

## Probing many-body interactions in the cyclotron resonance of *h*-BN/bilayer graphene/*h*-BN

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Unlike a conventional two-dimensional electron gas system, which has parabolic band structure, the nonparabolic band dispersion of mono- to few-layer graphene violates Kohn's theorem. Thus, Landau levels (LLs) in graphene are sensitive to many-body interactions. This modifies the LL spacing, depending on the location of the Fermi energy ( $E_F$ ). Such effects have been extensively studied in *h*-BN/monolayer graphene/*h*-BN through observation of inter-LL optical transitions known as cyclotron resonances (CRs). However, thus far, the influence of many-body interactions on the CR of bilayer graphene (BLG) has been rarely studied, even though BLG also possesses nonparabolic band dispersion. Here, we investigate CR in the *h*-BN/BLG/*h*-BN structure via magneto-photothermoelectric measurements under infrared laser irradiation. This method enables sensitive detection of cyclotron resonances while tuning  $E_F$  of BLG. The CR magnetic field value shifted significantly when  $E_F$  of BLG approached the charge-neutrality point (the Dirac point, DP). We attribute this to a change in the Fermi velocity of BLG near the DP, which occurs as a result of many-body interactions.

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The unique band structure of Landau-quantized mono- to few-layer graphene has been probed via the study of inter-Landau level transitions, which are also known as cyclotron resonances (CRs) [1–10]. Unlike electrical transport measurements, in which transport properties at the Fermi level are detected, CR measurement enables the detection of properties away from the Fermi level. Therefore, this method is a very powerful tool for investigating Fermi-level dependent changes in CR transitions, revealing variation in the inter-Landau level spacing as a function of Fermi energy. Pioneering research has been carried out recently on high-quality monolayer graphene encapsulated by the insulator *h*-BN and revealed the presence of a significant many-body interaction that modulates the energy gap for CR transitions, depending on the Fermi level of the graphene layer [5,6]. This finding raised a series of related questions that have been examined in theoretical as well as experimental studies [11,12]. This many-body interaction effect is in striking contrast to the behavior of a conventional two-dimensional electron gas system, which has a parabolic band structure and CR that is insensitive to many-body interactions, in accordance with Kohn's theorem [13]. Graphene provides a novel platform to investigate the correlation between CR and many-body interaction. Particularly, in bilayer graphene (BLG), the many-body interaction is expected to contribute to CR because BLG also possesses nonparabolic band dispersion (which is sometimes referred to as massive Dirac band structure) [11,13,14]. However, the effect of many-body interaction on CR has rarely been investigated in the case of BLG. Interaction-driven reconstruction

of the band structure has been observed in suspended BLG at zero magnetic field [15] and recent studies on the CR measurement of BLG revealed unconventional selection rules and discussed the possible contribution of many-body interaction [16]; however, no detailed investigation has been presented thus far. Herein, we demonstrate the influence of many-body interactions on the LLs of BLG encapsulated by *h*-BN via magneto-photothermoelectric effect measurements.

A schematic illustration of the device structure investigated in this study is presented in Fig. 1(a). A two-terminal *h*-BN/BLG/*h*-BN structure was placed on a 290-nm SiO<sub>2</sub>/highly doped Si substrate with Au/Cr electrodes. The channel region was shaped into a mesa structure by reactive ion etching with a mixture of CF<sub>4</sub>, Ar, and O<sub>2</sub>. The doped Si was used as a back gate to control the carrier density of the BLG. The sample was placed in a liquid He cryostat with a variable-temperature insert and superconducting magnet. In the experimental arrangement, light from a wavelength-tunable CO<sub>2</sub> laser (Access Laser Inc. Merit-G, wavelength  $\lambda$ , 9.24–10.675  $\mu\text{m}$ ) was delivered to the sample using a hollow-core optical fiber and light pipe; note that the laser light reaching the sample was unpolarized. Thus, the photovoltage generated between the two electrodes of the BLG was measured under low-temperature and high-magnetic field conditions [3,4,7,8].

The two-terminal conductance  $G$  was measured during the application of an AC current ( $I_{ac} = 10 \text{ nA}$ ) at a frequency of 18 Hz as its carrier density  $n$  (tuned by the back-gate voltage  $V_{BG}$ ) was varied at 2.0 K, and the results are shown in Fig. 1(b). This plot indicates ambipolar characteristics for the conductance. The photovoltage,  $V_{ph}$ , was measured during irradiation, as illustrated in Fig. 1(a). For these measurements, we used a lock-in detection method such that the CO<sub>2</sub> laser

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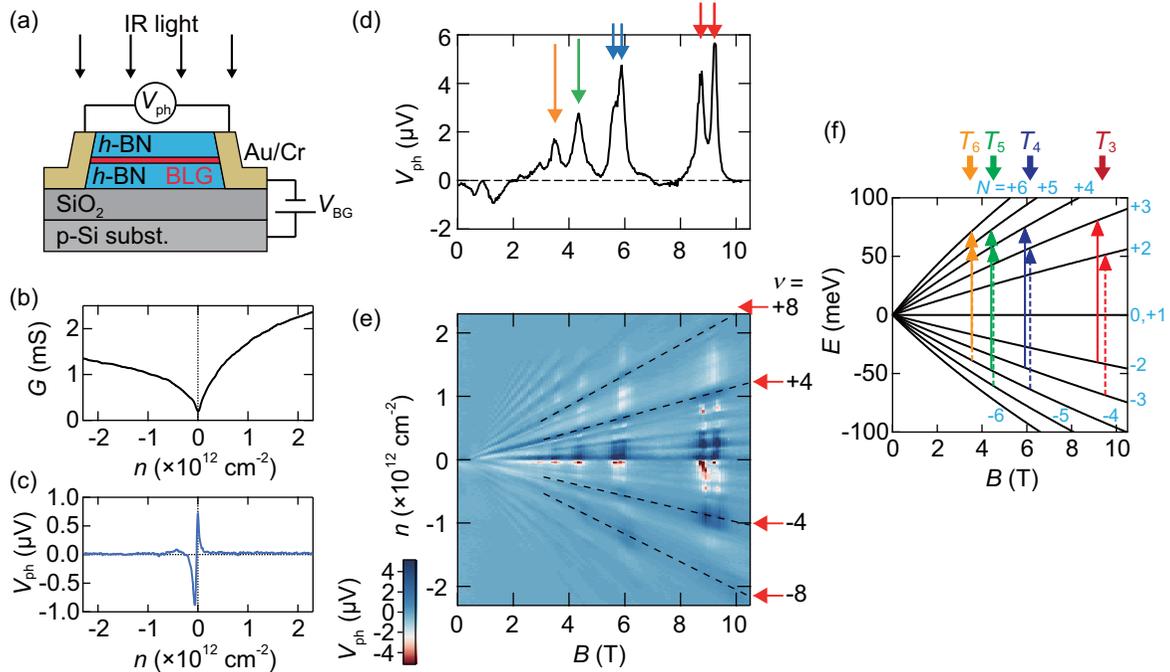


FIG. 1. (a) Schematic illustration of device structure. (b) Two-terminal conductance  $G$  as a function of carrier density  $n$ . (c) Photovoltage  $V_{\text{ph}}$  as a function of  $n$ . (d)  $V_{\text{ph}}$  as a function of magnetic field  $B$  at fixed  $n$  ( $n = 5.94 \times 10^{10} \text{ cm}^{-2}$ ). (e)  $V_{\text{ph}}$  as a function of  $B$  and  $n$ . (f) Energies of LLs with LL indices in the range of  $N = -6$  to  $+6$ ; cyclotron resonance transitions  $T_3$  to  $T_6$  are indicated by arrows. All the experimental data shown in this figure were acquired at a temperature of 2.0 K.

was modulated by an optical chopper at a frequency of 18 Hz and the photovoltage was measured using a lock-in amplifier. The variation of  $V_{\text{ph}}$  with  $n$  measured at zero magnetic field and  $T = 2.0 \text{ K}$  under irradiation at  $\lambda = 10.675 \mu\text{m}$  is shown in Fig. 1(c). In this plot,  $V_{\text{ph}}$  has a signal with a peak and dip structure centered around  $n = 0$ , the charge-neutrality point (Dirac point, DP), in contrast to the dip structure shown in Fig. 1(b). The peak and dip at the DP is reminiscent of the photothermoelectric effect [3,4]. It has been established that the photothermoelectric effect is the dominant mechanism for photovoltage generation in graphene devices [3,4,7]. In this mechanism, light absorption by graphene first increases its electron temperature and creates a temperature gradient at the junction between the graphene channel and the graphene in contact with the metal electrode. Subsequently, this induces a thermoelectric voltage at the junction between the graphene channel and the metal-covered graphene. Thus, the  $n$ -dependent shape of  $V_{\text{ph}}$  reflects the shape of the thermoelectric coefficient of BLG, which has a peak and dip structure near the DP [3,4,8,17–19]; this is consistent with our observations as shown in Fig. 1(c).

Next, the dependence of  $V_{\text{ph}}$  on the magnetic field  $B$  at fixed  $n = 5.94 \times 10^{10} \text{ cm}^{-2}$ ,  $\lambda = 10.675 \mu\text{m}$ , and  $T = 2.0 \text{ K}$  was measured, and the results are shown in Fig. 1(d). A series of peaks observed in the high- $B$  region is indicated by arrows in the figure. The variation of  $V_{\text{ph}}$  with  $B$  and  $n$  is shown as a 2D plot in Fig. 1(e), where a series of resonances is also apparent. We attributed these signals to BLG cyclotron resonances. In Fig. 1(f), the energies of Landau levels with different indices  $N$  are plotted with respect to  $B$ . Considering the irradiation energy  $E_{\text{ph}}$  at  $\lambda = 10.675 \mu\text{m}$  ( $E_{\text{ph}} = 116.14 \text{ meV}$ ) and the  $\Delta|N| = \pm 1$  selection rule for cyclotron resonance

transitions, several different transitions, namely  $T_3$ – $T_6$ , should be observable within the magnetic field range we studied. Each transition consists of two different channels: the  $T_3$  transition ( $N = -2 \rightarrow +3$  and  $N = -3 \rightarrow +2$  channels), the  $T_4$  transition ( $N = -3 \rightarrow +4$  and  $N = -4 \rightarrow +3$ ), the  $T_5$  transition ( $N = -4 \rightarrow +5$  and  $N = -5 \rightarrow +4$ ), and the  $T_6$  transition ( $N = -5 \rightarrow +6$  and  $N = -6 \rightarrow +5$ ). Because of the electron-hole asymmetry in the band dispersion of BLG [1,20,21], for the same  $|N|$ , the LL energies of electrons (positive  $N$ ) are always greater than those of holes (negative  $N$ ) for  $N > 2$ . For the  $T_3$  transition, the transition channel corresponding to  $N = -2 \rightarrow +3$  appeared at lower  $B$  field with respect to that for  $N = -3 \rightarrow +2$ . Similarly, for the  $T_4$  transition,  $N = -3 \rightarrow +4$  appeared at lower  $B$ -field values than  $N = -4 \rightarrow +3$ , and so on. Note that in principle more transitions can be identified, such as  $T_7$  and  $T_8$ , at low  $B$ ; however, these signals are too small to distinguish. For this reason, we discuss the CR transitions  $T_3$  to  $T_6$  in the present paper.

Next, in Figs. 2(a) and 2(b) we present detailed  $V_{\text{ph}}$  mapping for the  $T_3$ ,  $T_4$ , and  $T_5$  transitions as a function of  $B$  and  $n$ ; the black dashed straight lines in these figures are a guide to the eye. Comparing the experimental data with these lines reveals that the magnetic field value for the cyclotron resonance signal  $B_r$  of BLG is not constant as a function of  $n$ , instead exhibiting rather complex variation. In Fig. 2(a), the  $T_4$  and  $T_5$  transitions gradually shift lower values when  $n$  approaches zero. For the two different channels of the  $T_3$  transition presented in Fig. 2(b),  $B_r$  exhibits a sudden change to a lower value near  $n = 0$ . Selected traces from Figs. 2(a) and 2(b) are presented in Appendix A. These shifts in  $B_r$  with respect to  $n$  are not predicted by the single-particle model

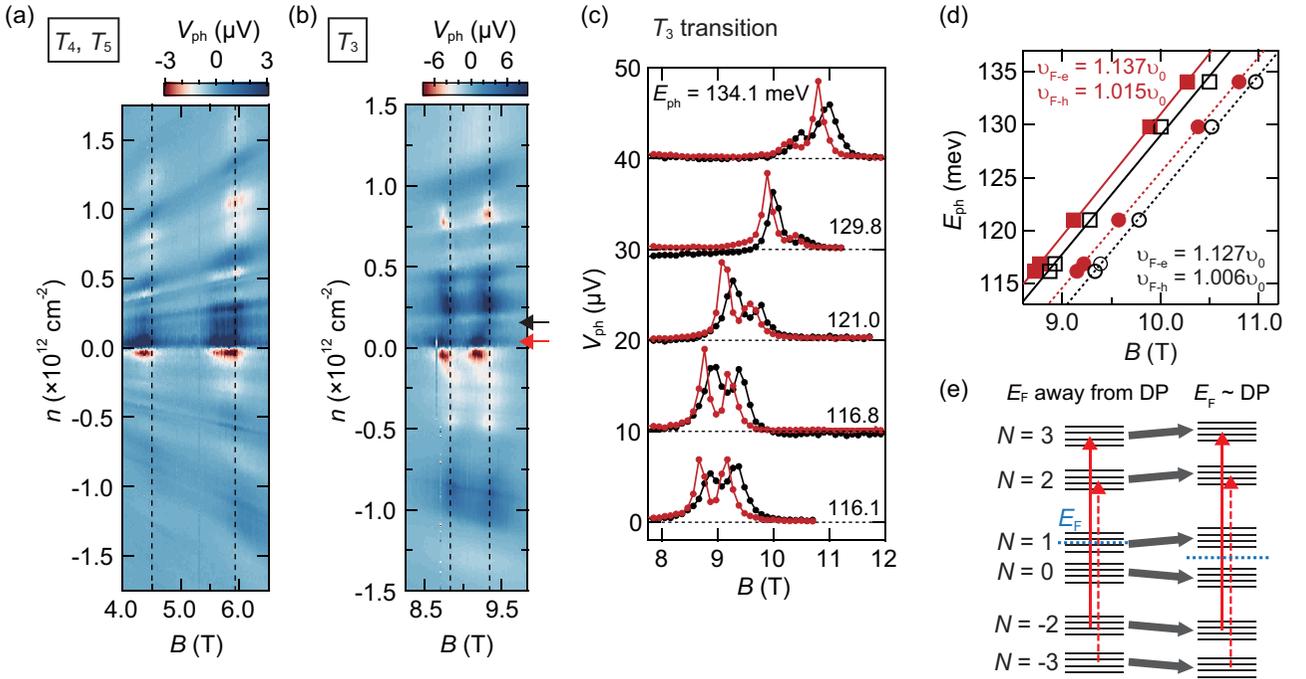


FIG. 2. (a), (b) Detailed mapping of  $V_{ph}$  as a function of magnetic field  $B$  and carrier density  $n$  at  $T = 2.0$  K under irradiation at a wavelength  $\lambda$  of  $10.675 \mu\text{m}$  for (a)  $T_4$  and  $T_5$  transitions, and (b)  $T_3$  transition. (c)  $V_{ph}$  vs  $B$  traces at selected  $\lambda$  (or  $E_{ph}$ ). The red lines correspond to the case where Fermi energy  $E_F$  being located close to the Dirac point, while black lines correspond to  $E_F$  being away from the DP. Traces are offset for clarity and the baselines (corresponding to  $V_{ph} = 0$ ) for each trace are indicated by the horizontal dashed lines. (d) Relationship between irradiation energy for the  $T_3$  transition and the magnetic field value of the cyclotron resonance. Solid and dashed lines indicate calculated results for the energies of each transition based on Eq. (1). In the figure,  $v_0$  is defined as  $1 \times 10^6$  m/s. (e) Schematic energy level diagram illustrating the  $E_F$  dependence of cyclotron resonance transitions.

(this model predicts that  $B_r$  is constant under variation of  $n$ ). Therefore, we believe that the shift in  $B_r$  with  $n$  is an effect of many-body interactions in BLG. Similar changes in  $B_r$  with  $n$  have been reported in  $h$ -BN/MLG/ $h$ -BN and discussed in terms of many-body interactions [5,6]; our result is the demonstration of an unambiguous signature of many-body interactions on BLG.

We measured  $V_{ph}$  versus  $B$  at the irradiation wavelengths of  $10.675$ ,  $10.611$ ,  $10.275$ ,  $9.552$ , and  $9.24 \mu\text{m}$ . For each wavelength, we examined two different  $n$  values,  $n = 4.0 \times 10^{10} \text{ cm}^{-2}$  and  $1.55 \times 10^{11} \text{ cm}^{-2}$ , corresponding to the vicinity of the DP and away from the DP, respectively [indicated by red and black arrows, respectively, in Fig. 2(b)]; these results are plotted in Fig. 2(c) and traces are offset for clarity in the figure. Overall, both peaks in the double-peak structure of the  $T_3$  transition shift with  $\lambda$ , as expected for CR. In addition, we found that the  $B_r$  for  $n$  values near to the DP (red line) are lower than those for  $n$  away from the DP (black line) for the same  $\lambda$ . The  $B_r$  values of the double-peak structures in Fig. 2(c) were extracted for two different  $n$  values, and these are plotted with respect to the irradiation energy  $E_{ph}$  as shown by the circles and the squares in Fig. 2(d). The LLs of BLG were calculated using the following equation [1]:

$$E_N = \frac{\text{sgn}(N)}{\sqrt{2}} \left[ (2|N| + 1)\Delta^2 + \gamma_1^2 - \sqrt{\gamma_1^4 + 2(2|N| + 1)\Delta^2\gamma_1^2 + \Delta^4} \right]^{1/2}, \quad (1)$$

where  $\gamma_1$  is the interlayer coupling energy and  $\Delta = \sqrt{2eBv_F\hbar}$ . Here,  $v_F$  denotes the Fermi velocity,  $e$  the elementary charge, and  $\hbar$  the reduced Planck constant. Then, the relationships between the transition energy and  $B_r$  for the two different channels in the  $T_3$  transition (between  $N = -2$  and  $+3$ , and between  $N = -3$  and  $+2$ ) were calculated, and these are plotted in Fig. 2(d) as solid and dashed lines, respectively. We found that the experimentally obtained peak positions were in good agreement with Eq. (1) plotted using the electron Fermi velocity  $v_{F-e} = 1.137 \times 10^6$  m/s, hole Fermi velocity  $v_{F-h} = 1.015 \times 10^6$  m/s, and  $\gamma_1 = 0.39$  eV for the data in the vicinity of the DP (red lines). In contrast to this, for the data away from the DP, we found that using  $v_{F-e} = 1.127 \times 10^6$  m/s,  $v_{F-h} = 1.006 \times 10^6$  m/s, and  $\gamma_1 = 0.39$  eV (black lines) resulted in good correspondence with the experimental data. Here, the different Fermi velocity values for the electrons and holes represent the electron-hole asymmetry of the band structure in BLG [1,20,21]. We assumed that the ratio  $v_{F-e}/v_{F-h}$  and the value of  $\gamma_1$  was constant for all the calculations. These comparisons allowed us to confirm our identification of BLG cyclotron resonances in the photothermoelectric measurements. In addition, we observed significantly different  $B_r$  values depending on the position of the  $E_F$  of BLG irrespective of the irradiation wavelength. The many-body interactions modify the energy splitting of the LLs, depending on the Fermi level, as illustrated in Fig. 2(e); when  $E_F$  is close to the DP, the spacing between the LLs increases as a result of many-body interactions [5,6]. The result shown here implies that for BLG there is a significant contribution from many-body

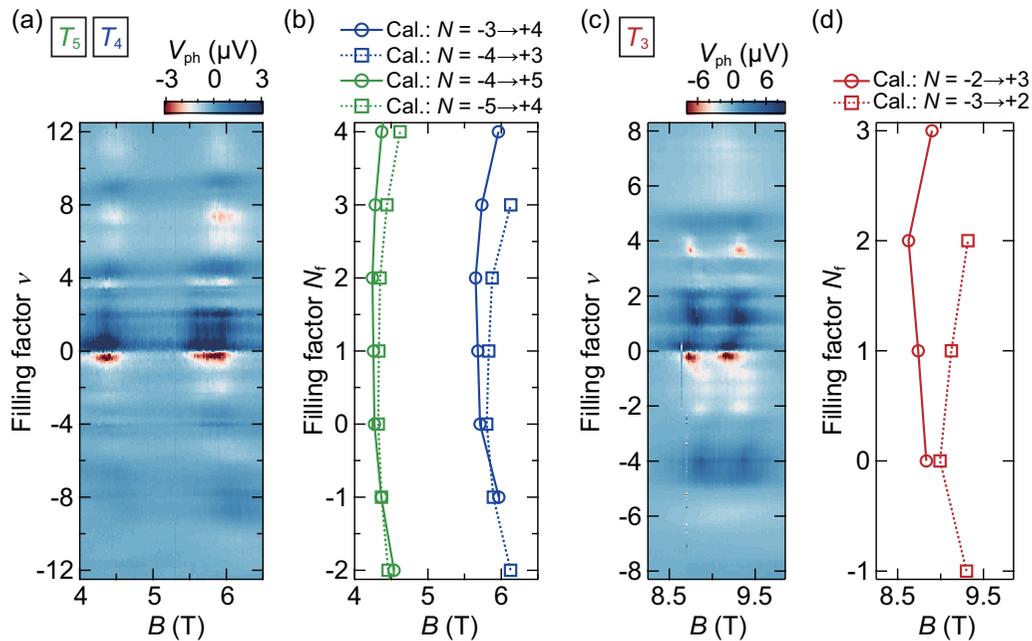


FIG. 3. (a), (c) Image plot of  $V_{ph}$  as a function of magnetic field  $B$  and quantum Hall filling factor  $\nu$  at  $T = 2.0\text{ K}$  under irradiation at a wavelength  $\lambda$  of  $10.675\ \mu\text{m}$  for the (a)  $T_4$  and  $T_5$  transitions and (c)  $T_3$  transition. (b), (d) Positions of CR transition estimated from the theoretical calculation using a many-body correction for the (b)  $T_4$  and  $T_5$  transitions, and (d)  $T_3$  transition plotted vs the number of filled Landau levels  $N_f$ . The theoretical calculation results are extracted from Ref. [22].

interactions to the LLs that modify the energy splitting of the LLs due to the change of Fermi velocity depending on  $E_F$ . From the vertical offset between the straight lines in Fig. 2(d), the difference in the inter-LL spacing for the  $T_3$  transitions ( $E_F$  close to the DP versus  $E_F$  away from the DP) is 2 meV.

Detailed many-body interaction corrections of the LLs of BLG were recently calculated and reported by Shizuya [22]. Here, we compare our results with these theoretical calculations. To do this,  $V_{ph}$  data presented in Figs. 2(a) and 2(b) are plotted as a function of quantum Hall filling factor  $\nu = hn/eB$  and magnetic field  $B$ , and the results are shown in Figs. 3(a) and 3(c), where  $h$  denotes the Planck constant. There are many horizontal lines that appear along constant  $\nu$  in Figs. 3(a) and 3(c). These are nonresonant background thermoelectric signal under irradiation. As far as the cyclotron resonance signal is sufficiently larger than this background signal, we can distinguish these two contributions (comparison between these contributions are presented in Appendix B). For comparison, the position of  $B_r$  expected from the theoretical calculation including many-body interaction is also presented in Figs. 3(b) and 3(d) with respect to the number of filled Landau levels  $N_f$ . Since the calculation reported in Ref. [22] was used to estimate the change of LL energies due to the many-body interaction contribution and normalized to the value obtained by neglecting many-body interaction effects, we converted the calculation result to the change of  $B_r$  by using Eq. (1) (details of this conversion procedure are presented in Appendix C). Here, only the adjustment parameter is Fermi velocity of BLG without many-body interaction contribution  $v_{F0}$ ; we used this value to adjust the offset position of  $B_r$  presented in Figs. 3(b) and 3(d) to match with experiment, while relative change of  $B_r$  with respect to  $N_f$  does not significantly alter with this procedure. We also note that the definition of the filling factor

$\nu$  in the experiment is not exactly the same as that of  $N_f$  as used in Ref. [22];  $N_f = -2, -1, 0, +2, +3, +4$  can be considered to be equivalent to  $\nu = -12, -8, -4, +4, +8$ , and  $+12$ , respectively. However,  $N_f = +1$  cannot be uniquely associated with  $\nu = 0$  because it is highly dependent on the valley and spin configuration of the lowest LLs of BLG ( $N = 0$  and  $+1$  in terms of the LL indices).

We noticed several interesting differences and similarities between the experiment and calculation. First, the experimental results for the  $T_4$  and  $T_5$  transitions showed a decrease of  $B_r$  from high  $\nu$  to  $\nu = 0$ . By contrast, the calculation results indicated the  $B_r$  decrease approaching  $N_f = 0$  or  $+2$  (corresponds to  $\nu = -4$  and  $+4$ , respectively), depending on the transition channel. Although both experiment and calculation results in Figs. 3(a) and 3(b) showed that change of  $B_r$  exhibits convex to the left shape with similar ratios, the peak filling factors are different. Because of the different peak  $N_f$  positions for different channels, in the calculation, the splitting between the two different channels in the  $T_3$  and  $T_4$  transitions is larger for  $N_f > 0$ . In the experimental data, such a tendency is not obvious. Second, the experimental results for the  $T_3$  showed a sharp reduction of  $B_r$  between  $\nu = -1$  and  $+1$ , while the calculation results indicated the  $B_r$  gradually decrease approaching  $N_f = 0$  or  $+2$  similar to the  $T_4$  and  $T_5$  transitions. As we discussed in Fig. 2, this sharp reduction of  $B_r$  in the experiment corresponds to the increase of energy separation of LLs between  $\nu = -1$  and  $+1$ , and such sharp change in the calculated results is not discussed in Ref. [22]. Although the origin of these above-mentioned discrepancies between the experimental and theoretical data is not clear at this moment, we suggest that our results indicate that the detail of the LL structure plays an important role in determining the electronic behavior of BLG. We note that the detailed sequence of LLs

(spin, valley, and orbit) may be different between experiment and theory. The calculations were made assuming a valley-dominant sequence in LLs, while we could not confirm the exact LL sequence in our device. The LL sequence in the range of  $\nu = -4$  to  $+4$  is sensitive to various parameters, such as interlayer bias and magnetic field; this could be the origin of the difference between the results obtained using our device and the calculation results presented in Ref. [22]. Our results may stimulate further theoretical work aimed at obtaining a complete understanding of the effects of many-body interactions in BLG.

In summary, we demonstrated cyclotron resonances in  $h$ -BN/BLG/ $h$ -BN structures via photothermoelectric mea-

surements under infrared laser irradiation. This method enables the detection of multiple cyclotron resonance transitions as the value of  $E_F$  for BLG is varied. The magnetic field value for the cyclotron resonance underwent a non-negligible shift when the  $E_F$  of BLG approached the DP. We attribute this to a many-body interaction effect occurring in the high-quality BLG. Our results revealed a significant contribution of many-body interaction effects to the CR of BLG and provide an effective method for probing these interaction effects in graphene heterostructures.

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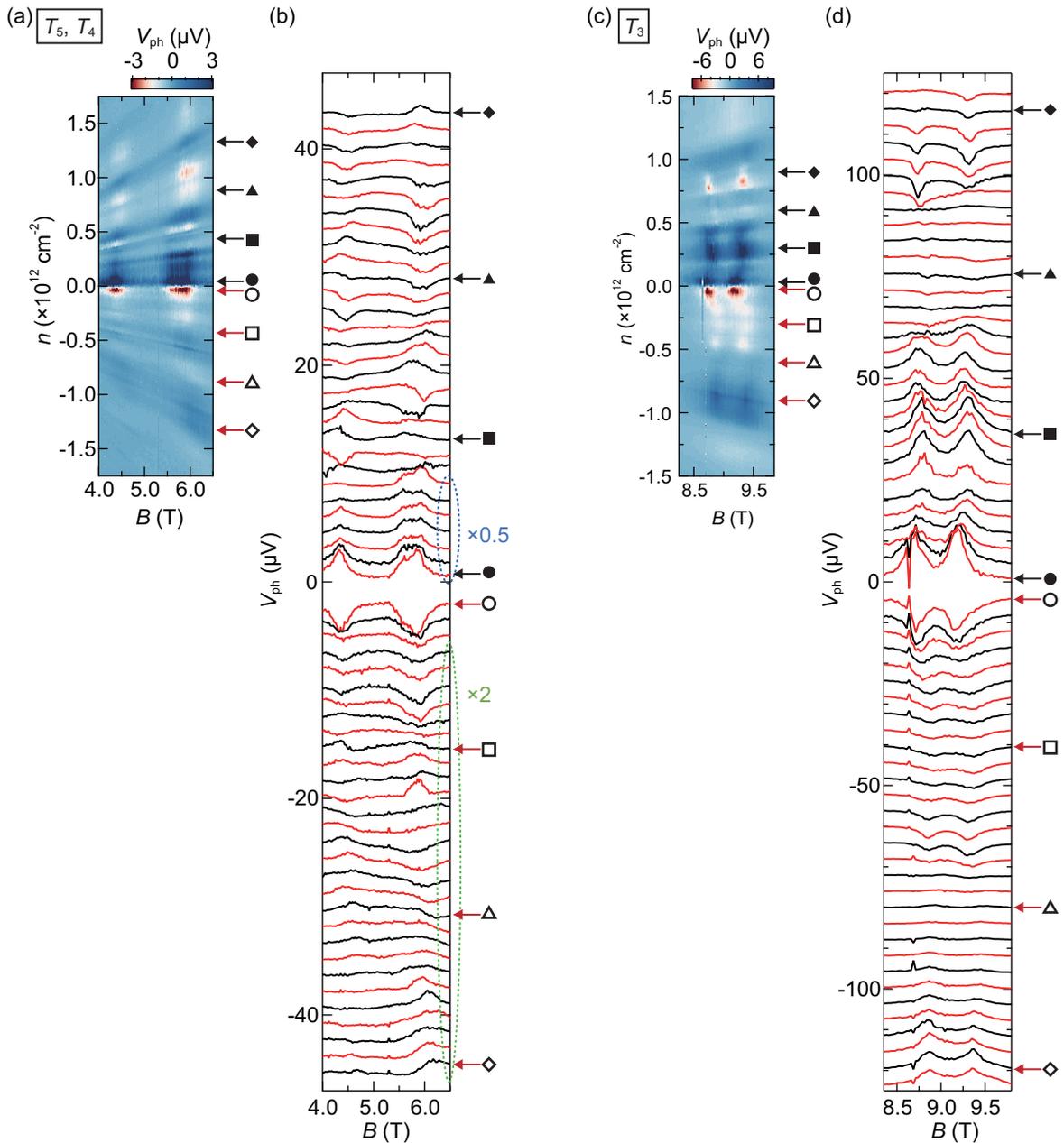


FIG. 4. (a), (c) Detailed mapping of  $V_{ph}$  as a function of magnetic field  $B$  and carrier density  $n$  at  $T = 2.0$  K under irradiation at a wavelength  $\lambda$  of  $10.675 \mu\text{m}$  for the (a)  $T_4$  and  $T_5$  transitions and (c) the  $T_3$  transition. (b), (d)  $V_{ph}$  vs  $B$  traces at selected  $n$  values for (b) the  $T_4$  and  $T_5$  transitions and (d) the  $T_3$  transition. The corresponding  $n$  values are indicated by circles, squares, triangles, and diamonds in panels (a) and (c). The traces are offset for clarity, and those indicated by blue and green dashed circles are multiplied by a factor of 0.5 and 2.0, respectively.

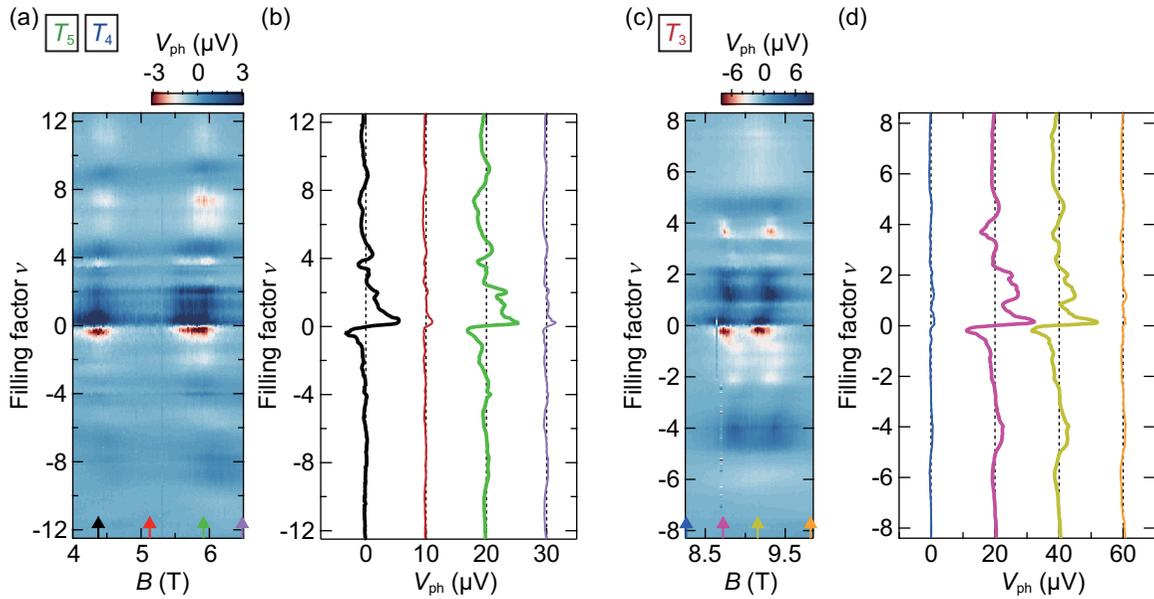


FIG. 5. (a), (c) Image plot of  $V_{ph}$  as a function of magnetic field  $B$  and quantum Hall filling factor  $\nu$  at  $T = 2.0$  K under irradiation at a wavelength  $\lambda$  of  $10.675 \mu\text{m}$  for the (a)  $T_4$  and  $T_5$  transitions and (c)  $T_3$  transition. (b), (d) Cross section of panels (a), (c) at constant  $B$ . The corresponding  $B$  values are indicated by arrows in panels (a), (c). The traces shown by thick lines are data at the cyclotron resonance and thin lines are the data corresponding to the background nonresonant thermoelectric signal.

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#### APPENDIX A: DETAIL OF PHOTOVOLTAGE DATA FOR $T_3$ , $T_4$ , AND $T_5$ CR TRANSITIONS

$V_{ph}$  vs  $B$  traces at selected  $n$  values for the  $T_3$  to  $T_5$  transitions are presented in Fig. 4.

#### APPENDIX B: COMPARISON BETWEEN CYCLOTRON RESONANCE SIGNAL AND BACKGROUND SIGNAL

Comparison between the cyclotron resonance signal and the background nonresonant thermoelectric signal is presented in Fig. 5.

#### APPENDIX C: EXTRACTION OF RELATIONSHIP BETWEEN $B_r$ AND $N_f$ FROM THEORETICAL CALCULATION

In the theoretical calculation reported by Shizuya [22], the change of LL energies due to the many-body interac-

tion contribution was estimated and results are normalized to the value obtained by neglecting many-body interaction effects. The magnetic field value used for the calculation was  $B = 20$  T, the interlayer bias  $u$  was zero, and  $\tilde{V}_c/\omega_c = 0.4$  was used for the strength of the Coulomb interaction  $\tilde{V}_c$  normalized to the cyclotron energy for monolayer graphene  $\omega_c$  [22–24]; here,  $\omega_c$  is used as a basic cyclotron energy. Using Eq. (1), the change of energy is first converted to the change of Fermi velocity; here we used  $\gamma_1 = 0.39$  eV and constant  $v_{F-e}/v_{F-h}$  ratio throughout the analysis. Thus, we used  $v_{F-e} = v_F$  for electrons and  $v_{F-h} = 0.892 \times v_F$  for holes. We set the LL energies of  $T_3$ ,  $T_4$ , and  $T_5$  transitions neglecting many-body interaction effects as 0.2, 0.285, and 0.36 eV, respectively. These are corresponding to the Fermi velocity without many-body interaction  $v_{F0}$  of  $1.035 \times 10^6$ ,  $1.041 \times 10^6$  m/s, and  $1.045 \times 10^6$  m/s, respectively. Next, by fixing the value of  $E_N$  in Eq. (1) as  $E_{ph}$  at  $\lambda = 10.675 \mu\text{m}$  ( $E_{ph} = 116.14$  meV), it was possible to convert the Fermi velocity into  $B_r$  value via Eq. (1) and extracted  $B_r$  was plotted in Figs. 3(b) and 3(d). The theoretical calculations were concerned with how the LL energy spacing changes with the number of filled LLs below  $E_F$  because of the interaction effect. Therefore, we believe that the relative change in the LLs with respect to  $N_f$  is not significantly altered by this conversion, which allows us to make a reasonable comparison between experiment and  $B_r$  extracted from the theoretical calculation.

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