# Electronic structure and magnetic properties of the effective spin $J_{eff} = \frac{1}{2}$ two-dimensional triangular lattice K<sub>3</sub>Yb(VO<sub>4</sub>)<sub>2</sub>

U. K. Voma<sup>®</sup>,<sup>1</sup> S. Bhattacharya<sup>®</sup>,<sup>2</sup> E. Kermarrec,<sup>2</sup> J. Alam,<sup>3</sup> Y. M. Jana<sup>®</sup>,<sup>3</sup> B. Sana<sup>®</sup>,<sup>4</sup> P. Khuntia,<sup>4</sup> S. K. Panda<sup>®</sup>,<sup>5,\*</sup> and B. Koteswararao<sup>®</sup>,<sup>1,†</sup>

<sup>1</sup>Department of Physics, Indian Institute of Technology Tirupati, Tirupati 517506, India

<sup>2</sup>Université Paris-Saclay, CNRS, Laboratoire de Physique des Solides, 91405, Orsay, France

<sup>3</sup>Department of Physics, University of Kalyani, Kalyani 741235, India

<sup>4</sup>Department of Physics, Indian Institute of Technology Madras, Chennai 600036, India

<sup>5</sup>Department of Physics, Bennett University, Greater Noida 201310, India

(Received 16 July 2021; revised 20 September 2021; accepted 28 September 2021; published 12 October 2021)

We report the structural, magnetic, specific heat, and electronic structure studies of the material  $K_3 Yb(VO_4)_2$ , which has two-dimensional triangular layers constituted by rare-earth magnetic  $Yb^{3+}$  ions. Magnetic susceptibility data show the absence of magnetic long-range order down to 0.5 K. No bifurcation is observed between zero-field-cooled and field-cooled magnetic susceptibility data, ruling out the possibility of spin-glassiness down to 0.5 K. From the fit to magnetic susceptibility data with Curie-Weiss law in the low-temperature region, the observed Curie-Weiss temperature ( $\theta_{CW}$ ) is about -1 K, implying an antiferromagnetic coupling between the  $Yb^{3+}$  ions. Magnetic field-dependent specific heat fits well with two-level Schottky behavior. The analysis of magnetization and specific heat data confirms that the  $Yb^{3+}$  ion hosts the effective spin  $J_{eff} = 1/2$  state. To provide a microscopic understanding of the ground state nature of the titled material, we carried out state-of-theart first-principles calculations based on density functional theory + Hubbard U and density functional theory + dynamical mean-field theory approaches. Our calculations reveal that the system belongs to the novel class of spin-orbit driven Mott Hubbard insulators and possesses large in-plane magnetocrystalline anisotropy.

DOI: 10.1103/PhysRevB.104.144411

## I. INTRODUCTION

Geometrically frustrated magnetism in two-dimensional (2D) magnetic materials draw significant attention in the scientific community due to their storming and unique magnetic properties. The strong quantum fluctuations enhanced by competing interaction between spins leads to unusual ground states. In S = 1/2 Heisenberg 2D triangular spin systems, the quantum fluctuations are more robust, which prevents magnetic long-range order (LRO) even at T = 0 K in the presence of off-diagonal anisotropic exchange interactions originating from spin-orbit coupling (SOC), and can exhibit the disordered ground state called quantum spin liquid (QSL) as contemplated by Anderson [1-4]. The spins in the QSL state can be highly entangled with each other, even at long distances. The QSL state has been proposed experimentally for various 2D geometrically frustrated magnetic systems (GFMSs), such as triangular and kagome lattices, with gapped and gapless fractionalized spin excitations without a conventional symmetry-breaking phase transition [5–7]. A few well-known S = 1/2 QSL materials in 2D GFMSs are  $\kappa$ -(BEDT-TTF)<sub>2</sub>Cu<sub>2</sub>(CN)<sub>3</sub> [8,9], EtMe<sub>3</sub>Sb[Pd(mit)<sub>2</sub>]<sub>2</sub> [10,11], and ZnCu<sub>3</sub>(OH)<sub>6</sub>Cl<sub>2</sub> [12–14].

Recently, interest in understanding the physics of S = 1/2 quantum magnetism has expanded from the 3*d* to 4*d*, 5*d*, and 4*f* rare-earth-based magnetic systems. The effective spin-1/2 can be realized in some of the Ru<sup>3+</sup>, Ir<sup>4+</sup>, Ce<sup>4+</sup>, Yb<sup>3+</sup>-based materials due to the strong spin-orbit coupling and crystal electric field (CEF) effects, which lead to exotic quantum phenomena. A few exemplar materials of this class are 4*d* honeycomb lattices  $\alpha$ -RuCl<sub>3</sub> [15], 5*d* honeycomb lattices  $A_2$ IrO<sub>3</sub>, (A = Li, Na, Cu) [16–18], and H<sub>3</sub>LiIr<sub>2</sub>O<sub>6</sub> [19], 4*f*-Yb<sup>3+</sup>-based triangular lattices YbMgGaO<sub>4</sub> [20–26], YbZnGaO<sub>4</sub> [27], and NaYb $X_2(X = \text{O}, \text{S}, \text{Se})$ , etc. [28–34].

In the compound YbMgGaO<sub>4</sub>, the magnetic, specific heat  $(C_p)$ , Muon spin relaxation ( $\mu$ SR), and inelastic neutron scattering (INS) measurements revealed the absence of static magnetic LRO down to several mK temperatures, despite an antiferromagnetic coupling strength with the Curie-Weiss temperature ( $\theta_{\rm CW}$ ) of -4 K. The magnetic specific heat  $C_m$ data in the low-temperature region follow the power-law temperature dependence as  $C_m \sim T^{\alpha}$ . Furthermore, the value of  $\alpha$  close to 2/3 suggests the possible realization of a gapless QSL state for the Heisenberg antiferromagnetic triangular lattice [20]. An electron spin resonance study revealed the anisotropic nature of the spin interactions [21]. The  $\mu$ SR relaxation rate exhibits a temperature-independent plateau behavior at low temperatures, suggesting persistent spin dynamics [22]. The INS measurements revealed continuous diffusive magnetic excitations suggesting that YbMgGaO<sub>4</sub> might host a gapless QSL with a spinon Fermi surface [23,25].

<sup>\*</sup>swarup.panda@bennett.edu.in

<sup>&</sup>lt;sup>†</sup>koteswararao@iittp.ac.in

While the isotropic perfect S = 1/2 2D triangular lattice model with nearest-neighbor (NN) interactions yields a 120° Néel state theoretically at T = 0 K [35,36], the origin of QSL state in the compound YbMgGaO<sub>4</sub> could be due to strong spin-orbit coupling (SOC) effects. From recent arguments, in comparison with YbZnGaO<sub>4</sub>, it was also pointed that YbMgGaO<sub>4</sub> showed a spin-glass-like ground state from the observations of frequency-dependent magnetic susceptibility [27], which was alternatively explained as a tiny spin freezing [26]. As the ground state of this system is still under debate due to the site mixing of Ga<sup>3+</sup> and Mg<sup>2+</sup> ions, the exploration of suitable candidate materials is required to understand the physics behind the 2D  $J_{eff} = 1/2$  triangular lattice whether the strong SOC or disorder-induced anisotropy drives the QSL state.

The study of rare-earth-based 2D triangular magnetic materials without site disorder has attracted attention in searching QSL states. The series of rare-earth chalcogenides NaYb $X_2$  were identified as promising QSL candidates. In the case of NaYbO<sub>2</sub>, no magnetic LRO down to 50 mK is revealed. Furthermore, a field-induced quantum phase transition was observed above an applied field of 2 T [29]. On the other hand, the pressure-induced metallic states were observed in NaYbSe<sub>2</sub> [33], indicating that these rare-earth chalcogenides offer an ideal venue to discuss QSL nature and superconductivity as predicted by Anderson. To understand further interesting properties of 2D triangular GFMS, there is a necessity to discover promising materials of this category.

Herein, we introduce another structurally perfect triangular lattice system  $K_3Yb(VO_4)_2$  [37], with the 2D triangular lattices of Yb<sup>3+</sup> ions. Yb<sup>3+</sup> hosts  $J_{eff} = 1/2$  moments as found below. Based on the measured magnetic and specific heat data, we find that the system does not exhibit any LRO down to 0.5 K. The obtained  $\theta_{CW}$  of -1 K indicates weak antiferromagnetic coupling between the Yb<sup>3+</sup> ions. This is further supported by the computed exchange interactions using the local spin-density approximation+Hubbard U (LSDA+U) method. We analyzed the detailed electronic structure based on LSDA+U and LDA+DMFT methods and found that the insulating state in  $K_3Yb(VO_4)_2$  arises due to the combined effects of SOC and electronic correlations. Our results indicate that this system possesses a large magnetic crystalline anisotropy. We also found that the dynamical correlation effects are crucial for accurately describing the f-multiplet spectra.

# **II. EXPERIMENTAL AND COMPUTATIONAL DETAILS**

We synthesized the polycrystalline material K<sub>3</sub>Yb(VO<sub>4</sub>)<sub>2</sub> using the conventional solid-state synthesis method. Initially, the rare-earth oxide Yb<sub>2</sub>O<sub>3</sub> was fired at 1000 °C for 6 h to remove the moisture and absorbed CO<sub>2</sub>. It was then mixed with K<sub>2</sub>CO<sub>3</sub>, V<sub>2</sub>O<sub>5</sub> in stoichiometric proportion and ground thoroughly. The pressed pellets were placed in an alumina crucible and fired at 750 °C for 48 h with several intermediate grindings. To confirm the single phase, x-ray diffraction measurements were carried out at room temperature. The x-ray tube having a Cu target with wavelength  $\lambda =$ 1.5406 Å was used. The temperature (*T*) and magnetic field (*H*)-dependent magnetization (*M*) were done using a vibrating sample magnetometer down to 5 K and superconducting quantum interference device magnetometer used to do the measurements down to 0.5 K, attached to a physical property measurement system (PPMS), Quantum Design, Inc. Specific heat as a function of temperature  $C_p(T)$  measurements were performed in several applied magnetic fields using the PPMS down to 2 K.

We have carried out both nonspin and spin-polarized electronic-structure calculations using density functional theory (DFT) [38,39] with local density approximation (LDA) and LSDA+U [40] approaches as implemented in the all-electron, full potential code WIEN2K [41]. The Brillouinzone integration is performed with a  $12 \times 12 \times 8k$ -mesh. To achieve energy convergence of the eigenvalues, the wave functions in the interstitial region were expanded in plane waves with a cutoff  $R_{MT}k_{max} = 8$ , where  $R_{MT}$  denotes the smallest atomic sphere radius and  $k_{max}$  represents the magnitude of the largest k vector in the plane-wave expansion. The valence wave functions inside the spheres are expanded up to  $l_{\text{max}} = 10$ , while the charge density is Fourier expanded up to a large value of  $G_{\text{max}} = 12$ . Based on the converged non-spin-polarized LDA solutions, we constructed the maximally localized Wannier function for the *f*-like bands, using WIEN2WANNIER [42] and WANNIER90 codes [43] to compute the hopping parameters between the effective Yb-forbitals.

We also carried out LSDA+U calculations using the full potential linearized augmented plane-wave method (FP-LAPW) as implemented in the RSPt code [44–46]. The consistency of the results from RSPt and WIEN2K provides further credence to our calculations. Using the LSDA+U solutions of RSPt, we employed the magnetic force theorem [47,48] to extract the effective intersite exchange parameters ( $J_{ij}$ ). A detailed discussion of the implementation of the magnetic force theorem in RSPt is provided in Ref. [49]. The  $J_{ij}$  are extracted in a linear-response manner via Green's function technique.

Considering that the many-body effects are extremely significant for the highly correlated f states, we also performed LDA+DMFT simulations using the same RSPt code [45]. In this implementation [50–53] of LDA+DMFT, the many-body corrections appear in a form that depends on a self-consistently calculated density matrix and on the correlated orbitals, which are 4f states on the Yb atoms in the present case. The effective impurity problem in the LDA+DMFT calculations has been solved through the Hubbard I (HIA) solver. The reported results are based on a single-shot simulation where the convergence of the self-energy has been achieved with 5000 Matsubara frequencies and the temperature is taken as 150 K.

To describe the electronic correlation effect within LSDA+U and LDA+DMFT approaches, we have taken U = 4.0 eV, J = 0.5 eV for Yb-*f* states which are obtained from constrained random phase approximation (cRPA) calculations [54] using the implementation of Ref. [55]. This method has been successfully used for several transition metal oxides. The first-principles estimation of U using cRPA ensures that the reported electronic and magnetic properties are completely parameter-free and thus, our approach is truly *ab initio*.

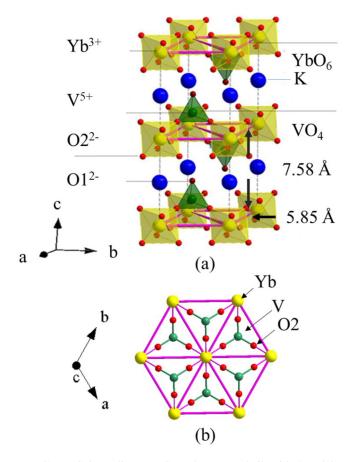


FIG. 1. (Color online.) (a) Crystal structure built with the  $YbO_6$  octahedra,  $VO_4$  tetrahedra, and K atoms. (b) The 2D triangular layers of Yb atoms are connected through V and O atoms [37].

# **III. STRUCTURAL DETAILS**

The structure of K<sub>3</sub>Yb(VO<sub>4</sub>)<sub>2</sub> belongs to the family of glaserite, having the general formula  $A_3R(VO_4)_2$ (*A*—alkali metal, *R*—rare-earth) with trigonal crystal system of  $P\overline{3}m1$  (No. 164) space group [37]. The measured x-ray diffraction data is used for the refinement using FULLPROFsoftware [56] as shown in Fig. 2. The refinement parameters are  $R_p \approx 13.8\%$ ,  $R_{wp} \approx 11.1\%$ , and  $\chi^2 \approx 4.1$ . The extracted lattice parameters a = b = 5.85 Å, c = 7.58 Å,  $\alpha = \beta = 90^\circ$ ,  $\gamma = 120^\circ$  are quite consistent with Ref. [37]. The position coordinates and occupancies of different atoms in the crystal structure are mentioned in Table I. The crystal structure is constituted with VO<sub>4</sub> tetrahedra, YbO<sub>6</sub> octahedra, and K atoms. Figure 1(a) shows the crystal structure of the K<sub>3</sub>Yb(VO<sub>4</sub>)<sub>2</sub> in which Yb atoms are placed

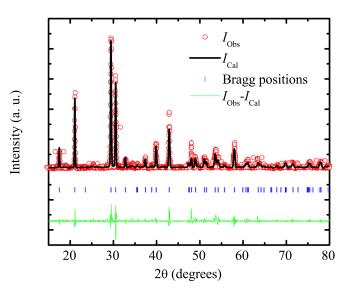


FIG. 2. (Color online.) Refinement of the x-ray diffraction data measured at room temperature for  $K_3$ Yb(VO<sub>4</sub>)<sub>2</sub> polycrystalline sample.

in a well-separated 2D triangular lattice with NN distance 5.85 Å. The interlayer separation 7.58 Å is larger than the intralayer distance of Yb-Yb. The ratio between the interlayer and intralayer distance  $(d_{inter}/d_{intra})$  is only 1.29. This ratio for the K<sub>3</sub>Yb(VO<sub>4</sub>)<sub>2</sub> compound is smaller than the values of 1.7 for NaYbO<sub>2</sub> and 2.4 for YbMgGaO<sub>4</sub>. However, it is somewhat similar to those of other 2D triangular layered materials with the ratio of  $d_{inter}/d_{intra} \sim 1.1$  for NaBaYb(BO<sub>3</sub>)<sub>2</sub> and  $d_{inter}/d_{intra} \sim 1.43$  for Rb<sub>3</sub>Yb(PO<sub>4</sub>)<sub>2</sub>, which show magnetic frustration and QSL features [57,58].

The bond length of Yb-O2 in YbO<sub>6</sub> octahedra is 2.19 Å. The environment of Yb<sup>3+</sup> holds  $D_{3d}$  point-group symmetry and is less distorted in comparison to NaYbO<sub>2</sub>, YbMgGaO<sub>4</sub>. The presence of the inversion center between the bonds precludes antisymmetric Dzyaloshinskii–Moriya (DM) exchange interactions. The 2D triangular layers are separated by K atomic layers. The possible magnetic exchange path in the titled compound is through Yb-O2-V-O2-Yb while it is through only O atoms in NaYbO<sub>2</sub> and YbMgGaO<sub>4</sub> [20,29]. In this path, the bond angles are Yb-O2-V  $\approx$ 164.4°, O2-V-O2  $\approx$ 108.7°

## **IV. RESULTS**

#### A. Magnetic properties

Temperature-dependent magnetization measurements were performed in the presence of a magnetic field 10 kOe. The

TABLE I. The atomic coordinates, atomic displacement parameters, occupancies of K<sub>3</sub>Yb(VO<sub>4</sub>)<sub>2</sub>.

Atom	Wyckoff position	x	у	Z	$U$ ( $\mathring{A}^2$ )	Occupancy
Yb(1)	1 <i>b</i>	1	0	0.5	0.01	1
K(1)	2d	0.6667	0.3333	1.2961	0.024	1
K(2)	1a	0	0	1	0.059	1
V(1)	2d	0.6667	0.3333	0.7474	0.012	1
O(1)	2d	0.6667	0.3333	0.9595	0.054	1
O(2)	6 <i>i</i>	0.3499	0.1750	0.6693	0.057	1

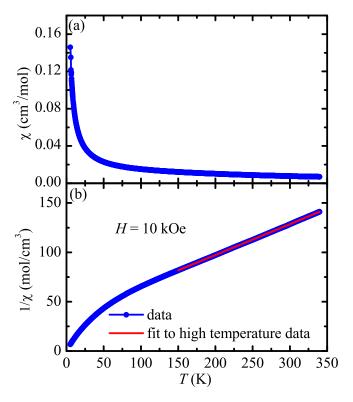


FIG. 3. (a)The magnetic susceptibility  $\chi(T)$  of K<sub>3</sub>Yb(VO<sub>4</sub>)<sub>2</sub> at the applied magnetic field 10 kOe. (b) The inverse-magnetic susceptibility data with the fit to the expression  $1/[\chi_0 + C_{\text{HT}}/(T - \theta_{\text{HT}})]$ .

magnetic susceptibility  $\chi$  and inverse-magnetic susceptibility  $\chi^{-1}$  as a function of temperature (T) down to 5 K is shown in Fig. 3. The  $\chi^{-1}$  data are fitted with the expression  $(T - \theta_{\rm HT})/C_{\rm HT}$  in a high-temperature region from 150 K to 340 K [see Fig. 3(b)]. The value of Curie constant at high temperature ( $C_{\rm HT}$ ) is obtained to be 3.2 cm<sup>3</sup>K/mol, which gives J = 7/2 and  $g_J = 1.28$ . The obtained value of  $g_J$  is close to the expected value  $g_J = 8/7 \simeq 1.14$ . The high-temperature Curie-Wiess temperature is found to be  $\theta_{\rm HT} \approx -110$  K. The large value of  $\theta_{\rm HT}$  is not due to the magnetic exchange couplings but it results from the CEF effect on the Yb atom. As the total angular momentum J = 7/2 (holds eightfold degeneracy) is in the CEF environment of  $D_{3d}$  symmetry, the energy levels split into four Kramers doublets by preserving the time-reversal symmetry. The energy difference between the ground-state doublet and the first excited state of Kramers doublet is defined as the CEF gap ( $\Delta_{\text{CEF}}$ ). We have tabulated the  $\Delta_{\text{CEF}}$  values for a few of  $Yb^{3+}$  based triangular materials along with the high-temperature values of  $\theta_{\text{HT}}$  (see Table II).

TABLE II. The crystal electric filed gaps( $\Delta_{\text{CEF}}$ ) of various Yb-based compounds.

2D triangular lattice	YbO <sub>6</sub> Environment	$\theta_{\mathrm{HT}}\left(\mathrm{K}\right)$	$\Delta_{\text{CEF}}(\text{K})$
NaYbS <sub>2</sub>	$D_{3d}$	-65	197 [31]
NaYbSe <sub>2</sub>	$D_{3d}$	-60	183 [ <mark>34</mark> ]
NaYbO <sub>2</sub>	$D_{3d}$	-100	404 [28]
$K_3$ Yb(VO <sub>4</sub> ) <sub>2</sub>	$D_{3d}$	-110	to be measured

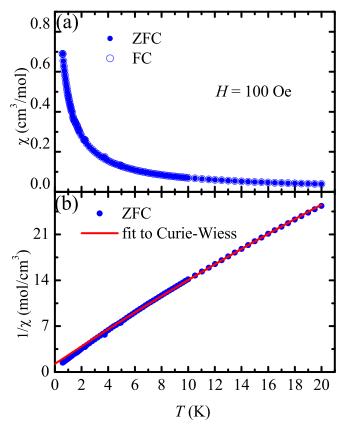


FIG. 4. (a) Temperature-dependent ZFC and FC  $\chi(T)$  plot in the range from 0.5 K to 20 K. (b) Inverse- $\chi$  versus *T* plot with the Curie-Weiss fit (represented by solid line).

As the value of  $\theta_{\rm HT}$  of K<sub>3</sub>Yb(VO<sub>4</sub>)<sub>2</sub> is close to the value of NaYbO<sub>2</sub> compound, the  $\Delta_{\rm CEF}$  of K<sub>3</sub>Yb(VO<sub>4</sub>)<sub>2</sub> could also be similar to that of NaYbO<sub>2</sub> (404 K) [28]. While the  $\Delta_{\rm CEF}$  is expected to be large (as we found  $\theta_{\rm HT}$  is about -110 K), the spin tends to lie in the ground state and hosts the  $J_{\rm eff} = 1/2$  at the low-temperature region.

The zero field cooled (ZFC) and field cooled (FC) susceptibility with temperature variation down to 0.5 K is shown in Fig. 4(a). No bifurcation is noticed, which represents the absence of spin freezing or spin glass transition. As shown in Fig. 4(b), the fit to the formula  $1/[\chi_0 + C_{\rm LT}/(T - \theta_{\rm LT})]$ in the temperature range 1.8 - 20 K gives  $\theta_{LT} \approx -1$  K. The temperature-independent susceptibility is found to be  $\chi_0 \approx$  $4.6 \times 10^{-3}$  cm<sup>3</sup>/mol. After subtracting the core diamagnetic susceptibility  $\chi_{dia}\approx -1.61\times 10^{-4} cm^3/mol$  calculated from the individual ions values [59], the obtained Van Vleck susceptibility is  $\chi_{VV} \approx 4.76 \times 10^{-3} \text{cm}^3/\text{mol}$ . The Curie constant  $C_{\rm LT}$  provides the magnetic moment  $\mu_{\rm eff} \approx 2.41 \,\mu_{\rm B}$ . As compared to the value  $\mu_{eff} \approx 4.53 \,\mu_B$  for free ions, the reduced value of the magnetic moment in the low-temperature region is due to the presence of J = 1/2 doublet as the ground state of Yb<sup>3+</sup> ion with the  $J_{\rm eff} = 1/2$  with  $g \approx 2.75$ . The nonlinear variation of the field-dependent magnetization plot at 1.8 K is shown in Fig. 5. The saturation magnetic moment is about 1.3  $\mu_{\rm B}/{\rm Yb^{3+}}$  obtained from the intercept of the linear fit as shown in Fig. 5(a). Figure 5(b) displays the M(H) data matches with the simulation to the Brillouin function for spin- $1/2, g \approx 2.6$  at  $T = 1.8 \text{ K}(> \theta_{\text{LT}})$ .

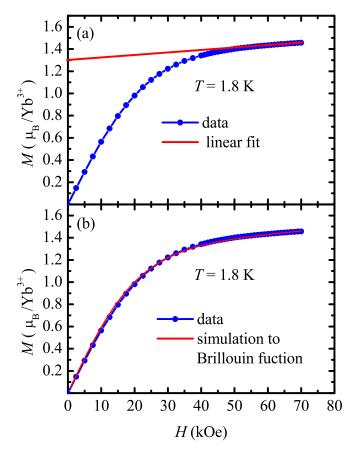


FIG. 5. (a) Magnetic field-dependent magnetization at T = 1.8 K. The solid straight line represents the extrapolation to linear fit in the range 60 - 70 kOe. (b) The data with simulation to Brillouin function for spin-1/2 and  $g \approx 2.6$ .

#### **B.** Specific heat measurements

The specific heat data as a function of temperature  $(C_p(T))$ were measured down to 1.8 K in different magnetic fields up to 90 kOe. As shown in Fig. 6(a), we did not observe any sharp transition in zero-field data. Field-dependent behavior is observed. A broad peak is seen in the presence of magnetic fields. The broad peak moves toward high temperatures with increasing magnetic fields due to the Zeeman splitting of the ground state Kramers doublet (J = 1/2). The two-level Schottky fit  $C = Nk_{\rm B} \frac{(\Delta/T)^2 e^{-\Delta/T}}{(1+e^{-\Delta/T})^2}$  to the  $C_p(H \,\text{kOe}) - C_p(0 \,\text{kOe})$  data is shown in Fig. 6(b). The extracted Zeeman energy gap  $(\Delta)$  between the energy levels of the ground-state doublet  $J = \pm 1/2$  increases linearly with the applied magnetic fields. The g value yielded from the slope of the linear fit to the expression  $\Delta = g\mu_{\rm B}H$  is about 2.5, is good agreement with the value estimated from the magnetic measurements.

#### C. Basic electronic structure

To begin, we have analyzed the band structure and partial density of states (PDOS), obtained using the LDA method. The results of our calculations are presented in Fig. 7. Close to the Fermi level, we find seven almost dispersion less bands which give rise to the sharp peak observed in the PDOS of Yb-f [Fig. 7(b)], implying the strongly localized nature of

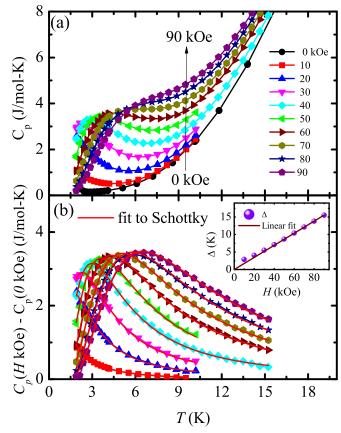


FIG. 6. (a) Temperature-dependent specific heat  $C_p$  at different applied magnetic fields from 0 kOe to 90 kOe. (b) The specific heat after subtracting the zero field data with the fit to Schottkey anomaly (see the text). The two energy level Schottky fit after subtracting the specific heat at 0 T. The inset shows the energy gap variation with applied magnetic fields.

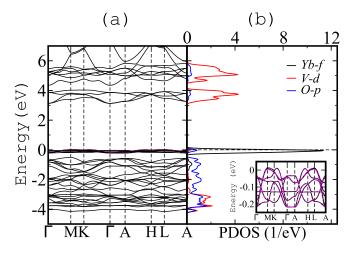


FIG. 7. Non-spin-polarized LDA. (a) Band dispersion along various high symmetry directions and (b) orbital projected partial density of states of Yb-f, V-d, and O-p states. For clarity, the f states are plotted after scaling the PDOS by a factor of 0.2. Inset of (b) shows the Wannier-interpolated bands superimposed on the LDA bands, plotted in the narrow energy region around the Fermi level.

TABLE III. Hopping integrals t (in meV) between the NN Yb-f states.

	$Yb-fxz^2$	Yb-fyz <sup>2</sup>
$Yb-fxz^2$	-1.5	-0.38
$\frac{Yb-fxz^2}{Yb-fyz^2}$	-0.38	-1.5

the f states. These states are also mostly occupied and thus consistent with the nominal  $3+(f^{13})$  charge state of Yb ions. The occupied O-p states appear in the energy range between -4 eV to -0.5 eV, while the V-d states are fully unoccupied, located above 3 eV from the Yb-f states. The hybridization between Yb-f and O-p states looks very weak.

Since the Yb-f states are well separated from the rest of the bands and they only contribute to the Fermi surface, we constructed the effective Wannier functions for these bands using the WANNIER90 formalism [43] where only the Yb-fstates were kept in the basis, and the rest of the orbitals were downfolded. In these calculations, we primarily find out the relevant orbitals for the magnetism and estimate the intersite hopping strengths between them. The Wannier interpolated bands along with the LDA bands are shown in the inset of Fig. 7(b) and the agreement is quite remarkable. The diagonalization of the obtained on-site blocks of the Ybf Hamiltonian, gives the eigenenergies -147, -128, -80, -80, -80, -56, -56 meV, corresponding to the eigenstates having predominant  $fy(3x^2 - y^2)$ ,  $fz^3$ , fxyz,  $fz(x^2 - y^2)$ ,  $fx(x^2 - 3y^2)$ ,  $fxz^2$ ,  $fyz^2$  characters, respectively. Since Yb is in  $f^{13}$  state, the above on-site energies indicate that all the lower-lying states  $(fy(3x^2 - y^2), fz^3, fxyz, fz(x^2 - y^2))$ ,  $fx(x^2 - 3y^2)$ ) are completely filled up and thus magnetically inactive. However, the topmost degenerate states which have predominant  $fxz^2$ ,  $fyz^2$  character, are partially filled up and would contribute to the local moment formation. The computed intersite hopping integrals between these two relevant orbitals is reported in Table III. Interestingly, the magnitudes of the hopping parameters come out to be very weak. This also implies that the magnetic exchange interactions  $(J_{ij})$  between the Yb ions would be small. The estimation of the  $(J_{ij})$  is discussed in the later part of the paper.

#### D. LSDA+U analysis of magnetic properties

Next, to provide a microscopic understanding of the experimentally observed magnetization, we estimated the different terms necessary for constructing the spin Hamiltonian for this system. Apart from the external magnetic field-dependent Zeeman term, spin dynamics of a system are governed by the isotropic Heisenberg exchange, anisotropic DM interaction, and the single-ion anisotropy or the magnetocrystalline anisotropy of the system. Using the formalism of Ref. [49], the estimated Yb-Yb magnetic-exchange interactions  $(J_{ij})$  come out to be 0.1 meV and antiferromagnetic in nature. This is consistent with the low-temperature value of Curie-Weiss temperature  $(\theta_{LT})$  obtained from the fitting of experimental susceptibility. We note that such small antiferromagnetic exchange in the triangular Yb network might promote magnetic frustration at a very low temperature which will oppose longrange ordering. The experimental magnetic data also show

TABLE IV. Energies of different magnetization axis with respect to the energy of *c*- axis magnetization ( $\Delta_E$ ). The corresponding spin moments  $\mu_s$ , orbital moments  $\mu_o$ , and total moments  $\mu_{tot}$  ( $\mu_s + \mu_o$ ) are tabulated.

	010 axis	110 axis	001 axis
$\Delta_E \text{ (meV/cell)}$	-98.4	-98.4	0.00
$\mu_s (\mu_{\rm B}/{\rm Yb})$	0.80	0.80	0.95
$\mu_o \left( \mu_{\rm B} / {\rm Yb} \right)$	1.93	1.93	1.89
$\mu_{tot} ~(\mu_{\rm B}/{\rm Yb})$	2.73	2.73	2.84

that the system does not have LRO down to 0.5 K. Although the Yb-*f* electrons possess large SOC, the presence of inversion symmetry in this system makes DM interactions be zero.

To determine the magnetocrystalline anisotropy, we have computed total energies by fixing the spin axis along various possible directions within the LSDA+U approach incorporating SOC. The computed energies, spin, and orbital moments are displayed in Table IV. Our calculations suggest that the Yb spins favor the *ab* plane as the preferred plane of magnetization. We also find that the spin moment for the prefer spin axis of the Yb<sup>3+</sup>ion is 0.80  $\mu_B$ , and the orbital moment is almost 2.4 times that of the spin moment, making the total moment (2.73  $\mu_B$ ). Another key finding of our LSDA+U+SOC calculations is that the system posses a large easy plane magnetocrystalline anisotropy energy. As displayed in

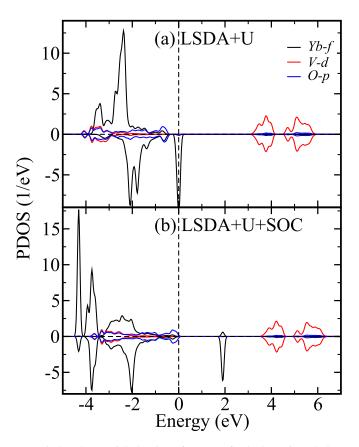


FIG. 8. The partial density of states of Yb-f, V-d, and O-p in the spin-polarized ground state obtained from LSDA+U and LSDA+U+SOC calculations.

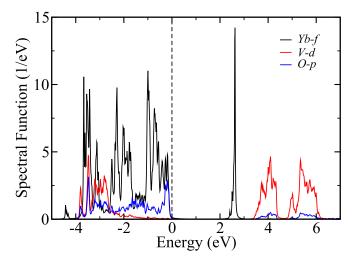


FIG. 9. The partial density of states of Yb-f, V-d, and O-p in the paramagnetic state, obtained from LDA+DMFT+SOC simulations.

Table IV, the *ab* plane is energetically favorable with the energy -98.4 meV.

The PDOS of the Yb-f, V-d, and O-p states for both the spin channels obtained using LSDA+U with, and without SOC has been shown in Fig. 8. We clearly see that SOC is crucial to open up the insulating gap in this system. Our results show that the majority Yb-f states are completely occupied and located between -4.5 eV to -1.8 eV, and the gap opens up in the minority channel. This is expected since Yb is in a nominal 3+ charge state  $(f^{13})$ , the first seven electrons occupy the majority channel, while the remaining six electrons fill up the minority f states, keeping only one level empty. The value of the insulating gap comes out to be 1.9 eV, which is a *p*-*f* gap as the *p* states appear just below the Fermi level. Therefore according to the LSDA+U theory, this system is a chargetransfer insulator, which is an unlikely electronic state for *f*-electron systems. However, it is well-known that LSDA+U has limited success in describing the electronic structure of f-electron systems. Moreover, the LSDA+U method works with symmetry-broken solutions, and thus an appropriate description of the paramagnetic electronic structure is outside its capabilities, necessitating the need of investigations using methods that are beyond the static mean-field approach.

## E. Electronic structure from LDA+DMFT

In view of the fact that an accurate treatment of the many-body electronic correlation is crucial for describing the correlated paramagnetic state of  $K_3$ Yb(VO4)<sub>2</sub>, we have employed LDA+DMFT with HIA incorporating SOC. In Fig. 9, we report the spectral function obtained in LDA+DMFT, which, for simplicity, we will also label as PDOS. The obtained band gap 2.2 eV, which is slightly larger than that of LSDA+U. Most importantly, contrary to the LSDA+U results, the gap is observed between the f – states, and the

 P. W. Anderson, Resonating valence bonds: A new kind of insulator? Mater. Res. Bull. 8, 153 (1973). origin of this gap is a combined effect of SOC and electronelectron correlations. Thus we can conclude that  $K_3Yb(VO_4)_2$ belongs to the very interesting class of spin-orbit driven Mott-Hubbard insulators. We note here that our LDA+DMFT calculations not only find out the correct nature of the insulating ground state but also provide the correct position of the *f* multiplets.

# V. DISCUSSION AND CONCLUSION

The ideal 2D Heisenberg triangular lattice hosts a 120° Néel-ordered state at absolute temperature T = 0 K [35,36]. In the presence of 3D couplings, the system will order at finite temperature. For example, the 2D triangular lattice materials Ba<sub>3</sub>CoSb<sub>2</sub>O<sub>9</sub> [60] and Ba<sub>3</sub>CoNb<sub>2</sub>O<sub>9</sub> [61] show magnetic LRO below temperatures 3.7 K and 1.4 K, respectively. Recently, there have been extensive theoretical studies on the effect of strong SOC coupling on a triangular lattice. As per the spinorbit coupled triangle lattice model, the possibility of various OSL phases was discussed. A OSL state would be achieved due to strong SOC, which mainly generates highly anisotropic interactions. In Ref. [62], a detailed study was carried out on the ground-state phase diagram, the effects on a spinon Fermi surface of the QSL in the presence of SOC and due to the presence of second-NN & third-NN couplings. The second-NN interactions create a Dirac OSL as the lowest energy state. The inclusion of even a very small third-NN interaction can greatly stabilize the QSL phase. In this line of theoretical studies, it is essential to synthesize and investigate 2D triangular quantum spin materials with possibly large SOC. Our title material is another type of material in addition to those of previously published materials YbMgGaO<sub>4</sub> and AYbX<sub>2</sub>. The theoretical band-structure calculations also confirmed that this material has large SOC and in-plane anisotropy.

In conclusion, we have synthesized and studied the magnetic properties and performed electronic structure calculations on a compound K<sub>3</sub>Yb(VO<sub>4</sub>)<sub>2</sub> having 2D triangular lattice of Yb<sup>3+</sup> ions. Our results confirm that Yb<sup>3+</sup> holds  $J_{\rm eff} = 1/2$  moments with an antiferromagnetic coupling with  $\theta_{\rm CW}$  about -1 K. No magnetic LRO was found down to 0.5 K. Electronic-structure calculations confirm that the system is a Mott insulator with large SOC and sizable magnetocrystalline anisotropy energy. Further low-temperature experiments, such as  $\mu$ SR, and INS, would be required to fully explore the nature of its ground state.

## ACKNOWLEDGMENTS

B.K. thanks the DST INSPIRE faculty award scheme and NFIG grant from IIT Tirupati. E.K. acknowledges financial support from the labex PALM for the QuantumPyroMan project (Project No. ANR10-LABX-0039-PALM). P.K. acknowledges funding by the Science and Engineering Research Board and Department of Science and Technology, India through research grants.

<sup>[2]</sup> Y.-D. Li, Y. Shen, Y. Li, J. Zhao, and G. Chen, Effect of spinorbit coupling on the effective-spin correlation in YbMgGaO<sub>4</sub>, Phys. Rev. B **97**, 125105 (2018).

- [3] Y.-D. Li, X. Wang, and G. Chen, Anisotropic spin model of strong spin-orbit-coupled triangular antiferromagnets, Phys. Rev. B 94, 035107 (2016).
- [4] X. Zhang, F. Mahmood, M. Daum, Z. Dun, J. A. M. Paddison, N. J. Laurita, T. Hong, H. Zhou, N. P. Armitage, and M. Mourigal, Hierarchy of Exchange Interactions in the Triangular Lattice Spin Liquid YbMgGaO<sub>4</sub>, Phys. Rev. X 8, 031001 (2018).
- [5] L. Balents, Spin liquids in frustrated magnets, Nature (London) 464, 199 (2010).
- [6] Y. Li, P. Gegenwart, and A. A. Tsirlin, Spin liquids in geometrically perfect triangular antiferromagnets, J. Phys.: Condens. Matter 32, 224004 (2020).
- [7] C. Broholm, R. J. Cava, S. A. Kivelson, D. G. Nocera, M. R. Norman, and T. Senthil, Quantum spin liquids, Science 367, 0668 (2020).
- [8] Y. Shimizu, K. Miyagawa, K. Kanoda, M. Maesato, and G. Saito, Spin Liquid State in an Organic Mott Insulator with a Triangular Lattice, Phys. Rev. Lett. 91, 107001 (2003).
- [9] T. Isono, T. Terashima, K. Miyagawa, K. Kanoda, and S. Uji, Quantum criticality in an organic spin-liquid insulator *k*-(BEDT-TTF)<sub>2</sub>Cu<sub>2</sub>(CN)<sub>3</sub>, Nat. Commun. 7, 13494 (2016).
- [10] S. Yamashita, Y. Nakazawa, M. Oguni, Y. Oshima, H. Nojiri, Y. Shimizu, K. Miyagawa, and K. Kanoda, Thermodynamic properties of a spin-1/2 spin-liquid state in a *k*-type organic salt, Nat. Phys. 4, 459 (2008).
- [11] S. Yamashita, T. Yamamoto, Y. Nakazawa, M. Tamura, and R. Kato, Gapless spin liquid of an organic triangular compound evidenced by thermodynamic measurements, Nat. Commun. 2, 275 (2011).
- [12] T. H. Han, J. S. Helton, S. Y. Chu, D. G. Nocera, J. A. Rodriguez-Rivera, C. Broholm, and Y. S. Lee, Fractionalized excitations in the spin-liquid state of a kagome-lattice antiferromagnet, Nature (London) 492, 406 (2012).
- [13] J. S. Helton, K. Matan, M. P. Shores, E. A. Nytko, B. M. Bartlett, Y. Yoshida, Y. Takano, A. Suslov, Y. Qiu, J.-H. Chung, D. G. Nocera, and Y. S. Lee, Spin Dynamics of the Spin-1/2 Kagome Lattice Antiferromagnet ZnCu<sub>3</sub>(OH)<sub>6</sub>Cl<sub>2</sub>, Phys. Rev. Lett. **98**, 107204 (2007).
- [14] P. Khuntia, M. Velazquez, Q. Barthélemy, F. Bert, E. Kermarrec, A. Legros, B. Bernu, L. Messio, A. Zorko, and P. Mendels, Gapless ground state in the archetypal quantum kagome antiferromagnet ZnCu<sub>3</sub>(OH)<sub>6</sub>Cl<sub>2</sub>, Nat. Phys. **16**, 469 (2020).
- [15] A. Banerjee, J. Q. Yan, J. Knolle, C. A. Bridges, M. B. Stone, M. D. Lumsden, D. G. Mandrus, D. A. Tennant, R. Moessner, and S. E. Nagler, Neutron scattering in the proximate quantum spin liquid α-RuCl<sub>3</sub>, Science **356**, 1055 (2017).
- [16] Y. Singh and P. Gegenwart, Antiferromagnetic Mott insulating state in single crystals of the honeycomb lattice material Na<sub>2</sub>IrO<sub>3</sub>, Phys. Rev. B 82, 064412 (2010).
- [17] Y. S. Choi, C. H. Lee, S. Lee, S. Yoon, W. J. Lee, J. Park, A. Ali, Y. Singh, J. C. Orain, G. Kim, J. S. Rhyee, W. T. Chen, F. Chou, and K. Y. Choi, Exotic Low-Energy Excitations Emergent in the Random Kitaev Magnet Cu<sub>2</sub>IrO<sub>3</sub>, Phys. Rev. Lett. **122**, 167202 (2019).
- [18] K. Mehlawat, A. Thamizhavel, and Y. Singh, Heat capacity evidence for proximity to the Kitaev quantum spin liquid in  $A_2$ IrO<sub>3</sub> (A = Na, Li), Phys. Rev. B **95**, 144406 (2017).

- [19] K. Kitagawa, T. Takayama, Y. Matsumoto, A. Kato, R. Takano, Y. Kishimoto, S. Bette, R. Dinnebier, G. Jackeli, and H. Takagi, A spin-orbital-entangled quantum liquid on a honeycomb lattice, Nature (London) 554, 341 (2018).
- [20] Y. Li, H. Liao, Z. Zhang, S. Li, F. Jin, L. Ling, L. Zhang, Y. Zou, L. Pi, Z. Yang, J. Wang, Z. Wu, and Q. Zhang, Gapless quantum spin liquid ground state in the two-dimensional spin-1/2 triangular antiferromagnet YbMgGaO<sub>4</sub>, Sci. Rep. 5, 16419 (2015).
- [21] Y. Li, G. Chen, W. Tong, L. Pi, J. Liu, Z. Yang, X. Wang, and Q. Zhang, Rare-Earth Triangular Lattice Spin Liquid: A Single-Crystal Study of YbMgGaO<sub>4</sub>, Phys. Rev. Lett. **115**, 167203 (2015).
- [22] Y. Li, D. Adroja, P. K. Biswas, P. J. Baker, Q. Zhang, J. J. Liu, A. A. Tsirlin, P. Gegenwart, and Q. M. Zhang, Muon Spin Relaxation Evidence for the U(1) Quantum Spin-Liquid Ground State in the Triangular Antiferromagnet YbMgGaO<sub>4</sub>, Phys. Rev. Lett. **117**, 097201 (2016).
- [23] J. A. M. Paddison, M. Daum, Z. Dun, G. Ehlers, Y. Liu, M. B. Stone, H. Zhou, and M. Mourigal, Continuous excitations of the triangular lattice quantum spin liquid YbMgGaO<sub>4</sub>, Nat. Phys. 13, 117 (2017).
- [24] Y. Li, D. Adroja, R. I. Bewley, D. Voneshen, A. A. Tsirlin, P. Gegenwart, and Q. Zhang, Crystalline Electric-Field Randomness in the Triangular Lattice Spin-Liquid YbMgGaO<sub>4</sub>, Phys. Rev. Lett. **118**, 107202 (2017).
- [25] Y. Shen, Y. D. Li, H. C. Walker, P. Steffens, M. Boehm, X. Zhang, S. Shen, H. Wo, G. Chen, and J. Zhao, Fractionalized excitations in the partially magnetized spin liquid candidate YbMgGaO<sub>4</sub>, Nat. Commun. 9, 4138 (2018).
- [26] Y. Li, S. Bachus, B. Liu, I. Radelytskyi, A. Bertin, A. Schneidewind, Y. Tokiwa, A. A. Tsirlin, and P. Gegenwart, Rearrangement of Uncorrelated Valence Bonds Evidenced by Low-Energy Spin Excitations in YbMgGaO<sub>4</sub>, Phys. Rev. Lett. **122**, 137201 (2019).
- [27] Z. Ma, J. Wang, Z. Y. Dong, J. Zhang, S. Li, S. H. Zheng, Y. Yu, W. Wang, L. Che, K. Ran, S. Bao, Z. Cai, P. Cermak, A. Schneidewind, S. Yano, J. S. Gardner, X. Lu, S. L. Yu, J. M. Liu, S. Li *et al.*, Spin-Glass Ground State in a Triangular Lattice Compound YbZnGaO<sub>4</sub>, Phys. Rev. Lett. **120**, 087201 (2018).
- [28] L. Ding, P. Manuel, S. Bachus, F. Gruler, P. Gegenwart, J. Singleton, R. D. Johnson, H. C. Walker, D. T. Adroja, A. D. Hillier, and A. A. Tsirlin, Gapless spin-liquid state in the structurally disorder-free triangular antiferromagnet NaYbO<sub>2</sub>, Phys. Rev. B **100**, 144432 (2019).
- [29] K. M. Ranjith, D. Dmytriieva, S. Khim, J. Sichelschmidt, S. Luther, D. Ehlers, H. Yasuoka, J. Wosnitza, A. A. Tsirlin, H. Kühne, and M. Baenitz, Field-induced instability of the quantum spin liquid ground state in the  $J_{\text{eff}} = 1/2$  triangular lattice compound NaYbO<sub>2</sub>, Phys. Rev. B **99**, 180401(R) (2019).
- [30] M. M. Bordelon, E. Kenney, C. Liu, T. Hogan, L. Posthuma, M. Kavand, Y. Lyu, M. Sherwin, N. P. Butch, C. Brown, M. J. Graf, L. Balents, and S. D. Wilson, Field-tunable quantum disordered ground state in the triangular lattice antiferromagnet NaYbO<sub>2</sub>, Nat. Phys. **15**, 1058 (2019).
- [31] R. Sarkar, Ph. Schlender, V. Grinenko, E. Haeussler, P. J. Baker, Th. Doert, and H.-H. Klauss, Quantum spin liquid ground state in the disorder free triangular lattice NaYbS<sub>2</sub>, Phys. Rev. B 100, 241116(R) (2019).

- [32] P. L. Dai, G. Zhang, Y. Xie, C. Duan, Y. Gao, Z. Zhu, E. Feng, C. L. Huang, H. Cao, A. Podlesnyak, G. E. Granroth, and D. Voneshen, Spinon Fermi Surface Spin Liquid in a Triangular Lattice Antiferromagnet NaYbSe<sub>2</sub>, Phys. Rev. X **11**, 021044 (2021).
- [33] Z. Zhang, Y. Yin, X. Ma, W. Liu, J. Li, F. Jin, J. Ji, Y. Wang, X. Wang, X. Yu, and Q. Zhang, Pressure induced metallization and possible unconventional superconductivity in spin liquid NaYbSe<sub>2</sub>, arXiv:2003.11479.
- [34] Z. Zhang, X. Ma, J. Li, G. Wang, D. T. Adroja, T. G. Perring, W. Liu, F. Jin, J. Ji, Y. Wang, X. Wang, J. Ma, and Q. Zhang, Crystalline electric-field excitations in quantum spin liquids candidate NaYbSe<sub>2</sub>, Phys. Rev. B **103**, 035144 (2021).
- [35] L. Capriotti, A. E. Trumper, and S. Sorella, Long-range Néel Order in the Triangular Heisenberg Model, Phys. Rev. Lett. 82, 3899 (1999).
- [36] S. R. White and A. L. Chernyshev, Neél Order in Square and Triangular Lattice Heisenberg Models, Phys. Rev. Lett. 99, 127004 (2007).
- [37] M. M. Kimani, L. Thompson, W. Snider, C. D. McMillen, and J. W. Kolis, Hydrothermal synthesis and spectroscopic properties of a new glaserite material, K<sub>3</sub>RE(VO<sub>4</sub>)<sub>2</sub> (RE = Sc, Y, Dy, Ho, Er, Yb, Lu, or Tm) with potential lasing and optical properties, Inorg. Chem. **51**, 13271 (2012).
- [38] P. Hohenberg and W. Kohn, Inhomogeneous electron gas, Phys. Rev. 136, B864 (1964).
- [39] R. O. Jones and O. Gunnarsson, The density functional formalism, its applications and prospects, Rev. Mod. Phys. 61, 689 (1989).
- [40] A. I. Liechtenstein, V. I. Anisimov, and J. Zaanen, Densityfunctional theory and strong interactions: Orbital ordering in Mott-Hubbard insulators, Phys. Rev. B 52, R5467 (1995).
- [41] K. Schwarz and P. Blaha, Solid state calculations using WIEN2k, Comput. Mater. Sci. 28, 259 (2003).
- [42] J. Kunes, R. Arita, P. Wissgott, A. Toschi, H. Ikeda, and K. Held, Wien2wannier: From linearized augmented plane waves to maximally localized Wannier functions, Comput. Phys. Commun. 181, 1888 (2010).
- [43] A. A. Mostofi, J. R. Yates, Y.-S. Lee, I. Souza, D. Vanderbilt, and N. Marzari, An updated version of wannier90: A tool for obtaining maximally-localised Wannier functions, Comput. Phys. Commun. 178, 685 (2008).
- [44] O. K. Andersen, Linear methods in band theory, Phys. Rev. B 12, 3060 (1975).
- [45] J. M. Wills and B. R. Cooper, Synthesis of band and model Hamiltonian theory for hybridizing cerium systems, Phys. Rev. B 36, 3809 (1987).
- [46] J. M. Wills, O. Eriksson, M. Alouni, and D. L. Price, *Electronic structure and physical properties of solids: The uses of the LMTO method* (Springer-Verlag, Berlin, 2000).
- [47] A. I. Liechtenstein, M. I. Katsnelson, V. P. Antropov, and V. A. Gubanov, Local spin density functional approach to the theory of exchange interactions in ferromagnetic metals and alloys, J. Magn. Magn. Mater. 67, 65 (1987).
- [48] M. I. Katsnelson and A. I. Lichtenstein, First-principles calculations of magnetic interactions in correlated systems, Phys. Rev. B 61, 8906 (2000).

- [49] Y. O. Kvashnin, O. Grånäs, I. Di Marco, M. I. Katsnelson, A. I. Lichtenstein, and O. Eriksson, Exchange parameters of strongly correlated materials: Extraction from spin-polarized density functional theory plus dynamical mean-field theory, Phys. Rev. B **91**, 125133 (2015).
- [50] A. Grechnev, I. Di Marco, M. I. Katsnelson, A. I. Lichtenstein, J. Wills, and O. Eriksson, Theory of bulk and surface quasiparticle spectra for Fe, Co, and Ni, Phys. Rev. B 76, 035107 (2007).
- [51] I. Di Marco, J. Minár, S. Chadov, M. I. Katsnelson, H. Ebert, and A. I. Lichtenstein, Correlation effects in the total energy, the bulk modulus, and the lattice constant of a transition metal: Combined local-density approximation and dynamical meanfield theory applied to Ni and Mn, Phys. Rev. B 79, 115111 (2009).
- [52] P. Thunström, I. Di Marco, A. Grechnev, S. Lebègue, M. I. Katsnelson, A. Svane, and O. Eriksson, Multiplet effects in the electronic structure of intermediate-valence compounds, Phys. Rev. B 79, 165104 (2009).
- [53] O. Grånäs, I. Di Marco, P. Thunström, L. Nordström, O. Eriksson, T. Björkman, and J. M. Wills, Charge self-consistent dynamical mean-field theory based on the full-potential linear muffin-tin orbital method: Methodology and applications, Comput. Mater. Sci. 55, 295 (2012).
- [54] F. Aryasetiawan, M. Imada, A. Georges, G. Kotliar, S. Biermann, and A. I. Lichtenstein, Frequency-dependent local interactions and low-energy effective models from electronic structure calculations, Phys. Rev. B 70, 195104 (2004).
- [55] L. Vaugier, H. Jiang, and S. Biermann, Hubbard U and Hund exchange J in transition metal oxides: Screening versus localization trends from constrained random phase approximation, Phys. Rev. B 86, 165105 (2012).
- [56] J. Rodríguez-Carvajal, Recent advances in magnetic structure determination by neutron powder diffraction, Physica B: Condens. Matter 192, 55 (1993).
- [57] S. Guo, A. Ghasemi, C. L. Broholm, and R. J. Cava, Magnetism on ideal triangular lattices in NaBaYb(BO<sub>3</sub>)<sub>2</sub>, Phys. Rev. Materials **3**, 094404 (2019).
- [58] S. Guo, R. Zhong, K. Górnicka, T. Klimczuk, and R. J. Cava, Crystal growth, structure, and magnetism of the 2D spin 1/2 triangular lattice material Rb<sub>3</sub>Yb(PO<sub>4</sub>)<sub>2</sub>, Chem. Mater. **32**, 10670 (2020).
- [59] P. W. Selwood, *Magnetochemistry*, 2nd ed. (Wiley-Interscience, New York, 1956), Chap. 2, p. 78.
- [60] H. D. Zhou, C. Xu, A. M. Hallas, H. J. Silverstein, C. R. Wiebe, I. Umegaki, J. Q. Yan, T. P. Murphy, J. H. Park, Y. Qiu, J. R. D. Copley, J. S. Gardner, and Y. Takano, Successive Phase Transitions and Extended Spin-Excitation Continuum in the S = 1/2 Triangular Lattice Antiferromagnet Ba<sub>3</sub>CoSb<sub>2</sub>O<sub>9</sub>, Phys. Rev. Lett. **109**, 267206 (2012).
- [61] K. Yokota, N. Kurita, and H. Tanaka, Magnetic phase diagram of the S = 1/2 triangular lattice Heisenberg antiferromagnet Ba<sub>3</sub>CoNb<sub>2</sub>O<sub>9</sub>, Phys. Rev. B **90**, 014403 (2014).
- [62] J. Iaconis, C. Liu, G. B. Halasz, and L. Balents, Spin liquid versus spin orbit coupling on the triangular lattice, SciPost Phys. 4, 003 (2018).