Highly efficient spin-orbit torque in a perpendicular synthetic ferrimagnet

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Perpendicular synthetic ferrimagnet (pSFi) due to the low stray field and net magnetization is expected to replace single ferromagnet as a free layer to optimize the memory devices for high storage density and low-energy consumption. Here, we investigate the dependence of exchange-coupling strength on the thickness of the spacer Ru and current-induced magnetization reversal due to spin-orbit torque in Ta/Pt/[Pt/Co]₂/Ru/[Co/Pt]₄/Pt structure with a perpendicular magnetic anisotropy. An oscillating interlayer exchange coupling as a function of Ru spacer layer thickness with a period of 1.16 nm is determined by combining the anomalous Hall effect and the polar magnetic-optical Kerr effect. Furthermore, current-controllable magnetization reversal experiments reveal that the magnetizations of top and bottom layers with antiferromagnetic coupling switch simultaneously due to the combination of spin-orbit torque generated from the two adjacent heavy-metal layers and the interlayer exchange torque. The SOT efficiency $\chi \sim 57.52 \text{ Oe}/(10^6 \text{ A/cm}^2)$, corresponding to an effective spin Hall angle $\xi_{DL} \sim 0.68$, is estimated by analyzing current-dependent anomalous Hall resistance with our proposed quasistatic balance equation of magnetic moments. In addition to the advantage of minimizing stray field acting on the storage layer, the observed low switching current density and high spin-orbit torque efficiency suggest that the pSFi structure with a high thermal stability factor has great potential to realize the high-density and low-power consumption of nonvolatile magnetic memory devices.

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I. INTRODUCTION

The magnetic tunnel junction (MTJ), due to its nonvolatility, high tunneling magnetoresistance ratio, and small size, has been widely used in magnetic sensor, storage, and logic devices, e.g., magnetic read head and magnetoresistive random access memory (MRAM) [1,2]. With massive data included in the current digital information, high-density and highefficiency MRAM development based on various materials and structures has acquired increasing attention. In traditional MTJs, the free layer usually consists of a single ferromagnetic layer [3,4]. As the reduction of MTJ cell size or more MTJ cells are patterned into a smaller space, the local stray field generated from the ferromagnetic layer becomes the predominant factor, degrading the performance of MRAM [5,6]. Compared with ferromagnet, antiferromagnet with zero net magnetic moments as the free layer can eliminate or minimize the stray field. However, the characteristics of the antiferromagnet, being insensitive to the external magnetic field and charge current and challenging to experimental manipulation and detection, still impede the further application of antiferromagnet in MTJs [7]. Fortunately, the synthetic antiferromagnet (SAF) and synthetic ferrimagnet (SFi), consisting of two antiferromagnetically coupled ferromagnetic layers and a nonmagnetic spacer, possess the advantages of reduced stray field and high thermal stability due to the strong interlayer exchange coupling, as well as keeping almost the same manipulation and detection of magnetization as the single ferromagnet layer [8,9]. The interlayer exchange coupling between two magnetic layers adjacent to the same nonmagnetic spacer can be referred to as the Ruderman-Kittel-Kasuya-Yosida (RKKY) interaction [10,11]. Based on RKKY interaction theory, this sandwich structure has an oscillatory interlayer exchange coupling as a function of the nonmagnetic spacer layer thickness. Therefore, the interlayer exchange coupling provides an extra degree of freedom to manipulate dynamical modes that may reduce the switching time of MTJs. In the SAF film with such exchange-coupling torque, current-driven domain-wall motion can be more efficient with a faster speed of up to \sim 750 m/s [12]. Recently, spin-orbit torque (SOT) has been brought up as a highly efficient and low-power consumption method to manipulate magnetization

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electronically [13–22]. Many experiments have been carried out in various systems, including simple NM/FM bilayers Pt/Co [13], Ta/CoFeB [14], TaOx/Py [18]; Bi-based topological insulators (Bi_{0.5}Sb_{0.5})₂Te₃ [23,24], Bi₂Se₃ [25,26]; and synthetic antiferromagnetic structures Co/Ru/[Co/Pt] [27], CoFeB/Ta/CoFeB [28], and Pt/Co/Ir multilayers [29], searching for promising systems with large SOT efficiency. SAF and SFi systems are potential candidates for high SOT efficiency, owing to the reduced stray field, interlayer exchange coupling, and probably additional sources of SOT from interfaces.

Although SOT in some SAF or SFi systems has been found experimentally [30,31], the quantitatively calculated SOT efficiency methods in the SAF and SFi structures are still insufficient and lack consistency. In this work, we systematically investigated the interlayer exchange-coupling (IEC) field and magnetic domain structure with different Ru thicknesses in Ta/Pt/[Pt/Co]₂/Ru/[Co/Pt]₄/Pt films by combining anomalous Hall effect and the polar magneticoptical Kerr effect techniques. We experimentally determined the optimum antiferromagnetic coupling thickness and the oscillating period of IEC. Two representative SFi films with different interlayer antiferromagnetic exchange-coupling fields were adopted to perform current-driven magnetization switching experiments. The magnetization switching critical current was lower than the single ferromagnet device. Furthermore, an alternative method of calculating the current-induced reduction of anomalous Hall resistance was proposed to quantify the SOT efficiency as high as $\chi =$ $57.52 \text{ Oe}/(10^6 \text{ A/cm}^2)$, corresponding to an effective spin Hall angle $\xi_{DL} = 0.68$.

II. EXPERIMENT DETAILS

 $Ta(4)/Pt(4)/[Pt(0.6)/Co(0.6)]_2/Ru(t_{Ru})/[Co(0.6)/Pt(0)]_2/Ru(t_{Ru})/$ $(.6)]_4/Pt(1)$ multilayer stacks (from the bottom to the top, thickness in nanometers) were deposited on thermally oxidized Si/SiO₂(300 nm) substrates via DC magnetron sputtering at a base vacuum better than 2×10^{-8} Torr. The thickness t_{Ru} of Ru space layer is a range of 0–2.5 nm. The deposition pressure was $\sim 5.0 \times 10^{-3}$ Torr Ar. The deposition rates for each layer Pt~0.027 nm/s, $Co\sim 0.018 \text{ nm/s}$, $Ru\sim 0.015 \text{ nm/s}$, and $Ta\sim 0.024 \text{ nm/s}$ were detected simultaneously using an in situ quartz crystal monitor. The studied devices were first patterned into Hall bar by combining electron-beam lithography and magnetron sputtering, as shown in Fig. 1(b). In the stack, the 4-nm-thick Ta layer was deposited as a buffer layer to improve surface smoothness and perpendicular magnetic anisotropy (PMA). When the charge current passes through the Hall bar, the spin current generated by the spin Hall effect (SHE) in the heavy-metal Pt would flow upward, exert spin-orbit torque on magnetic moments, and switch the magnetization of the Pt/Co multilayer. We adopted Co/Pt multilayers with different numbers as bottom and top FM layers for our experimental distinction between two FM layers. The magnetic properties of samples were characterized by polar magneto-optical Kerr effect (PMOKE) [32,33] and anomalous Hall effect (AHE) [34] measurements in the patterned Hall cross.



FIG. 1. (a) Schematic of a $Ta/Pt/[Pt/Co]_2/Ru/[Co/Pt]_4/Pt$ multilayer. (b) The optical microscope image of the Hall bar and the measurement configuration of anomalous Hall resistance.

III. RESULTS AND DISCUSSION

A. Interlayer exchange coupling

We first show the out-of-plane hysteresis of the heterostructures with different thicknesses of Ru spacer measured by PMOKE. Figure 2(a) shows that the PMOKE hysteresis loops exhibit a well-defined square shape under an out-of-plane magnetic field, similar to a single FM layer with strong PMA, indicating the magnetic moments of the bottom and upper [Co/Pt] multilayers with the labeled thicknesses of Ru spacer arrange parallelly with an interlayer ferromagnetic coupling. The coercive field H_c generally decreases with increasing thickness t_{Ru} of Ru spacer, resulting from the reduction in the interlayer exchange coupling and PMA of the upper [Co/Pt] layer, which depends on the thickness of the spacer (or buffer) layer Ru [35]. The PMOKE images also confirmed that [Co/Pt] multilayers exhibit a singledomain structure. However, Fig. 2(b) shows several separate switching fields with four intensity plateaus, suggesting the bottom and upper magnetic layers have an interlayer AFM exchange coupling for the labeled thicknesses of Ru spacer. The corresponding PMOKE images also indicate that [Co/Pt] multilayers form a single-domain structure.

To better illustrate the magnetization switching process of the bottom and upper layers, we adopt two representative AHE hysteresis loops corresponding to FM exchange coupling $(t_{Ru} = 1.5 \text{ nm})$ [Fig. 2(c)] and AFM $(t_{Ru} = 1 \text{ nm})$ [Fig. 2(d)] exchange coupling, respectively, with the external out-of-plane magnetic field and a small DC current of 0.5 mA. For the $t_{Ru} = 1.5$ nm sample, like the PMOKE hysteresis loop, Fig. 2(c) shows a single hysteresis loop, suggesting that the parallel magnetizations of the top and bottom layers switch together at the coercive field due to strong interlayer FM exchange coupling and non-negligible dipolar interaction. For the $t_{Ru} = 1.0$ nm sample, Fig. 2(d) shows four states forming three loops with the same Hall resistance difference value $\Delta R_{\rm H}$. Since anomalous Hall resistance $R_{\rm H}$ is proportion to the magnetization and thickness of the magnetic layer, $\Delta R_{\rm H}$ contributed from the upper [Pt/Co]₄ layer is twice as high as from the bottom $[Pt/Co]_2$ layer. Therefore, the minor loops at high magnetic field represent the magnetization switching of the bottom $[Pt/Co]_2$ layer, and the field shift of the minor loop is defined as the antiferromagnetic exchange coupling field $H_{\rm IEC,b}$ experienced by the bottom FM layer (denoted as $H_{\rm IEC}$ below for simplicity). The prime loop at the low magnetic



FIG. 2. (a), (b) Out-of-plane PMOKE hysteresis loops of the samples with FM (a) and AFM (b) interlayer exchange coupling. The top inset PMOKE images show magnetic domain structures during the field-driven magnetization switching process. The thickness of the Ru spacer is labeled. (c), (d) Normalized out-of-plane AHE hysteresis loop for samples with 1.5-nm- (c) and 1.0-nm- (d) thick Ru spacer. The blue and orange arrows depict the bottom and the upper magnetic moments. (e) Dependence of interlayer exchange-coupling field on thickness t_{Ru} of Ru spacer. The crosses represent the FM coupling samples. (f) The interlayer exchange-coupling strength J_{IEC} vs t_{Ru} . The solid curve is the RKKY formula fitting result.

field represents the switching between the two antiferromagnetic states (" $\uparrow\downarrow$ " and " $\downarrow\uparrow$ ", denoted as the "tail-to-tail" and "head-to-head" state, respectively), as illustrated in Fig. 2(d). In terms of energy, the parallel or antiparallel configurations of this studied magnetic sandwich structure are dominated by PMA, Zeeman energy, and interlayer exchange coupling [36]. When the external out-of-plane magnetic field is larger than the interlayer exchange-coupling field, the Zeeman energy becomes dominant, and magnetizations of both layers are along the external magnetic field. In contrast, when the external magnetic field is smaller than H_{IEC} , magnetizations of two layers are antiparallel, and magnetization of the upper thick [Co/Pt]₄ layer is parallel to the external magnetic field. Therefore, from the negative magnetic field to the positive



FIG. 3. (a), (d) Anomalous Hall resistance $R_{\rm H}$ hysteresis loops of Ta/Pt/[Pt/Co]₂/Ru control sample with only bottom magnetic layer (a) and $t_{\rm Ru} = 1.0$ -nm SFi sample (d) measured with a small DC current I = 0.5 mA under out-of-plane (black curve) and in-plane (red curve) magnetic fields. The arrows in (d) illustrate the magnetic moments' orientations of bottom and upper FM layers under an in-plane field. (b), (e) Current-induced switching of Ta/Pt/[Pt/Co]₂/Ru (b) and $t_{\rm Ru} = 1.0$ -nm SFi sample (e) under the labeled in-plane external fields $H_{\rm out}$ in the direction of the current. (c), (f) The critical switching current density $J_{\rm c}$ vs $H_{\rm in}$ for Ta/Pt/[Pt/Co]₂/Ru (c) and $t_{\rm Ru} = 1.0$ -nm SFi sample (f), respectively.

magnetic field, the four states are in the sequence of " $\downarrow \downarrow$ ", " $\uparrow \downarrow$ ", " $\downarrow \uparrow$," and " $\uparrow \uparrow$ " [inset in Fig. 3(d)].

The experimentally determined interlayer exchangecoupling field H_{IEC} of all samples with different thicknesses t_{Ru} of Ru spacer were summarized in Fig. 2(e), where the FM and AFM exchange coupling vary alternatively and decay with the increase of t_{Ru} . The spacer thickness with $0.5 \text{ nm} \leq t_{\text{Ru}} \leq 1.0 \text{ nm}$ and $1.8 \text{ nm} \leq t_{\text{Ru}} \leq 2.4 \text{ nm}$ correspond to the first and second AFM coupling regimes, respectively. The first peak of AFM coupling occurs at $t_{\rm Ru} \sim$ 0.9 nm with H_{IEC} up to 7.3 kOe and the second peak at $t_{\rm Ru} \sim 2.1$ nm with $H_{\rm IEC}$ up to 2.2 kOe. This oscillating interlayer exchange interaction is well consistent with an RKKY indirect exchange interaction [37]. This interlayer exchangecoupling strength for different thicknesses of Ru can be calculated by the equation $J_{\text{IEC}} = H_{\text{IEC}}M_{\text{s}}t_{\text{FM}}$ [38], where M_{s} and $t_{\rm FM}$ are the saturation magnetization and thickness of the bottom $[Pt/Co]_n$ multilayer, respectively. Furthermore, we adopted Yafet's RKKY model [39], considering twodimensional layers with a uniform distribution of spins. The spins within a layer are assumed to be aligned in parallel, and the interlayer coupling strength is in the form $J \sim Y(2k_{\rm F}t)$, where $Y(x) = \frac{x\cos x - \sin x}{2x^2} - \frac{1}{2} \int_x^\infty \frac{\sin y}{y} dy$, and $k_{\rm F}$ and t are the Fermi wave vector involved in the RKKY coupling and thickness of the Ru spacer, respectively. The second term of an oscillatory integration is neglected in fitting. The result gives $k_{\rm F} = 0.28 \,\text{\AA}^{-1}$, which is consistent with Zhao *et al.*'s work [40].

B. Current-driven magnetization reversal of SFi

Now we study current-induced SOT-driven magnetization switching in the AFM coupling samples. We also prepared a $Ta/Pt/[Pt/Co]_2/Ru$ device with only the bottom FM layer as a control group towards the studied SFi devices. Figure 3(a)presents the AHE hysteresis loops of the control sample under in-plane and out-of-plane magnetic fields, which exhibit a square loop indicating a well-defined PMA. Figure 3(b) records the anomalous Hall resistance during the scanning of a current I along the long side of the Hall bar under a fixed external magnetic field of ± 2 kOe parallel to the current (along the x axis). The switching polarity changes as the in-plane magnetic field direction reverses, consistent with the symmetry of current-induced SOT due to spin Hall and interfacial Rashba effects [41]. It is worth mentioning that the sweeping current started from the positive side in Fig. 3(b) and the first switching at negative current is incomplete, as the anomalous Hall resistance difference $\triangle R_{\rm H}$ is about one-half of that in the field-driven AHE measurement in Fig. 3(a). As a result, the switching at positive current occurred earlier, leading to the asymmetry of critical switching current shown in Fig. 3(c).

For the Ta/Pt/[Pt/Co]₂/Ru/[Co/Pt]₄/Pt SFi sample with $t_{Ru} = 1.0$ nm, the representative AHE hysteresis loops and the SOT switching curves are presented in Fig. 3(d) and Fig. 3(e), respectively. The perpendicular interlayer exchange-coupling field H_{IEC} is 4.7 kOe, obtained from the AHE hysteresis loop with the out-of-plane magnetic field. Meanwhile, when the applied in-plane magnetic field along the x axis reaches about 10.7 kOe, both magnetizations of the bottom and the upper FM layers switch to near parallel with the direction of the external magnetic field, as shown in Fig. 3(d). Combining the AHE hysteresis loops and the current-induced SOT switching loops [Fig. 3(e)], we conclude that the magnetization configurations consisting of two FM layers with interlayer AFM coupling are switching between the head-to-head and the tail-to-tail antiferromagnetic states. In the studied SFi sample, the current-induced SOT, mainly generated from the thick bottom Pt layer, acts on its adjacent bottom [Pt/Co]₂ layer and then drives the magnetization switching of the upper [Co/Pt]₄ layer through the dipolar interaction between layers and the interlayer AFM coupling-induced effective IEC field [29].

The critical switching current I_{sw} is defined by the current value where the $R_{\rm H}$ has a 50% switching magnitude in Fig. 3(b) and Fig. 3(e). Figure 3(c) and Fig. 3(f) show that although the thickness of the total magnetic layer in the SFi device is three times that of the FM layer in the control sample, the SFi device still has a comparable I_{sw} value with the single FM device. To straightforwardly compare the current-driven magnetization switching power efficiency between the FM- and SFi-based SOT devices, the critical switching current density J_{sw} was calculated by assuming the applied current flows uniformly in the Hall bar. The J_{sw} of the SFi device is $2.1 \times 10^7 - 2.7 \times 10^7$ A/cm² under the studied in-plane mag-

netic fields, slightly lower than $3 \times 10^7 - 4 \times 10^7$ A/cm² of the single FM control sample. If further considering the current shunting effect arising from the magnetic layer, the J_{sw} in the heavy-metal layers for the SFi device will be much lower than the single FM device. The significant reduction of the critical current density for the SFi device is expected to the additional current-induced SOT exerting on the upper [Co/Pt]₄ layer generated by the top 1-nm-thick Pt layer. As we know, the spin polarization of the spin currents generated from the bottom and top Pt layers are opposite. Moreover, the magnetizations of the bottom and the upper FM layers in the SFi device are antiparallel. Therefore, the bottom and top Pt layers-induced SOTs in the SFi device should be added and significantly reduce J_{sw} .

C. Estimation of current-induced SOT efficiency

The SOT efficiency is a critical factor related to the power consumption and operation speed of the magnetic memory device. It can be quantitatively characterized by the SOT-induced effective magnetic field $H_{\rm eff}$. Here, we will introduce an alternative way from previously reported methods [31,42,43] to characterize current-induced $H_{\rm eff}$ by analyzing current-dependent anomalous Hall resistance R_H under a large out-of-plane magnetic field measurement geometry. Figure 4(a) shows the AHE hysteresis loop of the $t_{Ru} =$ 2.0 nm SFi sample with a relatively weak interlayer AFM coupling $H_{\rm IEC} \sim 1.57$ kOe. Since AHE is proportional to the z component of the magnetization, the anomalous Hall resistivity can be expressed by $\rho_{\rm H} = 4\pi (R_{\rm s}^{\rm b} M_{\rm z}^{\rm b} + R_{\rm s}^{\rm u} M_{\rm z}^{\rm u})$ [34], where R_s^b , M_z^b , R_s^u , and M_z^u are the anomalous Hall coefficient and the z component of the magnetization of the bottom and upper FM layer, respectively. Based on the resistance change between the antiferromagnetic state and ferromagnetic state, we find that the anomalous Hall resistance follows a relation of $R_{\rm H}^{\rm b}$: $R_{\rm H}^{\rm u} = 2$: 3, where $R_{\rm H}^{\rm b}$ and $R_{\rm H}^{\rm u}$ are the anomalous Hall resistance contributed by the bottom FM and the upper FM layers, respectively. This ratio could attribute to the stronger spin-orbit coupling at the interfaces of $Pt(4)/[Pt/Co]_2/Ru(2)$ for the bottom FM layer and $Ru(2)/[Pt/Co]_4/Pt(1)$ for the upper FM layer due to the different thickness of Pt and the different stacking order of FM, Pt, and Ru [44]. The SOT switching curves with the various in-plane magnetic fields and the critical current density are also presented in Fig. 4(b) and Fig. 4(c). Compared to the $t_{Ru} = 1$ -nm SFi device with a large interlayer AFM coupling $H_{\rm IEC} \sim 4.85$ kOe, the $t_{\rm Ru}$ = 2-nm device exhibits a relatively low $J_{\rm sw}$ = 14.5 × 10^{6} –23.2 × 10^{6} A/cm² and a very small assistant in-plane magnetic field $H_{\rm in}^{\rm min} \sim 0.5$ kOe.

Figure 5(a) shows the current-dependent AHE hysteresis loops under different out-of-plane magnetic fields. The current is swept between 27 and -27 mA under different H_{out} varied from 3 to -3 kOe. Unlike the above current-dependent AHE hysteresis loop with inversion symmetry under in-plane fields, $R_{\rm H}$ vs *I* curves under the out-of-plane fields show symmetry and no hysteretic behavior. For instance, when the out-of-plane field of $H_{out} = 3$ kOe is applied, we find that magnetizations of both FM layers in SFi under small currents are forced to align parallel to the external field by directly comparing the value of $R_{\rm H}$ between $R_{\rm H}$ vs *I* and



FIG. 4. Current-induced magnetization switching of the AFM coupling sample $t_{Ru} = 2 \text{ nm}$ under an in-plane magnetic field. (a) Fielddependent R_H hysteresis loops measured with an out-of-plane magnetic field and a small DC current I = 0.5 mA. (b) DC current-dependent R_H hysteresis loops measured with different in-plane magnetic field H_{in} along the direction of applied current. (c) The critical switching current J_c vs in-plane H_{in} .

 $R_{\rm H}$ vs $H_{\rm out}$ loops [Fig. 4(a)]. However, the $R_{\rm H}$ shows a significant decrease with increasing current because currentinduced dampinglike spin-orbit torque tilts the magnetic moments in the FM layer due to the spin Hall and interfacial Rashba effects. $H_{\rm eff} = \sigma \times M$ is perpendicular to the magnetization direction (as σ , denoting the polarization of the spin current generated by the Pt layer, aligns on the *y* axis and *M* on the *z* axis) and causes the reduction of the *z* component of the magnetization and $R_{\rm H}$ in SFi. The bottom and upper Pt layers generate spin currents and exert SOTs on their adjacent FM layers. However, considering the spin-diffusion model [45] and different thicknesses of the bottom ($t_b = 4.6$ nm) and upper Pt layers ($t_u = 1.6$ nm), the current-induced effective magnetic field on the bottom FM layer is much larger than the upper FM layer.

To quantitatively calculate the SOT-induced $H_{\rm eff}$, we first need to preprocess the raw $R_{\rm H}(I)$ data in Fig. 5(a). When $H_{\rm out}$ is lower than $H_{\rm IEC} = 1.57$ kOe with small currents, magnetizations in SFi prefer a perpendicular antiparallel configuration, consistent with the $R_{\rm H}$ vs *I* curves below 15 mA obtained at $H_{\rm out} < 1$ kOe, while $H_{\rm out} > H_{\rm IEC} = 1.57$ kOe, the bottom and upper FM layers are parallel to the external field. Thus, we choose the $R_{\rm H}$ curve obtained at $H_{\rm AP} = H_{\rm out} =$ 0.1 kOe as the reference to remove the background signals consisting of longitudinal resistance and other systematic noise, and extract the current-induced deviation of the $R_{\rm H}$ at high fields. For better mathematical representations and convenience of analysis, we rewrite the anomalous Hall resistance of the bottom FM layers as follows:

$$\Delta R_{\rm H} = R_{\rm H}(I, H_{\rm P}) - R_{\rm H}(I, H_{\rm AP})$$

= $[R_{\rm H}^{\rm u}(I, H_{\rm P}) + R_{\rm H}^{\rm b}(I, H_{\rm P})]$
- $[R_{\rm H}^{\rm u}(I, H_{\rm AP}) - R_{\rm H}^{\rm b}(I, H_{\rm AP})]$
= $R_{\rm H0}^{\rm u}(\cos\theta_{\rm P}^{\rm u} - \cos\theta_{\rm AP}^{\rm u}) + R_{\rm H0}^{\rm b}(\cos\theta_{\rm P}^{\rm b} + \cos\theta_{\rm AP}^{\rm b}), (1)$

where θ is the tilting angle of the magnetic moments from the normal direction of the film and is confined in $-90^{\circ} \sim 90^{\circ}$. The superscripts u, b represent the upper FM layer and the bottom, the subscripts P, AP represent parallel state and antiparallel state, respectively. $R_{\rm H0}^{\rm u} \sim 0.170 \ \Omega$ and $R_{\rm H0}^{\rm b} \sim 0.115 \ \Omega$ are the anomalous Hall resistance of each layer with their magnetic moments along the normal direction of film at room temperature, determined from the out-of-plane AHE loop in Fig. 4(a). If taking into account the Joule heating effect on the magnetization of the FM layer under a large current, we include an additional current modification of $R_{\rm H}^{\rm u,b}$ = $R_{\rm H0}^{\rm u,b}(1-\beta J^2)$, where β is a relevant heating effect coefficient. Combined with the balance condition of magnetization of each layer $M \times (H_{out} + H_k - H_{IEC}) = M \times H_{eff}$, the external out-of-plane field H_{out} , effective PMA field H_k , interlayer exchange-coupling field H_{IEC} , and SOT effective field H_{eff} are



FIG. 5. Quantitative analysis of the current-induced SOT effective field of the AFM coupling sample $t_{Ru} = 2 \text{ nm}$. (a) The raw currentdependent anomalous Hall resistance R_H under a series of out-of-plane magnetic fields. The raw $R_H(I)$ includes a significant background noise consisting of the longitudinal resistance due to asymmetrically manufactured lateral electrodes, the Joule heating effect, and other systematic noise. (b) The difference of R_H between the parallel state at high fields and the antiparallel state at the low field, $H_{out} = 0.1 \text{ kOe}$. (c) Experimental data (symbol) and numerical fitting curves (solid lines) under $H_{out} = 3 \text{ kOe}$.

TABLE I. Calculated results of the effective SOT efficiency $\chi = H_{\text{eff}}/J$, the effective PMA field H_{k} , the IEC field H_{IEC} , and the heating effect coefficient β .

Experiment <i>R</i> _H vs <i>I</i> curves	$\beta(\times 10^{-4})$	χ [Oe/(10 ⁶ A/cm ²)]
$H_{\rm out} = 3 \rm kOe$	9.51	56.40
$H_{\rm out} = -3 \rm kOe$	9.41	58.64
Average values	9.46	57.52

canceled out. Considering that H_{out} and H_k are perpendicular to the sample film plane, H_{IEC} is antiparallel to the other FM layer, H_{eff} is perpendicular to the magnetic moments, and the vector balance equation can be reduced to a scalar form:

 $H_{\text{out}}\sin\theta_{\text{P}}^{\text{u}} + H_{\text{k}}^{\text{u}}\cos\theta_{\text{P}}^{\text{u}}\sin\theta_{\text{P}}^{u} - H_{\text{IEC}}^{\text{u}}\sin\left(\theta_{\text{P}}^{\text{u}} + \theta_{\text{P}}^{\text{b}}\right) = H_{\text{eff}}^{\text{u}}, \quad (2)$ $H_{\text{out}}\sin\theta_{\text{P}}^{\text{b}} + H_{\text{k}}^{\text{b}}\cos\theta_{\text{P}}^{\text{b}}\sin\theta_{\text{P}}^{\text{b}} - H_{\text{IEC}}^{\text{b}}\sin\left(\theta_{\text{P}}^{\text{u}} + \theta_{\text{P}}^{\text{b}}\right) = H_{\text{eff}}^{\text{b}}, \quad (3)$ $H_{\text{out}}\sin\theta_{\text{AP}}^{\text{u}} + H_{\text{k}}^{\text{u}}\cos\theta_{\text{AP}}^{\text{u}}\sin\theta_{\text{AP}}^{\text{u}} - H_{\text{IEC}}^{\text{u}}\sin\left(\theta_{\text{AP}}^{\text{u}} - \theta_{\text{AP}}^{\text{b}}\right) = H_{\text{eff}}^{\text{u}}, \quad (4)$

$$H_{\text{out}}\sin\theta^{b}_{\text{AP}} + H^{b}_{\text{k}}\cos\theta^{b}_{\text{AP}}\sin\theta^{b}_{\text{AP}} - H^{b}_{\text{IEC}}\sin\left(\theta^{u}_{\text{AP}} - \theta^{b}_{\text{AP}}\right) = H^{b}_{\text{eff}}.$$
(5)

We determined the effective PMA field of the bottom FM layer $H_k^b = 5.69$ kOe by fitting the in-plane AHE hysteresis loop of Ta/Pt/[Pt/Co]₂/Ru control sample by the equation $\frac{R_{\rm H}}{R_{\rm H0}} = \frac{H}{\sqrt{H^2 + H_k^2}}$. The overall PMA field of the SFi sample including the bottom and top FM layers was estimated by the area difference between the in-plane and out-of-plane magnetization loop [46], and then the effective PMA field of the upper FM layer $H_k^u = 2.10$ kOe was able to be deducted. The result shows that despite a relatively thick Ru spacer inserted between the upper and the bottom Co/Pt multilayers, the upper one still exhibits a considerable PMA and the SFi sample shows an overall PMA [Fig. 4(a)], consistent with the previous reports [46,47]. Considering the spin-diffusion model [45], the effective spin Hall angle is expressed by $\xi_{\rm DL} = \theta_{\rm DL} [1 - \operatorname{sech}(t_{\rm Pt}/\lambda_{\rm SF})]$, where $\theta_{\rm DL}$ is the intrinsic spin Hall angle of heavy metal. Taking the spin-diffusion length of Pt as 1.4 nm [14], the thickness is 1.6 and 4.6 nm for the upper and bottom Pt layers, respectively. Therefore, the ξ_{DL} of the upper Pt layer is about 4/9 of the bottom one and so is the effective SOT efficiency.

Figure 5(c) shows the calculation result vs the experiment data, which is numerically solved by the balance equation under $H_{out} = 3$ kOe with (solid red line) and without (solid blue line) considering the Joule heating effect. The obtained effective SOT efficiency $\chi = H_{eff}/J$ is summarized in Table I, where J is the current density of the total multilayer, calculated by assuming a uniform current density distribution.

From Table I, the SOT efficiency in our SFi sample with $t_{\text{Ru}} = 2.0 \text{ nm}$ reaches ~ 57.52 Oe/(10⁶ A/cm²), much higher than the previously reported value of 22 Oe/(10⁶ A/cm²) in the SAF Pt/[Co/Pd/Co]/Ru/[Co/Pd/Co] only with single Pt

layer [31] and one order larger than $7.5 \text{ Oe}/(10^6 \text{ A/cm}^2)$ in the single ferromagnetic Pt/Co/MgO system [42]. In these previous works, the quantitative calculation method of the SOT efficiency follows the scenario that magnetization-switching behavior is caused by currentinduced magnetic domain-wall motion. The Pt/FM with strong interfacial PMA and Dzyaloshinskii-Moriya interaction tends to form the Néel-type domain walls, where the magnetization moments in the domain wall are in the film plane so that the current-induced SOT effective field on the domain wall is perpendicular to the film plane. Opposite currents would facilitate or hinder domain-wall motion, resulting in the shift of the coercive field [42,43]. As a comparison, our method is based on the quasistatic process of the magnetization balance under the several external fields and the current-induced SOT effective field. In our measurement configuration, the upper and bottom FM layers are forced to a single domain by the large external out-of-plane field. Both the upper and bottom Pt layers inject spin currents with opposite polarity, tilting magnetizations of the adjacent FM layers and causing the reduction in anomalous Hall resistance. In addition, our method can avoid the complicated interference to the first- and second-harmonic Hall resistances under in-plane magnetic field measurement configuration caused by current-induced magnetic domain motion in the electrical heterodyne detection of current-induced SOT effective field [48-50]. For convenient comparison, we also calculated the effective spin Hall angle given by $\chi = \frac{\pi}{2} \frac{\hbar \xi_{\text{DL}}}{2e\mu_0 M_s f_{\text{FM}}}$ [42], where M_s is the saturated magnetization, $t_{\rm FM}$ is the thickness of FM layer, $\xi_{\rm DL}$ is the effective spin Hall angle; as well, \hbar , e, and μ_0 are the Planck constant, elementary charge, and vacuum permeability, respectively. In our $t_{Ru} = 2.0$ -nm SFi sample, $t_{FM} =$ $M_{\rm s} = 1020$ 0.6 nm and emu/cm³, $\chi =$ 57.52 Oe/(10⁶ A/cm²), and the calculated ξ_{DL} from the above formula is ~ 0.68 , also larger than the previously reported $\xi_{DL} \sim 0.47$ in completely compensated SAF system [31]. The different calculating models based on distinct physical scenarios obtain a slightly larger value of ξ_{DL} in the different Pt-based SAF systems, indicating the validity of our calculating model based on our proposed balance equation of magnetization under the out-of-plane field geometry. Moreover, our results demonstrate that using bottom and top Pt layers adjacent to the AFM coupling two FM layers in the SFi can significantly enhance current-induced effective SOT efficiency and provide a simple, easy method to implement and feasible approach for the development of energy-efficient SFi-based spin-orbitronics.

IV. CONCLUSIONS

In summary, we experimentally determined the oscillating interlayer exchange coupling as a function of Ru spacer-layer thickness with a period of 1.16 nm in a Ta/Pt/[Pt/Co]₂/Ru(t_{Ru})/[Co/Pt]₄/Pt stacked multilayer with a strong perpendicular magnetic anisotropy. Furthermore, in the first ($t_{Ru} = 1 \text{ nm}$) and the second ($t_{Ru} = 2 \text{ nm}$) interlayer AFM coupling regime SFi multilayers, we demonstrated current-induced SOT-driven magnetization reversal between the two antiferromagnetic

states. From the critical switching current directly compared with the single FM control sample and quantitative calculation of SOT-induced dampinglike effective field, our results suggest that the double enhancement of current-induced SOT efficiency generated by the high-conductivity Pt could be achieved through combining antiparallel magnetization configuration due to interlayer AFM coupling and opposite spin polarization at the bottom and top surfaces of Pt. Our results demonstrate that the SFi-based spin-orbitronics will be a practical approach to developing high-density, low-power consumption, fast-speed, high-durability nonvolatile memory devices because it possesses several advantages of reduced stray field, low critical operation current, and high thermal stability.

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