# Point defects in beryllium-doped GaN

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Detailed analysis of the defect-related photoluminescence (PL) in semi-insulating and *n*-type Be-doped GaN samples grown by molecular beam epitaxy is presented. The dominant PL bands in these samples are the ultraviolet (UVL<sub>Be</sub>), yellow (YL<sub>Be</sub>), red (RL<sub>Be</sub>), and green (GL2) bands. The UVL<sub>Be</sub> band is caused by electron transitions via the 0/- level of the Be<sub>Ga</sub> acceptor located at 113 meV above the valence band. The UVL<sub>Be</sub> band is quenched above 60 K, and the quenching is tunable by excitation intensity. The quenching of the YL<sub>Be</sub> above 200 K is likely related to an acceptor level at 0.3 eV. In semi-insulating samples, the quenching temperature is tunable with the intensity of the excitation laser. Based on the first-principles calculations, the YL<sub>Be</sub> band is preliminarily attributed to the Be<sub>Ga</sub>-V<sub>N</sub>-Be<sub>Ga</sub> complex. The new RL<sub>Be</sub> band is attributed to the internal transition in the Be<sub>Ga</sub>-V<sub>N</sub> complex with a deep +/0 transition level at about 0.95 eV.

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### I. INTRODUCTION

Gallium nitride (GaN) is one of the most important semiconductors for modern optoelectronics, particularly blue and ultraviolet light-emitting devices. The technology of these devices relies heavily on the doping processes to create regions with opposite conductivity types. While *n*-type GaN can be obtained relatively easily [1], achieving reliable *p*-type conductivity proved to be challenging. Indeed, the only known p-type dopant for GaN is Mg incorporated into the Ga site  $(Mg_{Ga})$ . The defect forms a 0/- transition level at 223 meV above the valence band maximum (VBM) [2]. Such ionization energy is too high to produce significant concentrations of holes (above mid-10<sup>18</sup> cm<sup>-3</sup>) [3]. An increase in hole concentration to the production-acceptable levels is commonly achieved by heavy doping ([Mg]  $\sim 10^{20}$  cm<sup>-3</sup>). High concentrations of Mg create significant lattice distortions leading to potential fluctuations and may contribute to scattering that lowers mobility. In addition, Mg acceptors are often heavily compensated by donors such as nitrogen vacancy (V<sub>N</sub>). As a result, *p*-type GaN:Mg samples are often poorly conductive.

A few experimental works indicate that beryllium (Be) could be a promising alternative for *p*-type doping of GaN [4,5]. Interestingly, the hole concentration of  $8 \times 10^{19}$  cm<sup>-3</sup> has been reported [6] in Be-implanted Mg-doped GaN. However, no reliable and reproducible *p*-type conductivity in Be-doped GaN has been demonstrated to date. Calculations show that Be can be incorporated into interstitial sites (Be<sub>i</sub>) even under N-rich conditions [7]. This leads to self-compensation by Be<sub>i</sub> double donors, which limits *p*-type conductivity [8].

The first-principles calculations initially predicted  $Be_{Ga}$  to be an acceptor with an ionization energy of 0.2 eV above the VBM [9–12]. More recent calculations [13,14] resulted in a

0/- transition level at 0.55–0.65 eV above the VBM. Such a deep level is an example of a small polaron [15]: the hole is self-trapped due to significant lattice distortions around the BeGa center. The localization occurs at the nearest-neighbor nitrogen atom that is moved  $\sim 0.7$  Å from its equilibrium position [16]. Recently, using photoluminescence (PL) measurements and hybrid functional calculations, we showed that  $Be_{Ga}$  in GaN also forms a shallow acceptor level at 113  $\pm$ 5 meV above the VBM [7]. Electron-hole recombination through this shallow level produces an ultraviolet luminescence band (UVL<sub>Be</sub>, hereafter) in the PL spectra. The band has a zero-phonon line (ZPL) at 3.38 eV and a series of LO phonon replicas with the Huang-Rhys factor of about 0.2. At low temperatures, the transitions proceed via the shallow donor-acceptor pair (DAP) mechanism. With increasing temperature from 18 to 50 K, the transitions transform from the DAP type into transitions from the conduction band minimum (CBM) to the same acceptor (eA transitions). Our calculations [7] also predict a small polaron state existing along with the shallow state. However, the former is not observed in the PL experiments because of the significantly lower hole-capture coefficient than that for the shallow state [7].

Another PL band commonly observed in GaN:Be layers grown by molecular beam epitaxy (MBE), namely, the YL<sub>Be</sub> band, is reported to have a maximum at 2.1–2.2 eV [3,17]. A similar strong yellow luminescence band appears in bulk crystals containing high concentrations of Be and oxygen ( $\sim 10^{19}$  cm<sup>-3</sup>), and was attributed to the Be<sub>Ga</sub>-O<sub>N</sub> complex [18]. Lamprecht *et al.* [19] suggested that the yellow band in these samples consists of three unresolved bands, and one of them (with a maximum at 2.08 eV) decays extremely slowly with time after the laser is switched off (with the lifetime exceeding 1 s at room temperature).

A red luminescence band from GaN:Be has been observed in Ref. [20], but no detailed characterization has been reported. The band appeared after annealing the samples at 900  $^{\circ}$ C in pure N<sub>2</sub> ambient for 2 h. As will be shown below,

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TABLE I. Parameters of Be-doped GaN samples. Samples with index "b" were annealed at 900 °C. Samples 0406b and 0410b contained two regions with drastically different properties.

	Doping		PL QE (%)				$N_A - N_D \ (\mathrm{cm}^{-3})$ from quenching of PL	
Sample	$[Be] (cm^{-3})$	Other	UVL <sub>Be</sub>	YL <sub>Be</sub>	RL <sub>Be</sub>	GL2	UVL <sub>Be</sub> <sup>a</sup>	$YL_{Be}^{b}$
0406a	$1 \times 10^{19}$		< 0.00003	0.8	0.6			
0406b1	$1 \times 10^{19}$		< 0.0001	0.7	0.01			
0406b2	$1 \times 10^{19}$		< 0.0001		0.5	0.02		
0408a	$5 \times 10^{17}$		0.0001	20	0.0002			$1 \times 10^{17}$
0408b	$5 \times 10^{17}$		0.06	20	0.007			$1 \times 10^{16}$
0410a	$1 \times 10^{18}$		< 0.0003	7	0.002			
0410b1	$1 \times 10^{18}$		0.03	5				
0410b2	$1 \times 10^{18}$		0.03		3	0.2		
0411a	$4 \times 10^{18}$		< 0.00001	5	< 0.0001			$1 \times 10^{17}$
0411b	$4 \times 10^{18}$		< 0.0001		10	2		
0413a	$1 \times 10^{18}$	Н	< 0.00003	0.5	0.07			
0413b	$1 \times 10^{18}$	Н	< 0.0001		10	3		
0414a	$1 \times 10^{19}$	Н	0.005	2	0.007			$4 \times 10^{17}$
0414b	$1 \times 10^{19}$	Н	0.5	50	0.03		$6 \times 10^{15}$	$1 \times 10^{17}$
0415b	$1 \times 10^{20}$	Н	0.04	1.5	1			
0416b	$1 \times 10^{18}$	In	0.12		10	2	$4 \times 10^{17}$	
0417a	$1 \times 10^{19}$	In	< 0.00003		10	1		
0417b	$1 \times 10^{19}$	In	< 0.00003	1.4	0.01			
0418a	$1 \times 10^{20}$	In	0.005	5	0.002			$1 \times 10^{17}$
0418b	$1 \times 10^{20}$	In	0.01		1	0.2		
0419a	$2 \times 10^{18}$		< 0.0001	10	< 0.0001			$3 \times 10^{17}$
0419b	$2 \times 10^{18}$		0.05		10	1		
0020-1	$7  imes 10^{18}$		< 0.001	25	< 0.01			
0020-2	$7 \times 10^{18}$		0.2	30	0.05		$2 \times 10^{15}$	
0020-3	$7 \times 10^{18}$		0.1	15	0.01			

<sup>a</sup>From Eq. (3) with  $C_{pA} = 10^{-6} \text{ cm}^3/\text{s}$ .

<sup>b</sup> From Eq. (3) with  $C_{pA} = 4 \times 10^{-7} \text{ cm}^3/\text{s}$ .

in samples where the red luminescence is not obscured by the yellow emission, it is accompanied by the green band known as GL2. The GL2 band is attributed to the internal transition in the  $V_N$  [21]. The GL2 band maximum is located at 2.35 eV, with the ZPL expected at 2.85 eV and the Huang-Rhys factor of 26.5.

In this work, we analyze in detail the PL data from Be-doped GaN grown by MBE and identify PL bands observed in these samples by comparing the properties of the PL bands with predictions of the first-principles calculations.

### **II. METHODS**

The Be-doped GaN layers were grown by MBE on *c*-plane sapphire substrates at the West Virginia University [22] (see Table I). About 10 Ga-polar samples with the thickness of the GaN:Be layer of about 1  $\mu$ m were grown on top of the ~0.1- $\mu$ m-thick undoped GaN. Three N-polar samples (0020-*i* with *i* = 1, 2, 3) were deposited directly on sapphire. Some of the samples were annealed at 900 °C in nitrogen ambient (marked with index b in Table I). Positron annihilation measurements, conducted on these samples, showed that the Be predominantly incorporated into Ga sites, forming the Be<sub>Ga</sub> defects with the concentration of at least 10<sup>17</sup> cm<sup>-3</sup>, possibly as a part of a complex involving oxygen or hydrogen [8]. Secondary ion-mass spectrometry (SIMS) confirmed the presence of Be with concentrations ranging from  $10^{17}$  to  $10^{20}$  cm<sup>-3</sup> in different samples (Table I). Further details on the growth of the samples can be found in [23]. Only one sample (N-polar sample 0020-1) was conductive *n* type, which was established from analysis of the PL data and Hall effect measurements, other samples were semi-insulating. Some samples (see Table I) were grown under atomic H and In surfactants under electron beam irradiation aimed to enhance the incorporation of Be into Ga sites [23].

The steady-state PL (SSPL) was excited with a He-Cd laser (25 mW, 325 nm), dispersed by the 1200 rules/mm diffraction grating in a 0.3-m monochromator, and detected by a Peltier-cooled photomultiplier tube. The neutral density filters were used to attenuate the excitation intensity in the range from  $10^{-5}$  to 0.13 W/cm<sup>2</sup>. Excitation intensities up to  $100 \text{ W/cm}^2$  were achieved by focusing the laser beam. The PL measurements were corrected for the optical elements and detector sensitivities with a calibrated tungsten-halogen lamp. The spectra measured as a function of wavelength  $\lambda$  were multiplied by  $\lambda^3$  in order to plot the spectra in units proportional to the number of emitted photons as a function of photon energy [24]. The time-resolved PL (TRPL) was excited with a pulsed nitrogen laser (pulse duration 1 ns, 6 Hz repetition rate, and photon energy 3.68 eV). The signal was analyzed with an oscilloscope. A closed-cycle optical cryostat was used to

carry out measurements in the temperature range from 18 to 320 K. The samples were studied under identical conditions. The PL quantum efficiencies (QE) for each PL band were found by comparison of the integrated intensity with that from calibrated GaN samples. The calibrated samples were grown by the metal-organic vapor phase epitaxy method and doped with C and Si. The carbon-related YL1 band in these samples has a very high internal quantum efficiency (IQE)  $\eta_{YL1}$  that is determined with high accuracy. The relative QE of an unknown band  $\eta_u$  can be determined as  $\eta_u = (I_u/I_{YL1})\eta_{YL1}$ , where  $I_u$  and  $I_{YL1}$  are the integrated intensities of the unknown and the calibration YL1 bands, respectively. Other details can be found in Refs. [24,25].

Theoretical calculations were performed using the Heyd-Scuseria-Ernzerhof (HSE) hybrid functional [26]. The HSE functional was tuned to fulfill the generalized Koopmans condition for the MgGa acceptor in GaN (fraction of exact exchange is 0.25, the range separation parameter is 0.161 Å<sup>-1</sup>) [27]. Our tests show that the generalized Koopmans condition is fulfilled by this parametrization of HSE for the Be<sub>Ga</sub> acceptor as well. In calculations of the optical transition levels, an experimental band gap of GaN (3.5 eV) is used. Since the above parametrization of HSE slightly underestimates the band gap (3.22 eV), to compare the defect optics with the experiment we essentially perform a scissor operation and move the conduction band up to the correct value. Calculations were performed in 300-atom hexagonal supercells at the  $\Gamma$  point, with plane-wave energy cutoffs of 500 eV. All defect atomic structures were relaxed within HSE to minimize forces to 0.05 eV/Å or less. Spurious electrostatic interactions in calculated total energies were corrected using the Freysoldt–Neugebauer–Van de Walle approach [28,29]. Defect formation energies were calculated following the procedure outlined in Ref. [30]. Adiabatic potentials used to plot the configuration coordinate diagrams were obtained by fitting into HSE computed total energies using harmonic approximation and mapping the atomic displacements  $\Delta R_i$  onto the configuration coordinate Q as  $\Delta Q^2 = \sum_{i,x,y,z} m_i \Delta R_i^2$ , where  $m_i$  are the atom masses. Elemental chemical potentials used in defect formation energy calculations were obtained from the total energies of the GaN growth competing phases. For example, in a nitrogen-rich growth regime the chemical potential of nitrogen is set to  $\mu_N(N_2)$  while that of gallium is set to  $\mu_{Ga}(Ga \text{ metal}) + \Delta H_f(GaN)$ , where  $\Delta H_f(GaN)$  is the formation enthalpy of GaN (computed to be -1.2 eV). The chemical potential of oxygen is assumed to be limited by the formation of gallium oxide Ga<sub>2</sub>O<sub>3</sub>. In turn, in the presence of oxygen, the formation of beryllium defects is assumed to be limited by the growth of beryllium oxide BeO. Binding energies of defect complexes are calculated as the formation energy differences between the complex and its constituents in the lowest-energy charge states.

#### **III. RESULTS AND DISCUSSION**

#### A. Main photoluminescence bands in Be-doped GaN

We observed four major defect-related bands in PL spectra from Be-doped GaN samples. Representative low-temperature PL spectra from two samples are shown in Fig. 1.



FIG. 1. The representative PL spectra from samples 0408b and 0411b dominated by the red ( $RL_{Be}$ ) and yellow ( $YL_{Be}$ ) bands, respectively. The ultraviolet PL band ( $UVL_{Be}$ ) and the exciton band with a sharp DBE peak are relatively strong in sample 0408b. Measurements were carried out in identical conditions at T = 18 K and under excitation intensity  $P_{exc} = 0.13$  W/cm<sup>2</sup>. The small-amplitude oscillations are due to the Fabry-Perot interference inside the GaN layer. The feature at about 1.7 eV is the PL emission from the sapphire substrate.

The main defect-related PL bands are the UVL<sub>Be</sub> band with the strongest peak at 3.38 eV, the broad YL<sub>Be</sub> band with a maximum at about 2.2 eV, the RL<sub>Be</sub> band with a maximum at about 1.8 eV, and the GL2 band with a maximum at 2.33 eV and full width at half-maximum of 0.25 eV. The positions and shapes are well reproduced in different samples. The estimated QEs of these bands are given in Table I. The GL2 band is attributed to the V<sub>N</sub> defect [21], while three other PL bands are related to Be as will be shown below. In some samples, additional features could be observed in PL spectra at certain temperatures or excitation intensities, such as the Mg-related UVL<sub>Mg</sub> band with the strongest peak at 3.28 eV and a broad blue band, which overlapped with the YL<sub>Be</sub> band. These features and the near-band-edge (NBE) emission are beyond the scope of this paper.

In two samples (0406b and 0410b), the optical properties varied greatly across the sample surface within the 5-mm sample size. Similar to what we observed earlier in Mg-doped MBE GaN [21], two regions with different PL spectra were observed, and the boundary between these regions was very sharp. An example is shown in Fig. 2 for sample 0410b.

We were unable to find a clear correlation between the appearance of defect-related PL bands and the following properties of the samples: concentration of Be, codoping with H or In, and the sample polarity (see Table I). In particular, the bright YL<sub>Be</sub> band was observed in 14 Ga-polar samples (including annealed samples) and all three N-polar samples. It was also very strong in the only conductive *n*-type sample (0020-1). The UVL<sub>Be</sub> band was observed in 9 out of 17 samples with the strong YL<sub>Be</sub> band. Nevertheless, some regularities were



FIG. 2. PL spectra at T = 18 K and  $P_{\text{exc}} = 0.13$  W/cm<sup>2</sup> from two regions of the sample 0410b. The dashed lines show the fits of the broad PL bands using Eq. (4).

noticed: (i) with almost no exceptions, the UVL<sub>Be</sub> band appeared in GaN:Be samples after they were annealed at 900 °C in nitrogen ambient (the samples containing letter b in the name). (ii) In all 8 samples with the GL2 band, the RL<sub>Be</sub> band was very strong and the YL<sub>Be</sub> band was absent (Table I). This rule is emphasized in samples 0406b and 0410b, where the YL<sub>Be</sub> band suddenly disappears in the region where the GL2 and RL<sub>Be</sub> bands are strong (Fig. 2). Note that in samples with the dominant YL<sub>Be</sub> band, a weak red band could be detected at T > 200 K after the quenching of the YL<sub>Be</sub> band. In Table I, the QE of this red band is given in the column labeled RL<sub>Be</sub>. However, because of its low intensity, we could not confirm or reject the assumption that this red band is RL<sub>Be</sub>.

It is important to note that no correlation could be found between the  $RL_{Be}$  and  $UVL_{Be}$  bands or between the  $YL_{Be}$ and  $UVL_{Be}$  bands. The ratio of peak intensities  $YL_{Be}/UVL_{Be}$ or  $RL_{Be}/UVL_{Be}$  varied from  $10^{-3}$  to  $10^3$  across different samples. This suggests that these bands are caused by three different defects. Therefore, neither  $YL_{Be}$  nor  $RL_{Be}$  originates from the deep polaronic acceptor state of the  $Be_{Ga}$  acceptor since the shallow state of this acceptor is responsible for the  $UVL_{Be}$  band [7]. The three Be-related PL bands will be analyzed in detail in Secs. III C–III E. In the following section we present the results of theoretical calculations in which formation energies and transition levels for a number of Be-related defects are calculated, and the pool of candidates for the defects responsible for the above PL bands is narrowed.

### B. Theoretical search for the PL bands candidates

At the initial stage of defect identification, HSE calculations for common Be-related point defects, including Be-containing complexes, were performed using smaller 128atom hexagonal GaN supercells. We have analyzed Be atoms substituting for gallium (Be<sub>Ga</sub>), nitrogen (Be<sub>N</sub>), the interstitial Be (Be<sub>i</sub>), as well as their donor-acceptor combinations with each other and common point defects, such as oxygen donor (O<sub>N</sub>), V<sub>N</sub>, and gallium vacancy (V<sub>Ga</sub>). Optical properties of the promising candidates were then computed using 300-atom supercells.

Figure 3 shows the summary of the Be-related defect energetics in GaN. The Be<sub>Ga</sub> is an acceptor, with HSE calculations predicting both shallow and deep polaronic acceptor states. The polaronic ground state of the hole localized on a neutral  $Be_{Ga}$  acceptor (shown with a solid line in Fig. 3) has been analyzed in detail recently [7] and is not revealed in PL experiments. On the other hand, the shallow state of the neutral  $Be_{Ga}$ acceptor (shown with a dashed line in Fig. 3) is suggested to be responsible for the UVL<sub>Be</sub> band observed in this work and is addressed below in Sec. III C. Both states compete for the photogenerated holes, and previous calculations show [7] that the delocalized shallow state captures the hole significantly more efficiently. This leads to the bright UVL<sub>Be</sub> originating from the shallow state of  $Be_{Ga}$ , and no observable PL from the polaronic state. The  $Be_N$  has higher a formation energy and displays a series of deep donor transition levels and a very deep 0/- acceptor level. Coulomb attraction can lead to the formation of a stable  $Be_{Ga}$ -Be<sub>N</sub> complex, which is a deep donor, although it has high formation energy, especially in *n*-type material. Interstitial Be<sub>i</sub> is a shallow double donor with a relatively low formation energy in *p*-type GaN, suggesting that self-compensation of Be<sub>Ga</sub> acceptor by Be interstitials is likely [31].

Overall, most Be complexes appear to be detrimental to the incorporation of the  $Be_{Ga}$  acceptors. For example, the  $Be_{Ga}$  binds into donor complexes with nitrogen, beryllium, and gallium interstitials, with the  $Be_{Ga}$ - $N_i$  having relatively low formation energy. The  $Be_{Ga}$ - $Ga_i$  complex is found to be unstable, with gallium interstitial atom pushing beryllium out of the gallium site, forming a beryllium interstitial. The  $Be_i$  also can form a shallow donor complex with the  $Be_{Ga}$ acceptor.

The Be<sub>Ga</sub> acceptor can form stable complexes with both gallium and nitrogen vacancies. The Be<sub>Ga</sub> complex with the V<sub>Ga</sub>, which is a weakly bound deep acceptor, is unstable in *n*-type material. The formation energies of the Be<sub>Ga</sub>-V<sub>Ga</sub> complex are also high, therefore it is not expected to form in significant quantities. The next-nearest-neighbor complex Be<sub>N</sub>-V<sub>Ga</sub> is found to be unstable: upon relaxation, the Be atom moves into the V<sub>Ga</sub>, forming a Be<sub>Ga</sub>-V<sub>N</sub> complex. Similarly, the Be<sub>i</sub>-V<sub>Ga</sub> complex is unstable, with Be moving into the vacancy, forming the Be<sub>Ga</sub> acceptor. The Be<sub>Ga</sub>-V<sub>N</sub> complex forms a negative-*U* center [32] with a value of *U* of about -0.1 eV. The formation energy of this complex is relatively low even in N-rich growth conditions, as shown in Fig 3. The HSE calculations suggest that optical transitions via the +/0 level of this donor complex cause the RL<sub>Be</sub> band (Sec. III E).

Oxygen is a common shallow donor in GaN, often responsible for *n*-type behavior of as-grown samples. It forms a stable complex with the  $Be_{Ga}$  acceptor. The  $Be_{Ga}$ - $O_N$  complex was recently proposed as a defect responsible for the yellow band in bulk Be-doped GaN [18]. Note that in the bulk samples the properties of the yellow band differ from the YL<sub>Be</sub> observed in the MBE-grown samples studied in this paper. Nevertheless, our HSE calculations suggest that the  $Be_{Ga}$ - $O_N$  complex is electrically neutral and does not have transition levels in the band gap. Therefore, we do not reproduce the attribution of any yellow band to this complex.



FIG. 3. Formation energies (in N-rich growth regime), charge states, and transition levels of Be-related defects in GaN.

A triplet complex  $Be_{Ga}-O_N-Be_{Ga}$  (not shown) is found to be very weakly bound, indicating that the  $Be_{Ga}-O_N$  and  $Be_{Ga}$ do not interact. Most triplet complexes considered here were found to have significant formation energies, and therefore unlikely to form in large amounts. However, even defects with relatively high formation energy can be created in the right conditions. The formation energy is an indicator of the likelihood of forming a defect in equilibrium. The samples studied in this work were grown by MBE, which is a relatively cold and highly nonequilibrium growth. Therefore, if there is a Coulomb attraction between the complex constituents during growth, the complexes can form in concentrations significantly different from those predicted by equilibrium thermodynamics. One example of this could be  $Be_{Ga}-V_N-Be_{Ga}$  which is negatively charged in *n*-type material. It is a promising candidate for the defect responsible for the  $YL_{Be}$ band because the experiment suggests an efficient capture of the photogenerated holes by the  $YL_{Be}$  defect. This behavior is expected for a negatively charged acceptor, such as  $Be_{Ga}-V_N-Be_{Ga}$ . The only other defect with such property is the  $Be_{Ga}-V_{Ga}$  complex, discussed above. However, calculations suggest that it is unstable in *n*-type material, where the  $YL_{Be}$  band is strong. In contrast, the  $Be_{Ga}-V_N-Be_{Ga}$  complex has binding energies of 1.5–1.9 eV and 0.8 eV in *p*-type and *n*-type materials, respectively. Although the latter may indicate a relatively weakly bound complex, there is likely a significantly larger barrier for the complex dissociation. The complex can be formed during the sample growth due to the Coulomb interaction between a positive donor  $Be_{Ga}$ - $V_N$  and a negative acceptor  $Be_{Ga}$ . After the sample cooling, TABLE II. HSE calculated transition levels of Be-related defects. Binding energies of Be complexes are given for the three values of the Fermi level corresponding to the *p*-type, semi-insulating, and *n*-type materials. Binding energies of triplet complexes are computed with respect to dissociating a triplet into Be<sub>Ga</sub> and a remaining doublet, i.e.,  $Be_{Ga}$ - $V_N$ ,  $Be_{Ga}$ - $Be_N$ , and  $Be_{Ga}$ - $Be_i$ .

			Binding energy (eV)			
Defect	$q_1/q_2$	Transition energy (eV)	$E_F \sim \text{VBM}$	$E_F \sim { m midgap}$	$E_F \sim \text{CBM}$	
Be <sub>Ga</sub>	0/- (shallow)	<0.2				
	0/- (polaronic)	0.58				
Be <sub>N</sub>	3 + /2 +	0.88				
	2 + /+	1.49				
	+/0	1.90				
	0/-	2.71				
Be <sub>Ga</sub> -Be <sub>N</sub>	2 + /+	2.48	4.7	4.1	0	
	+/0	3.15				
Be <sub>Ga</sub> -N <sub>i</sub>	2 + /+	0.71	0	1.9	0.2	
ou i	+/0	1.17				
Be <sub>Ga</sub> -Be <sub>i</sub>	+/0	>3.3	1.0	1.5	1.5	
Bei	2 + / +	>3.3				
	+/0	>3.3				
Be <sub>Ga</sub> -V <sub>Ga</sub>	0/-	1.05	0.5	0	-1.6	
	-/2-	1.70				
	2 - /3 -	1.90				
$Be_{Ga}$ -V <sub>N</sub>	2 + /+	1.02	1.9	1.4	1.4	
	+/0	0.93				
$Be_{Ga}$ -O <sub>N</sub>			1.8	1.8	1.8	
Be <sub>Ga</sub> -V <sub>N</sub> -Be <sub>Ga</sub>	+/0	1.76	1.5	0.8	0.8	
	0/-	1.52				
Be <sub>Ga</sub> -Be <sub>N</sub> -Be <sub>Ga</sub>	+/0	3.10	1.3	1.8	0.8	
Be <sub>Ga</sub> -Be <sub>i</sub> -Be <sub>Ga</sub>	,		0.7	1.1	1.0	

subsequent dissociation of the complex involves additional migration barriers for Be in GaN. The  $Be_{Ga}$ - $V_N$ - $Be_{Ga}$  complex is a negative-U center with a value of U of -0.24 eV. The YL<sub>Be</sub> band can be attributed to this complex, as described in Sec. III D. The energies of calculated transition levels with respect to the VBM and the complex binding energies are summarized in Table II.

### C. Ultraviolet band

The  $UVL_{Be}$  band was observed in half of the samples with the spectra dominated by the  $YL_{Be}$  (as in Fig. 1 for sample 0408b) and in half of the samples with the strong GL2 band (as in Fig. 4 for sample 0418a).

The NBE emission is dominated by the donor bound exciton (DBE) peak at 3.478 eV [33]. On the high-energy side of the DBE peak, the free-exciton (FE) peak appears as a shoulder at 3.484 eV (better resolved at T = 50 K). It is followed by the UVL<sub>Be</sub> band with the ZPL at 3.375 eV and two phonon replicas separated by the bulk LO phonon energy of 92 meV. This band is identified as the DAP transition between shallow donors and the 0/- level of the Be<sub>Ga</sub> acceptor (at low temperatures) [7]. The shape of the band suggests the Huang-Rhys factor of 0.2, typical for shallow acceptors [33]. The QEs of the UVL<sub>Be</sub> band in different samples are presented in Table. I. The ZPL blueshifts by 6 meV with increasing excitation intensity  $P_{exc}$  from  $10^{-5}$  to 0.1 W/cm<sup>2</sup> at low temperature. The shift agrees with the DAP origin of the transition. As temperature rises, the shallow donors (O<sub>N</sub> and

Si<sub>Ga</sub>) become ionized, and the DAP transitions transform into the eA transitions (from the conduction band to the same acceptor level). As a result, the DAP band is gradually replaced with the identical eA band, shifted by the donor ionization energy (about 20 meV) [33], with the ZPL at 3.395 eV. The eA transitions are best resolved above 50 K. Taking into account the FE binding energy (~26 meV) [34], the position of the 0/- transition level of the Be<sub>Ga</sub> acceptor is estimated to be  $113 \pm 5$  meV [7]. This makes Be<sub>Ga</sub> a dopant with the lowest acceptor level in GaN observed to date.

The dependence of the UVL<sub>Be</sub> intensity on temperature under different excitation intensities is shown in Fig. 5. The PL intensity does not change significantly at low temperatures and decreases exponentially above ~50 K. The temperature above which the decrease begins is tunable by excitation intensity and shifts to lower temperatures for lower excitation intensities. Such temperature behavior is similar to that of UVL<sub>Mg</sub>, BL<sub>Zn</sub>, and YL1 bands in high-resistivity GaN, related to the Mg<sub>Ga</sub> [2], Zn<sub>Ga</sub> [35], and C<sub>N</sub> [24] acceptors, respectively. The temperature dependence of PL intensity is traditionally fitted with the following expression [33]:

$$I(T) = \frac{I(0)}{1 + C \exp\left(-\frac{E_A}{kT}\right)},\tag{1}$$

where I(0) is the intensity in the low-temperature limit,  $E_A$  is the activation energy of the thermal quenching, and C is the preexponential factor. As an example, the dependence for  $P_{\text{exc}} = 0.016 \text{ W/cm}^2$  in Fig. 5 is fitted with Eq. (1) with



FIG. 4. The high-energy part of the PL spectrum of sample 0418a measured at  $P_{\text{exc}} = 0.13 \text{ W/cm}^2$ . At 3.444 eV, the fourth Raman line R4 from the He-Cd laser (3.814 eV) appears due to the interaction with the 92-meV bulk LO phonon mode. The ZPL of the DAP transition of the UVL<sub>Be</sub> band peaks at 3.375 eV with its first LO phonon replica situated 92 meV further. The transitions from the conduction band to the acceptor (eA) replace the DAP transitions at temperatures above 50 K.

parameters  $C = 3.4 \times 10^5$  and  $E_A = 70$  meV. However, the conventional interpretation of this formula, as the thermal emission of holes from the defect level at  $E_A$  above the VBM and recapture of these holes by nonradiative defects (the Schön-Klasens mechanism), fails to explain the shift of the exponential decrease region to higher temperatures when  $P_{\text{exc}}$  increases [36]. The abrupt and tunable quenching (ATQ) model can be utilized to explain such discrepancy, as described below.

The ATQ model introduced in Ref. [35] provides a plausible explanation for the UVL<sub>Be</sub> quenching. It involves an inverse population of defect levels with charge carriers at low temperatures due to preferential capture of photogenerated holes by radiative acceptors and electrons by nonradiative donors. Let  $T_0$  be the critical temperature defined as the intersection between extrapolated low-temperature dependence and the exponential drop in the Arrhenius plot (Fig. 5). At low temperatures in the steady-state conditions, almost all nonradiative donors become populated with photogenerated electrons. The fast capture of photogenerated holes by acceptors is followed by radiative transitions from the shallow donors or the conduction band to the acceptor. At  $T_0$  the concentrations of thermally emitted [proportional to  $\exp(-E_A/kT)$ ] and photogenerated holes become comparable. These holes, recaptured by the nonradiative donors, break the bottleneck in the nonradiative recombination channel and quickly depopulate the nonradiative donors within the very narrow temperature range. The limiting concentration of free holes that unlocks the nonradiative channel is proportional to the electron-hole generation rate G, which results in the tunability of  $T_0$  [35,36]. In this case, the  $T_0$  depends on G



FIG. 5. Temperature dependences of the UVL<sub>Be</sub> peak intensity divided by  $P_{\text{exc}}$  for sample 0414b at various excitation intensities. The low-temperature region and the exponential drop of the PL intensity linearly extrapolated in Arrhenius coordinates define the position of  $T_0$ .

as [35]

$$T_0 = \frac{E_A}{k \, \ln\left(QT_0^{3/2}/G\right)},\tag{2}$$

with

$$Q = C_{pA} \left(\frac{1}{\eta_0} - 1\right) (N_A - N_D) \frac{N_{v1}}{g},$$
 (3)

where  $C_{pA}$  is the hole-capture coefficient for the acceptor,  $\eta_0$ is the absolute IQE of the UVL<sub>Be</sub> band,  $N_A$  and  $N_D$  are the acceptor and shallow donor concentrations, g is the degeneracy of the acceptor level, and  $N_{v1}$  is the effective density of states in the valence band at T = 1 K. The G is calculated using absorption coefficient ( $\alpha = 10^5 \text{ cm}^{-1}$  for GaN at 325 nm [37]) as  $G = \alpha P_{\text{exc}} / \hbar \omega_{\text{exc}}$  under the assumption that the incident photons are absorbed uniformly within the layer of thickness  $\alpha^{-1}$ . Note that the quenching of the UVL<sub>Be</sub> band is tunable but does not look abrupt. As numerical calculations suggest, the initial abrupt drop of PL is obscured by the following exponential decrease with the activation energy  $E_A$ [36]. This is typical for shallow acceptors when their concentration is larger than the concentration of shallow donors but smaller than the total concentration of donors (radiative and nonradiative) [36].

The  $T_0(G)$  dependence for the UVL<sub>Be</sub> band in three samples is plotted in Fig. 6. If we consider both  $E_A$  and Q as fitting parameters (dashed lines in Fig. 6), we obtain  $E_A = 135$  meV and  $Q = 8 \times 10^{31}$  cm<sup>-3</sup> s<sup>-1</sup> K<sup>-3/2</sup> (sample 0416b) and  $E_A = 170$  meV and  $Q = 1 \times 10^{32}$  cm<sup>-3</sup> s<sup>-1</sup> K<sup>-3/2</sup> (sample 0414b), where  $E_A$  disagrees with the PL spectroscopy data [7], and Q results in a very large capture coefficient  $C_{pA}$ . Indeed, by taking IQE for the UVL<sub>Be</sub> band and the total concentration of Be obtained from SIMS analysis (e.g.,  $\eta_0 = 0.0012$  and  $N_A - N_D < 10^{18}$  cm<sup>-3</sup> for sample 0416b), we get  $C_{pA}$  from Eq. (3) larger than  $3 \times 10^{-5}$  and  $6 \times 10^{-5}$  cm<sup>3</sup>/s for samples 0414b and 0416b, respectively. Nevertheless, the model is



FIG. 6. Dependence of the critical temperature  $T_0$  on the electron-hole generation rate *G* for the UVL<sub>Be</sub> band in GaN:Be (samples 0416b, 04014b, and 0020-2, all semi-insulating). The fits using Eqs. (2) and (3) with the fixed  $E_A = 113$  meV are shown with the solid lines and reveal  $Q = 5 \times 10^{29}$  and  $2 \times 10^{27}$  cm<sup>-3</sup> s<sup>-1</sup> K<sup>-3/2</sup> for samples 0416b and 0414b, respectively.

still valid if we fix  $E_A$  to 113 meV (known from DAP to eA transformation) and make  $C_{pA} = 10^{-6} \text{ cm}^3/\text{s}$ , which is the crude estimate accurate to plus-minus order of magnitude. The fit accuracy somewhat worsens (solid lines in Fig. 6), but the parameter Q takes reasonable values  $(2 \times 10^{27})$  and  $5 \times 10^{29}$  cm<sup>-3</sup> s<sup>-1</sup>  $\tilde{K}^{-3/2}$  for samples 0414b and 0416b) that yield  $N_A - N_D = 6 \times 10^{15}$  and  $4 \times 10^{17}$  cm<sup>-3</sup> for samples 0414b and 0416b. Note that  $C_{pA}$  and  $(N_A - N_D)$  appear as product in Eq. (3) and cannot be determined independently. Nevertheless, it can be concluded that  $C_{pA} > 4 \times 10^{-7} \text{ cm}^3/\text{s}$ (otherwise,  $N_A - N_D > [Be]$  for sample 0416b), and the concentration of the Be<sub>Ga</sub> acceptors responsible for the UVL<sub>Be</sub> band is much lower than the concentration of defects responsible for the YL<sub>Be</sub> band in selected samples (Table I). The weaker  $T_0(G)$  dependence than expected for  $E_A = 113 \text{ meV}$ could be explained by the presence of the depletion region near the sample surface [36]. Hence, the ATQ model explains recombination kinetics in the bulk of the samples, but the experimental dependences are distorted by the surface effects.

Detailed HSE calculations of optical properties of the BeGa acceptor were presented in Ref. [7]. The HSE calculations predict that the Be<sub>Ga</sub> is a dual-nature acceptor, possessing both deep and shallow acceptor states. The deep state is obtained by the relaxation of the defect lattice geometry from the starting point where the Be-N bond is extended by about 0.7 Å from its equilibrium value. The shallow state can be obtained by relaxing the defect structure starting from the ideal GaN lattice. The deep state is a small polaron with a transition level calculated at 0.58 eV above the VBM. The deep state of the  $Be_{Ga}$  has not been observed experimentally, likely due to the low hole capture coefficient of the polaronic state (about two orders of magnitude lower than that of the shallow state). The shallow state shown in Fig. 7 is predicted to have a transition level at about 0.2 eV, a value overestimated by about 0.1 eV due to the supercell approach. Upon photoexcitation, the shallow state of



FIG. 7. Configuration coordinate diagram for the shallow state of the  $Be_{Ga}$  acceptor. In the ground state, acceptor is negatively charged. The photogenerated hole is efficiently captured (dashed arrow) to the shallow state of the acceptor, with subsequent radiative transitions calculated to have the PL maximum at 3.2 eV and the ZPL at 3.26 eV.

the  $Be_{Ga}$  acceptor efficiently captures a hole, with the capture coefficient estimated between  $10^{-6}$  and  $10^{-5}$  cm<sup>3</sup>/s [7], due to the absence of the potential barrier for this process (the dashed arrow in Fig. 7). Optical transitions via the shallow acceptor state of the  $Be_{Ga}$  are predicted at 3.26 eV (ZPL) and 3.20 eV (PL band maximum) in good agreement with the experiment. The calculated Huang-Rhys factor is 2.8, a value also overestimated due to the difficulties in describing a shallow defect state within the supercell approach. Both experimental data and theoretical results indicate that the UVL<sub>Be</sub> band in Be-doped GaN samples originates from the shallow state of  $Be_{Ga}$  acceptor.

### D. Yellow band

Figure 8 shows the broad  $YL_{Be}$  band with a maximum at 2.13 eV, which dominates the lower-energy portion of the spectrum in the majority of the GaN:Be samples. The band's shape can be fitted with the formula derived from the configuration coordinate model [21]

$$I(\hbar\omega) = I_0 \exp\left\{-2S_e\left(\sqrt{\frac{E_0 - \hbar\omega}{E_0 - \hbar\omega_{\max}}} - 1\right)^2\right\}, \quad (4)$$

where  $\hbar\omega_{\text{max}}$  is the position of the band maximum,  $S_e$  is the Huang-Rhys factor, and  $E_0$  is a parameter with the magnitude close to the ZPL energy. A reasonably good fit can be obtained with  $E_0 = 3.3 \text{ eV}$ ,  $\hbar\omega_{\text{max}} = 2.13 \text{ eV}$ , and  $S_e = 27$ . The band blueshifts by less than 20 meV with increasing  $P_{\text{exc}}$  from 0.01 to 100 W/cm<sup>2</sup>. It also significantly differs from the YL1 band attributed to C<sub>N</sub> defect that has the same maximum position. The shapes of the two bands are compared in Fig. 8, where the spectrum of the YL1 band is taken from the C-doped MOCVD GaN sample, details on which can be found in Ref. [24]. The temperature dependence of the intensity demonstrates even greater dissimilarity between the YL1 and YL<sub>Be</sub> bands.



FIG. 8. Normalized shapes of the YL<sub>Be</sub> band in GaN:Be samples compared to the YL1 band from the MOCVD-grown GaN:C sample cvd3784. The YL1 band is attributed to the C<sub>N</sub> defect [24]. The solid and dashed lines are calculated using Eq. (4) with the following parameters:  $E_0 = 2.67 \text{ eV}$ ,  $\hbar\omega_{\text{max}} = 2.17 \text{ eV}$ , and  $S_e = 7.6$  (the YL1 band) and  $E_0 = 3.3 \text{ eV}$ ,  $\hbar\omega_{\text{max}} = 2.13 \text{ eV}$ , and  $S_e = 27$  (the YL<sub>Be</sub> band).

The quenching of the  $YL_{Be}$  intensity with temperature occurs in two steps: a relatively small stepwise decrease is observed at about 100 K, and the second (usually abrupt) quenching begins at about 200 K. In semi-insulating samples, both quenching steps are tunable, and the second quenching is abrupt, the behavior similar to that in semi-insulating GaN doped with Zn [38]. The magnitude of the first step is sample dependent. In *n*-type GaN:Be sample, the quenching of the YL<sub>Be</sub> band is neither tunable nor abrupt, which is typical for *n*-type GaN [35]. Below, the temperature dependences of the YL<sub>Be</sub> band in *n*-type and semi-insulating GaN:Be samples are presented in two separate sections.

# 1. n-type GaN:Be

Only one of the studied samples (0020-1) demonstrated PL behavior typical for a conductive *n*-type GaN. In particular, the PL decay of the YL<sub>Be</sub> was nearly exponential at T > 100 K, and the PL quenching occurred by the Schön-Klasens mechanism. The Hall effect measurements at room temperature confirmed *n*-type conductivity with n = $6 \times 10^{17}$  cm<sup>-3</sup>. When decay of PL intensity after a laser pulse in TRPL measurements is close to exponential (but not exactly exponential), the PL lifetime can be found as the time corresponding to a maximum in the  $tI^{PL}(t)$  dependence [39]. Examples for the YL<sub>Be</sub> band in sample 0020-1 are shown in Fig. 9. The effective PL lifetime is 50  $\mu$ s at T = 100 K and decreases to 25  $\mu$ s at T = 200 K. The decrease in lifetime  $\tau$ is expected due to the thermal excitation of electrons from the shallow donors to the conduction band according to relation  $\tau = (nC_{nA})^{-1}$ , where *n* is the concentration of free electrons. With  $n = 4 \times 10^{17}$  cm<sup>-3</sup> at T = 200 K, we estimate that  $C_{nA} = 10^{-13} \text{ cm}^3/\text{s}$  for the defect responsible for the YL<sub>Be</sub> band. This value is close to the electron-capture coefficient



FIG. 9. The product of delay time and PL intensity decay after the excitation laser pulse for the YL<sub>Be</sub> band in *n*-type sample 0020-1. The solid lines are the dependences of the form  $te^{-t/\tau}$ . The maximum of the dependence corresponds to the effective lifetime of the band at a given temperature. At temperatures below 50 K, the method is inconclusive. With increasing temperature, lifetime decreases from 50  $\mu$ s at 100 K to 25  $\mu$ s at 200 K. The raw data were filtered using Wiener optimal filter.

for the major acceptors in undoped GaN:  $3.2 \times 10^{-12}$ ,  $0.68 \times 10^{-12}$ , and  $0.11 \times 10^{-12}$  cm<sup>3</sup>/s for the Mg<sub>Ga</sub>, Zn<sub>Ga</sub>, and C<sub>N</sub> acceptors [40].

The intensity of the YL<sub>Be</sub> band in *n*-type GaN:Be (sample 0020-1) is nearly independent of temperature up to ~150 K (the first step is very small). At higher temperatures, it decreases with the activation energy  $E_A = 0.3$  eV (Fig. 10). The characteristic temperature at which the quenching begins is not tunable by excitation intensity and can be meaningfully fitted with Eq. (1), provided that the preexponential factor is given by [35]

$$C = (1 - \eta_0)\tau C_{pA}N_{v1}T^{3/2}/g.$$
 (5)

Here,  $\eta_0$  is the IQE of the PL band,  $\tau$  is the characteristic lifetime of the PL before quenching,  $C_{pA}$  is the hole-capture coefficient, g the degeneracy factor, and  $N_{v1}$  is the effective density of states at T = 1 K. The PL lifetime of the YL<sub>Be</sub> band was determined from the TRPL measurements to be  $\tau =$  $25 \ \mu s$  at T = 200 K. From Eq. (5), with  $\eta_0 = 0.25$ , and  $N_{v1} =$  $3.5 \times 10^{15}$  cm<sup>-3</sup> K<sup>-3/2</sup>, the hole-capture coefficient can be found as  $C_{pA} = 4.0 \times 10^{-7}$  cm<sup>3</sup>/s and  $E_A = 0.30$  eV. A relatively large value of the hole-capture coefficient suggests that the defect responsible for the YL<sub>Be</sub> band is likely an acceptor which is negatively charged in the *n*-type sample.

### 2. Semi-insulating GaN:Be

For all semi-insulating GaN:Be samples, the  $YL_{Be}$  band abruptly quenched at temperatures lower than 200 K, and the attempts to fit the temperature dependence of the PL intensity with Eq. (1), resulted in unreasonably large sample-dependent activation energies (ranging from 600 to 1300 meV) and



FIG. 10. Temperature dependences of the peak PL intensity of the YL<sub>Be</sub> band in the *n*-type sample 0020-1 at different  $P_{\text{exc}}$ . The data for  $P_{\text{exc}} = 0.0047 \text{ W/cm}^2$  are fitted using Eqs. (1) and (5) with the following parameters:  $E_A = 0.3$  eV,  $C_{pA} = 4.0 \times 10^{-7} \text{ cm}^3/\text{s}$ ,  $N_{v1} = 3.5 \times 10^{15} \text{ cm}^{-3} \text{ K}^{-3/2}$ ,  $\tau = 25 \ \mu\text{s}$ , and  $\eta_0 = 0.25$ . The inset shows PL spectrum at T = 18 K (dotted line) and calculated shape using Eq. (4) with the following parameters:  $E_0 = 3.3 \text{ eV}$ ,  $\hbar\omega_{\text{max}} =$ 2.14 eV, and  $S_e = 27$ .

preexponential factors C (from  $10^{32}$  to  $4 \times 10^{39}$ ). Examples of such dependences for one of the samples are shown in Fig. 11.

Similar to the UVL<sub>Be</sub>, the exponential PL intensity drop starts at higher temperatures as the excitation intensity increases. Such temperature behavior of the PL is typical for semi-insulating samples [35]. This is another example where the ATQ model explains recombination kinetics and yields at least rough estimates of the parameters. It should be emphasized that in this case, fitting the temperature dependences of the PL intensity with Eq. (1) yields incorrect activation



FIG. 11. The temperature dependences of the peak YL<sub>Be</sub> intensity in the semi-insulating GaN:Be (sample 0408a). Excitation intensity  $P_{\text{exc}}$  is varied in the range  $2.9 \times 10^{-5} - 1.6 \times 10^{-2}$  W/cm<sup>2</sup>.



FIG. 12. Dependence of the critical temperature  $T_0$  on the electron-hole pair generation rate *G* for the YL<sub>Be</sub> band in semiinsulating GaN:Be samples. In the examples of fits with Eq. (2) shown with lines, parameters  $C_{pA} = 4 \times 10^{-7} \text{ cm}^3/\text{s}$ ,  $E_A = 0.30 \text{ eV}$ , and  $N_{v1} = 3.5 \times 10^{15} \text{ cm}^{-3} \text{ K}^{-3/2}$  are taken from the *n*-type sample analysis, and the obtained values of  $N_A - N_D$  are given in Table I.

energies. For example, in Fig. 11 the temperature dependence is fitted using Eq. (1) with the following parameters:  $E_A =$  1030 meV and  $C = 1 \times 10^{32}$ ,  $1 \times 10^{36}$ , and  $4 \times 10^{39}$  in order of decreasing  $P_{\text{exc.}}$ 

The  $T_0(G)$  dependence shown in Fig. 12 can be fitted with Eqs. (2) and (3), as in the case of the UVL<sub>Be</sub>. Using  $E_A = 0.30$  eV and  $C_{pA} = 4 \times 10^{-7}$  cm<sup>3</sup>/s, known from the *n*-type sample, and the IQE of the YL<sub>Be</sub> band determined from a comparison of the integrated YL<sub>Be</sub> intensity with calibrated GaN samples, the value of  $N_A - N_D$  can be obtained. For all the samples analyzed in such a way, it is smaller than the total concentration of Be atoms (Table I). Note that the obtained values are rough estimates because the quantum efficiency is usually found with the accuracy of plus-minus half an order of magnitude [41]. This shows that the ATQ model is valid and is consistent with the data obtained from the *n*-type sample.

The identification of the defect responsible for the  $YL_{Be}$ is difficult. There are several restrictions imposed on this identification by the experimental data: (a) The defect is likely an acceptor with a transition level at 0.3 eV above the VBM rather than a donor. This follows from high  $C_{pA}$  and low  $C_{nA}$ . (b) The defect is Be related, as the YL<sub>Be</sub> band is only observed in samples doped with Be. It is unlikely to be related to other impurities, common in GaN, but it could be a complex of Be with a native defect or a common impurity. (c) The  $YL_{Be}$  band is due to the transition of an electron from the conduction band (or a shallow donor) to an acceptor level at 0.3 eV above the VBM, and it is not a radiative capture of a hole by a level 0.3 eV below the CBM. This type of transition is supported by the fact that the bright  $YL_{Be}$  band is observed in the *n*-type sample, where the PL lifetime for this band is  $\sim 50 \ \mu s$  at 100 K. If this PL were due to the radiative capture of holes from the valence band, these slow transitions could not compete with fast nonradiative capture



FIG. 13. Configuration coordinate diagram for the  $Be_{Ga}-V_N-Be_{Ga}$  complex. In semi-insulating or *n*-type samples, the defect is negatively charged. The photogenerated hole can be captured (dashed arrows) either to the ground state of the hole, i.e., the neutral state  $Be_{Ga}-V_N-Be_{Ga}^0$ , or to the excited state  $Be_{Ga}-V_N-Be_{Ga}^{0*}$ . The transition via the ground 0/- level of the  $Be_{Ga}-V_N-Be_{Ga}^{0*}$  complex is predicted to be nonradiative. The transition where the electron recombines with the hole in the excited state is radiative with the PL maximum of 2.3 eV and ZPL of 3.2 eV.

of holes by other defects, such as the Mg<sub>Ga</sub> acceptor, which is present in GaN as contaminant. Finally, the YL<sub>Be</sub> band in the studied MBE GaN:Be samples differs from the yellow band in bulk GaN:Be. In the latter, the yellow luminescence is very strong at room temperature [42] and its quenching begins at T > 500 K [19].

Among the computed Be-related defects and complexes (Be<sub>i</sub>, Be<sub>N</sub>, Be<sub>Ga</sub>-O<sub>N</sub>, Be<sub>Ga</sub>-V<sub>N</sub>-Be<sub>Ga</sub>, V<sub>Ga</sub>-Be<sub>i</sub>, Be<sub>Ga</sub>-O<sub>N</sub>-Be<sub>Ga</sub>, Be<sub>Ga</sub>-Be<sub>N</sub>-Be<sub>Ga</sub>, Be<sub>Ga</sub>-Be<sub>i</sub>-Be<sub>Ga</sub>, Be<sub>Ga</sub>-N<sub>i</sub>, V<sub>Ga</sub>-Be<sub>N</sub>, Be<sub>Ga</sub>-Ga<sub>i</sub>, V<sub>Ga</sub>-Be<sub>Ga</sub>), none exhibit an acceptor level at around 0.3 eV. Note that we also did not reproduce the previously suggested attribution of the YL<sub>Be</sub> band to the Be<sub>Ga</sub>-O<sub>N</sub> complex [18]. Our calculations show that this complex does not have any transition levels in the band gap. The polaronic +/0 transition level of the Be<sub>Ga</sub>-O<sub>N</sub> complex is found below the VBM for several HSE functional parametrizations, including that reproducing the bulk GaN band gap. Attribution of the YL<sub>Be</sub> defect, indicating that it is unlikely to be a donor.

A possible explanation for the nature of the  $YL_{Be}$  band is the  $Be_{Ga}-V_N-Be_{Ga}$  complex. It is the only stable defect that is negatively charged for the Fermi energy above about 1.5 eV. This complex can help explain the  $YL_{Be}$  band under the assumption of the existence of an excited state for the hole around 0.3 eV above the VBM. A configuration coordinate diagram, which is a combination of the HSE calculations and experimental data, is presented in Fig. 13.

The YL<sub>Be</sub> band is not observed in samples with a strong GL2 band. This is likely because the Fermi level in these samples is below the 0/- level of the Be<sub>Ga</sub>-V<sub>N</sub>-Be<sub>Ga</sub> complex, computed at 1.5 eV. In this case, the defect is in the positive

charge state, as shown in Fig. 3 (negative-U center), and the excited state for the hole does not form. In semi-insulating or *n*-type samples, the  $Be_{Ga}$ - $V_N$ - $Be_{Ga}$  complex is in the negative charge state (lower adiabatic potential in Fig. 13). The photogenerated electron-hole pair raises this adiabatic potential by the energy  $E_g$  (upper dashed potential labeled Be<sub>Ga</sub>-V<sub>N</sub>- $Be_{Ga}^{-} + E_g$ ). From this state, a hole can be captured to the defect ground state (the potential labeled  $Be_{Ga}$ - $V_N$ - $Be_{Ga}^0$ ) as shown with a dashed arrow. This capture occurs without any appreciable potential barrier. The transition from the neutral state to the negative state, i.e., via the 0/- thermodynamic transition level, also exhibits a relatively low potential barrier of 0.25 eV, suggesting the mostly nonradiative nature of these transitions (all are shown with the dashed arrows). Experimental measurements suggest the existence of an excited state of the hole (the potential labeled  $Be_{Ga}$ -V<sub>N</sub>-Be<sup>0\*</sup><sub>Ga</sub>), for which the hole capture is also efficient and without a barrier (shown with a dashed arrow). If the defect lattice structure for the excited state of the hole is similar to that of the ground state, an assumption made in Fig. 13, there is no nonradiative recombination route from this excited state to the negative ground state. As a result, only radiative transition from the excited state to the ground state is possible. Taking the ZPL of the YL<sub>Be</sub> from the experiment to be 3.2 eV, HSE calculations yield a Franck-Condon shift [43] of 0.9 eV, placing the predicted PL maximum of the radiative transition at 2.3 eV, in a reasonable agreement with experiment.

### E. Red band

In samples with strong  $YL_{Be}$ , the red band is very weak (Table I) and can be resolved only after the quenching of the YL<sub>Be</sub> band, which makes its analysis and attribution difficult. The RL<sub>Be</sub> is strong in several annealed samples where it overlaps with the green GL2 band. Figure 14 shows typical SSPL spectra from the annealed sample 0416b. The RL<sub>Be</sub> band has a maximum at 1.77 eV and Huang-Rhys factor 20 according to Eq. (4). The GL2 band with a maximum at 2.33 eV is attributed to the internal transitions via defect levels of the  $V_N$  [21]. Its shape is well known, and it completely quenches by the room temperature, revealing a broadened shape of the  $RL_{Be}$  band. To determine the parameters of the  $RL_{Be}$  band at low temperatures, the spectrum should be deconvoluted. The  $RL_{Be}$  was not saturated up to  $P_{exc} = 0.13 \text{ W/cm}^2$ . The peak intensity of the RL<sub>Be</sub> band is independent of temperature up to 100 K and decreases by an order of magnitude by 300 K.

Analysis of TRPL, shown in Fig. 15, provides additional information about the RL<sub>Be</sub> band. Its shape in SSPL and TRPL experiments is the same, which indicates that the broad red band is caused by one defect. The PL decay after the laser pulse at T = 18 K is exponential for both RL<sub>Be</sub> and GL2 bands, with lifetimes about 2  $\mu$ s [Fig. 15(b)] and 250  $\mu$ s (not shown), respectively. The RL<sub>Be</sub> lifetime decreases by a factor of 3 in the temperature range from 18 to 200 K [Fig. 15(b)].

The RL<sub>Be</sub> band in the SSPL spectra can be confused with the RL1 [36], RL2 [44,45], or RY3 [46] bands in undoped GaN with the maxima at 1.73, 1.72, and 1.77 eV, respectively, unless additional time-resolved and temperature measurements are taken. The RL1 band often appears in *n*-type GaN grown by HVPE and is attributed to the DAP transition.



FIG. 14. SSPL spectra from Be-doped GaN (sample 0416b) at T = 18 K and selected excitation intensities. The red, green, and ultraviolet luminescence bands are denoted as RL<sub>Be</sub>, GL2, and UVL<sub>Be</sub>, respectively. The shapes of the bands (shown with green crosses and black circles) were simulated with Eq. (4), where  $E_0 = 2.7$  eV,  $\hbar\omega_{\text{max}} = 1.77$  eV, and  $S_e = 20$  for the RL<sub>Be</sub> and  $E_0 = 2.85$  eV,  $\hbar\omega_{\text{max}} = 2.33$  eV, and  $S_e = 26.5$  [21] for the GL2. We could not identify the feature in-between the GL2 and UVL<sub>Be</sub> bands, and it was not reproduced among the samples.

Unlike the RL<sub>Be</sub>, the decay of the RL1 is nonexponential at low temperature and becomes exponential with  $\tau \sim 1$  ms at T = 100 K. The RL2 band is observed in Ga-rich, semiinsulating GaN. It is caused by an internal transition from an excited state to the ground state of an unidentified defect and can be distinguished by the slow exponential decay after laser pulse [33]. Its lifetime decreases from 110 to 2  $\mu$ s with increasing temperature from 15 to 100 K [45]. The RY3 band is found in undoped *n*-type GaN grown with HVPE and consists of two components, namely, RL3 and YL3, both originating from the same defect [46]. A careful comparison of the properties of all these red bands in GaN shows that the RL<sub>Be</sub> is a new, Be-related PL band.

HSE calculations suggest that the RL<sub>Be</sub> band originates from the  $Be_{Ga}$ - $V_N$  complex. The configuration coordinate diagram for this defect is shown in Fig. 16. Calculations predict this complex to be a deep donor, with the +/0 transition level at 0.95 eV above the VBM. When the Fermi level is above the +/0 level, the defect is neutral in the ground state (the lower potential in Fig. 16). An electron-hole pair is created by the above-band-gap photoexcitation, raising the energy of the system by the GaN band gap of 3.5 eV (the dashed potential). Resonant excitation energy for this defect (3.42 eV) is close to the band-gap value. The photogenerated hole is captured by the BeGa-VN complex without a barrier (the dashed arrow in Fig. 16), releasing the excess energy of 0.95 eV as phonons and converting the defect into positively charged. The nonradiative transition from the positive to the neutral charge state of the complex is hindered by a large potential barrier for this transition of about 1 eV (the + and 0 potentials intersect at  $Q \sim 8.2$  amu<sup>1/2</sup> Å, with the energy of 3.6 eV), making this defect radiative. The radiative transition is shown with a downward arrow, which causes a red band with a calculated maximum of 1.73 eV and ZPL of 2.55 eV, in good agreement with the experimental results. Note that from the experiment the  $RL_{Be}$  band is caused by an internal transition: from an excited state presumably located close to the conduction band to the deep ground state of the donor. The transition of electrons from the conduction band to the ground state is much less efficient and could contribute to the tail in the  $RL_{Be}$  decay shown in Fig. 15(b). Most likely, the excited state is a hydrogenic Coulomb state appearing below the CBM only when the donor is positively charged.

With the above attribution of the YL<sub>Be</sub> and RL<sub>Be</sub> bands to the  $Be_{Ga}$ - $V_N$ - $Be_{Ga}$  and  $Be_{Ga}$ - $V_N$  complexes, we can explain the regularities in the appearance of these bands in different samples mentioned in Sec. III A. The key point is the position of the Fermi level, which depends on the relative concentrations of defects and may sharply change across a sample. Figure 17 shows schematically transition levels of the defects studied in this work. The concentrations of the  $O_N$ ,  $Be_{Ga}-V_N$ ,  $V_N$ , Be<sub>Ga</sub>, and Be<sub>Ga</sub>- $V_N$ -Be<sub>Ga</sub> defects are  $N_{D1}$ ,  $N_{D2}$ ,  $N_{D3}$ ,  $N_{A1}$ , and  $N_{A2}$ , respectively. For *n*-type GaN with the Fermi level pinned at the D1 (0/+) level, inequality  $N_{D1} > N_{A1} + N_{A2}$ holds. As the concentrations of acceptors increase, the Fermi level shifts to the A2 levels and stays there while inequality  $N_{A2} > N_{A1} - N_{D1}$  is valid. In both cases the YL<sub>Be</sub> band is strong because photogenerated holes are quickly captured by the excited state (at 0.3 eV above the VBM) of the negatively charged Be<sub>Ga</sub>-V<sub>N</sub>-Be<sub>Ga</sub> acceptors. A strong UVL<sub>Be</sub> band is observed in samples annealed at 900 °C to activate the acceptors, yet the concentration of the isolated Be<sub>Ga</sub> acceptors is lower than that of the  $Be_{Ga}$ -V<sub>N</sub>-Be<sub>Ga</sub> complexes (Table I). The RL<sub>Be</sub> and GL2 bands are weak because donors are less efficient in capturing holes. Further, the Fermi level is pinned at the D2 level in samples with  $N_{A2} < N_{A1} - N_{D1}$ . The sharp transition of the Fermi level from D2 and A2 occurs when  $N_{A2}$  exceeds  $(N_{A1} - N_{D1})$ . It may happen in the same samples where these concentrations are very close to each other and gradient of the concentrations exist. The conclusions are valid in a more general situation where  $N_{A1}$  represents all acceptors with transition levels below A2 and  $N_{D1}$  represents all donors with transition levels above A2. As  $N_{A2} < N_{A1} - N_{D1}$ , all the Be<sub>Ga</sub>-V<sub>N</sub>-Be<sub>Ga</sub> defects are positively charged, the acceptor excited state disappears, and no YL<sub>Be</sub> band can be observed. Note that recombination pathways are difficult to predict in semi-insulating semiconductors where nonlinear effects may lead to population inversion at low temperatures and tunable thermal quenching [35]. According to the model proposed in Ref. [35], the most efficient recombination channels are characterized by the fastest capture of holes below the critical temperature  $T_0$ , while recombination channels with the fastest capture of electrons dominate above  $T_0$ . The abrupt and tunable quenching of the YLBe band (Sec. III D) indicates that this band, as a very efficient hole trap, is strong in samples where the hole capture determines PL intensities. On the other hand, the RL<sub>Be</sub> and GL2 bands are strong in samples where the electron capture determines PL intensities. The related donors quickly capture photogenerated electrons thanks to the excited states close to the conduction band. Thus, a sharp boundary between the "yellow" and "red" regions in samples



FIG. 15. TRPL from sample 0416b. (a) The TRPL spectra at T = 100 K and selected time delays after the laser pulse. At longer time delays, the GL2 band with the characteristic lifetime of about 0.2 ms can be resolved (not shown). The SSPL spectrum at  $P_{\text{exc}} = 0.0047$  W/cm<sup>2</sup> is shown with the solid line for comparison. (b) Normalized decays at 1.8 eV at selected temperatures. The RL<sub>Be</sub> band decays exponentially and can be traced up to about 0.1 ms. The thick solid lines are the exponents with lifetimes 0.7 and 2.1  $\mu$ s.

0406b and 0410b (examples of PL spectra are shown in Fig. 2) can be explained by gradual change of the defect concentrations, which may result in an abrupt shift of the Fermi level, similar to what was observed in Ref. [21].

# **IV. CONCLUSIONS**

The experimental PL spectra from GaN:Be samples grown by MBE contain four major PL bands: ultraviolet  $UVL_{Be}$ , yellow  $YL_{Be}$ , red  $RL_{Be}$ , and green GL2. The  $UVL_{Be}$  band is caused by the electronic transitions from the conduction band (or shallow donors) to the 0/- shallow level of the  $Be_{Ga}$ acceptor located at 113 meV above the valence band. The quenching of the  $UVL_{Be}$  band (which was observed only in semi-insulating samples) is tunable by the excitation intensity.



FIG. 16. Configuration coordinate diagram for the  $Be_{Ga}-V_N$  complex. The photogenerated hole is captured by the  $Be_{Ga}-V_N$  defect, with subsequent radiative recombination with PL maximum calculated at 1.73 eV and ZPL at 2.55 eV.

The GL2 band is caused by the V<sub>N</sub> defects, and it appears only when the YL<sub>Be</sub> is absent and usually together with the stronger  $RL_{Be}$  band. The  $YL_{Be}$  is attributed to the  $Be_{Ga}\mathchar`-V_N\ma$  $Be_{Ga}$  acceptor. Its 0/- level is calculated at 1.5 eV above the VBM. To explain the experimental results, we propose that the negatively charged BeGa-VN-BeGa acceptor forms an excited state for the hole at 0.3 eV above the VBM. The radiative transitions of electrons from the conduction band to this level are more efficient than nonradiative transitions via the ground state, and the former cause the YL<sub>Be</sub> band. In *n*-type GaN:Be, the YL<sub>Be</sub> band is quenched by the Schön-Klasens mechanism and reveals the ionization energy of 0.3 eV and the holecapture coefficient of  $4 \times 10^{-7}$  cm<sup>3</sup>/s. In semi-insulating GaN:Be samples, the YL<sub>Be</sub> band is quenched by the abrupt and tunable quenching mechanism, and the quenching behavior agrees with above-mentioned parameters.

The RL<sub>Be</sub> band is attributed to the  $Be_{Ga}$ -V<sub>N</sub> donor with the +/0 level located at 0.95 eV above the VBM. First, a



FIG. 17. Band diagram with transition levels for the shallow  $O_N$  donor (D1),  $Be_{Ga}$ - $V_N$  complex (D2),  $V_N$  (D3),  $Be_{Ga}$  acceptor (A1), and  $Be_{Ga}$ - $V_N$ - $Be_{Ga}$  complex (A2). Radiative and nonradiative transitions are shown with wavy and dotted lines, respectively.

photogenerated hole is captured at this level, and the hydrogenic Coulomb excited state is formed near the conduction band. A free electron is captured by this state. Finally, the electron and hole recombine (the internal transition) to produce the  $RL_{Be}$  band. The decay of the  $RL_{Be}$  intensity after a laser pulse is exponential, and the characteristic PL lifetime (about 2  $\mu$ s) is weakly dependent on temperature between 18 and 200 K.

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