fig. 2(c)].

#### IV. SKYRMION MOTION DRIVEN BY BROADBAND TERAHERTZ PULSES

For our final results we apply a sequence of two time-asymmetric broadband terahertz pulses with period  $T$  and delay time  $\tau$  [Figs. 1(d) and 1(e)], where the length of the pulse head is 15 ps (i.e., around terahertz). The employed pulses are experimentally feasible [41]. The asymmetric

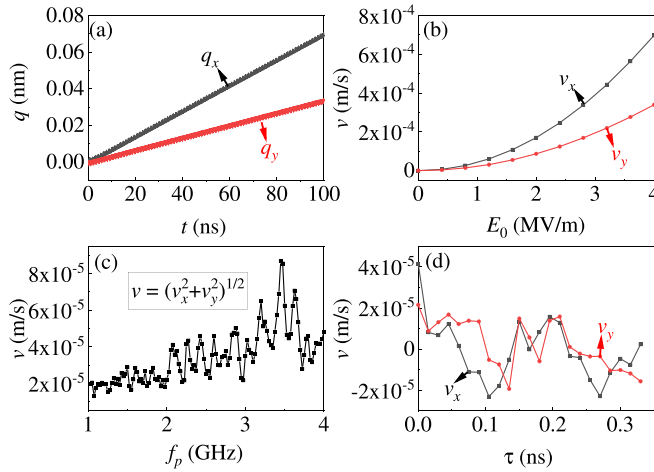


FIG. 5. (a) The dynamics of a skyrmion driven by two time-asymmetric pulses  $E_x(t)$  and  $E_y(t)$  with amplitude  $E_0 = 4$  MV/m,  $f_p = 1/T = 2.825$  GHz, and  $\tau = 0$ . (b)–(d) The velocity ( $v_x, v_y$ ) as a function of the pulse amplitude  $E_0$  (b),  $f_p = 1/T$  (c), and  $\tau$  (d).

pulses have a strong head with a short duration, and a much longer and weak part in the opposite direction [42,43]. Compared with the previous section and a single-frequency excitation problem, the periodic time-asymmetric pulse carries many frequencies (an integer multiple of the frequency  $f_p = 1/T$ ). Our simulations validated the fact that such a combination of two pulses  $E_x(t)$  and  $E_y(t)$  can govern the continuous motion of a skyrmion. As demonstrated in Fig. 5(a), for  $E_{z0} = E_{y0} = E_0 = 4$  MV/m,  $f_p = 1/T = 2.825$  GHz, and  $\tau = 0$ , the skyrmion velocities along the  $x$  and  $y$  axes are positive. The velocity increases with the pulse amplitude  $E_0$  quadratically [Fig. 5(b)]. This result is in agreement with the result obtained by means of the microwave excitation [Fig. 2(d)]. Changing the pulse period  $T$ , one changes the skyrmion speed, as shown in Fig. 5(c). Multiple peaks are observed in the  $v$  versus  $f_p$  curve, indicating resonance features. Furthermore, the direction and speed of skyrmion motion are affected by the delay time  $\tau$  between  $E_y(t)$  and  $E_z(t)$ ,

as demonstrated in Fig. 5(d). As distinct from Fig. 2(c) for microwave excitation, in the case of pulses, the dependence of ( $v_x, v_y$ ) on  $\tau$  is more sophisticated, as the skyrmion oscillations are excited by multiple frequencies.

## V. CONCLUSIONS

Controlling skyrmion dynamics and skyrmion transport is a challenging problem in skyrmionics. This is especially important from the point of view of possible applications of skyrmions in information storage and information processing. In this paper, we proposed protocols based on skyrmion driving with gigahertz microwave harmonic and terahertz broadband pulses. We proved that an applied microwave electric field with both out-of-plane and in-plane components drags the skyrmion persistently. In particular, the electric field's amplitude, frequency, and phase are critical parameters for controlling skyrmion motion. The effective torque that drives the skyrmion is traced back to two different types of oscillations in the skyrmion magnetic texture. The results obtained through micromagnetic simulations are supported by analytical considerations and are directly relevant for skyrmion-based spintronic devices.

## ACKNOWLEDGMENTS

The work is supported by the Shota Rustaveli National Science Foundation of Georgia (SRNSFG) (Grant No. FR-19-4049), the National Natural Science Foundation of China (Grants No. 12174452, No. 12074437, and No. 11704415), the Natural Science Foundation of Hunan Province of China (Grants No. 2022JJ20050 and No. 2021JJ30784), the Central South University Innovation-Driven Research Programme (Grant No. 2023CXQD036), the National Science Center in Poland by the Norwegian Financial Mechanism 2014–2021 under Polish-Norwegian Research Project NCN GRIEG (2Dtronics) Project No. 2019/34/H/ST3/00515 (J. Barnaś) and as Research Project No. DEC-2017/27/B/ST3/02881 (V.K.D.), and the DFG through SFB TRR227 and Project No. 465098690.

- [1] S. Mühlbauer, B. Binz, F. Jonietz, C. Pfleiderer, A. Rosch, A. Neubauer, R. Georgii, and P. Böni, *Science* **323**, 915 (2009).
- [2] X. Z. Yu, Y. Onose, N. Kanazawa, J. H. Park, J. H. Han, Y. Matsui, N. Nagaosa, and Y. Tokura, *Nature (London)* **465**, 901 (2010).
- [3] S. Luo and L. You, *APL Mater.* **9**, 050901 (2021).
- [4] R. Tomasello, E. Martinez, R. Zivieri, L. Torres, M. Carpentieri, and G. Finocchio, *Sci. Rep.* **4**, 6784 (2014).
- [5] J. Zázvorka, F. Jakobs, D. Heinze, N. Keil, S. Kromin, S. Jaiswal, K. Litzius, G. Jakob, P. Virnau, D. Pinna, K. Everschor-Sitte, L. Rózsa, A. Donges, U. Nowak, and M. Kläui, *Nat. Nanotechnol.* **14**, 658 (2019).
- [6] S. Zhang, A. A. Baker, S. Komineas, and T. Hesjedal, *Sci. Rep.* **5**, 15773 (2015).
- [7] A. Fert, V. Cros, and J. Sampaio, *Nat. Nanotechnol.* **8**, 152 (2013).
- [8] R. Wiesendanger, *Nat. Rev. Mater.* **1**, 16044 (2016).
- [9] X.-G. Wang, G.-H. Guo, A. Dyrdał, J. Barnaś, V. K. Dugaev, S. S. P. Parkin, A. Ernst, and L. Chotorlishvili, *Phys. Rev. Lett.* **129**, 126101 (2022).
- [10] X.-G. Wang, L. Chotorlishvili, G. Tatara, A. Dyrdał, G.-H. Guo, V. K. Dugaev, J. Barnaś, S. S. P. Parkin, and A. Ernst, *Phys. Rev. B* **106**, 104424 (2022).
- [11] J. Zang, M. Mostovoy, J. H. Han, and N. Nagaosa, *Phys. Rev. Lett.* **107**, 136804 (2011).
- [12] S.-Z. Lin, C. Reichhardt, C. D. Batista, and A. Saxena, *Phys. Rev. Lett.* **110**, 207202 (2013).
- [13] J. Iwasaki, M. Mochizuki, and N. Nagaosa, *Nat. Nanotechnol.* **8**, 742 (2013).
- [14] J. Iwasaki, A. J. Beekman, and N. Nagaosa, *Phys. Rev. B* **89**, 064412 (2014).
- [15] Y.-T. Oh, H. Lee, J.-H. Park, and J. H. Han, *Phys. Rev. B* **91**, 104435 (2015).

- [16] X. Zhang, Y. Zhou, and M. Ezawa, *Nat. Commun.* **7**, 10293 (2016).
- [17] B. Göbel, A. F. Schäffer, J. Berakdar, I. Mertig, and S. S. P. Parkin, *Sci. Rep.* **9**, 12119 (2019).
- [18] C. Psaroudaki and D. Loss, *Phys. Rev. Lett.* **120**, 237203 (2018).
- [19] C. Wang, D. Xiao, X. Chen, Y. Zhou, and Y. Liu, *New J. Phys.* **19**, 083008 (2017).
- [20] S. L. Zhang, W. W. Wang, D. M. Burn, H. Peng, H. Berger, A. Bauer, C. Pfleiderer, G. van der Laan, and T. Hesjedal, *Nat. Commun.* **9**, 2115 (2018).
- [21] K. Everschor, M. Garst, B. Binz, F. Jonietz, S. Mühlbauer, C. Pfleiderer, and A. Rosch, *Phys. Rev. B* **86**, 054432 (2012).
- [22] Y. Liu, N. Lei, C. Wang, X. Zhang, W. Kang, D. Zhu, Y. Zhou, X. Liu, Y. Zhang, and W. Zhao, *Phys. Rev. Appl.* **11**, 014004 (2019).
- [23] K.-W. Moon, D.-H. Kim, S.-G. Je, B. S. Chun, W. Kim, Z. Q. Qiu, S.-B. Choe, and C. Hwang, *Sci. Rep.* **6**, 20360 (2016).
- [24] W. Wang, M. Beg, B. Zhang, W. Kuch, and H. Fangohr, *Phys. Rev. B* **92**, 020403(R) (2015).
- [25] S.-Z. Lin, C. D. Batista, C. Reichhardt, and A. Saxena, *Phys. Rev. Lett.* **112**, 187203 (2014).
- [26] L. Kong and J. Zang, *Phys. Rev. Lett.* **111**, 067203 (2013).
- [27] Y.-H. Liu, Y.-Q. Li, and J. H. Han, *Phys. Rev. B* **87**, 100402(R) (2013).
- [28] P. Upadhyaya, G. Yu, P. K. Amiri, and K. L. Wang, *Phys. Rev. B* **92**, 134411 (2015).
- [29] X.-G. Wang, L. Chotorlishvili, G.-H. Guo, C.-L. Jia, and J. Berakdar, *Phys. Rev. B* **99**, 064426 (2019).
- [30] X.-G. Wang, L. Chotorlishvili, V. K. Dugaev, A. Ernst, I. V. Maznichenko, N. Arnold, C. Jia, J. Berakdar, I. Mertig, and J. Barnaś, *npj Comput. Mater.* **6**, 140 (2020).
- [31] X.-G. Wang, L. Chotorlishvili, N. Arnold, V. K. Dugaev, I. Maznichenko, J. Barnaś, P. A. Buczek, S. S. P. Parkin, and A. Ernst, *Phys. Rev. Lett.* **125**, 227201 (2020).
- [32] D. Yu, C. Sui, D. Schulz, J. Berakdar, and C. Jia, *Phys. Rev. Appl.* **16**, 034032 (2021).
- [33] T. Liu and G. Vignale, *Phys. Rev. Lett.* **106**, 247203 (2011).
- [34] H. Katsura, N. Nagaosa, and A. V. Balatsky, *Phys. Rev. Lett.* **95**, 057205 (2005).
- [35] B. Balasubramanian, P. Manchanda, R. Pahari, Z. Chen, W. Zhang, S. R. Valloppilly, X. Li, A. Sarella, L. Yue, A. Ullah, P. Dev, D. A. Muller, R. Skomski, G. C. Hadjipanayis, and D. J. Sellmyer, *Phys. Rev. Lett.* **124**, 057201 (2020).
- [36] A. Soumyanarayanan, M. Raju, A. L. Gonzalez Oyarce, A. K. C. Tan, M.-Y. Im, A. P. Petrović, P. Ho, K. H. Khoo, M. Tran, C. K. Gan, F. Ernult, and C. Panagopoulos, *Nat. Mater.* **16**, 898 (2017).
- [37] D. Yu, J. Kang, J. Berakdar, and C. Jia, *NPG Asia Mater.* **12**, 36 (2020).
- [38] M. Mochizuki, *Phys. Rev. Lett.* **108**, 017601 (2012).
- [39] V. P. Kravchuk, D. D. Sheka, U. K. Röbber, J. van den Brink, and Y. Gaididei, *Phys. Rev. B* **97**, 064403 (2018).
- [40] B. F. Miao, Y. Wen, M. Yan, L. Sun, R. X. Cao, D. Wu, B. You, Z. S. Jiang, and H. F. Ding, *Appl. Phys. Lett.* **107**, 222402 (2015).
- [41] M. T. Hassan, T. T. Luu, A. Moulet, O. Raskazovskaya, P. Zhokhov, M. Garg, N. Karpowicz, A. M. Zheltikov, V. Pervak, F. Krausz, and E. Goulielmakis, *Nature (London)* **530**, 66 (2016).
- [42] A. S. Moskalenko, Z.-G. Zhu, and J. Berakdar, *Phys. Rep.* **672**, 1 (2017).
- [43] A. Matos-Abiague and J. Berakdar, *Phys. Rev. Lett.* **94**, 166801 (2005).