Atomic-scale visualization of the *p-d* hybridization in III-V semiconductor surfaces doped with transition metal impurities

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The *p*-*d* hybridization of transition metal impurities in a semiconductor host is the mechanism that couples valence-band electrons and localized spins. We use scanning tunneling microscopy and spectroscopy combined with density functional theory to probe at the atomic-scale hybridization of Cr single impurities with a GaAs host. Combining spatial density of states mapping and in-gap state spectroscopy of the Cr substituted at the surface of the semiconductor, we give a detailed picture of the spatial extension and the electronic structure of the strongly anisotropic wave function of Cr on GaAs(110). First-principles calculations allow us to identify the electronic character and origin of each state and show that the main resonance peaks and the wave function with "drop-eye" lobes experimentally observed for 3d metal impurities in III-V semiconductors are direct local evidences of *p*-*d* hybridization.

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I. INTRODUCTION

The electronic properties of transition metal impurities introduced in a semiconductor host have been intensively studied in the 1970s and 1980s for microelectronics or optoelectronics applications (see, for instance, Refs. [1,2]). Interest in such systems grew during the 1990s because of the discovery of ferromagnetism in diluted magnetic semiconductors (DMSs). The origin of magnetic order in these materials has been ascribed to the carrier-mediated coupling between spins of doping transition metal dopants, which has been described by phenomenological models and first-principles calculations [3–7]. These theoretical works have shown that the main local cause of the ferromagnetic interaction in III-V semiconductors between transition metal atoms is the *p*-*d* hybridization between the *d* orbitals of the impurity and the *p* orbitals of host atoms.

Scanning tunneling microscopy (STM) and spectroscopy (STS) contributed greatly to the understanding of the physics of transition metal ions in semiconductors by imaging at the atomic scale impurities deposited on semiconductor surfaces or substituted to cations near the surface. STM and STS studies have been carried out on a GaAs surface for several elements: Mn [8-15], Fe [13,16,17], and Co [13,18]. Despite the different *d*-band fillings, the STS data show similar resonances in the band gap and the conductance maps at the corresponding resonance voltages reveal extended wave functions with "crablike" and "drop-eye" shapes. These results have been discussed qualitatively following the Mahadevan and Zunger approach developed for bulk materials [5], but no precise explanation of the origin of the shapes and their relations to the contributions of the p and d orbitals to the state has been so far given for surfaces. In spite of the large number of STM/STS studied showing similar results on transition metal impurities in III-V semiconductor surfaces, a complete description of the physical mechanism explaining the observed wave-function shape and resonance states is still missing. In this paper, we aim to understand the origin of these observations by shedding light, both experimentally and theoretically, on the link between STS spectroscopy and STM maps, i.e., between the electronic structure and spatial distribution of the density of states. Our analysis of the extended impurity states presents an intermediate description between the local chemical description, i.e., the d orbitals of the impurity hybridize with the *p* orbitals of the neighboring anions, and the physical description, i.e., the d orbitals hybridize with Bloch valence states at the Γ point. Such a description will enable a more precise understanding of the kinetic exchange mechanism enabling ferromagnetic ordering in those materials.

II. EXPERIMENTAL DETAILS

We explore by STM and STS the electronic states of Cr single atoms substituted to Ga in the first layers of a GaAs(110) surface and we combine experimental results with density functional theory (DFT) calculations. To our knowledge, Cr atoms have yet to be explored by STM on GaAs. It has been theoretically demonstrated that they behave as Mn and give rise to ferromagnetic coupling [5], but only a few DFT studies have focused on the electronic properties of transition metal impurities near a semiconductor surface [19–21]. Experimentally, while Cr and Mn induce different modifications in the electronic structure (energy position of the acceptor level, order of the resonance states), they both show effective magnetic coupling at low temperature [22]. Thus, our study of Cr by STM/STS allows us to complete the



FIG. 1. (a) and (b) Schematic three-dimensional view of the first three layers of the GaAs(110) surface with one Cr atom incorporated. As atoms are in red, Ga in gray, and Cr in green. (c)–(f) Constant current STM image of one Cr atom substituted to a Ga in the first layer of GaAs(110) [(c) and (e)] and in the second layer [(d) and (f)]. Ball and stick atomic models are superposed to the STM images; large balls correspond to atoms in the first layer while smaller balls correspond to atoms in the second layer as defined in (a) and (b). Parameters: 3.5 nm × 3.5 nm, (c) -1.5 V, 50 pA, *z* range 39 pm, (d) -1.5 V, 100 pA, *z* range 60 pm, (e) 1.5 V, 50 pA, *z* range 360 pm, and (f) 1.5 V, 60 pA, *z* range 444 pm.

understanding of the mechanism behind the transition metal doping of semiconductors.

To control the substitution of Ga by Cr in the first and second layers of the surface, we developed a tip-induced manipulation method. This gives the possibility of studying magnetic impurities as a function of their coordination number: three covalent bonds with the As neighbors in the case of Cr inserted in the first layer, noted Cr_{Ga1} and shown in Fig. 1(a), and four bonds in the case of Cr in the second layer, noted Cr_{Ga2} and shown in Fig. 1(b), which has the same coordination number as in the bulk. For these two configurations, we image the wave function of the impurity and measure the spectra. Combining the experimental spatial and energy information with first-principles total energy calculations, we obtain spatial maps of the different contributions, s, p, dof the wave function, which provide a detailed view of the hybridization between the d orbital of the Cr atom and the s-p orbitals of the anion.

Experiments were performed with a STM system at 4.2 K in ultrahigh vacuum ($<5 \times 10^{-11}$ mbar). The gap voltage was applied on the sample. We have cleaved *in situ p*-type highly doped (2×10^{19} cm⁻³) GaAs wafers in order to expose the

(110) surface and to perform so-called cross-sectional STM (X-STM) [23]. The sample was precooled in the STM cryostat and then transferred to a preparation chamber where a submonolayer quantity of Cr was deposited on the GaAs(110) surface, and replaced quickly in the STM for measurement at 4.2 K. As described by Kitchen et al. [10,13,24], transition metal adatoms deposited on GaAs(110) can be incorporated in the first surface layer. Mn, Fe, and Co adatoms on GaAs(110) show different surface dynamic and incorporation behaviors. For Cr, we find that adatoms can be incorporated in the first GaAs layer using tip manipulation [Fig. 1(a)]. Cr in the first layer can also be forced to move to a substitution position in the second layer [Fig. 1(b)]. In each case of substitution, we observe the extraction of a Ga atom visible as an adatom: black rings also reported in Refs. [10,13]. The mechanism of tip-induced substitution and atom manipulation will be described elsewhere [25].

III. ELECTRONIC STRUCTURE OF Cr ATOMS IN Ga SUBSTITUTION POSITION

Figures 1(c)-1(f) show constant-current STM images of Cr atoms in the Ga substitution position in the first and second layers of GaAs(110) for negative and positive tip-sample gap voltages. Because we control the incorporation with the tip, we are able to determine the exact Cr position before and after the incorporation processes. As expected for Ga substitution, Cr is localized in the Ga [110] columns (vertical lines in Fig. 1), which are imaged at positive voltage [26]. Cr_{Ga1} is imaged on a Ga [001] row (horizontal lines) of the first layer [Fig. 1(e)] while Cr_{Ga2} appears in between two Ga rows, i.e., in an As row of the first layer and Ga row of the second layer [Fig. 1(f)]. In other words, the Cr that substitutes a Ga of the first layer (respectively second layer) is symmetric with respect to the $(1\overline{1}0)$ plane crossing the Ga row (respectively As row) of the top surface layer. From these symmetry arguments, we can deduce unambiguously that the Cr is inserted in the second layer. In the first layer, we find similar patterns with drop-eye (negative voltage) and crablike (positive voltage) shapes as found on other transition metal impurities [12,13,17,18]; in the second layer the patterns change drastically. Such an observation of a transition metal atom in the second layer has been reported for Mn in Ref. [12], but no atomic resolution and no bias voltage dependence have been shown. It is noteworthy that in both layers the maximum of the electronic density of states is not localized exactly on the Cr atoms but distributed rather asymmetrically over several atomic lengths in a strongly anisotropic way.

Figure 2 presents differential conductance dI(V)/dV spectra measured on Cr, proportional to the local electronic density of states (LDOS). They show features similar to those measured on Mn, Fe, and Co [13,17,18,24]. Negative differential conductance is also observed due to the presence of a narrow resonance peak [27]. Depending on the exact spectra position, center or lobe, large in-gap resonances are observed in the GaAs gap near the conduction band and smaller peaks in the valence band.

In order to precisely identify the spatial distribution of each state, we performed differential conductance maps on a 52×52 grid. A conductance map taken at the energy of



FIG. 2. STS spectra measured on top of Cr atoms incorporated (a) in the first layer of the GaAs(110) surface and (b) in the second layer. Exact positions of the tip during the spectra, named the center or lobe, are indicated by small squares depicted in Figs. 1(e) and 1(f). Peaks observed on the spectra are indicated and labeled on each peak.

an electronic resonance represents the probability density of the corresponding wave function. Figure 3 shows dI(V)/dVmaps of Cr_{Ga1} (left) and Cr_{Ga2} (right) at the energies of the peaks observed in Fig. 2 (except peak p_{21} for which the signal is too low). For Cr_{Ga1} , the first state p_{11} [Fig. 3(a)] is weak and delocalized. In contrast, the second state p_{12} [Fig. 3(b)] is localized near the As neighbor atoms. The p_{13} state [Fig. 3(c)] is similar to p_{12} but present in addition to a signal contribution in between the As atoms, closer to the Cr position. For Cr_{Ga2} , the states p_{22} [Fig. 3(d)] and p_{24} [Fig. 3(f)] present an isotropic spatial extension while p_{23} [Fig. 3(e)] has a delocalized wave function. The anisotropic shape of the Cr atom in the constant-current image of Fig. 1(f) can be well reproduced by the summation of the conductance images at the positive bias of Figs. 3(e) and 3(f).

IV. COMPUTATIONAL DETAILS

To further explain and clarify the origin of the observed peaks in Fig. 2 and their spatial distribution in Fig. 3, we have carried out first-principles total energy calculations in the framework of density functional theory (DFT) as implemented in the plane-wave PWSCF code of the QUANTUM ESPRESSO distribution [28]. A local spin density approximation (LSDA) with norm-conserving pseudopotentials with the Perdew-Zunger exchange-correlation functional were employed. The GaAs(110) surface was modeled through the supercell method using a slab containing 13 atomic planes, each containing 2 atoms (26 atoms for the whole structure). As for the doped surface slabs, a 2×3 supercell was built containing 156 atoms in order to reduce the interaction between periodic replicas of dopants [see Supplemental Material (SM)



FIG. 3. dI(V)/dV maps of Cr in the Ga substitution position in the first surface layer (top row) and in the second layer (bottom row), 2 nm × 2 nm. Images are measured at the energies of the peaks observed in Fig. 2. Schematic ball and stick atomic models are superposed to STM images. Insets of each dI(V)/dV map: Calculated cross section on the (110) plane of ILDOS of Cr in the first surface layer (left) and in the second surface layer (right) at energy ranges corresponding to each peak of Fig. 4, indicated in brackets. Maps are integrated over a slice along [110] from the surface to the plane of the Cr_{Ga2} atom. Isodensity contours are marked by black lines and are separated by 0.005 $e/bohr^3$. Green dots indicate the position of the Cr atom. The whole color range on each ILDOS map is (in $e/bohr^3$ unit): 0.054 in (a), 0.011 in (b), 0.029 in (c), 0.026 in (d), 0.028 in (e), and 0.031 in (f).

[29] and references therein [5,28,30–39]]. We simulated the effect of Cr dopants in both the bulk and (110) GaAs surface. For each system the projected density of states (PDOS) was calculated by projecting the Kohn-Sham wave functions on an atomic orbital basis set in order to evaluate the contribution of each atom to the total DOS. Experimental constant-current STM images are here discussed in light of integrated local density of states (ILDOS) calculations in the framework of the Tersoff-Hamann approximation [38,39]. According to this assumption, the STM tunneling current is proportional to the integrated LDOS of the sample at the tip position. By employing this approach, constant-current STM images can hence be

directly compared to the integrated LDOS calculated within DFT. All the computational details of our study can be found in the Supplemental Material [29].

V. p-d HYBRIDIZATION

We calculated the electronic density of states projected on atomic orbitals for Cr-doped bulk GaAs and for a Cr atom in the first, second, and third layer of the GaAs surface. In the bulk case (see SM), the Cr site has T_d symmetry and produces a deep trap state within the gap that results from the hybridization of the Cr d orbitals and the p orbitals of the As atoms (see Fig. S1 and Table S1 of the SM). The tetrahedral crystal field of the zinc-blende host splits the d levels of the Cr atoms into e and t_2 multiplets, which are further split by the exchange interaction into spin-up and spin-down states. Hybridization finally splits the t_2 states into bonding and antibonding levels (e states have no orbital in the GaAs of the same symmetry to hybridize with), giving rise to six states in total (Figs. S2 and S7 of the SM). According to Ref. [5], this leads to two kinds of impurity states: the crystal field resonances (CFRs) that have d-orbital character and are localized on the transition metal ion, and the dangling bond hybrid (DBH) that contains a large *p*-orbital component due to the *p*-*d* hybridization.

When the Cr atom substitutes a Ga atom in the third layer of the surface (Fig. S6), the electronic structure does not differ too much from what we observe in the case of Cr doping of the bulk system. As one goes from the third to the second and first layer of the surface, the symmetry of the Cr site is lowered as evidenced by the evolution of first neighbor distances around the Cr impurity (see Table S2). For the Cr_{Ga1} substitution in the first layer, the threefold coordination and the surface buckling leads to C_{3v} point-group site symmetry. Furthermore, because of the change of the lattice parameters at the surface, a C_S site symmetry is finally obtained. As a consequence, the fivefold degeneracy of the *d*-orbital multiplet is completely lifted as shown in Fig. S7.

The insets of Fig. 4 show the total density of states for the Cr_{Ga1} and Cr_{Ga2} that exhibit three peaks for Cr_{Ga1} and four for Cr_{Ga2} , corresponding to what is observed experimentally in Fig. 2. Figure 4 shows the contributions of atomic orbitals to the total density of states (*d* and *p* orbitals, while *s* orbitals have a negligible contribution), for the two spin polarizations. All the peaks observed have a strong *d* contribution coming from the chromium, as well as an As-*p* contribution. For Cr_{Ga1} (respectively Cr_{Ga2}), this *p* contribution is especially strong for the peaks at -0.3 eV (-0.6 eV) and 0.7 eV (0.5 eV). For the peak at 0.7 eV for Cr_{Ga1} and the peaks at -0.1 and 0.8 eV for Cr_{Ga2} , the contribution of Ga-*p* orbitals is also significant as compared to the *d* contribution. This mixed character of the peaks is the consequence of *p*-*d* hybridization.

The insets of Fig. 3 show ILDOS of Cr_{Ga1} (left) and Cr_{Ga2} (right) at energies corresponding to the peaks of Fig. 4 and associated with the experimental maps. Here, we represent (110) planes of ILDOS integrated over a slice along [110] from the surface to the plane of the Cr_{Ga2} atom. These calculations reproduce well the dI/dV(V) experimental images, considering the well-known DFT inaccuracy in reproducing experimental energy peak positions, except for in Fig. 3(a) where the signal is too weak. For Cr_{Ga1} , the observed and



FIG. 4. Calculated spin-resolved density of states projected on the atomic orbitals for the Cr-doped (110) GaAs surface with the Cr atom in the (a) first and (b) second layer of the surface. The insets show the total density of states and the vertical black bars show the position of the maxima. The zero of the energy is set to the Fermi energy of the system. Spin up correspond to upper curves, and spin down to the lower ones.

simulated lobes are oriented towards the As first neighbors of the Cr, which can be explained by the strong As-p contribution to the density of states found in Fig. 4. Thus, the DFT results show that our STM observation of the delocalization and the anisotropy of the wave function, especially the density of states oriented towards the As neighbors giving rise to the two drop-eye lobes, is a direct demonstration of p-d hybridization observed here at the atomic scale.

Some states present wave functions with a rather compact shape centered around the Cr [insets of Figs. 3(a), 3(d) and 3(f)], while others are more delocalized with anisotropic lobes [insets of Figs. 3(b), 3(c) and 3(e)]. States centered on the Cr impurities have a CFR character, with a rather out-of-plane contribution, which could be described by d_{z^2} orbitals. In contrast, states with lobes pointing towards the anions have a DBH character with the symmetry of d_{xy} orbitals. One expects in this case a naturally strong σ bonding with the *p* orbitals of the As neighbors which have the same symmetry.

Because of the lowering of site symmetry from T_d in the bulk to C_S at the surface, the energy levels identified by STM spectroscopy and reproduced by the DFT calculations cannot be classified according to the irreducible representations t_2 and e of the T_d point group. Despite this, one can still identify two types of states, the localized states, essentially of d-orbital character, and the extended hybridized p-d states. Because these extended states spread over several unit cells,

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they should be better described as the hybridization of *d* orbitals with valence Bloch states at the Γ point [40,41].

VI. CONCLUSION

In conclusion, by combining STM and first-principles calculations, we were able to explain the origin of the anisotropic shape of the wave function of the Cr atom substituted to Ga in the GaAs (110) surface. The lobes observed by STM in GaAs doped by transition metals are the signature of the electronic hybridization of the atom with its host. In particular, the As-*p* orbitals hybridize with the Cr-*d* orbitals giving rise to "drop-eye" lobes localized around the As atoms, which are the main distinctive attributes of the wave function of transition metal impurities in GaAs. Our DFT calculations describe the electronic origin of the resonances observed in the semiconductor gap when doped with a transition metal, and show the significant weight of the As-*p*, as well as the Ga-*p* electrons in some cases. We also present the spin-resolved contribution of these states, whose experimental confirmation could be an interesting perspective of this work.

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