

Spin-orbit coupling induced ultrahigh-harmonic generation from magnetic dynamicsOusmane Ly^{1,*} and Aurelien Manchon^{1,2}¹*Physical Science and Engineering Division (PSE), King Abdullah University of Science and Technology (KAUST), Thuwal 23955-6900, Saudi Arabia*²*Aix-Marseille Université, CNRS, CINaM, Marseille, France*

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The generation of a nonlinear high-frequency response in solids from powerful optical pumps has gained momentum over the past decade. High-harmonic generation (HHG) in solids can be obtained from strong-field laser excitation, usually restricted to optical frequencies and limited both in amplitude and in harmonic order. Here, we demonstrate that high-harmonic emission can be achieved by exploiting conventional spin pumping, without the need for optical excitation. Considering a noncentrosymmetric (ferro- or antiferro-)magnet excited at a frequency ω , we demonstrate the emergence of HHG in two main regimes: (i) In the perturbative regime, where a weak spin-orbit interaction is considered, the carrier pumping features a number of harmonics with a cutoff order $n_{\max} < 10$. (ii) When the spin-orbit coupling strength is close to, or higher than, the s - d exchange energy, a strongly nonlinear regime resulting from resonantlike spin-flip scattering occurs leading to the emission of a large number of harmonics. This is in sharp contrast to conventional pumping, where the corresponding time-dependent currents simply oscillate with the frequency of the magnetic drive ω . Our proposal enables the enhancement of both spin and charge dynamics by orders of magnitude. This effect could be used to trigger high-frequency emission deep in the terahertz regime.

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Introduction. The recent boost in data transfer rates puts a daring strain on information technology. Sustaining such a growth rate requires the development of sources, detectors, and systems working in the so-called terahertz (THz) gap covering the frequency window from 0.1 to 10 THz (1 THz = 10^{12} Hz). This gap represents a challenge for conventional electronic devices due to carrier transit delays (~ 1 –10 ps), as well as for photonic devices due to thermal fluctuations (300 K \sim 6 THz). Nonetheless, designing efficient, room-temperature THz sources would constitute a key enabler to applications spanning from high-resolution imaging to extreme wideband wireless communication. The grand challenge posed by the THz gap is that it is located on the high end of electronic processes and on the low end of optical excitations. It is therefore difficult to emit a THz electromagnetic field using purely electronic mechanisms because the scattering time of the electronic carriers is typically in the THz range. A successful strategy exploited in quantum cascade lasers is to use semiconductor superlattices with small gaps in order to generate the required frequency [1]. Since the efficiency is low, one needs to multiply the number of gaps (hence the quantum cascade) and work at low temperature to quench thermal fluctuations. Another strategy is to exploit

optical rectification of a femtosecond laser pulse in semiconductors such as ZnTe [2]. An alternative approach uses an optically generated ultrafast spin current, i.e., a charge-neutral current carrying spin angular momentum [3]. In this geometry, a femtosecond laser pulse impinges on the surface of a thin ferromagnetic film and excites a superdiffusive spin current [4]. This spin current then penetrates into an adjacent layer possessing large spin-orbit coupling and is subsequently converted into a charge current via either the spin Hall effect [5] or the Rashba-Edelstein effect [6], depending on the considered heterostructure. This apparatus enables the conversion of a femtosecond laser pulse into a THz electromagnetic field [3,7,8]. Although promising, this solution relies on optical pumping and therefore lacks scalability.

In this Research Letter, we demonstrate that extremely efficient and ultrafast THz emission can be obtained by exploiting the internal dynamics in the presence of spin-orbit coupling to generate high harmonics in a device solely powered by conventional magnetic resonance. The driving force is given by adiabatic spin pumping [9,10], a widely used technique to generate pure spin currents out of ferromagnetic resonance, while the high-harmonic generation itself relies on the spin scattering events induced by spin-orbit coupling in the presence of a precessing magnetic order. Particularly, in the low-spin-orbit-interaction limit, we demonstrate that the carrier dynamics feature a low-harmonic emission with a cutoff order $n_{\max} < 10$. Our results apply to various spin-orbit coupling geometries including Rashba, Dresselhaus, and bulk spin-orbit interaction systems where the coupling to the magnetic precession is of either extrinsic or intrinsic nature.

Spin pumping [9] is an adiabatic process by which a precessing magnetic order $\mathbf{m}(t)$ (ferromagnetic or antiferromagnetic alike) injects a spin current into an adjacent metallic

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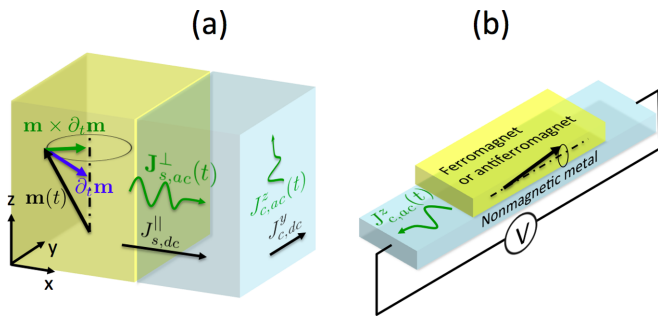


FIG. 1. Illustration of the spin pumping setup. (a) Schematics of the dc and ac spin pumping: A magnetic order precessing around its rest direction \mathbf{z} induces a spin current composed of a dc component, $\mathcal{J}_{s,dc}^{\parallel}$ (black), and an ac (green) component, $\mathcal{J}_{s,ac}^{\perp}$, whose spin polarization is aligned on $\mathbf{m} \times \partial_t \mathbf{m}$. We neglect the contribution from the imaginary part of the spin mixing conductance ($\sim \partial_t \mathbf{m}$). Via spin-orbit coupling, these spin currents are converted into a dc and an ac charge current flowing along y and z , respectively. (b) Corresponding simulation setup: The pumped charge current is collected along the direction about which the magnetic order precesses.

layer. This spin current possesses two components, a rectified one whose spin polarization is aligned along the precession axis, $\mathcal{J}_s \sim \langle \mathbf{m} \rangle$, and an oscillating contribution whose spin polarization is aligned perpendicular to the precession axis, $\mathcal{J}_s \sim \mathbf{m} \times \partial_t \mathbf{m}$. In a conventional spin pumping experiment, once injected into the normal metal, this spin current is converted into a charge current via spin-orbit coupling [10–12], which leads to dc and ac components [depicted in Fig. 1(a)]. This spin-to-charge conversion does not affect the spin dynamics itself as long as the spin-orbit coupling is negligible compared with the s - d exchange, and thereby only generates a harmonic charge current.

In the presence of spin-orbit coupling though, successive spin-flip events occur within one magnetic precession cycle, leading to the appearance of higher frequencies in the charge current signal (see Fig. 2). Subsequently, a phase corresponding to the dynamic frequency is accumulated as a

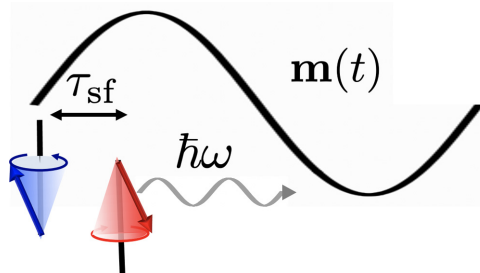


FIG. 2. Spin-flip-scattering-driven high-harmonic generation: In the presence of a precessing magnetic order (black curve) the spin-orbit interaction leads to spin-flip scattering. Subsequently, a phase corresponding to the fundamental frequency is accumulated in the electronic wave function. Under adiabatic magnetization dynamics, the spin-flip time τ_{sf} becomes very small compared with the period of the precessing magnetic order, and higher harmonics appear as a consequence of subsequent spin-flip scattering events during one fundamental cycle.

consequence of angular momentum conservation. When the spin-orbit coupling energy becomes comparable to the s - d exchange parameter, the full harmonic spectrum is excited with extremely strong amplitudes. This is in close analogy with the high-harmonic generation mechanism from gaseous media under laser excitation [13–15], where the electron wave packets undergo harmonic emission as they recollide with their parent atoms after a fraction of the laser oscillation cycle. When the magnetization dynamics operates at small frequencies, the emission of a huge number of harmonics is predicted [16].

Interestingly, our numerical simulations suggest the existence of a resonance condition associated with maximally excited high harmonics. This corresponds to the region of the parameter space where the s - d exchange energy is very close to the spin-orbit splitting. To provide an intuitive explanation of the reason behind the emergence of the strong nonlinearities underlying this regime, we find it convenient to borrow the Floquet theory language. In fact, upon applying the ac perturbation, sidebands develop in both Rashba and magnetic band structures. Therefore it is natural that the maximum excitation of the corresponding high harmonics occurs when both sidebands' spectra match. While the effect is not restricted to a particular type of spin-orbit interaction, the Rashba-like spin-orbit coupling constitutes a central paradigm to demonstrate the proposed effect. In fact, Rashba spin-orbit interaction has been found in a broad range of magnetic interfaces, from transition metal interfaces [10] to the surface of topological insulators [17] or in oxide heterostructures [18], and has the major advantage of being electrically tunable [19], offering a powerful means to control the high-harmonic generation.

Numerical simulations. To demonstrate the high-harmonic generation, we consider the setup depicted in Fig. 1(b). The numerical calculations are performed using the time-dependent quantum transport package T-KWANT [20–22], where the stationary scattering properties are obtained from the dc transport package KWANT [23]. We consider a two-dimensional tight-binding model including both exchange and Rashba spin-orbit coupling. The underlying Hamiltonian is given by

$$\mathcal{H}(t) = \mathcal{H}_0(t) + \mathcal{H}_R, \quad (1)$$

where

$$\mathcal{H}_0(t) = J \sum_r \hat{c}_r^\dagger [\hat{\sigma} \cdot \mathbf{m}(r, t)] \hat{c}_r - \gamma \sum_{\langle r, r' \rangle} (\hat{c}_r^\dagger \hat{c}_{r'} + \text{H.c.}), \quad (2)$$

with H.c. standing for the Hermitian conjugate, $\mathbf{m}(r, t)$ being the time-dependent magnetization, which also depends on position in the case of the antiferromagnetic dynamics. J is the s - d exchange energy between the conduction electrons and the local magnetic order. The operator $\hat{\sigma}$ represents the vector of Pauli matrices, and γ represents the tight-binding hopping energy. The operators \hat{c}_r^\dagger and \hat{c}_r are the creation and annihilation operators, respectively, at position r given by the coordinates x and y . The Rashba Hamiltonian is given by

$$\mathcal{H}_R = i\gamma\alpha_R \sum_r \hat{c}_{x,y}^\dagger (\hat{\sigma}_y \hat{c}_{x+1,y} - \hat{\sigma}_x \hat{c}_{x,y+1}) + \text{H.c.}, \quad (3)$$

with α_R being the Rashba parameter. The system is connected to two transversal normal leads, which allows for probing the pumped currents; see Fig. 1(b).

To compute the nonequilibrium charge current, the stationary scattering modes of the tight-binding system at different energies are obtained using KWANT. Subsequently, they are evolved forward in time according to the time-dependent Schrödinger equation,

$$i\hbar\partial_t\Psi_{\eta m\varepsilon}(t) = \mathcal{H}(t)\Psi_{\eta m\varepsilon}(t), \quad (4)$$

where η stands for the lead from which the state originates, m is the mode index, and ε is the transport energy. Furthermore, the time-dependent current at temperature T is obtained as

$$I(t) = \sum_{\eta m} \int \frac{d\varepsilon}{2\pi} f(\varepsilon, T) \Psi_{\eta m\varepsilon}^\dagger(t) \Psi_{\eta m\varepsilon}(t), \quad (5)$$

with $f(\varepsilon, T)$ being the Fermi distribution function at energy ε and temperature T . The evaluation of these integrals constitutes the most demanding task of the calculations. The numerical procedure followed to compute these quantities is presented in the Supplemental Material [16].

All the numerical calculations are performed at a chemical potential of 100 meV. Therefore the calculated currents are summed from the bottom of the bands to the considered energy. The s - d exchange coupling and the temperature of the system are set to $J = 500$ meV and $T = 0$ K, respectively, unless otherwise stated. To obtain the charge currents in the frequency domain, a discrete fast Fourier transform of the time-dependent signal is performed. In the data presented throughout this Research Letter, I_ω represents the absolute value of the normalized Fourier transform of $I(t)$ given by Eq. (5). Furthermore, we emphasize that the present effect is independent of the nature of the magnetic resonance and is only governed by the ratio of the spin-orbit coupling strength to the dynamic frequency. In fact, the high-harmonic generation is obtained for both ferromagnetic and antiferromagnetic resonances (see Supplemental Material [16]). Nonetheless, in the numerical method we use, the simulation time is set by the electron's energy and is of the order of the hopping parameter γ (typically of the order of 0.1 eV). In order to keep the computational cost reasonable, we have to consider a magnetic system whose resonance frequency is only two orders of magnitude smaller than the internal dynamics of the conduction spin. To comply with the numerical constraints, we therefore consider antiferromagnetic resonance (typically of the order of meV) rather than ferromagnetic resonance (typically of the order of μ eV). We stress that this does not affect the generality of our results.

In antiferromagnetic resonance the two sublattice magnetization vectors, \mathbf{m}_1 and \mathbf{m}_2 , undergo different precession modes of opposite chirality [24]. Without loss of generality, we consider the right-handed polarization of the order parameter, in which case both sublattice vectors rotate anticlockwise [25]. As a result, the antiferromagnet order parameter $\mathbf{n} = (\mathbf{m}_1 - \mathbf{m}_2)/2$ precesses with the same chirality, and a nonzero, albeit small, in-plane magnetization $\mathbf{m} = (\mathbf{m}_1 + \mathbf{m}_2)/2$ develops. As the sublattice magnetizations precess in time, the spin current pumped out of the antiferro-

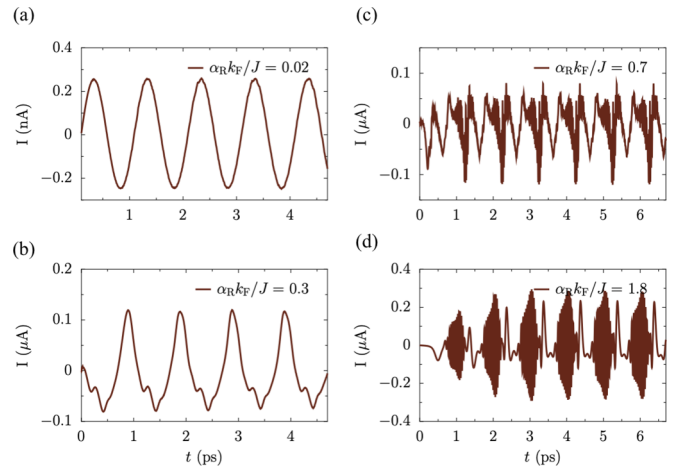


FIG. 3. (a)–(d) Time domain current signal as a function of Rashba strength: Time-dependent currents for different spin-orbit coupling strengths are displayed. Here, an exchange coupling of $J = 500$ meV is taken, and the precession angle is set at $\theta = 10^\circ$. Considering a lattice spacing of 5 Å, the value of α_R at $\alpha_R k_F / J = 1$ corresponds to 3.57 eV Å, which is very close to its value in Bi/Ag alloys [26] or in other bismuth-based topological insulators [27].

magnet reads [24]

$$\mathcal{J}_s = \text{Re}\{g^{\uparrow\downarrow}\}(\mathbf{m} \times \partial_t \mathbf{m} + \mathbf{n} \times \partial_t \mathbf{n}) - \text{Im}\{g^{\uparrow\downarrow}\} \partial_t \mathbf{m}, \quad (6)$$

where $g^{\uparrow\downarrow}$ is the interfacial spin mixing conductance. The symbols $\text{Re}\{\cdot\}$ and $\text{Im}\{\cdot\}$ stand for real and imaginary parts, respectively. In contrast to the ferromagnetic case, the spin current pumped out of an antiferromagnetic metal decomposes into a couple of ac spin currents: a ferromagneticlike contribution \mathcal{J}_m^s along the precession cone axis, given by the first and last terms of Eq. (6), and a staggered contribution \mathcal{J}_n^s rotating in the (x, y) plane, given by the second term of the same equation. In the region subjected to the spin-orbit interaction, the two ac spin current contributions are converted into ac charge currents in both y and z directions according to the inverse spin Hall effect [11].

High-harmonic generation from adiabatic pumping. The time dependence of the collected current is displayed in Fig. 3 for different Rashba strengths. We immediately identify three regimes. For $\alpha_R k_F / J \ll 1$, the current response is dominated by oscillations of frequency ω [Fig. 3(a)]. When the Rashba parameter becomes comparable to the s - d exchange, $\alpha_R k_F / J \sim 1$, the magnitude of the ac current substantially increases whereas involving oscillations with higher frequencies. Upon further increasing the Rashba parameter, $\alpha_R k_F / J > 1$, the amplitude of the signal decreases substantially with very weak components of the higher harmonics. Further numerical simulations suggest the reappearance of the highly excited harmonics regime when $\alpha_R k_F / J \gg 1$. However, the underlying parameter space corresponds to unrealistic spin-orbit coupling strengths.

For a more quantitative discussion, we report in Fig. 4 the Fourier transform of the charge current signals for different values of α_R . For $\alpha_R k_F / J \ll 1$ [Fig. 4(a)], the signal exhibits only one frequency, although we do observe the appearance of the two lowest harmonics. This is consistent with the

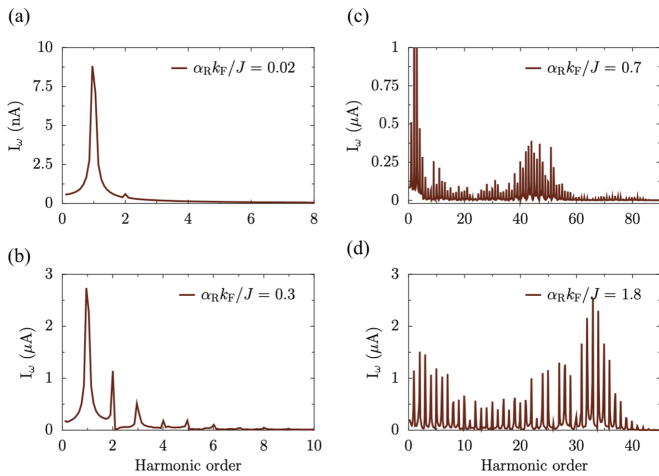


FIG. 4. (a)–(d) Frequency domain charge current as a function of Rashba strength: Fourier amplitudes of the charge current are shown at different spin-orbit coupling strengths in both perturbative and nonperturbative regimes. The antiferromagnetic dynamics parameters are the same as in Fig. 3.

adiabatic spin pumping theory [9,10]. Upon increasing the Rashba strength [Figs. 4(b) and 4(c)], higher harmonics progressively emerge with amplitudes slightly below the fundamental frequencies. Notice that the amplitudes of the higher harmonics are only one order of magnitude smaller than the fundamental harmonic at frequency ω . For the sake of comparison, Ref. [28] recently reported the optical generation of higher harmonics in graphene driven by internal electron thermalization. The authors observed harmonics up to the seventh order with amplitudes four orders of magnitude smaller than that of the fundamental mode. In contrast, our simulations demonstrate that even in the perturbative regime the intensities of the high harmonics remain of the same order as the amplitude of the fundamental frequency's response. Upon reaching the resonance, even higher number of harmonics are generated. We emphasize that at resonance, our simulations yield signals with evolving amplitudes. The corresponding steady states should be attained at some moment, presumably after a large number of magnetic cycles. This peculiar behavior of the HHG spectra has been recently reported in correlated electron systems [29]. Above resonance though, when $\alpha_R k_F / J > 1$ [Fig. 4(d)], the current response still display a large number of harmonics.

In order to offer a comprehensive picture of the high-harmonic generation, the current output is reported in Fig. 5 as a function of the spin-orbit strength $\alpha_R k_F / J$ and the harmonic order, the amplitude of the harmonic being given by the color scale. The resonance regime corresponding to the ultrahigh-harmonic generation is centered around $\alpha_R k_F / J = 1$ and extends from $\alpha_R k_F / J \approx 0.8$ to $\alpha_R k_F / J \approx 1.2$, indicating that the effect is robust against variations in the material's parameters and thereby providing a wide region of tunability. As a matter of fact, we observed that the signal bandwidth is proportional to the driving frequency ($\propto 1/\omega$), as shown in Fig. 6(a). Furthermore, it is worth emphasizing that the precession cone opening plays a crucial role in enhancing the amplitudes of the highest harmonics. Although Fig. 6(a)

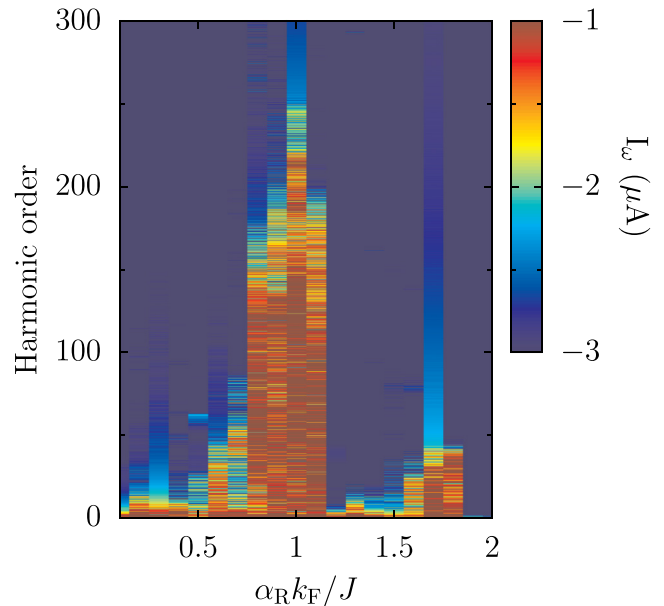


FIG. 5. Charge current amplitude of the harmonic spectrum as a function of spin-orbit coupling strength: The current amplitude (in logarithmic scale) is shown as a function of the harmonic order as well as the Rashba strength. The frequency of the dynamics as well as the precession angle are the same as in Fig. 3.

predicts an emission up to the 500th harmonic for the dynamic frequency considered in Fig. 5, only about two hundred of them exhibit strong enough amplitudes for the precession angle considered (here, $\theta = 10^\circ$). At larger precession angles all the higher harmonics can be excited with amplitudes comparable to the first-harmonic intensity (see the Supplemental Material [16]).

In contrast, upon reducing the pumping frequency, one can substantially enhance the number of harmonics. This is illustrated in the Supplemental Material [16], where the Fourier spectrum of the charge current computed for a driving frequency of 0.4 THz is shown. We notice that a similar decay in the number of generated harmonics with respect to ω has been reported in different solid-state systems under intense laser excitation [30–32].

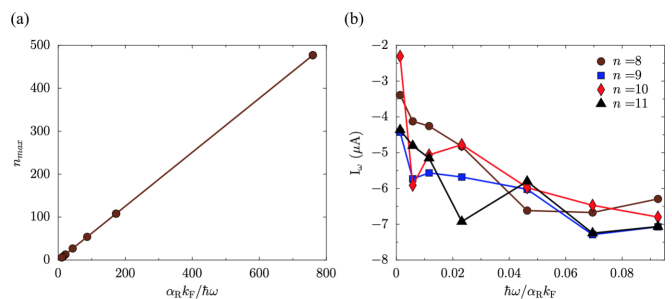


FIG. 6. Emission bandwidth and charge current amplitude as a function of the driving frequency: (a) Maximum number of harmonics as a function of the inverse of the fundamental frequency. (b) Amplitude of selected harmonics as a function of the driving frequency. The Rashba strength is tuned to the maximally excited regime.

Discussion. A crucial question we now wish to comment on is the applicability of our single-orbital model to realistic systems. As mentioned in the Introduction, adiabatic spin-to-charge conversion has been demonstrated in a wide variety of heterostructures accommodating both Rashba-like spin-orbit coupling and s - d exchange. Transition metal ferromagnets interfaced with topological insulators [17] and oxide heterostructures [19] are among the most promising structures. In these systems, Rashba-like spin-orbit coupling arises from a complex interfacial orbital hybridization scheme that is essentially overlooked in our model. Nonetheless, intense theoretical investigation of spin-orbit physics [33] (spin-orbit torque and spin-to-charge conversion) has established that in spite of its simplicity, modeling the interfacial spin-orbit coupling by an effective Rashba interaction is sufficient to properly describe the physics at stake and obtain reasonable orders of magnitude. Further calculations (not shown) demonstrate the robustness of the effect at room temperature. This represents a major advantage in terms of the applicability of the effect to real devices.

The present effect opens appealing perspectives for high-frequency emission deep into the THz gap. It is worth emphasizing that the effect requires two essential ingredients: strong spin-orbit coupling and oscillating magnetic order or magnetic field with in-plane components.

Now we discuss a possible experimental realization of our proposal. We stress that conventional spin-to-charge conversion heterostructures are suitable platforms to harness the effect. In fact, the very nature of Rashba spin-orbit coupling

makes this perspective quite appealing because it is directly related to the interfacial potential drop and therefore highly sensitive to a gate voltage, for instance. Whereas this electrical tuning of the Rashba strength has been demonstrated in several systems, oxide two-dimensional electron gases [19,34,35] stand out as the most versatile system. The recent demonstration of electrical switching of Rashba coupling [35] makes this perspective even more compelling. The Rashba strength can be as large as a few hundred meV, which seems reasonable as the effective s - d exchange experienced on the surface can be tuned by inserting a tunnel barrier, for instance. Furthermore, a strong enhancement of spin-orbit coupling strength in graphene to 80 meV has been recently reported [36], where the spin-orbit coupling strength can be controlled in a field effect transistor setup. This provides a variety of systems in which the effect can be observed. Finally, we stress that the effect is not limited to Rashba spin-orbit coupling systems. It is similarly expected to manifest in the presence of Dresselhaus or bulk spin-orbit interaction. Furthermore, it has been recently demonstrated that the effect can be observed in the presence of noncollinear antiferromagnets [37], where the spin-flip scattering is triggered by the underlying topological magnetic textures.

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