Planar triangular S = 3/2 magnet AgCrSe₂: Magnetic frustration, short range correlations, and field-tuned anisotropic cycloidal magnetic order

M. Baenitz,^{1,*} M. M. Piva,¹ S. Luther,^{2,3} J. Sichelschmidt,¹ K. M. Ranjith,¹ H. Dawczak-Dębicki,¹ M. O. Ajeesh,¹ S.-J. Kim,¹ G. Siemann,⁴ C. Bigi,⁴ P. Manuel,⁵ D. Khalyavin,⁵ D. A. Sokolov,¹ P. Mokhtari,¹ H. Zhang,¹ H. Yasuoka,¹ P. D. C. King,⁴ G. Vinai,⁶ V. Polewczyk,⁶ P. Torelli,⁶ J. Wosnitza,^{2,3} U. Burkhardt,¹ B. Schmidt,¹ H. Rosner,¹ S. Wirth,¹ H. Kühne,²

M. Nicklas^{,1} and M. Schmidt¹

¹Max Planck Institute for Chemical Physics of Solids, D-01187 Dresden, Germany

²Hochfeld-Magnetlabor Dresden (HLD-EMFL) and Würzburg-Dresden Cluster of Excellence ct.qmat,

Helmholtz-Zentrum Dresden-Rossendorf, 01328 Dresden, Germany

³Institut für Festkörper- und Materialphysik, TU Dresden, 01062 Dresden, Germany

⁴School of Physics and Astronomy, University of St Andrews, St Andrews KY16 9SS, United Kingdom

⁵ISIS Neutron and Muon Source, Rutherford Appelton Laboratory, Chilton, Didcot OX11 OQX, United Kingdom

⁶Istituto Officina dei Materiali (IOM)-CNR, Laboratorio TASC, Area Science Park, S.S. 14 km 163.5, Trieste I-34149, Italy

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Single crystals of the hexagonal triangular lattice compound AgCrSe₂ have been grown by chemical vapor transport. The crystals have been carefully characterized and studied by magnetic susceptibility, magnetization, specific heat, and thermal expansion. In addition, we used Cr-electron spin resonance and neutron diffraction to probe the Cr $3d^3$ magnetism microscopically. To obtain the electronic density of states, we employed x-ray absorption and resonant photoemission spectroscopy in combination with density functional theory calculations. Our studies evidence an anisotropic magnetic order below $T_N = 32$ K. Susceptibility data in small fields of about 1 T reveal an antiferromagnetic (AFM) type of order for $H \perp c$, whereas for $H \parallel c$ the data are reminiscent of a field-induced ferromagnetic (FM) structure. At low temperatures and for $H \perp c$, the field-dependent magnetization and AC susceptibility data evidence a metamagnetic transition at $H^+ = 5$ T, which is absent for $H \parallel c$. We assign this to a transition from a planar cycloidal spin structure at low fields to a planar fanlike arrangement above H^+ . A fully ferromagnetically polarized state is obtained above the saturation field of $H_{\perp S} = 23.7$ T at 2 K with a magnetization of $M_s = 2.8 \ \mu_B/Cr$. For $H \parallel c, M(H)$ monotonically increases and saturates at the same M_s value at $H_{\parallel S} = 25.1$ T at 4.2 K. Above T_N , the magnetic susceptibility and specific heat indicate signatures of two dimensional (2D) frustration related to the presence of planar ferromagnetic and antiferromagnetic exchange interactions. We found a pronounced nearly isotropic maximum in both properties at about $T^* = 45$ K, which is a clear fingerprint of short range correlations and emergent spin fluctuations. Calculations based on a planar 2D Heisenberg model support our experimental findings and suggest a predominant FM exchange among nearest and AFM exchange among third-nearest neighbors. Only a minor contribution might be assigned to the antisymmetric Dzyaloshinskii-Moriya interaction possibly related to the noncentrosymmetric polar space group R3m. Due to these competing interactions, the magnetism in AgCrSe₂, in contrast to the oxygen-based delafossites, can be tuned by relatively small, experimentally accessible magnetic fields, allowing us to establish the complete anisotropic magnetic H-T phase diagram in detail.

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I. INTRODUCTION

Covalently bonded two dimensional (2D) structures are frequently found with the triangular motif realized by a simple planar hexagonal lattice, in particular, but also by more complex distinguished 2D planar geometries such as the honeycomb lattice. Anisotropic metallic conductivity due to anisotropic hybridization of electronic states evolves through a bonding situation given by the crystal structure. The simplest examples are graphite and graphene crystallizing in a hexagonal and a honeycomb lattice, respectively. The latter exhibits very intriguing properties, such as high charge carrier mobility due to the formation of Dirac nodes near the Fermi level in the electronic band structure [1]. Other examples for inorganic 2D materials are hexagonal boron nitrides and transition metal chalcogenides [2]. The triangular lattice delafossite $PdCoO_2$ belongs to the latter material class, which is characterized by an unusually high in-plane charge carrier mobility [3,4]. Some organic BETS and ET salts also exhibit

^{*}Corresponding author: michael.baenitz@cpfs.mpg.de

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a layered triangular structure. They become metallic and even superconducting under pressure. Here the molecular Mott insulator κ -ET₂Ag₂(CN)₃ [5] shows in a remarkable way a pressure-induced crossover from a spin liquid in the Mott insulator state to a correlated Fermi liquid in the metallic state. Planar magnetic triangular lattices with spin-1/2 ions, such as Cu²⁺, favor the evolution of a gapless spin liquid ground state, e.g., $Ba_3CuSb_2O_9$ [6], which was already predicted by Anderson 40 years ago [7]. Recently, 2D magnetic van der Waals magnets, such as Cr₂Ge₂Te₆, CrCl₃, or RuCl₃, gained a lot of attention in view of device applications and fundamental research [8]. Some of them are metallic with a rather high charge carrier mobility along the layers, e.g., GdTe₃ [9]. Especially, if the structure lacks inversion symmetry a moderate spin-orbit interaction can promote the emergence of complex chiral magnetic textures, such as skyrmions [10]. Consequently, it is very appealing to study magnetic ions on a perfect triangular lattice, in a system with a strong 2Dlike conductivity, which in addition lacks inversion symmetry. Here, spin and charge degrees of freedom couple and, in the presence of a moderate spin-orbit interaction, spin-polarized bands, anisotropic complex magnetic ordering, piezoelectricity, multiferroicity, and an unconventional magnetotransport can be expected [11-13].

All these preconditions are fulfilled in the system AgCrSe₂ which in an extended sense belongs to the class of delafossites. Only recently a study on AgCrSe₂ single crystals confirmed reasonably metallic behavior in the plane, perpendicular to the c axis, with $\rho_{\perp} \approx 3 \text{ m}\Omega \text{ cm}$ and insulating behavior perpendicular to the plane, parallel to the c axis, with a resistivity ratio of about $\rho_{\parallel}/\rho_{\perp} \approx 100$ at 2 K [14,15]. This suggests that AgCrSe₂ is an anisotropic degenerated ptype semiconductor with a finite density of states (DOS) at the Fermi level, yielding a charge carrier density of about $7.6 \times 10^{19} \text{ cm}^{-3}$ at 300 K [14]. Early experimental studies on polycrystalline samples combined with band structure calculations already predicted in-plane ferromagnetism and spin-polarized bands at the verge of metallicity [16]. In particular, it should be emphasized that, unlike most delafossites which crystallize in the rhombohedral α -NaFeO₂ structure, space group $R\bar{3}m$ [4,17], AgCrSe₂ exhibits a hexagonal structure, with different Ag coordination, at room temperature. Moreover, AgCrSe₂ undergoes a structural transition at about 450 K from noncentrosymmetric polar R3m symmetry at low temperatures to centrosymmetric $R\bar{3}m$ symmetry at high temperatures [18–20]. Therefore, in strong contrast to most other delafossites, asymmetric exchange interactions between the Cr ions are possible in AgCrSe₂. This allows, in addition to the Heisenberg superexchange and a possible weak Ruderman-Kittel-Kasuya-Yosida (RKKY) exchange, a sizable Dzyaloshinskii-Moriya (DM) interaction between the magnetic ions [21]. This favors chiral magnetic phases in general and unconventional transport properties in particular. Prominent examples here are the B20 skyrmion compounds MnSi and FeGe [10,22], the half-Heusler compounds, such as Mn₃Sn [23], and the Cr-Nb chalcogenide $Cr_{1/3}NbS_2$ [24]. Furthermore, the spin-orbit interaction in combination with the polar space group supports the presence of a Rashba effect which is expected to have a strong impact on the electronic (magneto) transport.

Delafossite-type structures form as $A^{1+}R^{3+}X_2^{2-}$, where *A* is an alkaline metal (Li, Na, K, Rb, Cs) or a monovalent transition metal ion (Pd, Pt, or Cu, Ag), *R* is a trivalent transition metal or rare-earth ion which might be magnetic (Ti, V, Cr, Fe, Ce, or Yb) or nonmagnetic (Al, Ga, In, Tl, or Co, Rh), and *X* stands for a chalcogen [17]. So far, most of the research carried out was on oxygen-based delafossites, featuring a wide variety of topical phenomena, including superconductivity (Na_xCoO₂) [25], large thermoelectricity (Cu[Rh,Mg]O₂) [26], multiferroicity (CuFeO₂) [27], hydrodynamic 2D conductivity (PdCoO₂) [3], and spin-orbit driven frustration on a perfect triangular lattice (NaYbO₂) [28].

In that respect, it seems to be promising to move from the field of oxygen-based delafossites to the less studied nonoxygen delafossites with S, Se, or Te. The variation of the ionic radii of the mono- and trivalent ions mainly tunes the lattice parameters. The monovalent ion dominates the conductivity and has a strong impact on the density of states (DOS) at the Fermi level. The choice of the chalcogenide ion itself has a sizable impact on the band structure and the DOS. For example, the oxygen-based delafossite PdCoO₂ has a unique quasi-2D conductivity and the DOS at the Fermi level has predominant Pd character and shows a minor chalcogenide 2p-electron admixture. The same is true for its magnetic relative PdCrO₂ which is a rather unusual itinerant magnet with short range correlations and a rather strong antiferromagnetic (AFM) exchange. Both systems are an exception among oxygen-based delafossites whereas others, such as CuCrO₂ and AgCrO₂, are found to be rather bad metals. In contrast, in AgCrS₂ or AgCrSe₂ the spatially more extended 3(4)p states of S and Se promote the emergence of hybridized p states near the Fermi level which finally leads to reasonable metallic conductivity [14]. To some extent, this is also found in Cr chalcogenide spinel compounds [29,30], but the exchange here is three dimensional which is in strong contrast to Cr delafossites. The hybridization enhances correlation effects between spin and charge in general and together with the emergence of strong spin polarization, fosters unconventional magnetism and (magneto)transport.

As mentioned above, the non-oxygen-based chromium delafossites are hardly investigated and most of the research was done on polycrystalline material. We have been able to grow large high quality single crystals using vapor transport techniques. The single crystals allow us to study the temperature and field dependence of the anisotropic magnetism and to map out the H-T phase diagram of AgCrSe₂. Whereas the magnetism in chromium oxygen-based delafossites, e.g., CuCrO₂, is quite robust against applied magnetic fields and no saturation of the magnetization occurs up to 100 T [31], we show that the magnetism of AgCrSe₂ can be easily tuned to saturation by magnetic fields in the range of a few tens of teslas and that the expected saturation magnetization for $S = 3/2 \text{ Cr}^{3+}$ close to $3 \mu_{\rm B}/\text{Cr}$ is obtained. Furthermore, we combine our magnetization studies with heat capacity, thermal expansion, electron spin resonance, and neutron diffraction. The results are discussed in terms of a frustrated 2D triangular S = 3/2 lattice with competing exchange interactions among nearest neighbors (ferromagnetic) and third-nearest neighbors (antiferromagnetic) within the plane. The parameters used in the presented exchange model provide a very good description of the experimentally determined saturation fields and Weiss temperature. The neutron diffraction data confirm the magnetic transition to a complex planar cycloidal magnetic order with a rather long period (about 164 Å) in the (1,1,0) direction [32]. The temperature dependencies of specific heat, susceptibility, and neutron Bragg-peak intensities together with the rather small residual entropy ($0.2R \ln 4$) point to the emergence of anisotropic, possibly chiral, fluctuations in the vicinity of magnetic order.

The paper is organized as follows. After the overview on triangular lattice delafossite type systems, we present the applied methods in Sec. II. In Sec. III, we describe and discuss the experimental results: crystal growth, electronic structure, followed by the magnetic and thermodynamic bulk measurements (susceptibility, magnetization, specific heat, and thermal expansion) up to the two local probes applied (electron spin resonance spectroscopy and neutron scattering). We then describe the exchange in a 2D Heisenberg model and present the *H*-*T* phase diagram. Finally in Sec. IV, we summarize all conclusions and give an outlook on possible future experiments.

II. METHODS

Magnetization measurements were performed using magnetic property measurement systems (MPMS and MPMS3, Quantum Design) and the AC measurement system option of the physical property measurement system (PPMS, Quantum Design). The magnetization experiments in pulsed magnetic fields up to 50 T were performed at the Dresden High Magnetic Field Laboratory (HLD) with a compensated pickup-coil system in a pulse-field magnetometer in a home-built ⁴He cryostat and a pulsed magnet with an inner bore of 20 mm, powered by a 1.44 MJ capacitor bank [33]. Specific heat was recorded using the corresponding option of a PPMS. We investigated the electron spin resonance (ESR) of single crystalline AgCrSe₂ using a standard continuous-wave ESR setup at X-band frequency (9.4 GHz). The temperature was varied between 3 and 300 K with a He-flow cryostat. ESR can be detected by the absorbed power P of a transversal magnetic microwave field as a function of a static, external magnetic field $\mu_0 H$. To improve the signal-to-noise ratio, we used a lock-in technique by modulating the static field, which yields the derivative of the resonance signal dP/dH. The measured ESR spectra were fitted with a Lorentzian function including the influence of the counter-rotating component of the linearly polarized microwave field [34]. From the fit we obtained the linewidth ΔH and the resonance field H_{res} which determines the ESR g factor $g = hv/\mu_B H_{res}$. The ESR intensity I_{ESR} is a measure of the local static susceptibility of the probed ESR spin, i.e., in our case the local susceptibility of the Cr³⁺ spins [35]. We calculated $I_{\text{ESR}} \approx Amp \times \Delta H^2$ which approximates the integrated ESR absorption [36]. The thermal expansion experiments were performed in a PPMS, equipped with a custom-designed high resolution dilatometer [37]. Since temperature and magnetic field variations affect both the sample length and the length of the Be-Cu dilatometer cell, a high purity copper plate (ADVENT Research Materials, Ltd., 99.995% Cu) of the same thickness as the AgCrSe₂ sample was used to calibrate the cell background. Neutron powder

diffraction data were collected at the ISIS pulsed neutron and muon facility of the Rutherford Appleton Laboratory (UK) on the WISH diffractometer located at the second target station [38]. The sample was loaded into cylindrical 3 mm diameter vanadium cans and measured in the temperature range between 1.5 and 100 K (step size 5 K) using an Oxford Instruments cryostat. Rietveld refinements of the crystal and magnetic structures were performed using the FULLPROF program [39] against the data measured in detector banks at average 2θ values of 27° , 58° , 90° , 122° , and 154° , each covering 32° of the scattering plane. X-ray absorption (XAS) and resonant photoemission spectroscopy (resPES) measurements were performed at the APE-HE beamline at Elettra Sincrotrone, Italy. Samples were cleaved in situ at a base pressure lower than 10^{-10} mbar. The measurements shown here were performed using photon energies in the range of \sim 569–596 eV, with the sample held at a temperature of 100 K; very similar measurements were obtained at room temperature. XAS was performed in the total electron yield (TEY) mode. ResPES measurements were performed using a Scienta Omicron R3000 hemispherical electron energy analyzer. The measured Fermi edge of a gold reference sample was used for binding energy calibration for the resPES, as well as to reference the incident photon energy, assuming an analyzer work function of 4.4 eV. The gold sample has been prepared via argon sputtering to observe a clean surface. From the width of the measured Fermi edge of the gold reference sample, we estimate an experimental energy resolution of \sim 0.4 eV. Density functional theory (DFT) electronic structure calculations were performed using the full-potential FPLO code, version fplo18.00-52 [40-42]. The calculations were based on the localized density approximation (LDA) with the Perdew-Wang-92 exchange-correlation functional [43]. The correlation effect of the Cr 3d shell was taken into account by the LDA+U method in the atomic-limit flavor with U in the range of 0.5-6.0 eV. The spin-orbit coupling effect was treated nonperturbatively by solving the full Kohn-Sham-Dirac equation [44]. The rhombohedral unit cell in the space group No. 160 (R3m) was used, with the experimental lattice parameters of a = b = 3.6798 Å, c = 21.2250 Å [18]. The Brillouin zone was sampled with a k mesh of 8000 k points $(20 \times 20 \times 20 \text{ mesh}, 1540 \text{ points in the irreducible wedge})$ of the Brillouin zone). The experimentally measured DOS is additionally broadened as compared to the calculations due to finite lifetime effects as well as the experimental energy resolution. To aid comparison, the calculated DOS has been convoluted with a Gaussian of full width at half maximum equal to the experimental energy resolution of 0.4 eV.

III. RESULTS AND DISCUSSION

A. Single-crystal growth, crystal structure, and characterization

We have grown high quality $AgCrSe_2$ single crystals with lateral dimensions of a few millimeters via chemical transport reaction using chlorine as transport agent. In a first step polycrystalline $AgCrSe_2$ material has been synthesized by a direct reaction of the elements silver (powder 99.999%, Alfa Aesar), chromium (powder 99.99%, Alfa Aesar), and selenium (pieces 99.999%, Alfa Aesar, powdered) at 800 °C



FIG. 1. Hexagonal lattice structure of $AgCrSe_2$ (left) and morphology of two crystals used in this study (right). The lateral extension corresponds to the (a, b) plane and the direction perpendicular to it is the *c* axis.

in evacuated fused silica tubes within 14 days. Starting from this microcrystalline powder material, AgCrSe₂ crystallized by a chemical transport reaction in a temperature gradient from 900 °C (source) to 800 °C (sink), and a transport agent concentration of 3 mg/cm³ chlorine. After 6 weeks, the experiment was stopped by quenching the ampoule in cold water. Selected crystals were characterized by energydispersive x-ray spectroscopy (EDXS), wavelength-dispersive x-ray spectroscopy (WDXS), x-ray powder diffraction, Laue x-ray diffraction, and differential scanning calorimetry (DSC). At 300 K, AgCrSe₂ crystallizes in a hexagonal structure (with R3m crystal symmetry) with alternating AgSe₄ layers and $CrSe_6$ octahedral layers along the *c* axis [see Fig. 1 (left)] and lattice constants of a = 3.6824(3) Å and c = 21.233(1)Å, determined by powder x-ray diffraction. Figure 1 (right panel) shows two crystals from different crystal growths. Magnetization measurements were performed on both crystals in great detail (see also the Supplemental Material [45]). High field magnetization measurements and electron spin resonance were performed on MS1212 and specific heat studies on MS1262 and MS1212. Furthermore, the samples were investigated with respect to the structural phase transition between 350 and 450 K by differential scanning calorimetry (DSC). Specific heat obtained by DSC was recorded on crystal MS1212 upon heating and cooling. The heating and cooling speed was 20 K/min. A hysteretic phase transition is clearly visible (see the Supplemental Material [45]). The chemical composition of AgCrSe₂ crystals was studied locally by energy-dispersive x-ray spectroscopy (EDXS) (details in the Supplemental Material [45]). Only rather small deviations from the nominal stoichiometry were found. Although the variations are small (and close to the experimental error), the trend is that the crystals all have a slightly lower silver content and an increased chromium content, which formally corresponds to $Ag_{0.92}Cr_{1.08}Se_2$. Especially the silver content seems to be important for the metallic conductivity as shown in a separate study [15]. A silver deficiency might lead to a higher metallic conductivity [46] of the crystals. It seems that a rather slight silver deficiency is an inherent feature of our crystals. Initial resistivity and Hall measurements on our AgCrSe₂ crystals [15] and our ESR study (see Sec. IIIE)



FIG. 2. (a) X-ray absorption spectroscopy at the Cr $L_{2,3}$ edge, indicating a dominant Cr³⁺ valence. (b) Angle-integrated resonant photoemission measurements of the valence band electronic structure, measured at the photon energies marked by the points in (a) which span across the L_3 edge. (c) The Cr partial density of states extracted experimentally as the difference of the on- and off-resonant PES spectra (hv = 576.5 eV and 569.4 eV, respectively; solid blue line with shading). The dashed lines show the corresponding Cr partial DOS as determined by nonmagnetic DFT, and by LDA+*U* calculations for U = 0.75 eV and 3 eV, respectively.

clearly indicate metallic conductivity, which is consistent with our EDX results and previous reports [46].

B. Electronic structure

Figure 2(a) shows XAS measurements of the Cr $L_{2,3}$ edge. Its shape is characteristic of a dominant Cr³⁺ configuration [47–49], and is similar to the XAS measured from PdCrO₂ [48,49]. A Cr $3d^3$ electronic configuration would thus be expected to first order, with a half-filled t_{2g} shell. In the absence of strong electronic correlations or the formation of local magnetic moments, this would lead to a metallic ground state. Such itinerant Cr states are indeed obtained from our nonmagnetic density functional calculations within the local density approximation [Fig. 2(c) and Fig. 3]. In contrast, our measurements of the valence DOS [Fig. 2(b)] indicate only a weak step at the Fermi level, with the majority of the occupied DOS located at higher binding energy.

Our photoemission measurements were performed with photon energies spanning the Cr L_3 x-ray absorption edge [Fig. 2(b)]. We observe a marked increase in the spectral weight of the peak in the DOS centered at ~ 1.5 eV binding energy when the photon energy is tuned into resonance with the corresponding $\operatorname{Cr} 2p-3d$ transition. This indicates that this feature has a dominantly Cr-derived character, whose spectral weight becomes enhanced "on-resonance." To investigate this in more detail, we take the difference of the photoemission spectra measured on and just below the resonance energy, allowing us to extract an experimental measure of the Cr partial DOS [Fig. 2(c)]. This confirms that there is negligible Cr DOS at the Fermi level. As our measurements are performed well above the magnetic ordering temperature of AgCrSe₂ (see below), this provides initial evidence for the persistence of a well-defined local moment above T_N .



FIG. 3. Total and partial electronic densities of states of AgCrSe₂. (a) Nonmagnetic metallic solution with dominating Cr 3*d* states at E_F . (b) Ferromagnetic insulating state including spin-orbit coupling for U = 0.75 eV and (c) U = 3 eV.

In PdCrO₂, which has similar Cr-derived local moments persisting above T_N , the electronic structure of the CrO₂ subsystem is best described as Mott insulating [48,50]. In AgCrSe₂, however, the larger Se orbitals may lead to increased hybridization. Indeed, a lack of definition in the L_3 -edge XAS pre-peak structure as compared to PdCrO₂ is consistent with an increased hybridization with the ligand, similar to that observed in other Cr-based chalcogenide and halide magnets such as $Cr_2Ge_2Te_6$ [51] and CrI_3 [52]. This, in turn, would weaken the electronic correlations. To quantify this, we compare our experimental Cr partial DOS with that calculated from DFT [Fig. 2(c) and Fig. 3]. A clear disagreement is found with the nonmagnetic DFT calculations, where a large Cr DOS is obtained at the Fermi level, unlike that obtained experimentally. We thus compare with magnetic LDA+U calculations, where the strength of the Hubbard-Uparameter is varied. Taking a value of U = 3 eV, typical for Cr-based oxides [53,54], we find that the Cr DOS is peaked at too high a binding energy as compared to the experiment. Moreover, rather than having a single dominant peak as for the U = 3 eV calculations, the experimental partial DOS has a double-peak structure with spectral weight distributed throughout the valence band. Indeed, much better agreement with both the locations and overall shape of the experimental DOS is obtained for calculations using a low U value of 0.75 eV. This points to a much more weakly correlated state as compared to, e.g., PdCrO₂, where the Cr-derived states in AgCrSe₂ become more strongly hybridized with the ligand states. This can be expected to have an important influence on the magnetic ordering in AgCrSe₂, as discussed in detail below.

Carrying out DFT calculations for different settings with respect to magnetism or electron correlation can provide a deeper understanding for different features in the underlying electronic structure, in particular the influence of the different constituents. Figure 3 shows the total and partial DOSs resulting from such calculations. Figure 3(a) shows a nonmagnetic calculation, resulting in a metallic solution with dominating, half-filled t_{2g} Cr 3d states (in terms of the local $CrSe_6$ octahedron) at the Fermi level E_F . With respect to the Cr states, this solution is in clear contrast to the Cr partial DOS determined from photoemission experiments discussed above, and also experiments which find the compound to be a doped semiconductor with a small charge carrier density and magnetic moments on the Cr site. However, the position of the Se and Ag states in the valence band meets the expectations from related compounds: a rather narrow Ag-dominated band complex around -4 eV and a broad Se contribution spread throughout the valence band due to hybridization with both Cr and Ag.

To reflect more of the experimental properties, including the local Cr moment should provide considerable improvement, leading to a split of the Cr t_{2g} states with full spin polarization and the opening of a band gap. To approximate the experimentally observed complex noncollinear in-plane magnetic structure with a long propagation vector (see below), we use ferromagnetic (FM) order. As expected from a local moment picture, we find the system to be insulating with a gap of about 12 meV (not shown). The experimentally observed metallic conductivity with a small charge carrier concentration is related to a inherent small Ag off-stoichiometry of our crystals and the related self doping.

However, compared to the PES data, the FM calculation yield still a too high Cr contribution near E_F . A likely explanation for this discrepancy is Coulomb correlations in the Cr 3d shell. Since such correlation effects are insufficiently described by standard DFT, we apply FM LDA+U calculations to take them into account in a mean field way. As discussed above, a rather moderate value of U = 0.75 eV fits the PES data best [see Figs. 3(b) and 2(c)]. Besides an increase of the band gap, the respective small downshift of the Cr 3d states leads to a mixture of Cr 3d and Se 4p states near E_F with a larger weight for the Se states. A larger U value of 3 eV, typical for Cr-based oxides [53,54], moves the Cr 3d states too far down in energy [see Figs. 3(c) and 2(c)]. In such a scenario, the states near E_F are heavily dominated by Se 4p contributions [see Fig. 3(c)], resulting in sizeably increased dispersion of the respective bands [55].

Having adjusted U to fit the PES data, we further analyze the resulting band structure. In a tight binding model for the t_{2g} states, we find a dominant in-plane dispersion with about equal contribution from first- and third-nearest neighbors. The inclusion of spin-orbit coupling (SOC) leads to a significant additional split of the order of 300 meV (on the Γ -Z line)



FIG. 4. Temperature dependence of the magnetic susceptibility $(\chi_{\parallel} \text{ and } \chi_{\perp})$ of AgCrSe₂ (MS1212) measured at $\mu_0 H = 1$ T (left). The solid line corresponds to a Curie-Weiss fit. Each measurement was first performed in zero-field-cooled (zfc) and then in field-cooled (fc) mode. Inverse of the susceptibility as a function of temperature (right). Note that a paramagnetic contribution for $H \parallel c$ of $\chi_{0,\parallel} = 0.0005$ emu/mol was required for a proper Curie-Weiss fit (CW) at high temperatures. Most likely this stems from a Van Vleck contribution (χ_{VV}) (estimated from high field measurements; Fig. 9) and a small and negative diamagnetic contribution from the capton sample holder $\chi_{0,\parallel} = \chi_{VV,\parallel} + \chi_{dia}$.

for the top of the valence band. The details will be published elsewhere [55].

C. Magnetic susceptibility and magnetization

Figure 4 shows the magnetic susceptibility of AgCrSe₂ as a function of temperature in a magnetic field of 1 T applied in the (a, b) plane $H \perp c$ and in the c direction $H \parallel$ c. Below the ordering temperature of $T_N \approx 32$ K a strong magnetic anisotropy is observed. Above T_N , the magnetic anisotropy disappears and a pronounced maximum at $T^* =$ 46.3 K is found in $\chi_{\perp}(T)$ and $\chi_{\parallel}(T)$. Above 150 K, $\chi_{\perp}(T)$ and $\chi_{\parallel}(T)$ can be well fitted by a Curie-Weiss (CW) law, yielding a positive Weiss temperature of $\theta = +75$ K and an effective moment of $\mu_{eff} = 3.57 \ \mu_{B}/Cr$. This value of $\mu_{\rm eff}$ is slightly smaller than the theoretical prediction for the spin-only value of trivalent Cr $(3d^3)$ with S = 3/2 and $\mu_{\rm eff}^{\rm theo} = 3.87 \ \mu_{\rm B}$. A maximum at about 50 K, a Weiss temperature around 70 K, and an effective moment of about $\mu_{\rm eff} = 3.52 \ \mu_{\rm B}/{\rm Cr}$ have been also reported in earlier studies on polycrystalline powdered samples of AgCrSe₂ [16,56]. However, upon lowering the temperature the susceptibility measurements on the powder show a structureless drop in susceptibility after passing through the maximum at about 50 K. To our knowledge, so far neither directional measurements on single crystals nor detailed studies on the field dependence of the magnetization were reported for the Cr-sulfide or the Cr-selenide delafossite systems in the literature. Thorough early neutron diffraction experiments on polycrystalline AgCrSe₂ show a complex planar cycloidal spin arrangement in the (1,1,0) direction with a large periodicity of about 164 Å in zero field [32]. In the c direction the FM planes are antiferromagnetically coupled which leads to a global AFM order. This is a distinct difference from the $R\bar{3}m$ Cr-oxygen



FIG. 5. First temperature derivative of the magnetic susceptibility (χ_{\parallel} and χ_{\perp}) of AgCrSe₂ (MS1212) as a function of temperature. The maximum in susceptibility at $T^* = 46.3$ K (Fig. 4) is given by the high temperature zero crossing of the derivative. The ordering temperature of $T_N = 32$ K is indicated by a maximum in the derivative for $H \perp c$ and the second zero crossing in the derivative for $H \parallel c$.

delafossites, such as AgCrO₂, CuCrO₂, or PdCrO₂, where a planar 120° order has been established [57–59]. In contrast to the Cr-sulfide or Cr-selenide systems, the Cr oxygen-based delafossites always possess large negative Weiss temperatures ($\theta = -160$ K for AgCrO₂, $\theta = -211$ K for CuCrO₂, and $\theta = -500$ K for PdCrO₂ [60–62]), indicating a predominant AFM exchange. For nonoxygen Cr delafossites the exchange becomes quite complex and studies on polycrystalline samples evidence positive Weiss temperatures for AgCrSe₂, NaCrSe₂, CuCrSe₂, NaCrS₂, and KCrS₂, as well as negative Weiss temperatures for AgCrS₂, CuCrS₂, and LiCrS₂ [32,56,57,63].

We use the first temperature derivative of the magnetic susceptibility $d\chi/dT$ to determine the magnetic ordering temperature (see Fig. 5). For fields in the (a, b) plane we find a clear change in the slope of the $\chi_{\perp}(T)$ curve which gives a pronounced peak at $T_N = 32$ K, whereas in the c direction a zero crossing of the derivative of $\chi_{\parallel}(T)$ indicates the magnetic order at the same temperature within the measurement uncertainties. The position of the isotropic maximum at 46.3 K in $\chi_{\parallel}(T)$ and $\chi_{\parallel}(T)$ is defined by the second zero crossing in the first derivative. We note that the measurements were performed in zero-field-cooled (zfc) and field-cooled (fc) mode and that no branching could be observed. This evidences that there is no hysteretic behavior due to short range order, domains, or other glassy-like effects. Furthermore, this behavior is reproducible across many growth series of AgCrSe₂ crystals (see equivalent measurements on MS1257 crystal in the Supplemental Material [45]). The Weiss temperature of $\theta = +75$ K and the ordering temperature of $T_N = 32$ K give a frustration parameter of $f = \theta/T_N = 2.3$. At first sight and compared to the oxy-chromium delafossites with large negative Weiss temperatures and predominant in-plane AFM interaction, this seems to contradict a strong frustration. However, we point out that in the AgCrSe₂ we have AFM and FM interactions in the plane (see Sec. III G).

The effect of an increase of the magnetic field on $\chi_{\perp}(T)$ and $\chi_{\parallel}(T)$ is demonstrated in Fig. 6. The maximum at about



FIG. 6. Temperature dependence of the magnetic susceptibility of AgCrSe₂ (MS1212) measured at various magnetic fields for $H \perp c$ (left) and $H \parallel c$ (right). All measurements are performed in zfc/fc mode.

 $T^* = 46$ K remains rather robust against increasing fields for both directions. There is almost no field effect on $\chi_{\perp}(T)$ and $\chi_{\parallel}(T)$ toward higher temperatures. In contrast, there are dissimilar field dependencies below T^* : for $H \perp c$ the susceptibility $\chi_{\perp}(T)$ increases strongly with field, whereas for $H \parallel c$ there is only a rather small increase detectable. This is a first evidence for a field-induced metamagnetic transition in the $H \perp c$ direction. We further investigated this effect by AC susceptibility and magnetization measurements up to 14 T. Here the field-induced transition at $H^+(T)$ becomes evident by the evolution of a pronounced peak in the AC susceptibility [Fig. 7(a)] and a slope change of the magnetization M(H)[Fig. 7(b)]. For $H \parallel c$ these features are absent.



FIG. 7. AC susceptibility (a) and DC magnetization (b) versus field for $H \parallel c$ and $H \perp c$ at various temperatures as indicated. The DC and AC magnetization were measured following a zfc protocol and by increasing the field from zero to 14 T followed by warming up to 200 K between the individual cycles.



FIG. 8. Magnetization versus field for $H \perp c$. Open symbols represent data from measurements in static fields in a PPMS (at the MPI) and solid lines represent high field magnetization data recorded in pulsed fields at the HLD.

The magnetization M(H) was measured for $H \perp c$ and $H \parallel c$, shown in Figs. 8 and 9, respectively, in fields up to 14 T, using a PPMS and in pulsed magnetic fields up to 50 T at the HLD. Data on a polycrystalline sample can be found in the Supplemental Material [45]. For $H \perp c$ a field-induced metamagnetic transition at $H^+(5 \text{ K}) = 5 \text{ T}$ in M(H) is followed by a saturation of the magnetization at $M_s = 2.8 \mu_B/\text{Cr}$ above $H_s = 23.7 \text{ T}$ (Figs. 8 and 10). Figure 10 shows the first derivative of the magnetization dM/dH at various temperatures. $H^+(T)$ is defined by the peak in the derivative, in good agreement with the AC susceptibility results. The crossover to saturation at high fields is broadened toward higher temperatures. We use the half height of the high field step in the first derivative as a measure for the transition to saturation



FIG. 9. Magnetization versus field for $H \parallel c$. Open symbols represent data from measurements in static fields in a PPMS and solid lines represent high field magnetization data obtained in pulsed fields at the HLD. The dashed line corresponds to the linear in field Van Vleck contribution ($M_{VV} = H \chi_{VV\parallel}$) above 40 T with $\chi_{VV\parallel} = 0.0008$ emu/mol. The inset shows the first field derivative of the magnetization versus field for $H \parallel c$ at various temperatures. The saturation field H_S is given by a step in the derivatives.



FIG. 10. First field derivatives of the magnetization versus field for $H \perp c$ at various temperatures. The metamagnetic transition field H^+ is defined by a pronounced peak, whereas the onset of saturation at H_S is given by a step in the derivatives.

at H_s . From the ESR an isotropic saturation magnetization of about $M_s = gJ = 3 \ \mu_B/Cr$ is expected for J = 3/2 and g = 2 (see Sec. III E on the ESR results). The experimentally determined saturation magnetization of 2.8 μ_B/Cr does not fully reach the value predicted by the ESR. Possible reasons for that might be an orbital moment contribution, in addition to the spin-only moment, or shielding effects from itinerant conduction electrons with admixed Cr $3d^3$ character.

D. Specific heat and thermal expansion

Figure 11(a) presents the specific heat (C_p) of AgCrSe₂ as a function of temperature in the temperature range from 2 to 280 K. In strong contrast to oxygen-based Cr delafossites, such as CuCrO₂ [64] and PdCrO₂ [62], no clear λ -type anomaly indicating a magnetic phase transition can be observed. The absence of a strong signature might be due to the complex cycloidal magnetic order triggered by the noncentrosymmetric structure which promotes an extended spin entanglement (about 164 Å in (1,1,0) direction [32]), the frustration due to competing AFM and FM exchange, short range correlations, and emergent fluctuations. Only a tiny anomaly at the phase transition at about 33 K can be resolved in the specific heat data (see Fig. 12). A broad maximum can be found in the zero-field magnetic specific heat (C_{mag}) as a function of temperature [see Fig. 11(b)]. The presence of this broad peak centered around $T^* = 43$ K is in agreement with the maximum observed in the magnetic susceptibility (see Fig. 4) and once again points to the presence of strong frustration in AgCrSe₂. For planar isotropic triangular lattices the theory predicts this maximum with an absolute value of $C_{\text{mag}}(T^*) = 0.4R$ [65,66]. Even so most of the model calculations are performed for S = 1/2 ions, and our experimental value of $C_{\text{mag}}(T^*) \approx 0.36R$ for a S = 3/2 Cr lattice is close to this prediction. The application of magnetic fields leads to a broadening of this peak as can be seen in Fig. 11(b). To obtain the magnetic part of the specific heat C_{mag} , we subtract the phonon and electronic contributions determined by fitting a combination of Einstein, Debye, and linear terms



FIG. 11. (a) Temperature dependence of the zero-field specific heat C_p of an AgCrSe₂ single crystal. (b) C_p/T vs T for various fields for $H \parallel c$ (left axis) and magnetic specific heat C_{mag} at zero field as function of temperature (right axis). The maximum in C_{mag} at $T^* = 43$ K is clearly visible and the maximum value $C_{\text{mag}}(43 \text{ K})$ corresponds to 0.36*R*.

to the data. The details are described in the Supplemental Material [45]. In zero field the integration of C_{mag}/T from 2 to 70 K yields a reduced magnetic entropy of about 18% of $R \ln 4$. This reduced entropy might be the fingerprint of the complex cycloidal order and evolving fluctuations toward



FIG. 12. Thermal expansion coefficient α measured in *c* direction as function of temperature (left scale) together with C_p/T (expanded view) (right scale). The dashed vertical line marks the largest anomaly in the expansion at $T_N \approx 33$ K.

long range order as evidenced by neutron diffraction (see Sec. III F). In low dimensional strongly frustrated quantum magnets it is frequently found that the entropy is reduced due to strong frustration and associated fluctuations of the moments. Usually the entropy recovers and the signature of the order sharpens upon the application of magnetic field due to quenching AFM fluctuations and the polarization of the magnetic contribution to higher temperatures upon increasing field, which points to the importance of the FM exchange component [see Fig. 11(b)]. Due to the broad feature and the large nonmagnetic phonon contribution we cannot reliably determine $C_{\text{mag}}(T, H)$ from the experimental data set in magnetic fields.

In contrast to AgCrSe₂, other non-oxygen-based Cr triangular lattice systems within the R3m symmetry group (AgCrS₂, CuCrS₂) undergo an additional structural phase transition to a lower symmetry group at low temperatures, and therefore show a pronounced anomaly associated with the simultaneous structural and magnetic order in the low temperature heat capacity [57,68,69]. Furthermore, they have negative Weiss temperatures; i.e., they have predominant AFM exchange in the plane. The specific heat of CuCrSe₂ is more similar to our results [70] and the system shows no symmetry reduction toward low temperatures. Here one also finds a rather broad peak in the magnetic specific heat and only a tiny anomaly at the magnetic ordering temperature of about 50 K and a reduced magnetic entropy of about 75% of $R \ln 4$. Furthermore, CuCrSe₂ is metallic, undergoes a transition from $R\bar{3}m$ to R3m at 365 K, and has a positive Weiss temperature $(\theta = +5 \text{ K})$ indicating some in-plane FM exchange making the system a close relative of $AgCrSe_2$ [71].

To gain further insight into the nature of the phase transition, thermal expansion was measured in the temperature range from 80 K down to about 6 K. Here, the linear thermal expansion coefficient α is defined as

$$\alpha = \frac{1}{L}\frac{dL}{dT},\tag{1}$$

where L is the length of the sample (in this case along the crystallographic c direction). The values of α obtained in fields $\mu_0 H = 0$, 1, and 3 T are presented in Fig. 12. The data at zero field clearly confirm a transition at $T \approx 33$ K, which is not of first order. The latter may explain the only small hump seen in the C_p/T data at this temperature, plotted for comparison in Fig. 12. Great care was taken to accurately calculate α from the measured sample length; in fact, a second sample was measured to confirm the broad hump feature right above the transition temperature. Moreover, the thermal expansion measured in small magnetic fields applied parallel to crystallographic c direction corroborates the thermodynamic nature of the transition. As indicated by the dashed line in Fig. 12, the transition is observed at nearly constant temperature for $\alpha \parallel c$ and within fields up to 3 T. We note that as a result of the platelet-like shape of the samples (see Fig. 1), thermal expansion could so far only be measured along the crystallographic c direction, even though a comparison to the neutron data for other directions would be highly desirable. A comparison with the thermal expansion of Cr-sulphur systems $(ACrS_2, A = Cu, Ag, Au)$ clearly shows, as already mentioned



FIG. 13. (a) Evolution of the Cr^{3+} ESR spectra with temperature, (b) g factor anisotropy at 295 K, and temperature dependence of ESR linewidth and (c) inverse ESR intensity for magnetic fields $H \perp c$ and $H \parallel c$. Solid lines are fits to the linewidth data with a model assuming a spin relaxation via Z_2 vortices (see Refs. [72,74] and main text) and a Curie-Weiss law, respectively.

in the discussion of the specific heat, a different behavior since in these systems the magnetic phase transition is accompanied by a structural phase transition [69]. In contrast, our results on the thermal expansion of $AgCrSe_2$ clearly evidence the absence of any structural phase transition across the magnetic transition.

E. Electron spin resonance

Typical ESR signals at four temperatures are shown in Fig. 13(a). The spectral shapes are well defined as indicated by the Lorentzian line shape [red solid line in Fig. 13(a)]. The ESR *g* factor, as determined from the resonance field at T = 295 K, shows an uniaxial anisotropy as indicated by the red solid line in Fig. 13(b) with $g_{\parallel} = 2.00(4)$ and $g_{\perp} = 1.98(2)$ for the external field along the *c* axis and in the basal plane, respectively. The temperature dependence of the linewidth is displayed in the upper frame of Fig. 13(c). Toward the magnetic ordering temperature a divergent broadening reflects the growing importance of Cr^{3+} spin correlations. The

solid lines in Fig. 13(c) depict a relaxation model assuming short range spin correlations with chiral Z_2 vortex fluctuations. This model was previously applied to AgCrO₂ [72] and it leads to an exponential linewidth dependence on a reduced temperature scale $T/T_{\rm m} - 1$ as highlighted in the inset with $T_{\rm m}$ denoting the melting temperature of the vortex lattice. It is noteworthy that the same critical exponent of 0.37 as for AgCrO₂ can describe the data reasonably well suggesting a similar character of spin fluctuations in both systems. For the related system AgCrS₂ which, as already mentioned, has a structural phase transition across the magnetic phase transition, a slightly increased critical exponent of 0.42 is found [73]. Toward high temperatures the linewidth shows a weak increase which may indicate a broadening becoming dominated by a spin relaxation toward conduction electrons. The local Cr^{3+} susceptibility χ_{ESR} , as determined from the ESR intensity, nicely follows a Curie-Weiss law for temperatures above ≈ 150 K; see lower panel of Fig. 13(c). The Weiss temperature agrees with $T_{\rm m} = 37$ K which determines the linewidth divergence as discussed above.

F. Neutron diffraction

Neutron diffraction experiments were carried out on powdered polycrystalline material. The polycrystalline sample was characterized in full detail (see the Supplemental Material [45]). The susceptibility shows a maximum at about 50 K (frequently taken as the order temperature), a Weiss temperature around 70 K, and an effective moment of about $\mu_{\rm eff} = 3.52 \ \mu_{\rm B}$ in good agreement with earlier results on AgCrSe₂ powder [16,56]. Refinement of the crystal structure was done in the noncentrosymmetric space group R3m. The obtained structural parameters are summarized in the Supplemental Material [45] in Table S3. The crucial step to achieve a good fitting quality was to refine anisotropic thermal parameters for Ag and Se2 (see Supplemental Material [45]). The large values of the β_{11} and β_{22} parameters likely indicate a presence of cation disorder over several positions on the tetrahedral holes as originally discussed by Engelsman et al. in an early work [32]. The noncentrosymmetric nature of the crystal structure of AgCrSe₂ implies that a Lifshitz-type invariant is allowed in the Landau free-energy decomposition similar to the well-known case of the room temperature multiferroic BiFeO₃ [75], which also has a polar trigonal structure. In the latter system, the presence of the Lifshitz invariant results in a long-period cycloidal magnetic ground state with the polar c axis confined within the plane of spin rotations. At a microscopic level, this magnetic ground state is stabilized by antisymmetric exchange interactions associated with the polar structural distortions [76]. By analogy, one can assume that a similar situation might take place in AgCrSe₂. Indeed, a long-period cycloidal magnetic structure has been reported for this compound by Engelsman et al. based on neutron diffraction data [32]. However, the spins were found to be within the (a, b) plane, which is not consistent with the mechanism where the cycloidal order is stabilized by the antisymmetric exchange. To verify this crucial point, we undertook additional neutron powder diffraction measurements, targeting to explore the possibility of the ground state similar to BiFeO₃. In agreement with [32], the magnetic reflections appearing



FIG. 14. (a) Rietveld refinement of the neutron diffraction data collected at T = 1.5 K with the forward-scattering detector bank [$R_{\text{Bragg}}(\text{nuclear}) = 6.24\%$ and $R_{\text{Bragg}}(\text{magnetic}) = 3.48\%$]. The cross symbols and solid red line represent the experimental and calculated intensities, respectively, and the blue line below is the difference between them. Tick marks (green) indicate the positions of Bragg peaks: nuclear (top), magnetic (middle), and vanadium can (bottom). Inset shows integrated intensity of the diffraction pattern in the *d*-spacing range of 12–15 Å, where the strongest magnetic satellite (0.037, 0.037, 3/2) is observed, as a function of temperature. (b) Schematic representation of the long-period modulated magnetic structure of AgCrSe₂.

below 50 K [Fig. 14(a), inset] can be indexed by the k =(0.037, 0.037, 3/2) propagation vector. The reflections were found to be notably broader than the nuclear diffraction peaks indicating a finite correlation length of the magnetic order. This might be associated with the size of magnetic domains naturally expected for this propagation vector with three-arm star. The quantitative refinement of the magnetic structure [Fig. 14(a)] was done in a polar coordinate system where the spatial position of the cycloidal plane was controlled by the polar angle θ which was freely refined along with the size of Cr moments. The obtained magnetic structure [Fig. 14(b)] is very close to the one reported by Engelsman et al. [32] with no statistically significant deviation of the cycloidal plane from the (a, b) plane, $\theta = 89(7)^{\circ}$. The standard deviation for θ is however rather big indicating that a small deviation might exist but more precise single-crystal data are required to confirm that. Thus the magnetic structure confirmed in the present study strongly indicates that the long-period modulated state in AgCrSe₂ is stabilized by competing symmetric exchange



FIG. 15. Unit cell volume as a function of temperature. Inset shows the temperature dependence of the unit cell parameters.

interactions rather than a competition between symmetric and antisymmetric exchange like in BiFeO₃ or in other systems with noncentrosymmetric crystal structures [10,25,27]. The ordered moment at T = 1.5 K is 2.53(5) μ_B , which is significantly smaller than the expected value for the S = 3/2 Cr³⁺ cations and the saturation value obtained in the high magnetic field magnetization measurements (Figs. 8 and 9). This experimental result might be related to the presence of a disordered component associated with the structural disorder or might indicate a presence of strong spin fluctuations persisting down to very low temperatures.

Above the transition temperature to the magnetically ordered state, a pronounced diffuse magnetic scattering is observed (see Supplemental Material [45]) revealing the presence of well-defined spin correlations. The diffuse scattering remains up to 100 K indicating that the spin correlations start to develop at temperatures significantly higher than the magnetic transition temperature. This is a typical behavior for magnetically frustrated systems which further supports the conclusion that the modulated state in AgCrSe₂ is stabilized by competing exchange interactions. The developing spin correlations and the transition to the ordered state are accompanied by a visible lattice effect (Fig. 15) with a negative thermal expansion in the temperature range of 50 K < T <100 K. This evidences that lattice distortions play an essential role in releasing frustration and establishing the long range ordered magnetic ground state.

G. Competing Heisenberg exchange between Cr ions

Delafossite compounds containing chromium inside a distorted chalcogenide octahedra typically cannot be described with an exchange model containing nearest-neighbor interactions only [68]. A finite saturation field for the magnetization M(H) together with a positive Curie-Weiss temperature of the susceptibility $\chi(T)$ demonstrates that we are faced with at least two competing exchange parameters. Preliminary density functional calculations [55] suggest that the dominant exchange interactions are ferromagnetic $J_1 < 0$ between nearest neighbors and antiferromagnetic between third-nearest neighbors with $J_3 = O(|J_1|)$. Together with a small but finite single-ion anisotropy D > 0 we thus use a minimal Hamiltonian of the form

$$\mathcal{H} = \sum_{i=1}^{\nu} \mathcal{H}(i),$$

$$\mathcal{H}(i) = D(S_i^z)^2 - g\mu_{\rm B}\mu_0 \vec{H} \vec{S}_i$$

$$+ \frac{1}{2} J_1 \sum_{j \in \mathrm{nn}(i)} \vec{S}_i \vec{S}_j + \frac{1}{2} J_3 \sum_{j \in \mathrm{3n}(i)} \vec{S}_i \vec{S}_j, \qquad (2)$$

for ν magnetic ions, ignoring possible symmetry-allowed symmetric and antisymmetric exchange anisotropies as well as second-neighbor and interplane exchange.

A high-temperature expansion for the magnetic susceptibility [77,78] yields

$$\theta_{\rm CW}^{\parallel} = -\frac{s(s+1)}{3k_{\rm B}}z(J_1+J_3) + \frac{(2s-1)(2s+3)}{15k_{\rm B}}D,\qquad(3)$$

$$\theta_{\rm CW}^{\perp} = -\frac{s(s+1)}{3k_{\rm B}}z(J_1 + J_3) - \frac{(2s-1)(2s+3)}{30k_{\rm B}}D \qquad (4)$$

with s = 3/2 and z = 6. Here, the symbols \parallel and \perp indicate the field direction relative to the direction of the single-ion anisotropy.

The saturation field $\mu_0 H_{\rm S}^{\parallel}$ of the magnetization M(H) is the strength of the applied magnetic field where the sample reaches the fully polarized state with moment $M_{\rm S}$ per Cr ion. It is given by [65,79]

$$\mu_0 H_{\rm S}^{\parallel} = \frac{2s^2}{M_{\rm S}} [D + J(0) - J(\vec{Q})],\tag{5}$$

where $M_{\rm S} = g_{\parallel} \mu_{\rm B} s$ and \bar{Q} is the ordering vector of the magnetic phase in the *xy* plane perpendicular to the field. Here we assume \vec{H} points into the direction of the single-ion anisotropy defining the global *z* direction. The Fourier transform of the exchange tensor in the *xy* plane is given by

$$J(\vec{k}) = \frac{1}{\nu} \sum_{\langle ij \rangle} J_{ij} e^{-i\vec{k}(\vec{R}_i - \vec{R}_j)} = \frac{1}{2} \sum_n J_n e^{-i\vec{k}\vec{R}_n}, \qquad (6)$$

where the sum runs over all bonds *n* connecting a fixed site *i* with its neighbors. Minimizing the classical energy $vs^2J(\vec{Q})$ for the Hamiltonian (2) above with respect to the components of the ordering vector yields a series of magnetic phases. With $\alpha := J_3/J_1, J_1 < 0$ we obtain the following two:

Ferromagnetic phase. For $\alpha \ge 0$ the ground state trivially is a ferromagnet, i. e., $\vec{Q} = 0$, and $J(0) = 3(J_1 + J_3)$. The saturation field in this case is determined by the single-ion anisotropy *D* alone. This remains true also for $-1/4 \le \alpha < 0$: even a frustrating AFM third-neighbor exchange $J_3 > 0$ with $J_3 < |J_1|/4$ does not destroy the fully polarized ground state.

Spiral phase. For $\alpha < -1/4$ or $J_3 > |J_1|/4$ the classical ground state is a spiral along [110] with an incommensurate \vec{Q} vector,

$$\vec{Q} = \left(2\cos^{-1}\left(\frac{1}{2\sqrt{2}}\sqrt{5 - \frac{\sqrt{\alpha(\alpha - 2)}}{\alpha}}\right), \\ \times \frac{2}{\sqrt{3}}\cos^{-1}\left(\frac{\sqrt{5 - \frac{\sqrt{\alpha(\alpha - 2)}}{\alpha}}}{2\sqrt{2}[\sqrt{\alpha(\alpha - 2)} - \alpha]}\right)\right).$$
(7)

Correspondingly we obtain

$$J(\vec{Q}) = -\frac{J_1}{4} \left(1 + \frac{J_1}{2J_3} + 5\frac{J_3}{J_1} \right) - \frac{J_3}{4} \left(1 - \frac{2J_1}{J_3} \right)^{3/2}$$
(8)

for the ground state energy and

$$\mu_0 H_{\rm S}^{\parallel} = \frac{2s^2}{M_{\rm S}} \left[D + \frac{J_1}{4} \left(13 + \frac{J_1}{2J_3} + 17\frac{J_3}{J_1} \right) + \frac{J_3}{4} \left(1 - \frac{2J_1}{J_3} \right)^{3/2} \right]$$
(9)

for the saturation field. This is the case for $AgCrSe_2$.

Experimentally, we have obtained a Curie-Weiss temperature $\theta = +75$ K, approximately independent of the field direction. The saturation field directed parallel to the crystallographic *c* direction is obtained as $\mu_0 H_{\rm S}^{\parallel} = 25.1$ T with a saturation moment $M_{\rm S} = 2.8 \,\mu_{\rm B}/{\rm Cr}$ ion. Ignoring the small single-ion anisotropy, justified by the directional independence of θ , we obtain $J_1 = -1.73$ meV = $-20k_{\rm B}$ K and $J_3 = 0.86$ meV = $10k_{\rm B}$ K.

Two remarks are due on the size of the single ion anisotropy D. Although we find that D must be small compared to the absolute values of the exchange constants, it is nonzero. A finite D > 0 along the c direction "forces" the Cr moments into the (a, b) plane. Because of that, a saturation field in the (a, b) plane does not depend on D [80]; therefore we may obtain an estimate of D via

$$D = \frac{\mu_0}{2s^2} M_{\rm S} \left(H_{\rm S}^{\parallel} - H_{\rm S}^{\perp} \right) = 0.05 \text{ meV} = 0.6k_{\rm B} \text{K}$$
(10)

with $\mu_0 H_{\rm S}^{\perp} = 23.7$ T in the (a, b) plane.

The metamagnetic transition we observe at a field $\mu_0 H^+ = 5$ T at low temperatures supports this scenario: Any field having a component perpendicular to the direction of *D* breaks the rotational symmetry of the Hamiltonian around *D*. For small fields, the ordered moments remain in the plane and form a "distorted helix" until H^+ is reached: a transition to a fan phase occurs. For a purely AFM nearest-neighbor exchange *J*, the critical field is given by $\mu_0 H^+ = (2s^2/M_S)\sqrt{DJ}$ [80,81], and we expect a similar scaling with an effective exchange constant $J_{\text{eff}} \gg D$ derived from the exchange structure of our model, Eq. (2).

H. Single-crystal H-T phase diagram

The magnetic exchange interactions in AgCrSe₂ are very different from those in the oxygen-based Cr delafossites. Whereas the latter are characterized by a predominant and a very strong AFM nearest-neighbor interaction, AgCrSe₂ features an interplay of FM nearest-neighbor and AFM third-nearest-neighbor interactions. As a consequence, AgCrSe₂ shows a cycloidal order with large modulation length (about 164 Å) along the (1,1,0) direction [32], whereas the oxygen-based Cr delafossites exhibit a robust 120° order on the triangular lattice. In AgCrSe₂, the application of magnetic fields first results in a modulation of the magnetic structure and, due to the smaller magnitude and different nature of the exchange interactions, it is possible to ferromagnetically align the moments in rather small fields of only about 25 T. That is different in the Cr-oxygen delafossites, where the saturation



FIG. 16. *H*-*T* phase diagram of AgCrSe₂, obtained from various methods for magnetic fields $H \perp c$ and $H \parallel c$. The ordered state 1 represents the cycloidal phase for $H \perp c$ below $H^+(T)$ [see Fig. 14(b)], whereas phase 2 represents a planar fan phase for inplane fields [above $H^+(T)$] and a more conelike phase for fields in *c* direction.

fields are estimated to be an order of magnitude higher, e.g., 240 T in CuCrO₂ [82]. AgCrSe₂ is thus characterized by a favorable combination of competing interactions between Cr ions and thermal excitations, which finally leads to a tunable magnetic ground state and the emergence of magnetic fluctuations at the verge of magnetic order.

Figure 16 shows the H-T phase diagram of AgCrSe₂ for both directions, $H \perp c$ and $H \parallel c$. We note that the *H*-*T* phase diagram of polycrystalline AgCrSe₂, shown in the Supplemental Material [45], displays some marked differences from that of the single crystal due to the strong 2D nature of the exchange interactions. In high magnetic fields, AgCrSe₂ displays an isotropic behavior; i.e., almost the same saturation fields are found for both field directions. For $H \perp c$ a metamagnetic phase transition appears at about $H^+ = 5$ T, which corresponds to about 1/5 of the saturation field. For spin-1/2 triangular lattices with 120° order a metamagnetic transition at a value of 1/3 is predicted [83,84] and found for example in $Ba_3CoSb_2O_9$ [85]. Above H^+ our results suggest a planar fan-type magnetic order in AgCrSe₂. For fields in the c direction our data are consistent with a continuous tilting of the moments out of the plane where the tilt angle increases upon increasing the field. These results motivate future neutron diffraction experiments on single crystals to solve the magnetic structure in applied magnetic fields.

Moreover, at high temperatures we have revealed a region of competing interactions characterized by magnetic fluctuations before $AgCrSe_2$ orders magnetically at lower temperatures. These magnetic fluctuations also influence the electronic transport properties of $AgCrSe_2$ [15]. Inelastic neutron scattering studies are needed to investigate the excitation spectrum of these fluctuations.

IV. SUMMARY AND CONCLUDING REMARKS

In summary, we studied the H-T phase diagram of AgCrSe₂ in great detail. We identified paramagnetic, long ranged ordered, and field polarized regimes. Whereas the Cr-oxygen delafossites crystallize in the $R\bar{3}m$ space group and are characterized by a very strong AFM nearest-neighbor interaction, which then usually leads to a planar 120° order, the Cr-sulfur and Cr-selenide delafossites display transitions from the $R\bar{3}m$ group to lower symmetries. Furthermore, higher order magnetic exchange interactions play an important role, which finally leads to a larger variation in the magnetic ground states; 120°, stripe, spin-spiral, and cycloidal-type ordered states are observed. In addition to the symmetry reduction from $R\bar{3}m$ to R3m at high temperatures, a further symmetry reduction is usually found for the Cr-sulfur delafossites at the onset of magnetic order. This effect is not observed in AgCrSe₂. In this respect, AgCrSe₂ is a model system for the study of a planar Cr triangular lattice with dissimilar Heisenberg-like interactions.

Our comprehensive study with local and bulk probes shows that AgCrSe₂ is an anisotropic cycloidal magnet with emerging anisotropic laterally extended magnetic fluctuations. For magnetic fields applied in the (a, b) plane, we find a metamagnetic phase transition, which is not present for fields parallel c. Whereas we could study the magnetic structure in zero-field by neutrons diffraction, the magnetic structure in magnetic fields is still not known. From our data we also cannot rule out chiral magnetic textures in applied magnetic fields, which is certainly an attractive project left for future neutron studies.

The experimentally established H-T phase diagram is consistent with a planar Heisenberg model, in which the nearest-neighbor interaction, unlike in the Cr-oxygen delafossites, is ferromagnetic and the third-nearest-neighbor interaction is antiferromagnetic. In AgCrSe₂ the interactions among the Cr ions have just the right strength to be tuned by experimentally accessible magnetic fields. Based on our theoretical model and on the temperature dependence of the lattice parameters obtained from neutron diffraction, we suspect that the magnetic properties might be easily tuned by hydrostatic pressure or uniaxial stress. In this respect, AgCrSe₂ is a model system for the study of a planar Cr^{3+} triangular lattice with dissimilar Heisenberg-like interactions.

The photoemission and x-ray absorption data supporting this publication can be accessed at [89].

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- A. H. Castro Neto, F. Guinea, N. M. R. Peres, K. S. Novoselov, and A. K. Geim, The electronic properties of graphene, Rev. Mod. Phys. 81, 109 (2009).
- [2] S. Z. Butler, S. M. Hollen, L. Cao, Y. Cui, J. A. Gupta, H. R. Gutiérrez, T. F. Heinz, S. S. Hong, J. Huang, A. F. Ismach *et al.*, Progress, challenges, and opportunities in two-dimensional materials beyond graphene, ACS Nano 7, 2898 (2013).
- [3] P. J. W. Moll, P. Kushwaha, N. Nandi, B. Schmidt, and A. P. Mackenzie, Evidence for hydrodynamic electron flow in PdCoO₂, Science **351**, 1061 (2016).
- [4] A. P. Mackenzie, The properties of ultrapure delafossite metals, Rep. Prog. Phys. 80, 032501 (2017).
- [5] Y. Shimizu, T. Hiramatsu, M. Maesato, A. Otsuka, H. Yamochi, A. Ono, M. Itoh, M. Yoshida, M. Takigawa, Y. Yoshida, and G. Saito, Pressure-Tuned Exchange Coupling of a Quantum Spin Liquid in the Molecular Triangular Lattice κ-(ET)₂Ag₂(CN)₃, Phys. Rev. Lett. **117**, 107203 (2016).
- [6] H. D. Zhou, E. S. Choi, G. Li, L. Balicas, C. R. Wiebe, Y. Qiu, J. R. D. Copley, and J. S. Gardner, Spin Liquid State in the *S* = 1/2 Triangular Lattice Ba₃CuSb₂O₉, Phys. Rev. Lett. **106**, 147204 (2011).

- [7] P. W. Anderson, Resonating valence bonds: A new kind of insulator?, Mater. Res. Bull. 8, 153 (1973).
- [8] K. S. Burch, D. Mandrus, and J.-G. Park, Magnetism in twodimensional van der Waals materials, Nature (London) 563, 47 (2018).
- [9] S. Lei, J. Lin, Y. Jia, M. Gray, A. Topp, G. Farahi, S. Klemenz, T. Gao, F. Rodolakis, J. L. McChesney *et al.*, High mobility in a van der Waals layered antiferromagnetic metal, Sci. Adv. 6, eaay6407 (2020).
- [10] S. Mühlbauer, B. Binz, F. Jonietz, C. Pfleiderer, A. Rosch, A. Neubauer, R. Georgii, and P. Böni, Skyrmion lattice in a chiral magnet, Science 323, 915 (2009).
- [11] K. F. Wang, J.-M. Liu, and Z. F. Ren, Multiferroicity: The coupling between magnetic and polarization orders, Adv. Phys. 58, 321 (2009).
- [12] M. Fiebig, T. Lottermoser, D. Meier, and M. Trassin, The evolution of multiferroics, Nat. Rev. Mater. 1, 16046 (2016).
- [13] A. Manchon, H. C. Koo, J. Nitta, S. M. Frolov, and R. A. Duine, New perspectives for Rashba spin-orbit coupling, Nat. Mater. 14, 871 (2015).

- [14] R. Yano and T. Sasagawa, Crystal growth and intrinsic properties of $ACrX_2$ (A = Cu, Ag; X = S, Se) without a secondary phase, Cryst. Growth Des. **16**, 5618 (2016).
- [15] H. Zhang (unpublished).
- [16] U. K. Gautam, R. Seshadri, S. Vasudevan, and A. Maignan, Magnetic and transport properties, and electronic structure of the layered chalcogenide AgCrSe₂, Solid State Commun. 122, 607 (2002).
- [17] M. A. Marquardt, N. A. Ashmore, and D. P. Cann, Crystal chemistry and electrical properties of the delafossite structure, Thin Solid Films 496, 146 (2006).
- [18] A. van der Lee and G. A. Wiegers, Anharmonic thermal motion of Ag in AgCrSe₂: A high-temperature single-crystal x-ray diffraction study, J. Solid State Chem. 82, 216 (1989).
- [19] B. Li, H. Wang, Y. Kawakita, Q. Zhang, M. Feygenson, H. L. Yu, D. Wu, K. Ohara, T. Kikuchi, K. Shibata *et al.*, Liquid-like thermal conduction in intercalated layered crystalline solids, Nat. Mater. **17**, 226 (2018).
- [20] D. W. Murphy, H. S. Chen, and B. Tell, Superionic conduction in AgCrS₂ and AgCrSe₂, J. Electrochem. Soc. **124**, 1268 (1977).
- [21] I. E. Dzyaloshinskii, Theory of helicoidal structures in antiferromagnets. I. Nonmetals, Sov. Phys. JETP 19, 960 (1964).
- [22] H. Wilhelm, M. Baenitz, M. Schmidt, U. K. Rößler, A. A. Leonov, and A. N. Bogdanov, Precursor Phenomena at the Magnetic Ordering of the Cubic Helimagnet FeGe, Phys. Rev. Lett. 107, 127203 (2011).
- [23] S. Nakatsuji, N. Kiyohara, and T. Higo, Large anomalous Hall effect in a non-collinear antiferromagnet at room temperature, Nature (London) 527, 212 (2015).
- [24] Y. Cao, Z. Huang, Y. Yin, H. Xie, B. Liu, W. Wang, C. Zhu, D. Mandrus, L. Wang, and W. Huang, Overview and advances in a layered chiral helimagnet Cr_{1/3}NbS₂, Mater. Today 7, 100080 (2020).
- [25] K. Takada, H. Sakurai, E. Takayama-Muromachi, F. Izumi, R. A. Dilanian, and T. Sasaki, Superconductivity in two-dimensional CoO₂ layers, Nature (London) 422, 53 (2003).
- [26] H. Kuriyama, M. Nohara, T. Sasagawa, K. Takubo, T. Mizokawa, K. Kimura, and H. Takagi, High-temperature thermoelectric properties of delafossite oxide CuRh_{1-x}Mg_xO₂, in 2006 25th International Conference on Thermoelectrics (IEEE, Vienna, Austria, 2006), pp. 97–98.
- [27] J. T. Haraldsen, F. Ye, R. S. Fishman, J. A. Fernandez-Baca, Y. Yamaguchi, K. Kimura, and T. Kimura, Multiferroic phase of doped delafossite CuFeO₂ identified using inelastic neutron scattering, Phys. Rev. B 82, 020404(R) (2010).
- [28] K. M. Ranjith, D. Dmytriieva, S. Khim, J. Sichelschmidt, S. Luther, D. Ehlers, H. Yasuoka, J. Wosnitza, A. A. Tsirlin, H. Kühne, and M. Baenitz, Field-induced instability of the quantum spin liquid ground state in the $J_{\text{eff}} = 1/2$ triangular-lattice compound NaYbO₂, Phys. Rev. B **99**, 180401(R) (2019).
- [29] P. Baltzer, P. Wojtowicz, M. Robbins, and E. Lopatin, Exchange interactions in ferromagnetic chalcogenide spinels, Phys. Rev. 151, 367 (1966).
- [30] R. Huang and N. L. Orbach, Systematics of the right angle nearest neighbor exchange interaction in *d*³ ions, J. Appl. Phys. **39**, 426 (1968).
- [31] A. Miyata, O. Portugall, D. Nakamura, K. Ohgushi, and S. Takeyama, Ultrahigh magnetic field phases in the frustrated

triangular-lattice magnet CuCrO₂, Phys. Rev. B **96**, 180401(R) (2017).

- [32] F. M. R. Engelsman, G. A. Wiegers, F. Jellinek, and B. van Laar, Crystal structures and magnetic structures of some metal (I) chromium (III) sulfides and selenides, J. Solid State Chem. 6, 574 (1973).
- [33] Y. Skourski, M. D. Kuz'min, K. P. Skokov, A. V. Andreev, and J. Wosnitza, High-field magnetization of Ho₂Fe₁₇, Phys. Rev. B 83, 214420 (2011).
- [34] D. Rauch, M. Kraken, F. Litterst, S. Süllow, H. Luetkens, M. Brando, T. Förster, J. Sichelschmidt, A. Neubauer, C. Pfleiderer, W. J. Duncan, and F. M. Grosche, Spectroscopic study of metallic magnetism in single-crystalline Nb_{1-y}Fe_{2+y}, Phys. Rev. B **91**, 174404 (2015).
- [35] A. Abragam and B. Bleaney, *Electron Paramagnetic Resonance* of *Transition Ions* (Oxford University Press, Oxford, 2012).
- [36] T. Gruner, J. Wykhoff, J. Sichelschmidt, C. Krellner, C. Geibel, and F. Steglich, Anisotropic electron spin resonance of YbIr₂Si₂, J. Condens. Matter Phys. 22, 135602 (2010).
- [37] R. Küchler, T. Bauer, M. Brando, and F. Steglich, A compact and miniaturized high resolution capacitance dilatometer for measuring thermal expansion and magnetostriction, Rev. Sci. Instrum. 83, 095102 (2012).
- [38] L. C. Chapon, P. Manuel, P. G. Radaelli, C. Benson, L. Perrott, S. Ansell, N. J. Rhodes, D. Raspino, D. Duxbury, E. Spill *et al.*, Wish: The new powder and single crystal magnetic diffractometer on the second target station, Neutron News 22, 22 (2011).
- [39] J. Rodríguez-Carvajal, Recent advances in magnetic structure determination by neutron powder diffraction, Physica B (Amsterdam, Neth.) 192, 55 (1993).
- [40] K. Koepernik and H. Eschrig, Full-potential nonorthogonal local-orbital minimum-basis band-structure scheme, Phys. Rev. B 59, 1743 (1999).
- [41] I. Opahle, K. Koepernik, and H. Eschrig, Full-potential bandstructure calculation of iron pyrite, Phys. Rev. B 60, 14035 (1999).
- [42] For the code, see http://www.fplo.de.
- [43] J. P. Perdew and Y. Wang, Accurate and simple analytic representation of the electron-gas correlation energy, Phys. Rev. B 45, 13244 (1992).
- [44] H. Eschrig, M. Richter, and I. Opahle, Chapter 12: Relativistic solid state calculations, in *Relativistic Electronic Structure Theory*, Theoretical and Computational Chemistry, edited by P. Schwerdtfeger (Elsevier, Netherlands, 2004), Vol. 14, pp. 723–776.
- [45] See Supplemental Material at http://link.aps.org/supplemental/ 10.1103/PhysRevB.104.134410 for details of sample preparation, characterization, results of additional measurements, and calculations. It includes Refs. [19,34,86–88].
- [46] M. Tang, Z. Chen, C. Yin, L. Lin, D. Ren, B. Liu, B. Kang, and R. Ang, Thermoelectric modulation by intrinsic defects in superionic conductor Ag_xCrSe₂, Appl. Phys. Lett. **116**, 163901 (2020).
- [47] D. Meyers, S. Mukherjee, J.-G. Cheng, S. Middey, J.-S. Zhou, J. B. Goodenough, B. A. Gray, J. W. Freeland, T. Saha-Dasgupta, and J. Chakhalian, Zhang-Rice physics and anomalous copper states in A-site ordered perovskites, Sci. Rep. 3, 1834 (2013).
- [48] V. Sunko, F. Mazzola, S. Kitamura, S. Khim, P. Kushwaha, O. J. Clark, M. D. Watson, I. Marković, D. Biswas, L. Pourovskii,

T. K. Kim, T.-L. Lee, P. K. Thakur, H. Rosner, A. Georges, R. Moessner, T. Oka, A. P. Mackenzie, and P. D. C. King, Probing spin correlations using angle-resolved photoemission in a coupled metallic Mott insulator system, Sci. Adv. 6, eaaz0611 (2020).

- [49] H.-J. Noh, J. Jeong, B. Chang, D. Jeong, H. S. Moon, E.-J. Cho, J. M. Ok, J. S. Kim, K. Kim, B. I. Min, H.-K. Lee, J.-Y. Kim, B.-G. Park, H.-D. Kim, and S. Lee, Direct observation of localized spin antiferromagnetic transition in PdCrO₂ by angle-resolved photoemission spectroscopy, Sci. Rep. 4, 3680 (2015).
- [50] F. Lechermann, Hidden Mott insulator in metallic PdCrO₂, Phys. Rev. Mater. 2, 085004 (2018).
- [51] M. D. Watson, I. Marković, F. Mazzola, A. Rajan, E. A. Morales, D. M. Burn, T. Hesjedal, G. van der Laan, S. Mukherjee, T. K. Kim, C. Bigi, I. Vobornik, M. Ciomaga Hatnean, G. Balakrishnan, and P. D. C. King, Direct observation of the energy gain underpinning ferromagnetic superexchange in the electronic structure of CrGeTe₃, Phys. Rev. B 101, 205125 (2020).
- [52] A. Frisk, L. B. Duffy, S. Zhang, G. van der Laan, and T. Hesjedal, Magnetic x-ray spectroscopy of two-dimensional CrI₃ layers, Mater. Lett. 232, 5 (2018).
- [53] O. Janson, S. Chen, A. A. Tsirlin, S. Hoffmann, J. Sichelschmidt, Q. Huang, Z. J. Zhang, M. B. Tang, J. T. Zhao, R. Kniep, and H. Rosner, Structure and magnetism of Cr₂[BP₃O₁₂]: Towards the quantum-classical crossover in a spin-3/2 alternating chain, Phys. Rev. B 87, 064417 (2013).
- [54] O. Janson, G. Nenert, M. Isobe, Y. Skourski, Y. Ueda, H. Rosner, and A. A. Tsirlin, Magnetic pyroxenes LiCrGe_2O_6 and LiCrSi_2O_6 : Dimensionality crossover in a nonfrustrated S = 3/2 Heisenberg model, Phys. Rev. B **90**, 214424 (2014).
- [55] S. Kim (unpublished).
- [56] P. F. Bongers, C. F. van Bruggen, J. Koopstra, W. P. F. A. M. Omloo, G. A. Wiegers, and F. Jellinek, Structures and magnetic properties of some metal (I) chromium (III) sulfides and selenides, J. Phys. Chem. Solids 29, 977 (1968).
- [57] J. M. Vandenberg-Voorhoeve, Structural and magnetic properties of layered chalcogenides of the transition elements, in *Optical and Electrical Properties* (Springer, Netherlands, 1976), pp. 423–457.
- [58] S. Seki, Y. Onose, and Y. Tokura, Spin-Driven Ferroelectricity in Triangular Lattice Antiferromagnets $ACrO_2$ (A = Cu, Ag, Li, or Na), Phys. Rev. Lett. **101**, 067204 (2008).
- [59] D. Billington, D. Ernsting, T. E. Millichamp, C. Lester, S. B. Dugdale, D. Kersh, J. A. Duffy, S. R. Giblin, J. W. Taylor, P. Manuel *et al.*, Magnetic frustration, short-range correlations and the role of the paramagnetic Fermi surface of PdCrO₂, Sci. Rep. 5, 12428 (2015).
- [60] Y. Oohara, S. Mitsuda, H. Yoshizawa, N. Yaguchi, H. Kuriyama, T. Asano, and M. Mekata, Magnetic phase transition in AgCrO₂, J. Phys. Soc. Jpn. **63**, 847 (1994).
- [61] K. Kimura, H. Nakamura, K. Ohgushi, and T. Kimura, Magnetoelectric control of spin-chiral ferroelectric domains in a triangular lattice antiferromagnet, Phys. Rev. B 78, 140401(R) (2008).
- [62] H. Takatsu, H. Yoshizawa, S. Yonezawa, and Y. Maeno, Critical behavior of the metallic triangular-lattice Heisenberg antiferromagnet PdCrO₂, Phys. Rev. B 79, 104424 (2009).

- [63] S. Kobayashi, H. Ueda, C. Michioka, and K. Yoshimura, Competition between the direct exchange interaction and superexchange interaction in layered compounds LiCrSe₂, LiCrTe₂, and NaCrTe₂ with a triangular lattice, Inorg. Chem. 55, 7407 (2016).
- [64] T. Okuda, Y. Beppu, Y. Fujii, T. Onoe, N. Terada, and S. Miyasaka, Specific heat of delafossite oxide $\text{CuCr}_{1-x}\text{Mg}_x\text{O}_2$ ($0 \le x \le 0.03$), Phys. Rev. B 77, 134423 (2008).
- [65] B. Schmidt and P. Thalmeier, Frustrated two-dimensional quantum magnets, Phys. Rep. 703, 1 (2017).
- [66] B. Bernu and G. Misguich, Specific heat and high-temperature series of lattice models: Interpolation scheme and examples on quantum spin systems in one and two dimensions, Phys. Rev. B 63, 134409 (2001).
- [67] A. P. Ramirez, Chapter 4: Geometrical frustration, Handbook of Magnetic Materials 13, 423 (2001).
- [68] A. V. Ushakov, D. A. Kukusta, A. N. Yaresko, and D. I. Khomskii, Magnetism of layered chromium sulfides $MCrS_2$ (M = Li, Na, K, Ag, and Au): A first-principles study, Phys. Rev. B **87**, 014418 (2013).
- [69] T. Kanematsu, Y. Okamoto, and K. Takenaka, Large magneticfield-induced strain at the magnetic order transition in triangular antiferromagnet AgCrS₂, Appl. Phys. Lett. **118**, 142404 (2021).
- [70] G. C. Tewari, M. Karppinen, and A. K. Rastogi, Effects of competing magnetic interactions on the electronic transport properties of CuCrSe₂, J. Solid State Chem. **198**, 108 (2013).
- [71] A. Gagor, D. Gnida, and A. Pietraszko, Order disorder phenomena in layered CuCrSe₂ crystals, Mater. Chem. Phys. **146**, 283 (2014).
- [72] M. Hemmida, H.-A. Krug von Nidda, and A. Loidl, Traces of Z₂-vortices in CuCrO₂, AgCrO₂, and PdCrO₂, J. Phys. Soc. Jpn. 80, 053707 (2011).
- [73] W. Gao, L. Shi, Z. Ouyang, Z. Xia, Z. Wang, B. Liu, H. Li, Y. Zou, L. Yu, L. Zhang *et al.*, Competing spin fluctuations and trace of vortex dynamics in the two-dimensional triangularlattice antiferromagnet AgCrS₂, J. Phys.: Condens. Matter **30**, 265802 (2018).
- [74] M. Hemmida, Electron Spin Resonance in Frustrated Two- and Three-Dimensional Chromium Magnets, Ph.D. thesis, Universität Augsburg (2012).
- [75] A. M. Kadomtseva, A. K. Zvezdin, Y. F. Popov, A. P. Pyatakov, and G. P. Vorob'ev, Space-time parity violation and magnetoelectric interactions in antiferromagnets, J. Exp. Theor. Phys. 79, 571 (2004).
- [76] A. K. Zvezdin and A. P. Pyatakov, On the problem of coexistence of the weak ferromagnetism and the spin flexoelectricity in multiferroic bismuth ferrite, Europhys. Lett. 99, 57003 (2012).
- [77] H.-J. Schmidt, A. Lohmann, and J. Richter, Eighth-order hightemperature expansion for general Heisenberg Hamiltonians, Phys. Rev. B 84, 104443 (2011).
- [78] D. C. Johnston, Influence of uniaxial single-ion anisotropy on the magnetic and thermal properties of Heisenberg antiferromagnets within unified molecular field theory, Phys. Rev. B 95, 094421 (2017).
- [79] B. Schmidt and P. Thalmeier, Quantum fluctuations in anisotropic triangular lattices with ferromagnetic and antiferromagnetic exchange, Phys. Rev. B 89, 184402 (2014).

- [80] S. I. Abarzhi and A. V. Chubukov, Spin reorientation in hexagonal antiferromagnets, J. Condens. Matter Phys. 2, 9221 (1990).
- [81] E. Rastelli and A. Tassi, Spin configurations of *ABX*₃ antiferromagnets in an external magnetic field, Phys. Rev. B 50, 16475 (1994).
- [82] Y. A. Sakhratov, L. Svistov, P. Kuhns, H. Zhou, and A. Reyes, Magnetic phases of the quasi-two-dimensional antiferromagnet CuCrO₂ on a triangular lattice, Phys. Rev. B 94, 094410 (2016).
- [83] H. Kawamura and S. Miyashita, Phase transition of the Heisenberg antiferromagnet on the triangular lattice in a magnetic field, J. Phys. Soc. Jpn. 54, 4530 (1985).
- [84] L. Seabra, T. Momoi, P. Sindzingre, and N. Shannon, Phase diagram of the classical Heisenberg antiferromagnet on a triangular lattice in an applied magnetic field, Phys. Rev. B 84, 214418 (2011).

- [85] Y. Shirata, H. Tanaka, A. Matsuo, and K. Kindo, Experimental Realization of a Spin-1/2 Triangular-Lattice Heisenberg Antiferromagnet, Phys. Rev. Lett. 108, 057205 (2012).
- [86] H. Liu, J. Yang, X. Shi, S. A. Danilkin, D. Yu, C. Wang, W. Zhang, and L. Chen, Reduction of thermal conductivity by low energy multi-Einstein optic modes, J. Materiomics 2, 187 (2016).
- [87] S. Roychowdhury, M. K. Jana, J. Pan, S. N. Guin, D. Sanyal, U. V. Waghmare, and K. Biswas, Soft phonon modes leading to ultralow thermal conductivity and high thermoelectric performance in AgCuTe, Angew. Chem. Int. Ed. 57, 4043 (2018).
- [88] H. Zhu, C. Zhao, P. Nan, X.-m. Jiang, J. Zhao, B. Ge, C. Xiao, and Y. Xie, Intrinsically low lattice thermal conductivity in natural superlattice (Bi₂)_m(Bi₂Te₃)_n thermoelectric materials, Chem. Mater. **33**, 1140 (2021).
- [89] See https://doi.org/10.17630/514dae28-fb4e-4b2d-91a8f262d14f3e05.
- [90] See http://www.trieste.NFFA.eu.