

Suppressed incommensurate order in swedenborgite $\text{Ca}_{0.5}\text{Y}_{0.5}\text{BaCo}_4\text{O}_7$

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Swedenborgite $\text{Ca}_{0.5}\text{Y}_{0.5}\text{BaCo}_4\text{O}_7$ (CYBCO) with geometrically frustrated kagome and triangular lattices exhibits a disordered ground state in spite of strong antiferromagnetic couplings between the Co spins. The character of the disordered state has been debated due to ambiguous Co states in the triangular layers. Here, we perform single-crystal diffuse neutron scattering experiments to fully characterize the short-range spin correlations in CYBCO. Through reverse Monte Carlo and self-consistent Gaussian approximation analyses, we confirm that the Co ions in both the kagome and triangular layers are magnetic, and the interlayer couplings, together with the lattice distortion, promote an incommensurate magnetic order that is suppressed possibly by exchange disorder. Our work clarifies the short-range spin correlations in CYBCO and establishes a general correspondence between unequal interactions and incommensurate spin correlations on the swedenborgite lattice.

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In geometrically frustrated magnets, the ground state configurations exhibit an enormous degeneracy due to competing interactions, which may lead to exotic correlated states without magnetic long-range order (LRO) [1]. A prototype example is the two-dimensional antiferromagnetic Heisenberg model on the kagome lattice (KHAFM) [2]. In the classical limit, the ground state of the KHAFM is only weakly constrained by a local zero-moment rule, leading to a classical spin-liquid state with power-law correlations [3,4]. In real materials, however, perturbations from magnetostriction or further-neighbor interactions often relieve the degeneracy and induce magnetic LRO, making it challenging to realize a classical spin-liquid state as theoretically predicted.

The discovery of a disordered ground state in swedenborgite $\text{Ca}_{0.5}\text{Y}_{0.5}\text{BaCo}_4\text{O}_7$ (CYBCO) has drawn great attention [5–11]. As shown in Fig. 1(a), the Co ions in CYBCO form alternating triangular (Co1) and kagome (Co2) layers in the ab plane. Although magnetization measurements reveal a Curie-Weiss temperature of -2200 K suggesting strong antiferromagnetic (AFM) couplings between the Co spins, LRO has not been detected by neutron diffraction down to 1.2 K [5,6]. As the powder-averaged magnetic diffuse scattering

closely resembles the KHAFM spin-liquid state [12], it is proposed that the Co1 ions in the triangular layers may be of the nonmagnetic $S = 0$ Co^{3+} configuration so that the Co2 spins realize a KHAFM [6]. However, more recent reverse Monte Carlo (RMC) analyses of the powder neutron scattering data suggest an extrinsic scenario where both the Co1 and Co2 ions are magnetic and the LRO is mainly suppressed by the exchange disorder between the Co spins in the presence of randomly distributed Ca and Y ions [13,14]. A single-crystal study is needed to directly resolve the spin correlations in reciprocal space and unambiguously determine the origin of the disordered state in CYBCO.

Here, we report our diffuse neutron scattering study of a CYBCO crystal. Strong modulation of the spin correlations along the c axis is observed, which indicates a nonzero interlayer coupling that is confirmed in our RMC and self-consistent Gaussian approximation (SCGA) analyses. In the ab plane, incommensurate spin correlations are observed. By comparing the spin correlations under different perturbations, we are able to ascribe the incommensurability to unequal exchange interactions that can be induced by lattice distortions. Our work clarifies the ground state of CYBCO as an incipient incommensurate magnetic order that is suppressed by exchange disorder, and establishes a general correspondence between unequal interactions and incommensurate spin correlations on the swedenborgite lattice.

Single crystals of CYBCO were grown by the floating zone method [5,15]. Details for the sample preparation and basic

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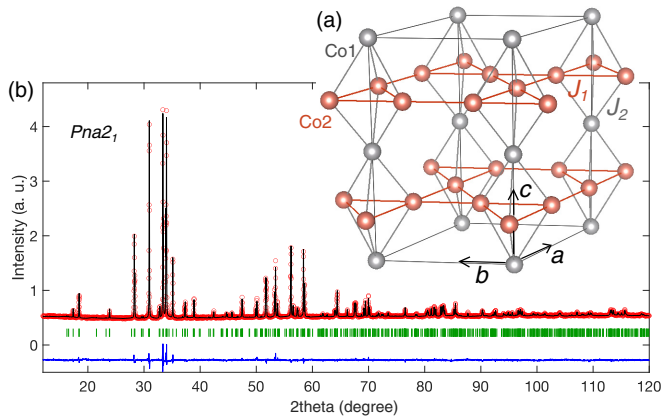


FIG. 1. (a) The Co ions in CYBCO form a lattice of alternating triangular (Co1) and kagome (Co2) layers in the ab plane. The crystal structure is shown in the hexagonal unit cell. J_1 (J_2) denotes the couplings within the kagome layers (between the kagome and triangular layers). (b) Refinement results of the XRD data measured at room temperature for pulverized CYBCO crystals. Data points are shown as red circles. The calculated pattern is shown as the black solid line. The vertical bars show the positions of the Bragg peaks for CYBCO with space group $Pna2_1$. The blue line at the bottom shows the difference of measured and calculated intensities.

characterizations can be found in the Supplemental Material [16] (see also Refs. [17–25] therein). Figure 1(b) summarizes the refinement results of the x-ray diffraction (XRD) data collected at room temperature on pulverized CYBCO crystals. Our diffraction data reveal the space group to be orthorhombic $Pna2_1$, which is the same as that of the parent compounds $\text{CaBaCo}_4\text{O}_7$ [26–28] and YBaCo_4O_7 [29] at room temperature, but different from the hexagonal $P6_3mc$ [5,6] or trigonal $P31c$ [13] space group reported previously. Such a difference may arise from the variance in the oxygen content [30], which is determined to be $\text{O}_{7.14(6)}$ in our annealed crystals through a thermal gravimetric analysis (TGA). The weak orthorhombic distortion causes a $\sim 0.4\%$ shrinkage along the a axis from the hexagonal symmetry [31]. The Ca and Y ions are randomly distributed over the same site with a fractional weight

of 0.52(1) and 0.48(1), respectively. The complete refined structural parameters are summarized in the Supplemental Material [16].

To characterize the short-range spin correlations in CYBCO, we perform single-crystal diffuse neutron scattering experiments on the CORELLI elastic diffuse scattering spectrometer at the Spallation Neutron Source (SNS), Oak Ridge National Laboratory [16,32]. The top half of Fig. 2 presents the representative scattering patterns in the $(hk0)$, $(hk2)$, and $(h0l)$ planes measured at $T = 2$ K, well below the successive spin freezing transition temperatures of ~ 15 , 50, and 250 K observed in magnetic susceptibility [5,16]. Indices in the diffuse patterns are denoted in the hexagonal system for convenience. The nuclear Bragg peaks with half-integer indices are consistent with the orthorhombic distortion, while the broad diffuse signal is in agreement with the absence of magnetic LRO as previously reported [6,13]. However, the diffuse scattering intensities are strongly modulated along the c axis: Intensities are concentrated in the planes with integer l as revealed in Fig. 2(c); and the scattering patterns in $(hk0)$ and $(hk2)$ are very different. These observations are not consistent with defining CYBCO as a KHAFM system because the spin correlations in a KHAFM exhibit no modulation out of the kagome plane. Instead, the observed diffuse patterns, especially the relatively narrow peak width along $(00l)$, are more similar to the quasi-one-dimensional order observed in YBaCo_4O_7 that arises from the relatively strong interlayer couplings [33].

A RMC analysis was performed to fit the diffuse signal over volumes in reciprocal space [16,34,35]. This is a model-free method that allows the spin-spin correlations to be extracted and subsequently used as a starting point to construct an effective spin Hamiltonian. Considering the strong modulation of the diffuse scattering intensity along the c axis, both the Co1 and Co2 ions are assumed to be magnetic with an equal moment size of $S = 3/2$ [13,14]. As shown in Fig. 2, our RMC simulations reproduce the intensity distributions in reciprocal space, including the disparate patterns in the $(hk0)$ and $(hk2)$ planes together with the quasi-one-dimensional order along the c axis. The representatives of the extracted

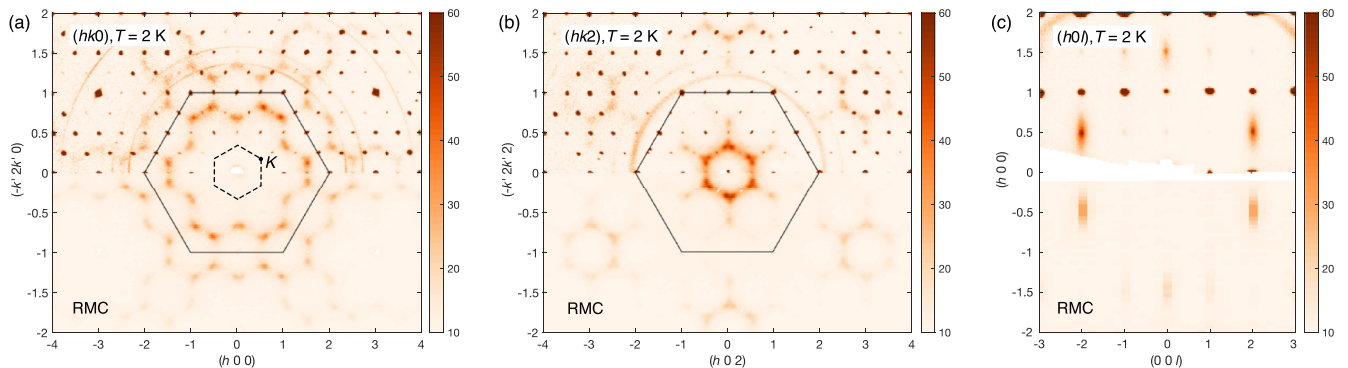


FIG. 2. Short-range spin correlations in CYBCO in the (a) $(hk0)$, (b) $(hk2)$, and (c) $(h0l)$ planes. In each panel, the upper half is the experimental data collected on CORELLI at 2 K, and the lower half is the calculated spin correlations from the RMC simulations. In (a) and (b), the solid line indicates the periodicity of the diffuse scattering pattern in the $(hk0)$ and $(hk2)$ planes. In (a), the dashed line outlines the first Brillouin zone boundary with the $K(\frac{1}{3}\frac{1}{3}0)$ point indicated. The additional ringlike scattering in the experimental data arises from the sample environment.

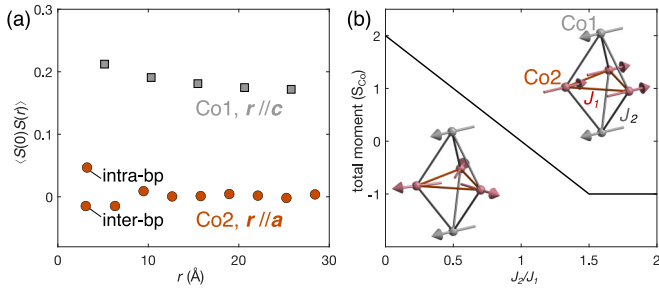


FIG. 3. (a) Spin correlations $\langle S(0) \cdot S(r) \rangle$ as a function of distance r calculated through RMC. Gray squares (red circles) are the correlations for the Co1 (Co2) spins along the c (a) axis. For the first-neighbor Co2 spins at $r \sim 3.2$ Å, correlations within the bipyramids (intra-bp) and out of the bipyramids (inter-bp) are calculated separately. Error bars representing the standard deviations are smaller than the size of the symbol. (b) Total moment of the spin bipyramid as a function of J_2/J_1 . Insets are representative ground states for infinitely small J_2/J_1 (left) and $J_2/J_1 \geq 1.5$ (right).

spin-spin correlations $\langle S_i \cdot S_j \rangle$ in real space are summarized in Fig. 3(a). The interlayer correlations between the Co1 spins are higher than ~ 0.17 even at a large separation of 5 layers (~ 26 Å) and are thus of a ferromagnetic (FM) character. In contrast, the in-plane correlations of the Co2 spins along the a axis decay rapidly to zero at increasing distances. Interestingly, the Co2 spins in the bipyramid units (intra-bp) exhibit FM correlations, which appears to be contradictory with the AFM couplings in the kagome layers.

The bipyramid unit of the swedenborgite lattice with antiferromagnetically coupled spins provides a qualitative explanation for the observed correlations [8,10,33]. Assuming the in-plane and out-of-plane couplings to be J_1 and J_2 , respectively, Fig. 3(b) shows the total moment of the bipyramid unit in the ground state as a function of J_2/J_1 . Even at infinitesimal J_2 , the total moment is close to $2S_{\text{Co}}$, meaning the two apical Co1 spins tend to be parallel, which explains the FM correlations among the Co1 spins along the c axis. For increasing J_2/J_1 , the Co1 spins stay parallel, while the three Co2 spins in the basal plane gradually change from an AFM 120° configuration at $J_2 = 0$ to a parallel configuration at $J_2 \geq 1.5J_1$. Thus our observed FM correlations for the Co2 spins within the bipyramid units are consistent with the AFM J_1 couplings in the kagome layers if relatively strong AFM interlayer couplings J_2 are considered.

Similar conclusions can also be drawn with a lattice model that incorporates the J_1 and J_2 couplings. Starting from the Hamiltonian $\mathcal{H} = J_1 \sum_{i,j \in 1} S_i \cdot S_j + J_2 \sum_{i,j \in 2} S_i \cdot S_j$, we explore the short-range spin correlations using the SCGA method [16,36–41]. At $J_2 = 0$, the J_1 - J_2 model is equivalent to the KHAFM, where the spin correlations are well understood in the classical regime [3,4]. The interaction matrix of the KHAFM has a flat eigenband at the bottom [16], indicating the absence of magnetic order at the mean-field level. When spin fluctuations are considered, a correlated paramagnetic phase with dipolarlike spin correlations will emerge, which is signified by pinch points in the diffuse scattering pattern [3,42]. As presented in Fig. 4(a), a similar correlated paramagnetic phase is realized on the swedenborgite lattice for $J_2/J_1 < \sqrt{2}/2$ [8].

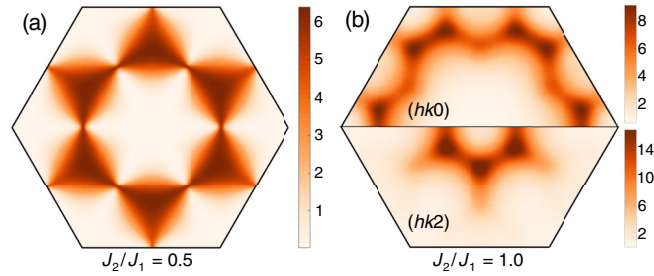


FIG. 4. The diffuse neutron scattering pattern in the $(hk0)$ plane calculated through the SCGA method for $J_2/J_1 = 0.5$ at reversed temperature $\beta = 100$ (a) and in $(hk0)$ and $(hk2)$ planes calculated for $J_2/J_1 = 1.0$ at $\beta = 4.5$ (b). The hexagon outlines the same region as the solid hexagon in Fig. 2. Pinch points arising from the flat eigenbands disappear at $J_2/J_1 > \sqrt{2}/2$, giving rise to a pattern that is similar to the experimental results.

Above this threshold, the eigenband at the bottom becomes dispersive [8,16], indicating the existence of a magnetic order at the mean-field level. Figure 4(b) presents the diffuse scattering patterns calculated by the SCGA method at $J_2/J_1 = 1$ that is representative for the $J_2/J_1 \geq \sqrt{2}/2$ regime [8]. The intensity distribution is very different from that of the KHAFM in Fig. 4(a), but reproduces the main features observed in CYBCO as shown in Fig. 2. Thus, via both the RMC and the SCGA calculations, the existence of the interlayer couplings J_2 in CYBCO is unambiguously established.

For the J_1 - J_2 Heisenberg model on the swedenborgite lattice, the magnetic LRO predicted in the mean-field theory can be removed by spin fluctuations, which increases the ordering threshold to $J_2/J_1 = 3/2$ according to classical Monte Carlo simulations [8,10]. As the diffuse scattering patterns at elevated temperatures are similar on both sides of the threshold, the J_1 - J_2 model cannot distinguish whether the disordered ground state in CYBCO is intrinsic due to spin fluctuations or extrinsic due to exchange disorder.

A closer look at the experimental and calculated patterns allows us to differentiate the intrinsic and extrinsic scenarios. Although the J_1 - J_2 model reproduces the main features of the diffuse scattering pattern, it fails to capture the details around K , $(\frac{1}{3}\frac{1}{3}0)$, and its equivalent points. As shown in Fig. 2 (also see Fig. 5 for greater detail), the maxima of the diffuse scattering intensities are slightly shifted from the K points along the Brillouin zone boundary, revealing incommensurate spin correlations that are not predicted by the J_1 - J_2 model. Although similar incommensurate correlations have been observed in swedenborgites, e.g., $\text{LuBaCo}_4\text{O}_7$ [43,44] and $\text{CaBaCo}_2\text{Fe}_2\text{O}_7$ [45], their microscopic origins are unclear and the perturbation terms to the J_1 - J_2 Hamiltonian still remain to be determined. If the perturbation terms further relieve the ground state degeneracy, the disordered ground state in CYBCO is more likely extrinsic due to exchange disorder as proposed in Ref. [13].

To understand the origin of incommensurate spin correlations in CYBCO and the related compounds, we first explore the perturbations from Dzyaloshinskii-Moriya interactions (DMIs) and further-neighbor exchange interactions. As discussed in the Supplemental Material [16], a variety of diffuse

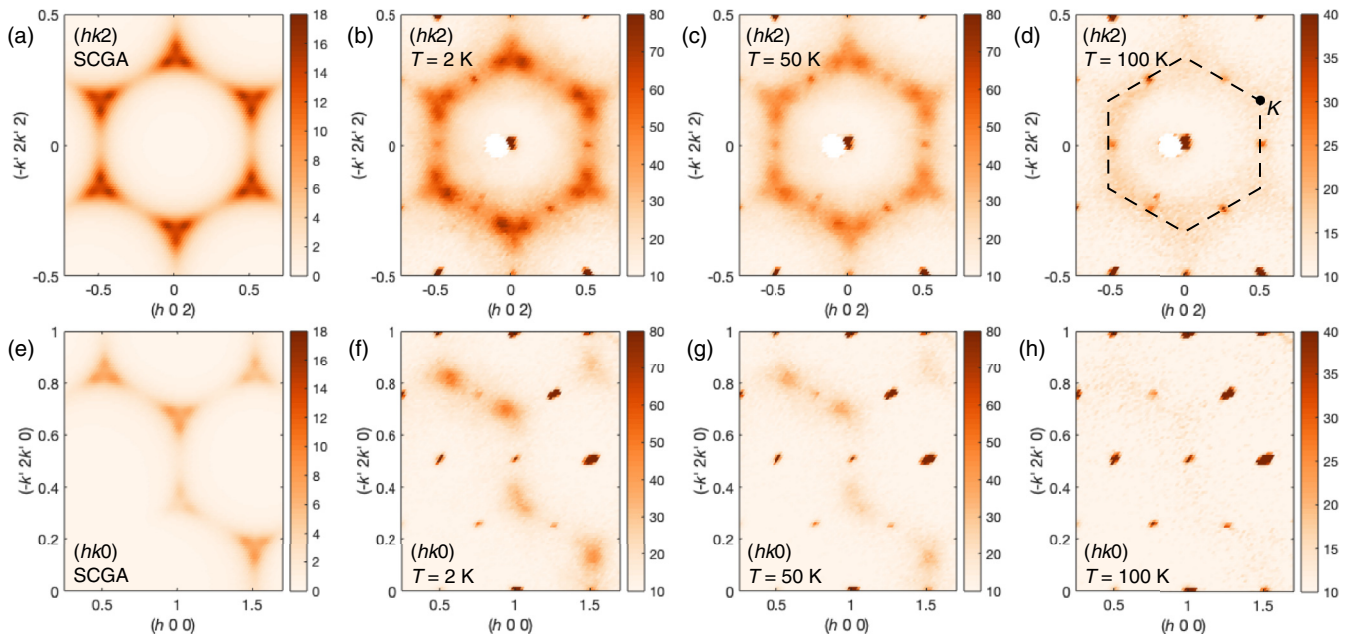


FIG. 5. Diffuse neutron scattering pattern in the $(hk2)$ plane (a) and $(hk0)$ plane (e) calculated by the SCGA method using a J_{1a} - J_{1b} - J_{1c} - J_2 model at $\beta = 3.2$, where $J_{1a} = 0.9$, $J_{1b} = 1.0$, and $J_{1c} = 1.1$ are the distinctive first-neighbor couplings in the kagome layer due to lattice distortion. The calculated intensities are averaged over equally populated domains. Zoomed-in plot for the experimental diffuse scattering patterns in the $(hk2)$ plane (b)–(d) and $(hk0)$ plane (f)–(h). Data were collected at (b), (f) 2 K, (c), (g) 50 K, and (d), (h) 100 K. The dashed line in (d) outlines the first Brillouin zone boundary.

patterns are observed under perturbations, although none of them exhibits incommensurate correlations as observed in our experiment. This suggests the necessity for perturbations other than DMIs or further-neighbor couplings.

Since the orthorhombic lattice distortion breaks the three-fold rotation symmetry along the c axis, we next consider a minimal J_{1a} - J_{1b} - J_{1c} - J_2 model with unequal J_1 coupling strengths in the kagome layers. It is noteworthy that unequal interactions may also arise from local distortions due to chemical disorder even in the absence of a uniform lattice distortion. The diffuse patterns calculated by the SCGA method with $J_{1a} = 0.9$, $J_{1b} = 1.0$, $J_{1c} = 1.1$, and $J_2 = 1.0$ are shown in Fig. 5 together with the temperature evolution of the experimental data. After averaging over the orthorhombic domains, our minimal model successfully reproduces the incommensurate correlations. The slight mismatch around the K points in the $(hk0)$ plane may arise from unequal domain populations or further perturbations that are not considered in our minimal model. Similar incommensurate correlations are obtained by introducing unequal J_2 couplings. Our calculations thus reveal the importance of unequal couplings in stabilizing incommensurate spin correlations in CYBCO and the related compounds. Furthermore, as unequal interactions relieve the ground state degeneracy and result in a magnetic LRO transition at $T_N \sim 0.3J_1$ in our minimal model, we are able to conclude that the disordered ground state in CYBCO is more likely extrinsic due to exchange disorder.

The temperature dependence of the diffuse pattern also supports the extrinsic origin of the suppressed order in CYBCO. As shown in Fig. 5, the intensity distribution, including the relative strengths of the incommensurate satellites, stays

almost constant below ~ 50 K. Such a weak temperature dependence contradicts the intrinsic spin-liquid state predicted for $J_2/J_1 < 1.5$ [8,10]. Instead, it implies a spin freezing scenario where the short-range spin correlations are prevented from developing into a LRO due to exchange disorder [13]. The extrinsic scenario is further corroborated by comparing the spin correlations in the related swedenborgites, as an AFM LRO has been observed in both the parent compounds YBaCo_4O_7 [15,29,44,46–48] and $\text{CaBaCo}_4\text{O}_7$ [26–28,31,49].

Although the discovery of the magnetoelectric effect in $\text{CaBaCo}_4\text{O}_7$ has drawn great attention to this family of compounds [27,50–54], the effect of local or lattice distortion on the spin correlations has remained barely explored. Therefore, the correspondence between unequal interactions and incommensurate spin correlations established in our work should have broad impacts on understanding the magnetic and magnetoelectric properties of swedenborgites. Especially, for doped swedenborgites, similar incommensurate spin correlations may emerge due to local distortions induced by chemical disorder even without a uniform lattice distortion [55–57].

We have shown that the previously proposed intrinsic scenario of uncoupled kagome layers in swedenborgites is not consistent with our single-crystal diffuse neutron scattering experiments. Rather, we determine the disordered ground state in CYBCO to be an incipient incommensurate magnetic order that is suppressed by exchange disorder. By comparing the spin correlations on the swedenborgite lattice under different perturbations, we are able to explain the incommensurate spin correlations in CYBCO by unequal interactions that are induced by lattice distortion. This correspondence between

unequal interactions and incommensurate spin correlations can be applied to other swedenborgite families of compounds.

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