

## Microscopic probe of magnetic polarons in antiferromagnetic $\text{Eu}_5\text{In}_2\text{Sb}_6$

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Colossal magnetoresistance (CMR) emerges from intertwined spin and charge degrees of freedom in the form of ferromagnetic clusters also known as trapped magnetic polarons. As a result, CMR is rarely observed in antiferromagnetic materials. Here we use electron spin resonance (ESR) to reveal microscopic evidence of the formation of magnetic polarons in antiferromagnetic  $\text{Eu}_5\text{In}_2\text{Sb}_6$ . First, we observe a reduction of the  $\text{Eu}^{2+}$  ESR linewidth as a function of the applied magnetic field consistent with ferromagnetic clusters that are antiferromagnetically coupled. Additionally, the  $\text{Eu}^{2+}$  line shape changes markedly below  $T' \sim 200$  K, a temperature scale that coincides with the onset of CMR. The combination of these two effects provides strong evidence that magnetic polarons grow in size below  $T'$  and start influencing the macroscopic properties of the system.

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### I. INTRODUCTION

Low-carrier-density materials containing divalent europium are prone to exhibiting colossal magnetoresistance (CMR) [1,2], and one explanation for this phenomenon is the formation of magnetic polarons [3]. These quasiparticles are a result of free carriers at low densities that self-trap in ferromagnetic clusters around  $\text{Eu}^{2+}$  local moments [4]. There are several Eu-based materials with different crystal structures and magnetic ground states that host these emergent quasiparticles, but most of these systems display ferromagnetic order at low temperatures [3,5–9].

With the advent of nontrivial topology in condensed-matter physics, a question that naturally arises is the role of topology in strongly correlated systems such as those exhibiting CMR [10,11]. Further, the interplay between magnetism and nontrivial band topology is predicted to give rise to emergent topological quantum phenomena, such as the axion insulating state in  $\text{MnBi}_2\text{Te}_4$  [12–15]. Just like  $\text{Mn}^{2+}$  in  $\text{MnBi}_2\text{Te}_4$ ,  $\text{Eu}^{2+}$  could play a similar role in a nontrivial background. Motivated by the prediction of topological phases in nonsymmorphic crystal structures [16], here we focus on nonsymmorphic  $\text{Eu}_5\text{In}_2\text{Sb}_6$ , which was recently synthesized in single-crystalline form [17]. Band structure calculations for the uncorrelated analog  $\text{Ba}_5\text{In}_2\text{Sb}_6$  reveal conflicting results regarding its topology [18–23], and a microscopic investigation of these materials is imperative.

Orthorhombic  $\text{Eu}_5\text{In}_2\text{Sb}_6$  has three distinct  $\text{Eu}^{2+}$  sites, which give rise to two antiferromagnetic (AFM) transitions at  $T_{N1} = 14$  K and at  $T_{N2} = 7$  K.  $\text{Eu}_5\text{In}_2\text{Sb}_6$  also exhibits CMR that peaks at  $-99.999\%$  for magnetic fields of  $H = 9$  T and temperatures just above  $T_{N1}$ . Recent studies argue that magnetic polarons start to form below  $T' \approx 210$  K, a temperature scale characterized by different macroscopic signatures: a deviation from the Curie-Weiss law, the appearance of an anomalous Hall effect, and the onset of CMR [17].

The strong exchange interaction between conduction electrons and  $\text{Eu}^{2+}$   $4f$  moments combined with the lack of an orbital moment in  $\text{Eu}^{2+}$  ions makes  $\text{Eu}_5\text{In}_2\text{Sb}_6$  an ideal test bed to be explored by electron spin resonance (ESR). The ESR linewidth  $\Delta H$  is inversely proportional to the spin-spin relaxation time  $T_2$ , which can be affected by internal fields, a distribution of exchange interactions, and the spin-flip scattering between the  $4f$  moments and conduction electrons [24–26]. The latter is also known as the Korringa mechanism. Additionally, the  $g$  value, which is proportional to the resonance field  $H_r$ , also gives information about internal fields and their nature as well as the interaction between  $4f$  moments and the conduction electrons [25,26]. In systems with magnetic polarons, the spin-flip scattering is reduced as a function of the applied magnetic field  $H$ , which is accompanied by a negative MR due to the increase of the quasiparticle size. Consequently,  $T_2$  increases, and there is an unusual narrowing of  $\Delta H$  as a function of  $H$  [27]. ESR was previously employed to investigate magnetic polarons in  $\text{EuB}_6$  [27] and Eu-based clathrates [28] as well as in  $d$ -electron systems in combination with muon spin rotation [29–32].

In this paper, we report a microscopic ESR investigation of  $\text{Eu}_5\text{In}_2\text{Sb}_6$  [17] as a function of different microwave frequencies and crystallographic directions. The reduction of the  $\text{Eu}^{2+}$  ESR linewidth as a function of  $H$  is a microscopic fingerprint of the presence of ferromagnetic clusters. Importantly, below  $T' \approx 200$  K a marked change in the  $\text{Eu}^{2+}$  ESR line shape is driven by the increase of the microwave skin depth effect. These two experimental results not only provide evidence of the presence of magnetic polarons in this system but also demonstrate that polarons start to influence the macroscopic properties of the system at  $T' \approx 200$  K.

Importantly, the  $\text{Eu}^{2+}$  spin dynamics sheds light on the relevant magnetic exchange interactions in  $\text{Eu}_5\text{In}_2\text{Sb}_6$ . The  $\text{Eu}^{2+}$  ESR  $\Delta H$  angle dependence reveals an anisotropy in the spin-flip scattering that resembles that of the electrical

resistivity, which suggests that the observed angular dependence is connected to a residual Fermi surface anisotropy. The  $\text{Eu}^{2+}$  ESR temperature-dependent  $g$  value shows a slight, but systematic, reduction as a function of  $H$ , which corroborates the presence of AFM correlations between polarons. Finally, the temperature and angle dependences of the  $g$  value for different crystallographic directions reveals an interplay of FM and AFM short-range interactions in the  $ab$  plane and a FM component along the  $c$  axis.

## II. METHODS

Single-crystalline samples of  $\text{Eu}_5\text{In}_2\text{Sb}_6$  were synthesized by a combined In-Sb flux described elsewhere [17]. Resistivity measurements were performed using a four-probe configuration in a commercial low-frequency AC bridge in voltage mode with an applied voltage of  $V = 200 \mu\text{V}$ . ESR measurements were performed for single crystals in  $X$ -band ( $\nu = 9.4$  GHz) and  $Q$ -band ( $\nu = 34$  GHz) commercial spectrometers equipped with a goniometer and a He-flow cryostat in the temperature range of  $15 \leq T \leq 300$  K. The crystals have a rodlike shape, and the  $c$  axis is the long axis. Typical sample sizes are  $0.5 \times 0.5 \times 3 \text{ mm}^3$ . Particular care was taken to avoid any possible sample size effects in the ESR measurements. Due to the smaller cavity and the crystal shape we were not able to obtain  $Q$ -band measurements for fields applied parallel to the  $c$  axis. The ESR spectra were analyzed using the software SPEKTROLYST.

## III. RESULTS AND DISCUSSION

Figures 1(a) and 1(b) show the  $\text{Eu}^{2+}$  ESR spectra with  $H$  parallel to the  $b$  axis at  $T = 300$  K for the  $X$  and  $Q$  bands, respectively. The  $b$  axis is identified in the inset of Fig. 1(a). The red solid lines are the best fits to the  $\text{Eu}^{2+}$  ESR spectra, represented by the power absorption derivative  $dP/dH$  as a function of  $H$ :

$$\frac{dP}{dH} \propto (1 - \alpha) \frac{d}{dx} \left( \frac{1}{1 + x^2} \right) + \alpha \frac{d}{dx} \left( \frac{x}{1 + x^2} \right), \quad (1)$$

where  $\alpha$  is the asymmetric parameter of the line shape and  $x = 2(H - H_r)/\Delta H$  [33]. As shown in Fig. 1, there is a reduction of the  $\text{Eu}^{2+}$  ESR  $\Delta H$  from low ( $X$  band) to high frequency ( $Q$  band) even at room temperature. This reduction reveals that the  $\text{Eu}^{2+}$  resonance is homogeneous in the paramagnetic state, indicating the good quality of the samples, and that there is a reduction of the spin-flip scattering as a function  $H$ .

The asymmetry of the  $\text{Eu}^{2+}$  ESR line shape, which will be reflected in the  $A/B$  ratio defined in Fig. 1(b), is a consequence of the microwave skin depth  $\delta = \sqrt{\rho/\pi\nu\mu_0\mu_r}$ , where  $\rho$  is the resistivity,  $\mu_0$  is the vacuum permeability, and  $\mu_r$  is the relative permeability. The skin depth, in a semiclassical view, is a consequence of the local shielding currents of carriers driving electromagnetic fields out of phase [25,26,34,35]. In other words, the evolution of  $\delta$  is a reflection of the evolution of the local AC resistivity around our  $\text{Eu}^{2+}$  probe [36–38]. If the sample size  $L$  is much smaller than  $\delta$ , one obtains a symmetric Lorentzian line shape ( $A/B = 1$ ;  $\alpha = 0$ ). In a metallic environment, the thickness to skin depth ratio  $\lambda = L/\delta \gg 1$ ,

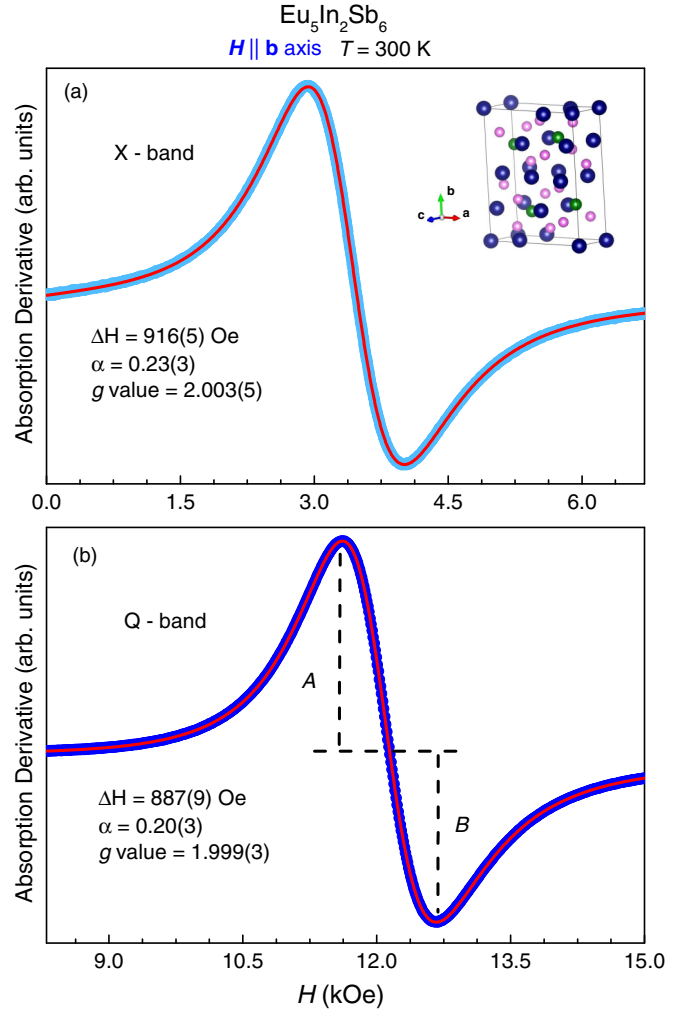


FIG. 1. (a)  $X$ - and (b)  $Q$ -band  $\text{Eu}^{2+}$  ESR spectra for  $\text{Eu}_5\text{In}_2\text{Sb}_6$ .  $H$  is applied parallel to the  $b$  axis. The inset in (a) shows the crystalline structure.  $A$  ( $B$ ) shown in (b) denotes the distance from the base line to the peak (valley). The red solid lines are fits explained in the text.

and one obtains a Dysonian line shape ( $A/B \approx 2.7$ ,  $\alpha \approx 0.55$ ) [33,39].

The Dyson model for the  $\lambda$  dependence of  $\alpha$  considers the microwave penetration in a flat plate [40,41]. In this model,  $\alpha$  is given by

$$\alpha = \frac{\sinh^2\lambda - \sin^2\lambda}{(\cosh\lambda + \cos\lambda)^2}. \quad (2)$$

Figure 2(a) shows the  $T$  dependence of  $\lambda$ , which is derived from DC electrical resistivity, in  $\text{Eu}_5\text{In}_2\text{Sb}_6$  for two different  $H$ . Because the difference between zero field and 1 T is negligible, we used the zero-field resistivity to simulate the  $T$  dependence of  $\alpha$  for the  $X$  band, as shown by the red solid line in Fig. 2(b). Below  $T' \approx 200$  K, there is a clear decrease of  $\alpha$  for all crystallographic axes. This temperature scale coincides with the onset of CMR and the deviation of the Curie-Weiss behavior [17]. Our results therefore corroborate the scenario in which the formation of trapped magnetic polarons reduces the number of free carriers, changing the environment around

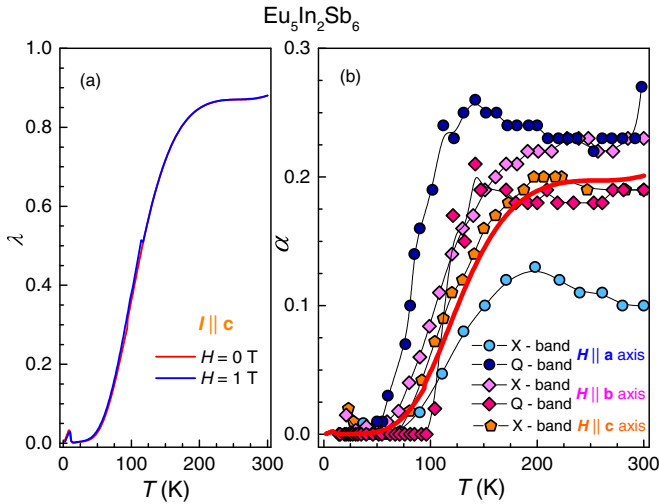


FIG. 2. (a)  $\lambda$  for current  $I$  applied parallel to the  $c$  direction and (b)  $\alpha$  for different directions and microwave frequencies as a function of temperature. The red solid line is a simulation described in the text.

the  $\text{Eu}^{2+}$  site concomitantly with the global properties, which in turn increases the microwave penetration.

To uncover the anisotropy of  $\text{Eu}_5\text{In}_2\text{Sb}_6$ , we turn to the angle dependence of the  $\text{Eu}^{2+}$  ESR  $\Delta H$  and  $g$  factor at  $T = 35$  and  $300$  K, shown in Fig. 3. The anisotropy of  $\Delta H$  in the  $ab$  plane is less pronounced than its out-of-plane anisotropy, which suggests the presence of an orthorhombic contribution due to weak crystal field effects [26,42]. Nonetheless, the  $\text{Eu}^{2+}$  ESR  $\Delta H$  is also connected to  $T_2$ , and the resistivity anisotropy in the  $ab$  plane resembles the anisotropy in  $\Delta H$ , as shown in Fig. 3(b). A similar angular dependence for both physical quantities indicates the presence of anisotropic magnetic scattering stemming from anisotropic magnetic interactions between  $\text{Eu}^{2+}$  ions. In fact, a  $g$  factor

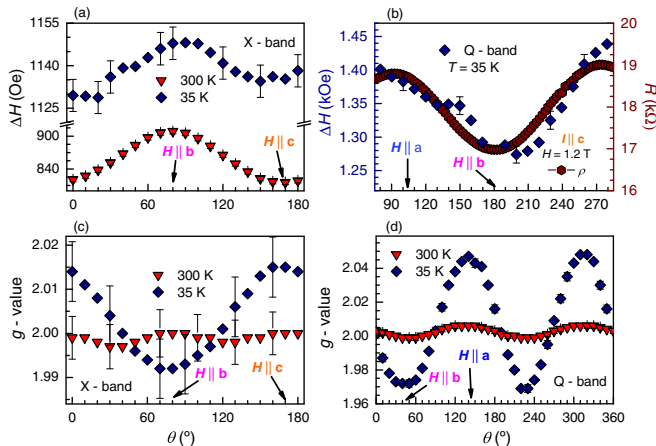


FIG. 3. Anisotropy of the (a)  $X$ - and (b)  $Q$ -band  $\text{Eu}^{2+}$  ESR  $\Delta H$ . The current  $I$  was applied parallel to the  $c$  axis in the resistivity measurement. The brown hexagonal symbols show the resistivity anisotropy at  $T = 35$  K. (c)  $X$ - and (d)  $Q$ -band  $\text{Eu}^{2+}$   $g$ -value anisotropy at  $T = 300$  and  $35$  K. The anisotropy in the  $X$  band went from  $H$  applied parallel from the  $b$  to the  $c$  axis, while  $H$  was applied from the  $b$  to the  $a$  axis in the  $Q$  band.

anisotropy is observed even at room temperature, as shown in Figs. 3(c) and 3(d). The experimental  $\text{Eu}^{2+}$   $g$  value,  $g = h\nu/\mu_B H_r$ , is obtained from the analysis of the  $\text{Eu}^{2+}$  ESR spectra using Eq. (1). Here  $h$  is the Planck constant, and  $\mu_B$  is the Bohr magneton.  $\text{Eu}^{2+}$  is a localized  $S$  ion ( $L = 0$ ), and its second-order crystal field effects cannot account for the  $g$ -value anisotropy [25–27,43]. Therefore, such anisotropy is an indication that even at room temperature short-range magnetic interactions are substantial in  $\text{Eu}_5\text{In}_2\text{Sb}_6$ , a rare occurrence in localized  $4f$ -electron materials. At  $T = 35$  K, the anisotropy is even more pronounced. Such  $g$ -value anisotropy typically stems from internal fields and supports the presence of complex magnetic interactions in the paramagnetic phase of  $\text{Eu}_5\text{In}_2\text{Sb}_6$ . Demagnetization effects do not fully describe the  $g$ -factor anisotropy (see the Appendix).

Figures 4(a) and 4(b) show the  $T$  dependence of the  $\text{Eu}^{2+}$  ESR  $\Delta H$  for two different microwave frequencies at high and low temperatures, respectively. Figure 4(a) shows a systematic reduction of the  $\text{Eu}^{2+}$  ESR  $\Delta H$  at higher  $H$  ( $Q$  band) at high temperatures. Such a reduction appears even at room temperature, which can be explained by a reduction of the spin-flip scattering. According to Ref. [17], the dominant coupling between  $4f$  local moments and conduction electrons at high temperatures is ferromagnetic, and the resulting ferromagnetic clusters therefore increase in size as a function of  $H$  [26,35]. Although the high-temperature data show a reduction of the  $\text{Eu}^{2+}$   $\Delta H$ , a Korringa-like behavior of the  $\text{Eu}^{2+}$   $\Delta H$   $T$  dependence is absent. Korringa behavior is reflected in the positive linear-in- $T$  dependence of  $\text{Eu}^{2+}$   $\Delta H$ . This result indicates that, even at high temperatures, the internal fields due to  $\text{Eu}^{2+}$  spin-spin interaction are dominant.

Notably, below  $T^* \sim 50$  K the  $\text{Eu}^{2+}$  ESR linewidth increases rapidly with decreasing temperature [Fig. 4(b)]. This crossover region likely stems from the strong short-range interactions between polarons as previously suggested by the breakdown in activated behavior in resistivity, the strong AFM correlations in magnetic susceptibility, and the Schottky anomaly of the specific heat [17]. Because the  $\text{Eu}_5\text{In}_2\text{Sb}_6$  structure hosts three different  $\text{Eu}^{2+}$  sites, complex local magnetic fields and anisotropic  $\text{Eu}^{2+}$  spin-spin interactions are expected. Anisotropic short-range magnetic interactions create different magnetic environments, which results in inhomogeneous broadening [26,35,44]. This type of broadening is expected when strong local internal magnetic fields start to play a role, which in the case of  $\text{Eu}_5\text{In}_2\text{Sb}_6$  occurs near a magnetic transition with enhanced interactions between polarons. As a matter of comparison, at  $T^* \sim 50$  K the  $\text{Eu}^{2+}$  ESR line shape starts to distort for the  $X$  band, which explains the small upturn in  $\alpha$  observed in this region in Fig. 2(b). This is another indication that inhomogeneous broadening is responsible for such a crossover region.

Figures 4(c) and 4(d) show the  $\text{Eu}^{2+}$  ESR  $g$  value as a function of temperature. At high temperatures, there is a systematic reduction of the  $\text{Eu}^{2+}$   $g$  value as the frequency is increased from the  $X$  to  $Q$  band. This reduction stems from short-range interactions between  $\text{Eu}^{2+}$  ions, which generates local AFM fields. Positive  $g$  values are related to FM internal fields, whereas negative  $g$  values result from AFM interactions. Therefore, a systematic reduction of the  $g$  value as a function of  $H$  will result in an increase of AFM internal fields

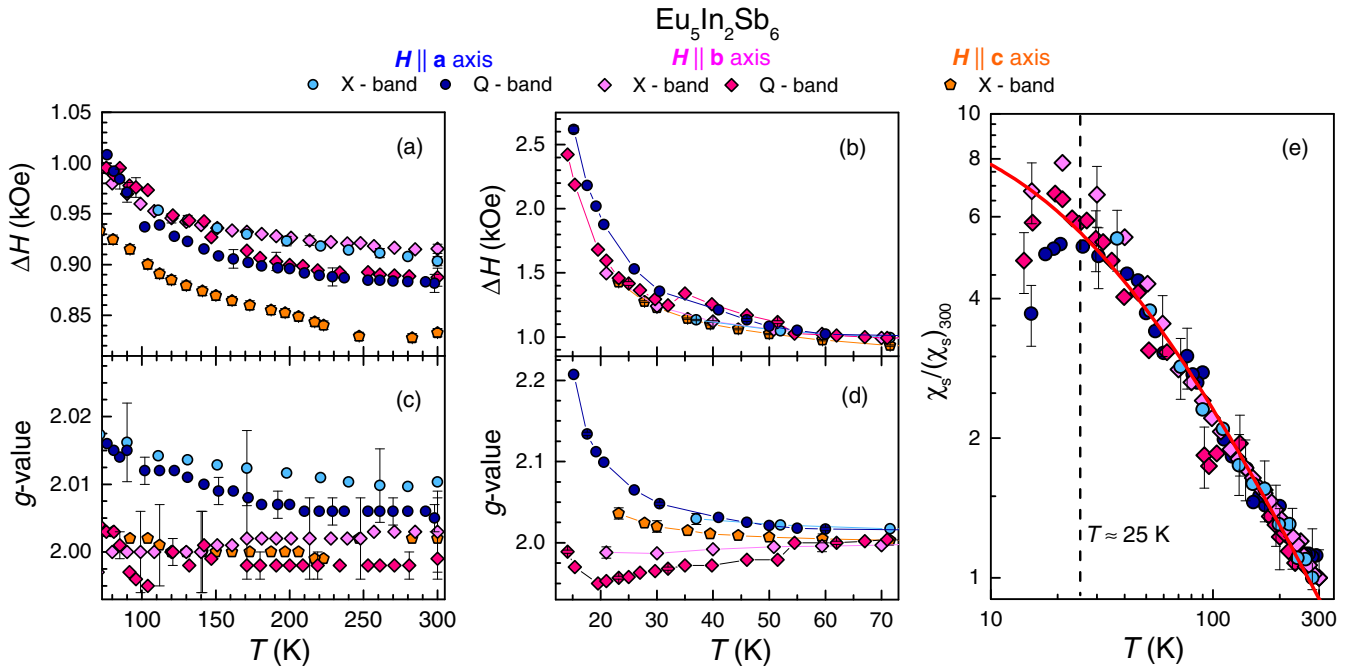


FIG. 4. High ( $70 \leq T \leq 300$  K) and low ( $15 \leq T \leq 70$  K)  $T$  dependences of the  $\text{Eu}^{2+}$  ESR (a) and (b)  $\Delta H$  and (c) and (d)  $g$  value for  $X$  and  $Q$  bands for different crystallographic directions. The solid lines are guides to the eye. (e)  $\text{Eu}^{2+}$  spin susceptibility  $\chi_s$ , normalized by its value at  $T = 300$  K for different crystallographic directions. The red solid line is a Curie-Weiss-like curve with  $\theta = -28$  K.

as a function of the microwave frequency. This result supports the magnetic polaron scenario and shows microscopically that the interaction between polarons is AFM.

Because the  $g$  value is an important probe of local magnetic interactions, a closer look at its temperature dependence in the paramagnetic phase can provide insights into the magnetic structure of  $\text{Eu}_5\text{In}_2\text{Sb}_6$  below  $T_{N1}$ . Figure 4(d) shows the low-temperature behavior of the  $\text{Eu}^{2+}$   $g$  value. Along the  $c$  and  $a$  axes, the  $g$  value increases on cooling, whereas a decrease is observed along the  $b$  axis. The  $g$ -value temperature dependence for  $T \geq 20$  K sheds light on the complex magnetic structure of  $\text{Eu}_5\text{In}_2\text{Sb}_6$  that arises from competing AFM and FM interactions in the  $ab$  plane where the spins lie. In particular, a FM component along  $a$  is consistent with the small net moment and the increase of the magnetic susceptibility on cooling through  $T_{N1}$  for fields applied along the  $a$  axis [17]. This magnetic structure differs from the proposed axion insulator scenario [17], which invites spectroscopic measurements to determine the magnetic structure of  $\text{Eu}_5\text{In}_2\text{Sb}_6$  as well as further calculations taking into account the experimentally determined magnetic structure.

An alternative scenario to the  $\text{Eu}^{2+}$  spin dynamics could rely on the opening of a spin gap [45–48] rather than magnetic polarons physics. In general, such an opening is less expected in  $\text{Eu}^{2+}$ -based compounds due to their negligible spin-orbit coupling. The experimental signature of a spin gap should be observed in the  $\text{Eu}^{2+}$  spin susceptibility  $\chi_s$  [48–51]. Figure 4(e) shows  $\chi_s \propto g^2 I_{\text{ESR}}$ , where  $I_{\text{ESR}}$  is the  $\text{Eu}^{2+}$  ESR intensity, as a function of temperature:  $\chi_s$  is normalized by its value at 300 K.  $\chi_s$  shows a Curie-Weiss-like behavior [ $\chi_s \propto 1/(T - \theta)$ , where  $\theta$  is the Curie-Weiss temperature, red solid line] with  $\theta = -28$  K. The obtained  $\theta$  is at the same magnitude as the  $\theta$  obtained by magnetization ( $\sim 30$  K) [17], but

with opposite sign. The negative sign reflects the presence of an AFM ground state. For  $T \leq 25$  K there is a clear reduction of  $\chi_s$ . In addition, the opening of a spin gap, if present, would also be evidenced in the ESR spin dynamics. The  $\text{Eu}^{2+}$   $\Delta H$  and  $g$  value greatly increase at this temperature range for all directions [Figs. 4(b) and 4(d)]. More specifically, there is an increase of the  $g$  value for  $H$  parallel to the  $b$  axis for  $T \leq 20$  K, which could be interpreted as another signature of a spin gap opening; however, other mechanisms such as short-range interactions or strong magnetic fluctuations could also be associated with all these signatures. Nonetheless, such signatures for  $T \leq 20$  K clearly show that the effects at higher temperatures are not associated with the opening of a spin gap or strong magnetic fluctuations and most likely originate from the magnetic polarons physics.

Our results shed microscopic light on three basic energy scales:  $T' \sim 200$  K,  $T^* \sim 50$  K, and  $H$  dependence. At  $T' \sim 200$  K, trapped magnetic polarons start to become sizable, which causes a decrease in carrier density. An increase in  $\delta$  is therefore observed on cooling, and consequently, a change in the  $\text{Eu}^{2+}$  line shape takes place. Conversely, the effect of  $H$  is to polarize more carriers around the  $\text{Eu}^{2+}$  magnetic ions, which gives rise to spin-dependent scattering. As a result we obtain a reduction of the spin-flip scattering, which causes unusual narrowing of the  $\text{Eu}^{2+}$  linewidth, and, macroscopically, a CMR [17]. Although decreasing the temperature at a constant  $H$  also increases the size of the magnetic polarons, this effect does not dramatically change the spin-dependent scattering, as evidenced by the  $\text{Eu}^{2+}$  ESR  $\Delta H$   $T$  dependence for  $T \geq 150$  K. If the spin-flip scattering were to decrease significantly, we would obtain an increase of the difference of the  $\text{Eu}^{2+}$   $X$ - and  $Q$ -band linewidths as a function of temperature, which is not the case [Fig. 4(a)]. At  $T^* \sim 50$  K, the trapped

polarons start to interact, which results in different magnetic states at the  $\text{Eu}^{2+}$  site and the appearance of inhomogeneous broadening. Note that magnetic polarons are still localized at  $T^*$  because an insulating Lorentzian  $\text{Eu}^{2+}$  line shape is still observed and the resistivity still increases on cooling. This is consistent, for instance, with the appearance of AFM correlations in the magnetic susceptibility at  $T^* \sim 40$  K [17]. Finally, at  $T_{N1}$  the polarons become delocalized, which results in a significant drop in the resistivity of  $\text{Eu}_5\text{In}_2\text{Sb}_6$  [17].

#### IV. CONCLUSION

In summary, we performed electron spin resonance in the antiferromagnetic insulator  $\text{Eu}_5\text{In}_2\text{Sb}_6$  using different microwave frequencies in the temperature range of  $15 \leq T \leq 300$  K. Our  $\text{Eu}^{2+}$  ESR spin dynamics analysis revealed a decrease of the  $\text{Eu}^{2+}$  ESR linewidth when going from low to higher  $H$ , consistent with the presence of ferromagnetic clusters. Below  $T' \sim 200$  K, the change in the asymmetry of the  $\text{Eu}^{2+}$  line shape reveals a marked change in  $\delta$  due to the increase in the magnetic polaron size. At  $T^* \sim 50$  K, strong interpolaron antiferromagnetic interactions cause an inhomogeneous broadening and  $g$ -value changes due to anisotropic short-range interactions. Our microscopic analysis sheds light on the complex magnetic structure of  $\text{Eu}_5\text{In}_2\text{Sb}_6$  and invites other spectroscopic measurements to investigate its putative axion insulating phase.

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#### APPENDIX: DEMAGNETIZATION EFFECTS

Demagnetization effects are important whenever systems are uniformly magnetized [52]. In other words, if the sample size is small compared to the skin depth of the microwave, we

should look for such effects. The anisotropy of the  $g$  value could be a result of the shape of the crystal and may not necessarily be due to an intrinsic magnetic anisotropy [43,53].

In our case, the skin depth at  $T = 300$  K is  $\delta^{300K} = 0.2$  mm, while for  $T = 35$  K it is  $\delta^{35K} = 25$  mm. Due to our sample dimensions ( $0.5 \times 0.5 \times 3$  mm<sup>3</sup>), we are going to evaluate only the effects at  $T = 35$  K. The resonance frequency in the presence of demagnetization effects is given by

$$\omega_0^2 = \gamma^2 [H + (N_y - N_z)M][H + (N_x - N_z)M], \quad (\text{A1})$$

where  $\gamma = e/mc$  is the gyromagnetic factor,  $H$  is the applied magnetic field,  $M$  is the magnetization, and  $N_i$  ( $i = x, y, z$ ) is the demagnetizing factors, with  $\sum_i N_i = 1$  [52,53]. The simplest case is the thin plate, where  $N_x = N_y = 0$  and  $N_z = 1$  when the magnetic field is perpendicular to the plate [52].

For a paramagnetic material we have  $M = \chi H$ , where  $\chi$  is the magnetic susceptibility. We also note that

$$g = \frac{\hbar\omega_0}{\mu_B H} = \frac{g_e}{H} \sqrt{[H + (N_y - N_z)M][H + (N_x - N_z)M]}, \quad (\text{A2})$$

where  $\mu_B$  is the Bohr magneton,  $\hbar$  is the Planck constant divided by  $2\pi$ , and  $g_e \approx 2.002$  is the free-electron  $g$  value. Using Eq. (A2) in (A1) and the fact that we are probing the paramagnetic phase, we obtain

$$g = g_e \sqrt{[1 + (N_y - N_z)\chi][1 + (N_x - N_z)\chi]}. \quad (\text{A3})$$

In order to analyze  $N_i$ , as a first approximation, we assumed a rectangular prism form of the measured crystals. A complete description of the method to obtain the demagnetizing factors for a rectangular prism is given in Ref. [54]. We obtain  $N_x = N_z \approx 0.46$ ,  $N_y \approx 0.08$  when  $H$  is parallel to the  $a$  axis;  $N_y = N_z \approx 0.46$ ,  $N_x \approx 0.08$  for  $H$  parallel to the  $b$  axis; and, finally,  $N_x = N_y \approx 0.46$ ,  $N_z \approx 0.08$  when  $H$  is parallel to the  $c$  axis.

Using the value of the molar magnetic susceptibility  $\chi_m$  reported in Ref. [17], we can calculate  $\chi = \chi_m D / M_m$ , where  $D$  is the density and  $M_m$  is the molar mass. Using  $D = 6.77$  g/cm<sup>3</sup> and  $M_m = 1719.94$  g/mol, we obtain  $\chi = 0.011$ . Finally, using Eq. (A3), the demagnetizing contribution to the  $g$ -value anisotropy is  $\Delta g^{ab} = g^{H\parallel a} - g^{H\parallel b} = 0$  and  $\Delta g^{cb} = g^{H\parallel c} - g^{H\parallel b} = 0.013$ .

Experimentally, we obtained  $\Delta g_{exp}^{ab} = 0.075(5)$  and  $\Delta g_{exp}^{cb} = 0.023(5)$ . Although imperfections in the crystal could result in a finite  $\Delta g^{ab}$ , the experimental value is substantial and above any experimental uncertainty, especially when compared with  $\Delta g^{cb}$ , for example. This result clearly shows that the  $g$ -value anisotropy is related to intrinsic magnetic anisotropy and is not due to demagnetizing effects. Moreover,  $\Delta g_{exp}^{cb}$  is almost two times larger than the demagnetizing factor. Although the anisotropy out of the plane influences these effects, intrinsic magnetic anisotropy is also present.

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