Letter

Maximizing intrinsic anomalous Hall effect by controlling the Fermi level in simple Weyl semimetal films

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(Received 3 January 2022; revised 15 March 2022; accepted 25 April 2022; published 2 May 2022)

A large intrinsic anomalous Hall effect (AHE) originating in the Berry curvature has attracted growing attention for potential applications. The recently proposed magnetic Weyl semimetal EuCd₂Sb₂ provides an excellent platform for controlling the intrinsic AHE because it only hosts a Weyl-point-related band structure near the Fermi energy. Here, we report the fabrication of EuCd₂Sb₂ single-crystalline films and control of their anomalous Hall effect by a film technique. As also analyzed by first-principles calculations of energy-dependent intrinsic anomalous Hall conductivity, the obtained anomalous Hall effect shows a sharp peak as a function of carrier density, demonstrating a clear energy dependence of the intrinsic AHE.

DOI: 10.1103/PhysRevB.105.L201101

Topological semimetals, characterized by a massless Dirac band dispersion in the low-energy excitation, exhibit unique magnetotransport due to their nontrivial band topology in the momentum space [1–4]. Recently reported magnetic topological semimetals further enrich the understanding of magnetotransport, where entanglement between magnetism and nontrivial topology can lead to exotic magnetotransport such as a large anomalous Hall effect (AHE) [5–7]. Integration of the Berry curvature for all occupied states gives rise to a large intrinsic contribution to anomalous Hall conductivity. Namely, anomalous Hall conductivity is closely related to the electron occupation determined by the position of the Fermi level [7,8].

Paired Weyl points (WPs) in magnetic Weyl semimetals can be viewed as monopoles with opposite chirality corresponding to the sources (W+) and sinks (W-) of the Berry curvature [Fig. 1(a)]. Due to the Berry flux of paired WPs, anomalous Hall conductivity $\sigma_{\rm xy,AHE}$ is expected to exhibit a large peak at the energy position of the WPs ($E_{\rm W}$) [9,10] and be strongly dependent on the Fermi level. Specifically, $\sigma_{\rm xy,AHE}$ can be maximized if the Fermi level can be adjusted to $E_{\rm W}$ [11,12]. However, such an energy dependence of $\sigma_{\rm xy,AHE}$ has not been demonstrated yet due to high carrier densities ($\sim 10^{20} - 10^{22}$ cm⁻³) and complicated band structures of conventional magnetic Weyl semimetals, while the modulation of $\sigma_{\rm xy,AHE}$ has been attempted by chemical doping and pressure application for $\rm Co_3Sn_2S_2$ [13–16], $\rm Mn_3Sn$ [17–20], and $\rm Mn_3Ge$ [21].

In this context, EuCd₂As₂ and isostructural EuCd₂Sb₂, where one of three Cd atoms is substituted with Eu in the parent Dirac semimetal Cd₃As₂, provide an ideal platform for experimentally demonstrating the peculiar energy dependence of intrinsic anomalous Hall conductivity. This is because they have a simple band structure near the Fermi energy (E_F) and much lower carrier densities ($\sim 10^{18} - 10^{19}$ cm⁻³) [22,23]. On the other hand, difficulties in the growth of thin films have prevented the study of carrier density dependence with taking these advantages.

EuCd₂Sb₂ has a trigonal crystal structure with space group $P\bar{3}m1$ [23–26]. It consists of an alternate stacking of triangular Eu layers and Cd₂Sb₂ layers [Fig. 1(b)]. Eu atoms contribute to magnetism in this compound, forming an A-type antiferromagnetic structure below the Néel temperature $T_N = 7.4$ K with Eu²⁺ magnetic moments lying in the ab plane [25,26]. As shown in Fig. 1(c), four pairs of WPs (W₁–W₄) near E_F along the k_z direction are protected by C_{3z} symmetry when the magnetic Eu moments are ferromagnetically polarized along the c axis under the out-of-plane magnetic field [23]. There are no other bands near E_F and all the hole carriers occupy the WP-related valence bands. Therefore, it is expected that the Fermi level dependence of intrinsic anomalous Hall conductivity can be demonstrated by modulating the hole carrier densities in EuCd₂Sb₂ with film techniques.

Here, we report the fabrication of single-crystalline EuCd₂Sb₂ films by molecular beam epitaxy and an investigation of their anomalous Hall effect using film techniques. By adjusting the Fermi level with controlling Sb flux conditions and also performing electrostatic gating experiments, we find that their anomalous Hall effect is largely enhanced compared to bulks and strongly dependent on the carrier density

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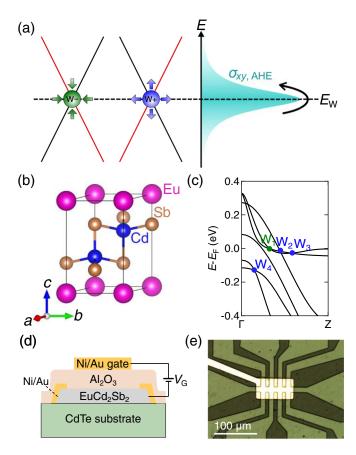


FIG. 1. (a) Energy dispersion of paired Weyl points (WPs) and energy-dependent anomalous Hall conductivity $\sigma_{xy,AHE}$. Weyl points W+/W- are the source/sink of the Berry curvature. (b) Crystal structure of EuCd₂Sb₂ [24] drawn using VESTA [27]. (c) Energy dispersion calculated for EuCd₂Sb₂ films, showing four pairs of WPs near the Fermi energy. They emerge along the Γ -Z direction in the Brillouin zone when magnetic moments are forcedly aligned along the c axis. Blue/green circles represent WPs (W₁–W₄) with plus/minus chirality. (d) Cross-sectional schematic illustration and (e) top-view photograph of the electrostatic gate device fabricated from a EuCd₂Sb₂ film, where holes are depleted (accumulated) when V_G is positively (negatively) biased.

with a sharp peak, as also demonstrated by first-principles calculations.

EuCd₂Sb₂ films were grown in an Epiquest RC1100 chamber [28–31] on single-crystalline (111)A CdTe substrates. The in-plane lattice mismatch between EuCd₂Sb₂ and CdTe is 2.4% as shown in Fig. 2(b). CdTe substrates were etched with 0.01% Br₂-methanol before loading them into the chamber and then heated to 750 °C with Cd flux supplied to obtain an atomically smooth surface [28]. After annealing the substrate, it was cooled to the growth temperature of 360 °C. The beam equivalent pressures were measured by an ionization gauge, and were set to 1.2×10^{-5} Pa for Eu, 5.0×10^{-4} Pa for Cd, and 8.5×10^{-6} Pa for Sb during the codeposition, which is the same growth condition as EuCdSb₂ films on Al₂O₃ (0001) substrates [30]. This Cd-rich growth condition offers advantages in reducing carrier densities in EuCd₂Sb₂ films, because Cd deficiency is a major origin of the hole carriers. The films were then annealed in situ at 500 °C for 5 min under

exposure of Cd flux. The film thickness was set at 50 nm, and the growth rate was about 0.07~Å/s.

The films were patterned to Hall bars with a channel width of 10 μ m through conventional photolithography, Ar ion milling, and chemical wet etching processes: 10-nm-thick Ni and 50-nm-thick Au electrodes were deposited for ohmic contact by electron beam evaporation, and then 30-nm-thick Al₂O₃ was deposited as the gate dielectric by atomic layer deposition, as shown in Figs. 1(d) and 1(e). Low-temperature magnetotransport was measured using a Quantum Design physical property measurement system cryostat equipped with a 9-T superconducting magnet. Hall measurements were performed using a lock-in technique. The excitation current was kept constant at 0.5 mA with a frequency of 13 Hz. For gating experiments, dc bias ($V_{\rm G}=-8$ to +8 V) voltage was applied to the gate electrode.

First-principles calculations of the band structure with spin-orbit coupling were performed using the VASP package [32–34] for experimentally determined film lattice parameters. The generalized gradient approximation of Perdew-Burke-Ernzerhof was adopted for the exchange-correlation functional [35]. The correlation effect was considered by a Hubbard U correction of U = 4.5 eV for the Eu-f orbitals [36], which was determined by comparing the band structures revealed by angle-resolved photoemission spectroscopy and first-principles calculations [23]. A $16 \times 16 \times 10$ k-point mesh with the Monkhorst-Pack scheme [37] was used for the Brillouin zone sampling of the primitive cell and Gaussian smearing with a width of 0.02 eV was applied. From the Bloch states obtained in the density functional theory (DFT) calculation, a Wannier basis set is constructed by using the WANNIER90 code [38]. The basis consists of s, f-character orbitals localized at the Eu site, s, d-character orbitals at the Cd, and s, p-character orbitals at the Sb. The intrinsic anomalous Hall conductivity is computed using a k-point mesh of $300 \times 300 \times 300$ [39].

Figure 2 shows the structural characterization of the $EuCd_2Sb_2$ film. As shown in the x-ray diffraction (XRD) θ - 2θ scan in Fig. 2(a), reflections from the (001) $EuCd_2Sb_2$ lattice planes are observed without any impurity phases. Its out-of-plane lattice constant along the c axis is calculated to be 7.73 Å. Figure 2(c) shows a cross-section image of the $EuCd_2Sb_2$, taken by high-angle annular dark-field scanning transmission electron microscopy. The periodic atomic arrangement corresponding to the $EuCd_2Sb_2$ crystal structure in Fig. 2(d) is clearly confirmed. Elemental maps are also taken by energy dispersive x-ray spectrometry, as shown in Figs. 2(e)–2(g). The alternate stacking of Eulope Supersive Supersive

Figure 3 summarizes the fundamental magnetotransport of the EuCd₂Sb₂ film. As shown in Fig. 3(a), the longitudinal resistivity ρ_{xx} exhibits a metallic behavior in the whole temperature regime. Below 50 K, ρ_{xx} gradually increases upon cooling until it shows a clear kink at 7.4 K. Then it exhibits a sudden drop upon further cooling. This kink observed at 7.4 K corresponds to the Néel temperature T_N [23,25,26]. The kink disappears at the out-of-plane magnetic field B=9 T, where the Eu²⁺ magnetic moments are completely aligned

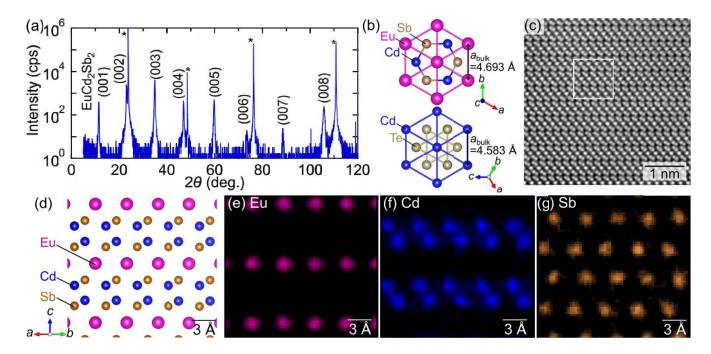


FIG. 2. (a) XRD θ -2 θ scan of a EuCd₂Sb₂ film grown on a CdTe substrate. Substrate peaks are marked with an asterisk. (b) Crystal structures of the EuCd₂Sb₂ film and CdTe substrate, viewed along the out-of-plane direction. (c) Cross-sectional image of the EuCd₂Sb₂ film, taken by high-angle annular dark-field scanning transmission electron microscopy. (d) Atomic arrangement of EuCd₂Sb₂ viewed along the [110] direction. Energy dispersive x-ray spectrometry maps taken for (e) Eu L, (f) Cd L, and (g) Sb L edges in the boxed region in (c).

along the c axis [23,26]. This low-temperature behavior can be understood considering the scattering of conduction electrons by the localized Eu^{2+} spins. Figure 3(b) presents the magnetoresistance (MR) taken by sweeping the out-of-plane magnetic field at various temperatures. At T=2.0 K, a peak ends at the saturation field of $B_{\rm sat}=3.4$ T, and which shifts to lower fields upon increasing temperature and then disappears above $T_{\rm N}$. This peak below $B_{\rm sat}$ is ascribed to an increase of magnetic scattering in the canted spin structure. At high fields above $B_{\rm sat}$, the Eu^{2+} spins are fully polarized along the c axis, resulting in reduced magnetic scattering. At higher temperatures above $T_{\rm N}$, the peak becomes smaller and shifts to higher magnetic fields. Finally, the peak disappears and conventional positive MR appears.

Figure 3(c) shows the Hall resistivity ρ_{vx} measured at various temperatures. At temperatures above 50 K, Hall resistivity depends almost linearly on the magnetic field. In contrast, it deviates from the linear behavior upon cooling below 50 K. Here, ρ_{yx} is expressed as $\rho_{yx} = R_H B + \rho_{yx,AHE}$ with the ordinary Hall coefficient $R_{\rm H}$ and the anomalous Hall resistivity $\rho_{\rm vx,AHE}$. The deviation from the linear behavior disappears above B_{sat} , showing a clear contribution of the anomalous Hall term (see Supplemental Material [40]). By subtracting the ordinary term with a linear fit, the anomalous term is obtained as shown in Fig. 3(d). $\rho_{yx,AHE}$ taken at T = 2.0 Kexhibits a kink at $B_{\text{sat}} = 3.4 \text{ T}$. With increasing temperature, B_{sat} shifts to lower fields below T_{N} and then disappears above $T_{\rm N}$, as confirmed in MR. In addition, a broad but pronounced peak appears around B_{sat} below T_{N} , showing a deviation from the magnetization behavior. While this peak suggests the existence of the so-called topological Hall term, it is unlikely that this is caused by the real-space spin Berry phase on the noncoplanar spin configuration during a simple spin polarization process. Rather, this may be understood by intrinsic AHE corresponding to the band-structure changes during the polarization process, as also reported for other Eu compounds [41–44].

Here, we define the saturation value of $\rho_{yx,AHE}$ at 9 T as $\rho_{yx,AHE}^{sat}$. It is expected that $\rho_{yx,AHE}$ is dominated by intrinsic AHE in the forced ferromagnetic phase. In addition, σ_{xx} and $\sigma_{xy,AHE}$ are calculated by

$$\sigma_{xx} = \frac{\rho_{xx}(B = 0 \text{ T})}{\left(\rho_{yx \text{ AHE}}^{\text{sat}}\right)^2 + \rho_{xx}(B = 0 \text{ T})^2},$$
 (1)

and

$$\sigma_{\text{xy,AHE}} = \frac{\rho_{\text{yx,AHE}}^{\text{sat}}}{\left(\rho_{\text{yx,AHE}}^{\text{sat}}\right)^2 + \rho_{\text{xx}}(B = 0 \text{ T})^2}.$$
 (2)

AHE has been roughly categorized into three regimes based on the range of σ_{xx} [6,45]. For EuCd₂Sb₂ films in this study, σ_{xx} is below $1\times 10^4~\Omega^{-1}~\rm cm^{-1}$, and the carrier density is located between $0.3\times 10^{19}~\rm and~4.8\times 10^{19}~\rm cm^{-3}$. This suggests that the anomalous Hall velocity induced by the Berry curvature is suppressed by following the scaling relation $\sigma_{xy,AHE} \propto \sigma_{xx}^{1.6}$. With reducing the hole carrier density of EuCd₂Sb₂ films at 2.0 K, $\rho_{yx,AHE}$ increases at first, decreases, and then increases again as shown in Fig. 3(e). As confirmed in Fig. 3(f), modulating carriers with electrostatic gating also follow this trend

In order to discuss the carrier density dependence of AHE in the dirty metal regime [6,45], we show the carrier density dependence of $\sigma_{xy,AHE}/\sigma_{xx}^{1.6}$ obtained by measuring

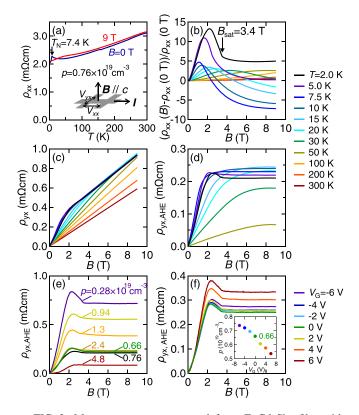


FIG. 3. Magnetotransport measured for a EuCd₂Sb₂ film with a carrier density $p=0.8\times 10^{19}~\rm cm^{-3}$. (a) Temperature dependence of longitudinal resistivity ρ_{xx} , with a clear kink at the Néel temperature $T_{\rm N}=7.4~\rm K$. The inset shows the measurement configuration. (b) Magnetoresistance $[\rho_{xx}(B)-\rho_{xx}(0~\rm T)]/\rho_{xx}(0~\rm T)$ taken with sweeping the out-of-plane magnetic field at various temperatures. The saturation field is estimated $B_{\rm sat}=3.4~\rm T$ at $T=2.0~\rm K$. (c) Hall resistivity ρ_{yx} taken at various temperatures. (d) Anomalous Hall resistivity $\rho_{yx,AHE}$, obtained by subtracting the ordinary term at various temperatures. Anomalous Hall resistivity $\rho_{yx,AHE}$ of EuCd₂Sb₂ films with (e) different carrier densities and (f) electrostatic gating at 2.0 K.

EuCd₂Sb₂ films at 2.0 K, as shown in Fig. 4(a). Remarkably, $\sigma_{xy,AHE}/\sigma_{xx}^{1.6}$ exhibits a large peak at about $p=1\times 10^{19}$ cm⁻³ and the same trend is confirmed by continuously modulating the carrier density with electrostatic gating. We also confirm that a similar large peak is observed in the plots of $\sigma_{xy,AHE}$ and $\sigma_{xy,AHE}/\sigma_{xx}$ (see Supplemental Material [40]). $\sigma_{xy,AHE}/\sigma_{xx}^{1.6}$ values previously reported for bulk single crystals [23] also follow the same trend as revealed by the set of film measurements. Therefore, the observed peak is ascribed to a successful adjustment of the Fermi level to $E_{\rm W}$.

In order to understand the enhancement of $\sigma_{xy,AHE}/\sigma_{xx}^{1.6}$ more quantitatively, we perform first-principles calculations of the band structure and intrinsic $\sigma_{xy,AHE}$. As shown in Fig. 4(c), $\sigma_{xy,AHE}$ exhibits a sharp peak at about $E-E_F=-0.02$ eV, which corresponds to the energy position of W₂ and W₃ in Fig. 4(b). The energy can be converted to the carrier density by integrating the density of states from $E-E_F=0$ eV. As confirmed in Fig. 4(d), $\sigma_{xy,AHE}$ exhibits a clear carrier

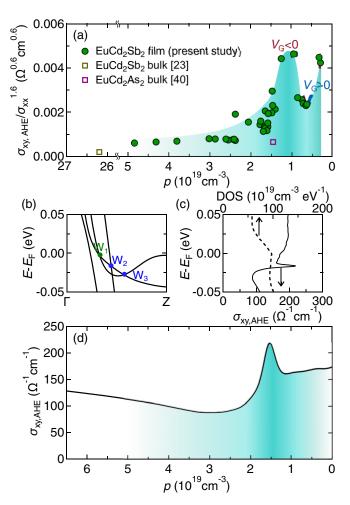


FIG. 4. (a) Carrier density dependence of $\sigma_{xy,AHE}/\sigma_{xx}^{1.6}$ in EuCd₂Sb₂ films, compared to bulks of EuCd₂Sb₂ [23] and EuCd₂As₂ [41]. Electrostatic gating data obtained for low carrier samples ($p < 1 \times 10^{19} \text{ cm}^{-3}$) are also plotted with curves, colored by the sign of V_G . (b) Magnified energy dispersion. (c) $\sigma_{xy,AHE}$ and density of states (DOS) calculated as a function of energy. (d) $\sigma_{xy,AHE}$ plotted for carrier density converted from DOS.

density dependence consistent with the experimental data, demonstrating that the Fermi level of EuCd₂Sb₂ films passes through the energy position of W₂ and W₃.

In summary, we have systematically investigated the carrier density dependence of the intrinsic anomalous Hall conductivity by adjusting the Fermi level in simple magnetic Weyl semimetal EuCd₂Sb₂ films. The peak observed for $\sigma_{xy,AHE}/\sigma_{xx}^{1.6}$ has been also reproduced by first-principles calculations of energy-dependent intrinsic anomalous Hall conductivity. Our findings have provided transport evidence of intrinsic anomalous Hall conductivity originating in WPs. The present work paves the way for further exploring the potential of WP-based exotic magnetotransport using film techniques.

This work was supported by JST PRESTO Grant No. JPMJPR18L2 and JST CREST Grant No. JPMJCR16F1, Japan and by Grant-in-Aid for Scientific Research (B) No. JP21H01804 from MEXT, Japan, and by TEPCO Memorial Foundation, Japan.

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