# **Determination of the crystal field and nature of x-ray linear dichroism for Co-O with local octahedral, tetrahedral, and tetragonal symmetries**

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Cobalt oxides with multiple local Co-O coordination environments such as octahedral, tetrahedral, and tetragonal networks display versatile electronic and magnetic properties which have attracted great interest in many fields. Understanding the ground-state properties and determining the fundamental band gap remain challenges in cobalt-based compounds and thin films, which have been investigated here using synchrotron-based Co  $L_{23}$ -edge x-ray absorption measurements followed by configuration interaction cluster calculations. We focus on the detailed Co *L*23-edge absorption spectral variations in different octahedral crystal fields as well as in the less investigated tetrahedral and tetragonal systems, taking into account Co ions with different valence states. From a quantitative comparison between the simulated spectrum and an accurately measured absorption spectrum of a specified compound, the crystal field value can be extracted from the Co  $L_{23}$ -edge absorption spectrum, which is complementary to the results obtained in optical measurements and other calculations. Furthermore, Co *L*<sub>23</sub>-edge x-ray linear dichroism shows the same spectral evolutions as a result of either local  $CoO<sub>6</sub>$  cluster with tetragonal symmetry or the magnetic exchange field, whereas both coexist in most antiferromagnetic cobalt oxide thin films. Detailed temperature and polarization-dependent Co *L*23-edge absorption measurements have been proposed to distinguish both contributions, which show different spectral variations due to the specified modifications of the ground and final states at different temperatures. Our results offer theoretical guidance for understanding the multiplet structure of Co  $L_{23}$ -edge absorption spectrum, obtaining the precise crystal field value for cobalt oxides with versatile coordinations, and explaining the underlying mechanism of x-ray linear dichroism, as well as understanding the fundamental physical properties and their potential applicability of cobalt oxides and their thin films.

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## **I. INTRODUCTION**

Cobalt oxides are of particular interest due to their diverse magnetic, electronic, and optical properties  $[1-3]$  as well as due to their rich technological applications such as solid oxide fuel cells, oxidization catalysts, gas sensors, and membranes for oxygen separation  $[4–7]$ , etc. Among them, two representative classes of cobalt oxides are the spinel  $Co<sub>3</sub>O<sub>4</sub>$  structural compounds where the variation of the cations on octahedrally and tetrahedrally coordinated sites can be used to tune the ground-state properties determining the potential optoelectronic applications  $[8-10]$  and the  $ACoO<sub>3</sub>$  (A  $=$  Alkaline earth metal or lanthanide) perovskite compounds where the complicated phase diagram can be strongly modified by the *A* site cations with different ionic radii [\[3,11,12\]](#page-7-0), as will be focused on below. In the ionic limit, cobalt cations can adopt multiple valence states with  $Co^{2+}$ ,  $Co^{3+}$ , and  $Co^{4+}$ , corresponding to Co  $3d^7$ , Co  $3d^6$ , and Co  $3d^5$  electronic configurations,

respectively. Moreover, cobalt ions are susceptible to multiple spin states. Both diverse valence states and multiple spin states serve as the driving forces for the aforementioned distinct physical properties.

Most cobalt oxides exhibit insulating behaviors while the origin of the band gap remains controversial. Depending on the competition between electron-electron Coulomb interaction energy  $U_{dd}$  and the charge transfer energy  $\Delta$  representing the charge fluctuation energy to move one electron from the ligand hole *L* to the Co 3*d* site, the band gap can be forms of the *p* − *d* type, composed of different kinds of orbitals or the  $d - d$  type due to Coulomb interaction [\[13\]](#page-7-0). For spinel  $Co<sub>3</sub>O<sub>4</sub>$  and the isostructural compounds, the determination of the fundamental band gap is more complicated due to the coexistence of local octahedral and tetrahedral networks. For example, the value of the band gap in  $Co<sub>3</sub>O<sub>4</sub>$  is still under debate and remains elusive, which has been reported as 2.2, 1.6, 1.2, or 0.76 eV in literature [\[14–16\]](#page-7-0). Our recent work reported a fundamental band gap of  $\sim 0.8$  eV in Co<sub>3</sub>O<sub>4</sub> epitaxial thin film using combined x-ray spectroscopies, optical spectroscopy and theoretical calculations, which can be ascribed to the tetrahedrally coordinated  $\text{Co}^{2+}$  cations [\[10\]](#page-7-0). Aiming

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for providing a fundamental understanding of the ground-state properties and, in particular, the crystal field splitting of cobalt oxide compounds which is important for clarifying the band gap issue, here we performed configuration interaction (CI) cluster calculations considering Co-O clusters with octahedral and tetrahedral networks, using experimentally measured Co *L*23-edge absorption spectra of perovskite and spinel structures as fingerprints.

Furthermore, accompanying the demand for miniaturization of electronic materials and the fast development of thin-film deposition techniques, transition metal thin films have expanded into a booming field. Strain engineering has been proven as one of the efficient external stimuli in tuning novel electronic properties, which generally can lower the crystal symmetry. We thus performed CI cluster calculations considering a  $CoO<sub>6</sub>$  cluster with tetragonal symmetry to understand the multiplet effects and the ground-state properties. X-ray linear dichroism originating from the spectral difference of different linearly polarized x-ray beams is expected due to the anisotropic electron occupations in different orbitals within the tetragonal crystal field. However, the linear dichroic effect is more complicated for common antiferromagnetic Co-based thin films since here magnetic exchange interaction gives rise to the same linear dichroism as lowering of the crystal symmetry from cubic to tetragonal. The question is how to separate the contributions from magnetic exchange field and tetragonal crystal field as well as to clarify the fundamental ground-state properties. Based on our CI cluster calculations, further temperature- and polarization-dependent absorption measurements have been suggested to distinguish the aforementioned two contributions, as will be presented in detail below.

In this paper, experimentally measured Co  $L_{23}$ -edge absorption spectra have been used as fingerprints to understand the multiplet structures based on CI cluster calculations considering Co-O clusters of different electronic configurations. In the following, we present the simulated absorption spectra at Co  $L_{23}$ -edge for Co  $3d^7$ , Co  $3d^6$ , and Co  $3d^5$  electronic configurations with local octahedral coordination environment in Sec. III A and with tetrahedral symmetry in Sec. [III B.](#page-3-0) From a comparison between the simulated spectrum and the measured absorption spectrum of a specified compound, we can extract the ground-state properties and the crystal field split-ting energy. In Sec. [III C,](#page-3-0) the Co  $L_{23}$ -edge absorption spectra with tetragonal symmetry are calculated, where the natural linear dichroism has been observed due to the anisotropic symmetries of 3*d* orbitals and the strict parity selection rules. We focus on the linear dichroic effect in Sec. [III D](#page-4-0) and show that the magnetic exchange field may bring the same linear dichroism as lowering the crystal symmetry from cubic to tetragonal. Further temperature, and polarization-dependent absorption measurements have been proposed to distinguish both contributions. Finally, the conclusion.

## **II. EXPERIMENTAL AND COMPUTATIONAL DETAILS**

Synchrotron-based transition metal *L*23-edge x-ray absorption measurement is an element-specified method showing strong sensitivity to the ground-state properties such as valence state of transition metal ions, magnetic exchange field, orbital occupations under different symmetries, and crystal field splitting as well as spin-orbit coupling, etc. To have the experimentally measured Co  $L_{23}$ -edge absorption spectra as fingerprints for CI cluster calculations, we grew high quality epitaxial  $ZnCo<sub>2</sub>O<sub>4</sub>$ ,  $CoAl<sub>2</sub>O<sub>4</sub>$ , and  $SrCrO<sub>3</sub>$  thin films by pulsed laser deposition technique. Spinel  $ZnCo<sub>2</sub>O<sub>4</sub>$  and CoAl<sub>2</sub>O<sub>4</sub> thin films with thicknesses of  $\sim$ 30 nm were deposited on  $(001)$ -oriented MgAl<sub>2</sub>O<sub>4</sub> substrates (see Ref. [\[10\]](#page-7-0) for details). The Co *L*23-edge x-ray absorption spectra of  $ZnCo<sub>2</sub>O<sub>4</sub>$  thin films with  $Co<sup>3+</sup> 3d<sup>6</sup>$  in octahedral symmetry as well as  $CoAl<sub>2</sub>O<sub>4</sub>$  with  $Co<sup>2+</sup> 3d<sup>7</sup>$  in tetrahedral symmetry were performed at the soft x-ray beamline, Australian Synchrotron  $[10]$ . High quality epitaxial SrCoO<sub>3</sub> thin film has been deposited on the  $(001)$ -oriented SrTiO<sub>3</sub> substrate with a thickness of ∼10 nm (see Ref. [\[17\]](#page-7-0) for experimental details). The absorption spectrum of  $SrCoO<sub>3</sub>$  thin film with  $Co<sup>4+</sup>$  3 $d<sup>5</sup>$  electronic configuration in octahedral symmetry was measured at beamline 4B9B of the Beijing Synchrotron Radiation Facility [\[17\]](#page-7-0).

However, understanding the transition metal *L*23-edge absorption spectrum is difficult since multiplet effects arising from the overlap between the core state and valence state electron wave functions are important. The transition probabilities calculated by first principles calculations are inadequate for transition metal *L*23-edge absorption spectrum based on a single particle model. Therefore, the theory for CI calculation of a transition metal-oxygen cluster was established years ago, which shows the advantages in providing a quantitative description of *L*23-edge absorption spectrum based on a many-body electron basis. We refer to the literature as well as our previous reports for the backgrounds and details on performing CI cluster calculations [\[18–23\]](#page-7-0). Note that the energy parameters here are calculated by constructing singleparticle molecular orbitals as linear combinations of atomic Hartree-Fock orbitals, rather than the orbitals obtained from *ab initio* band-structure calculations. In this paper, CI cluster calculations considering Co-O clusters of different electronic configurations were performed. The splitting of different energy levels for Co and oxygen ions arranged in octahedral, tetrahedral, and tetragonal networks due to crystal field effects are illustrated in Fig. [1.](#page-2-0) The energy parameters denoting the crystal field splitting are  $\Delta_o$  and  $\Delta_t$  for octahedral and tetrahedral symmetries, respectively. The tetragonal distortion can be modeled by two additional energy parameters, i.e.,  $\Delta_{eg}$  and  $\Delta_{t2g}$ , denoting the energy differences between  $d_{3z^2-r^2}$ and  $d_{x^2-y^2}$ , as well as between  $d_{xz,yz}$  and  $d_{xy}$  levels, respectively. We used  $\Delta_{eg} = 2\Delta_{t2g}$  in the first approximation in the present calculations to account for the anisotropic hybridization strengths between  $e_g$  and  $t_{2g}$  orbitals since the hopping magnitude of  $e_g$ -O 2p orbitals is twice as large as that of the  $t_{2g}$ -O 2*p* orbitals.

## **III. RESULTS AND DISCUSSIONS**

#### **A.** CoO<sub>6</sub> cluster with octahedral symmetry  $(O_h)$

We used the experimentally measured Co  $L_{23}$ -edge absorption spectra of different electronic configurations as fingerprints, i.e., CoO with  $\text{Co}^{2+}$  3*d*<sup>7</sup> [\[24\]](#page-7-0), perovskite EuCoO<sub>3</sub> [\[25\]](#page-7-0) and spinel  $ZnCo<sub>2</sub>O<sub>4</sub>$  compounds with  $Co<sup>3+</sup> 3d<sup>6</sup>$  [\[10\]](#page-7-0), as well

<span id="page-2-0"></span>

FIG. 1. Schematic views of transition metal ion Co surrounded by O ions with (a) octahedral, (b) tetrahedral, and (c) tetragonal symmetry. Illustrations of the corresponding energy level diagram in presence of different crystal field are shown below.  $\Delta_o$  and  $\Delta_i$ represent the energy splitting between  $t_{2g}$  and  $e_g$  orbitals in octahedral and tetrahedral symmetries, respectively. Two energy parameters  $\Delta_{eg}$ and  $\Delta_{t2g}$  have been used to model the tetragonal crystal field effect.

as SrCoO<sub>3</sub> compounds with  $Co<sup>4+</sup> 3d<sup>5</sup>$  electronic configurations [\[17\]](#page-7-0). The features of the measured spectra can be well captured in the simulated spectra shown as bold curves in Figs. 2(a)–2(c) at specific  $\Delta_{\theta}$  values, i.e.,  $\Delta_{\theta} \sim 0.6 \text{ eV}$  for CoO,  $\Delta_0 \sim 0.8 \text{ eV}$  for EuCoO<sub>3</sub> and ZnCo<sub>2</sub>O<sub>4</sub>, and  $\Delta_0 \sim$ 0.6 eV for SrCoO3. These octahedral crystal field splitting



FIG. 2. The calculated isotropic spectra with a variation of  $\Delta_{o}$ within the range between 0 and 2.4 eV from top to bottom, in comparison with the experimental measured Co *L*23-edge absorption spectra for (a)  $\text{Co } 3d^7$  [\[24\]](#page-7-0), (b)  $\text{Co } 3d^6$  [\[10,25\]](#page-7-0), and (c)  $\text{Co } 3d^5$  [\[17\]](#page-7-0). The bold curves denote the spectra showing the best agreement with the experimental spectra at specific  $\Delta_{\rho}$  values. The rest of the energy parameters are shown in Table [I.](#page-3-0) Grey dashed lines are guided for eyes with gradual increase of splitting. Panels (d)–(f) show the corresponding peak splitting  $\Delta E$  versus different  $\Delta_o$  values. The grey dot-dashed line in each panel displays the condition that the peak energy splitting  $\Delta E$  is equal to  $\Delta_o$ .

values are comparable to the results reported in literature from other calculations or experiments [\[10,24,26–28\]](#page-7-0). The rest of the energy parameters are listed in Table [I.](#page-3-0) The Slater parameters used in the present calculations are scaled to 80% of the values for a free ion, taking into account the intraatomic CI inside a solid. For CoO (Co<sup>2+</sup>  $3d^7$  O<sub>h</sub>), similar  $U_{dd}$  and  $\Delta$  values have been reported before [\[13,26,29\]](#page-7-0). The comparable  $U_{dd}$  and  $\Delta$  values imply that the band gap is an intermediate character between the charge-transfer and Mott Hubbard regimes and a dominant 3*d*<sup>7</sup> electronic configuration. The smaller  $\Delta$  value compared to  $U_{dd}$  for  $\text{Co}^{3+}$ in  $EuCoO<sub>3</sub>$  and  $ZnCo<sub>2</sub>O<sub>4</sub>$  compounds suggests that the band gap is of  $p - d$  type, making them charge transfer insulators. Recently, an optical band gap of  $p - d$  charge transfer type was reported by Samanta, using full potential linearized augmented plane wave method based on the density functional theory(DFT) [\[30\]](#page-7-0). In comparison of the best-fitting energy parameters obtained from present calculations as shown in Table [I,](#page-3-0) a decrease of the charge transfer energy value  $\Delta$  as Co going from  $Co^{2+}$  to  $Co^{4+}$  is visible, which is related to the decrease of formal 3*d* electron number and the lowering of the 3*d* orbitals. Potze *et al.* reported comparable energy values in  $SrCoO<sub>3</sub>$  compound in atomic-multiplet calculations  $[28]$ . The SrCoO<sub>3</sub> compound with a negative  $\Delta$  value indicates a strong covalent effect and the ground state is dominant by the ligand hole character with  $3d^6L$  electronic configuration, i.e., the nominal charge state is not  $\text{Co}^{4+}$  but strongly compensated by O 2*p* holes.

CI calculations for  $CoO<sub>6</sub>$  octahedron with cubic symmetry have been performed for different Co electronic configurations with the crystal field  $\Delta$ <sub>o</sub> as the only free parameter. Figures  $2(a)-2(c)$  exhibit the calculated absorption spectra with a variation of the crystal field splitting value  $\Delta_{o}$  from 0 to 2.4 eV at an interval of 0.2 eV from top to bottom spectra. Globally, an expansion of the multiplet structure is suggested as  $\Delta$ <sub>o</sub> increases due to the increased energy splitting between  $t_{2g}$  and  $e_g$  energy levels. At high  $\Delta_o$  values, abrupt changes in the spectra are visible, indicating high-spin to low-spin state transitions. With cubic symmetry, the 3*d* orbitals are split into lower-lying  $t_{2g}$  orbitals with threefold degeneracy and high-lying *eg* orbitals with twofold degeneracy. With small octahedral crystal fields, Co ions favor the occupation of  $t_{2g}$ orbitals. Hund's rule tends to align the spins parallel, leading to the high spin electronic configuration as the ground state. However, for larger  $\Delta$ <sub>o</sub> values, the crystal field exceeds the energy gain of spin pairing, Hund's rule is broken and the spin configuration changes to low-spin. The spin state transition appears at  $\Delta_o \sim 1.8 \text{ eV}$  for Co 3*d*<sup>7</sup>,  $\Delta_o \sim 2.4 \text{ eV}$  for Co 3*d*<sup>6</sup>, and  $\Delta_0 \sim 1.4 \text{ eV}$  for Co  $3d^5$ , considering the full multiplet interactions. We note that the crystal field values appearing in the spin-state transitions are comparable to these proposed in literature, i.e.,  $\Delta_o$  between 1.5 eV to 2 eV for Co 3*d*<sup>7</sup> [\[31\]](#page-7-0),  $\Delta_o$ between 2 eV to 2.5 eV for Co 3*d*<sup>6</sup> [\[31\]](#page-7-0), and  $\Delta_0 \sim 1.2 \text{ eV}$  for  $Co 3d<sup>5</sup>$  in SrCoO<sub>3</sub> compound [\[28\]](#page-7-0).

We further extract the peak splitting  $\Delta E$ , i.e., the energy differences between peaks  $a_1$  and  $a_2$  for Co  $3d^7$ , peaks  $b_1$  and  $b_2$  for Co 3 $d^6$ , peaks  $c_1$  and  $c_2$  for Co 3 $d^5$  at the  $L_3$  edge, versus different  $\Delta$ <sub>o</sub> values, as shown in Figs. 2(d)–2(f).  $\Delta E$  is clearly deviated from the grey dot-dashed line representing the same energy value between the energy splitting at the  $L_3$  edge

<span id="page-3-0"></span>TABLE I. List of the values used for present CI calculations of different electronic configurations, including the  $F_{dd}^2$  and  $F_{dd}^4$  Slater parameters for  $d-d$  interactions, the  $F_{pd}^2$ ,  $G_{pd}^1$  and  $G_{pd}^3$  Slater integrals for  $p-d$  interactions, the  $d-d$  Coulomb interaction  $U_{dd}$ , the attractive interaction  $U_{pd}$  between the core hole and the 3*d* electron, the charge transfer energy  $\Delta$  representing the energy required to move one electron from the ligand to Co 3*d* site, as well as the hopping magnitude expressed in terms of Slater-Koster parameters *pd*σ and *pd*π, with  $p d\sigma / p d\pi = 2.17$  reflecting the anisotropic hybridization strengths. All the values are in unit of eV.

Configuration	$\mathbf{r}_{dd}$			$G_{pd}^1$	$G_{pd}^3$	$U_{dd}$	$U_{pd}$		$pd\sigma$
$Co^{2+}3d^{7}O_{h}$	12.395	7.707	7.259	5.349	3.068	6.5	8.2	6.5	1.2
$Co^{3+}3d^{6}O_{h}$	13.421	8.394	7.899	5.947	3.384	5.5	7.0	2.0	0.5
$\text{Co}^{4+}3d^5O_h$	14.372	9.034	8.544	6.525	3.716	7.5	9.8	$-2.0$	1.2
$Co^{2+}3d^{7}T_{d}$	12.395	7.707	7.259	5.349	3.068	6.5	8.2	4.0	0.5

and crystal field parameter  $\Delta_o$ . The peak splitting  $\Delta E$  shows a monotonic increase as  $\Delta_o$  increases, which can be used as an energy parameter to evaluate the crystal field parameter, but not directly equal to  $\Delta_o$  in magnitude. Crystal field splitting  $\Delta$ <sub>o</sub> exhibits as one of the crucial parameters in determining the optoelectronic properties. From a quantitative comparison of the simulated spectrum to an accurately measured absorption spectrum of a specified compound, one can extract the crystal field strength  $\Delta$ <sub>o</sub> from Co  $L_{23}$ -edge soft x-ray absorption spectrum, which is complementary to the results obtained from optical measurements and provides a benchmark for choosing the proper  $e - e$  Coulomb interaction energy  $U_{dd}$  value in other theoretical calculations [\[32,33\]](#page-8-0).

#### **B.** CoO<sub>4</sub> cluster with tetrahedral symmetry  $(T_d)$

Tetrahedral coordinated Co exists as one of the important structural ingredients in cobalt oxides,e.g., the layered cobaltates family such as  $YBaCo<sub>4</sub>O<sub>7</sub>$  composed of kagome layers of tetrahedrally coordinated Co [\[34\]](#page-8-0) and the Co-based spinel family containing both the tetrahedral and octahedral sites such as  $Co<sub>3</sub>O<sub>4</sub>$  and  $CoAl<sub>2</sub>O<sub>4</sub>$ , etc. [\[10\]](#page-7-0). However, CI calculations only have been intensively studied for  $CoO<sub>6</sub>$  clusters with local octahedral coordination, but much less for the tetrahedral case. CI calculations thus have been performed to exam the influences of tetrahedral crystal field  $\Delta_t$  on the absorption spectra for a CoO<sub>4</sub> cluster with different Co valence states. We have not found the absorption spectra for  $Co<sup>6+</sup>$  and  $Co<sup>5+</sup>$ with local tetrahedral symmetries in literature, to the best of our knowledge. Figure  $3(a)$  shows the experimental measured  $Co L<sub>23</sub>$ -edge absorption spectra for  $Co Al<sub>2</sub>O<sub>4</sub>$  with  $Co 3d<sup>7</sup>$ electronic configuration in tetrahedral symmetry [\[10\]](#page-7-0). Our cluster calculation with the best-fitting energy parameters can reproduce the experimental spectrum well, shown as the bold curve with  $\Delta_t \sim 0.8$  eV in Fig. 3(a). The other parameters are also included in Table I. This tetrahedral crystal field of ∼0.8 eV for CoAl2O4 obtained from Co *L*23-edge absorption spectrum is comparable to the results suggested from optical absorption measurement, as reported in our recent paper [\[10\]](#page-7-0).

Figures  $3(a)-3(c)$  show the calculated absorption spectra at different tetrahedral crystal field splitting values, i.e.,  $\Delta_t$  from 0 to 2.0 eV at an interval of 0.2 eV. Overall, the spectral evolutions  $\cos 3d^7$  and  $\cos 3d^6$  as  $\Delta_t$  increases are similar to the spectra reported by van der Laan. However, their calculated spectra are lacking reproduction of the full multiplet structures since only the transition probability in the form of  $3d^n \rightarrow$  $2p^53d^{n+1}$  has been considered [\[31\]](#page-7-0). For Co 3d<sup>7</sup>, dramatic variations of the spectra have been observed as  $\Delta_t$  increases

from 0 to 1.0 eV. We note that for  $Co3d<sup>7</sup>$ , only one spin configuration  $e_g^2 \uparrow e_g^2 \uparrow t_{2g}^{3\uparrow}$  is allowed and no spin-state transition thus is expected. The multiplet structures are related to the spin-orbit coupling of the  $\overline{\text{Co}}^{2+}$  ions. For Co 3*d*<sup>6</sup> and Co 3*d*<sup>5</sup> with tetrahedral symmetry, the energy parameters used for the absorption spectra calculated for tetrahedral symmetry are the same as these used for octahedral symmetry. The spectra for zero crystal field corresponding to a spherical symmetry are identical for both octahedral and tetrahedral coordination environments. With  $\Delta_t$  increasing, we observe a splitting of the excitation peaks, which are marked as black arrows in Figs.  $3(b)$  and  $3(c)$ , indicative of an enhanced tetrahedral crystal field splitting. We further note that a linear combination of CI simulated spectra with different Co valence states in octahedral and tetrahedral symmetries can be used to capture the experimental absorption spectrum of a spinel structure with integer and even with mixed valence states in both octahedral and tetrahedral sites [\[35\]](#page-8-0). This is favorable since depending on the material synthesis conditions, spinel Co oxide with mixed valence states is common in practical cases, which determines the multifunctional physical behaviors and applications.

#### **C. CoO6 with tetragonal symmetry**

In this section, we further consider the CI calculated spectra for  $CoO<sub>6</sub>$  under a local tetragonal symmetry for Co ions of



FIG. 3. The calculated isotropic spectra with a variation of tetrahedral crystal field  $\Delta_t$  between 0 and 2 eV from top to bottom for (a)  $\cos 3d^7$ , (b)  $\cos 3d^6$  and (c)  $\cos 3d^5$  electronic configurations. The rest of the energy parameters are listed in Table I. The experimental measured Co *L*<sub>23</sub>-edge absorption spectrum for CoAl<sub>2</sub>O<sub>4</sub> with Co 3*d*<sup>7</sup> in tetrahedral symmetry [\[10\]](#page-7-0) was used as a fingerprint for calculations. The bold curve in panel (a) represents the spectrum with the best reproduce of the experimental spectrum with  $\Delta_t \sim 0.8 \text{ eV}$ .

<span id="page-4-0"></span>

FIG. 4. The calculated Co  $L_{23}$ -edge absorption spectra for  $E \perp c$ and  $E \parallel c$  incoming photon polarizations at different crystal field splitting values, i.e.,  $\Delta_{t2g}$  of 240 meV, 120 meV, 60 meV, 0 meV, −60 meV, −120 meV, and −240 meV from top to bottom spectra, for (a)  $\text{Co } 3d^7$ , (b)  $\text{Co } 3d^6$ , and (c)  $\text{Co } 3d^5$  electronic configurations, respectively. Panels (e) and (f) show the corresponding linear dichroic spectra, i.e.,  $(XAS_{E\perp c} - XAS_{E\parallel c})$  at different  $\Delta_{t2g}$  values.

different electronic configurations. A lowering of the crystal symmetry from cubic to tetragonal is particularly useful for strain engineering of functional oxide thin films, which has been verified as an effective approach to tailor the electronic properties in strongly correlated transition metal oxide thin films  $[36-38]$ . For CoO<sub>6</sub> coordination complex under tetragonal symmetry, the  $e_g(t_{2g})$  manifold further splits into  $d_{x^2-y^2}$ and  $d_{3z^2-r^2}$  ( $d_{xz}$ ,  $d_{yz}$  and  $d_{xy}$ ) orbitals. In responses of the different in-plane stress, reorientations of the spin direction and orbital momentum may appear [\[39,40\]](#page-8-0). Due to the anisotropic nature of the orbitals, the selection rules restrict the dipole allowed transition in certain manners. X-ray linear dichroism, i.e., the probe of the solid with different linearly polarized electromagnetic waves, shows the sensitivity to the orbitals of the transition metal ion under different local symmetries, the corresponding orbital occupations and the orbital response to lattice variations for a particular ion.

To model the crystal field effect under tetragonal symmetry, three parameters, i.e.,  $\Delta_o$ ,  $\Delta_{eg}$  and  $\Delta_{t2g}$ , are necessary as shown in Fig.  $1(c)$ . For the energy difference between  $t_{2g}$  and  $e_g$  levels, we used the optimized  $\Delta_o$  values, i.e.,  $\Delta_{\rho} = 0.6$  eV for Co 3*d*<sup>7</sup> in CoO,  $\Delta_{\rho} = 0.8$  eV for Co 3*d*<sup>6</sup> in ZnCo<sub>2</sub>O<sub>4</sub>, and  $\Delta_0 = 0.6$  eV for Co 3*d*<sup>5</sup> in SrCoO<sub>3</sub>. And we use  $\Delta_{eg}$   $(E_{d3z^2-r^2} - E_{dx^2-y^2}) = 2\Delta_{t2g}(E_{dxz,yz} - E_{dxy})$  to parametrize the tetragonal crystal field in the first approximation. Figures  $4(a)$ – $4(c)$  display the simulated spectra at different  $\Delta_{t2g}$  values ranging from  $-240$  meV to 240 meV with light polarization parallel  $(E \parallel c)$  and perpendicular  $(E \perp c)$  to the crystal *c* axis. Firstly, the simulated spectra show a polarization dependence for  $\Delta_{t2g} \neq 0$ , indicating a nature linear dichroism. As the crystal field  $\Delta_{t2g}$  increases, the dichroic effect which is defined as the difference between the absorption spectra calculated for  $E \parallel c$  and  $E \perp c$  polarizations increases for both positive and negative  $\Delta_{t2g}$  values, as shown in Figs.  $4(e) - 4(g)$ . The signs are opposite between positive and negative tetragonal crystal fields for  $CoO<sub>6</sub>$  with all three electronic configurations, reflecting perfectly the opposite strain imposed on the corresponding thin films, which, however, are not interchangeable simply by reversing their respective signs due to the orbital symmetry and the multiplet effects.

A comparison of the excitation peak for different linear polarizations reflects the electronic configuration of Co ions. For  $\text{Co } 3d^7$ , only one hole exists in the  $t_{2g}$  energy level considering the high spin configuration with  $\Delta_{\rho} = 0.6 \text{ eV}$ . The first excitation peak  $p_1$  corresponds to the transition from  $2p$  core level to the lowest empty states of  $t_{2g}$  orbitals in the one-electron picture. The hole in  $t_{2g}$  shell can be either in  $d_{xy}$  or  $d_{xz,yz}$  orbitals, the first excitation peak  $p_1$  thus shows strong sensitivity for different photon polarizations. With  $\Delta_{t2g} = -240$  meV, a large peak intensity is observed for  $E \perp c$  whereas little peak appears for  $E \parallel c$  polarization. With  $\Delta_{t2g} = 240 \,\text{meV}$ , opposite behavior exists with a large peak intensity for  $E \parallel c$  polarized incoming wave. With a negative tetragonal crystal field effect ( $\Delta_{t2g} < 0$ ), the  $t_{2g}$  orbitals split to low-lying  $d_{xz,yz}$  and high-lying  $d_{xy}$  energy levels where the former is fully occupied, leaving only the excitation probability for the high-lying  $d_{xy}$  orbitals. Due to the parity selection rule, the transition to  $d_{xy}$  orbital with  $E \parallel c$  photon polarization is forbidden, corresponding to the diminishing excitation peak  $p_1$  intensity for  $E \parallel c$  polarized light. In a similar way, unpopulated states only exist in high-lying *dxz*,*yz* orbitals for  $\Delta_{t2g} > 0$ . Peak  $p_1$  intensity almost vanished for  $E \perp c$  polarized light. The disappearance of the first excitation peak  $p_1$  in response to different incoming photon polarizations is gradual and increases as the crystal field varies. This can be attributed to the spin-orbit coupling which prefers a spherical charge distribution. Otherwise an abrupt change as  $\Delta_{t2g}$  switches on is expected if one neglects the spin-orbit coupling. In a similar way, we can understand the changing of the peak intensities with different linear polarizations and the opposite responses of the linear dichroism with opposite tetragonal crystal fields for  $CoO<sub>6</sub>$  with  $3d<sup>6</sup>$  and  $3d<sup>5</sup>$  electronic configurations, respectively.

## **D. X-ray linear dichroism and temperature dependent absorption spectra**

Besides the splitting of the energy levels with different tetragonal crystal fields that cause the linear dichroic effect, magnetic ordering and exchange field can also give rise to linear dichorism. One of the unique characterization of cobalt oxides is the spin degree of freedom, which is distinctive from other 3*d* transition metal oxides. The magnetic exchange field thus usually needs to be included in cobalt oxides. Figures  $5(a)$ – $5(c)$  show the absorption spectra simulated for  $CoO<sub>6</sub>$  3*d*<sup>7</sup>, Co 3*d*<sup>6</sup>, and Co 3*d*<sup>5</sup> electronic configurations under cubic symmetry with different linear photon polarizations at an exchange field from 0 meV to 50 meV along out-ofplane direction (crystal *c* axis). We note that the magnitude of exchange field up to 50 meV considered here covers the exchange field for CoO with  $3d^7$  [\[41,42\]](#page-8-0), EuCoO<sub>3</sub> and LaCoO<sub>3</sub> with  $3d^6$  [\[2\]](#page-7-0), and SrCoO<sub>3</sub> with  $3d^5$  [\[43\]](#page-8-0) at 0 K in literature. As the exchange field switches on, a linear dichorism is clearly visible. With an applied exchange field, both the initial state electron occupation in different orbitals and the final state vary. We note that the linear dichoric spectra for  $E \perp c$  and  $E \parallel c$  incoming photon polarizations are similar to that originating from positive tetragonal crystal field effects shown in

<span id="page-5-0"></span>

FIG. 5. The calculated Co  $L_{23}$ -edge absorption spectra for  $E \perp c$ and  $E \parallel c$  incoming photon polarizations at 0 K with different exchange field values, i.e., 0 meV, 10 meV, 20 meV, 30 meV, 40 meV, and 50 meV from bottom to top spectra, for (a)  $\cos 3d^7$ , (b)  $\cos 3d^6$ , and (c)  $\text{Co } 3d^5$  electronic configurations.

Fig. [4.](#page-4-0) This is because applying an exchange field along the out-of-plane direction favors a preferred orbital momentum along the same direction due to spin-orbit coupling. Taking  $\cos 3d^7$  as an example, only one unpopulated state exists in the  $d_{xz,yz}$  orbital level which allows a large intensity with *E*  $\parallel$  *c* polarized light due to the spin-orbit coupling, whereas the *dxy* orbital is fully occupied, leaving no transition probability for dipole-allowed transition with  $E \perp c$ . Therefore, the electronic configuration is the same as positive tetragonal crystal field effect with a lower energy of the  $d_{xy}$  orbtial and a high energy for  $d_{xz,yz}$  orbitals. As the exchange field increases, the linear dichroism increases for  $\text{Co} 3d^7$ . When the exchange field is above the threshold of 30 meV, the linear dichroism varies negligibly. The threshold exchange filed values below are 20 meV and 10 meV for Co  $3d^6$  and Co  $3d^5$ , respectively.

As suggested in Figs. [4](#page-4-0) and 5, x-ray linear dichroism shows similar changes due to tetragonal crystal field and magnetic exchange field effect which brings difficulties to explore the underlying mechanism. The question would be how to distinguish them, for which we performed temperature-dependent simulations for  $CoO<sub>6</sub>$  clusters with different electronic configurations. The effect of temperature as an external parameter has been considered in present CI cluster calculations through adding the Boltzmann statistics for the state populations; for details we refer to the papers by Haverkort *et al.* [\[20\]](#page-7-0), Tanaka and Jo [\[29\]](#page-7-0), and our previous calculations [\[21](#page-7-0)[,44\]](#page-8-0).

Figure 6 shows the temperature-dependent  $Co L_3$ -edge isotropic spectra and the absorption spectra for  $E \perp c$  and  $E \parallel c$  incoming photon polarizations in the presence of either tetragonal crystal field or magnetic exchange field for  $Co 3d<sup>7</sup>$ . The simulated isotropic spectra exhibit negligible temperature dependence at different magnetic exchange fields [Fig.  $6(a)$ ] and tetragonal crystal fields [Fig.  $6(b)$ ]. However, the polarization-dependent absorption spectra show spectral variations as temperature changes. Figures  $6(c)$ – $6(e)$  show the polarization-dependent simulated spectra at different temperatures, i.e., 20 K, 50 K, 100 K, 150 K, 200 K, and 300 K for magnetic exchange fields  $H_{ex} = 10 \,\text{meV}$ , 20 meV, and 30 meV, respectively. As temperature rises, the first excitation peak  $p_1$  becomes lower for  $E \parallel c$  polarization whereas the intensity of peak  $p_1$  decreases for  $E \perp c$  polarization. The temperature here includes two contributions, i.e., the thermal effects which influence the electronic population as temperature increases following the Boltzmann statistics, and the correlated effects due to magnetic exchange interactions or tetragonal lattice distortions. We note that the polarizationdependent simulated spectra with tetragonal crystal field show small changes as temperature varies, as shown in Figs.  $6(f)$ –6(h). Therefore, the polarization-dependent variations in Figs.  $6(c)$ –6(e) are mainly contributed by the magnetic exchange field rather than the tetragonal lattice distortion or the thermal effects.

The simulated spectra for  $CoO<sub>6</sub>$  with  $Co3d<sup>6</sup>$  electronic configuration show different temperature dependence as temperature varies. As shown in Figs.  $7(a)$  and  $7(b)$ , the isotropic spectra show small temperature-dependent changes at different exchange fields, whereas the isotropic spectra show strong



FIG. 6. Temperature-dependent variations of the absorption spectra at  $\text{Co } L_3$  edge with  $\text{Co } 3d^7$  electronic configuration. Panel (a) shows the temperature-dependent isotropic spectra for 10 meV, 20 meV, and 30 meV magnetic exchange field. Panel (b) exhibits the temperaturedependent isotropic spectra for tetragonal symmetry with  $\Delta_{t2g} = 60$  meV, 120 meV, and 240 meV. Panels (c)–(h) show the temperaturedependent absorption spectra for both  $E \parallel c$  and  $E \perp c$  incoming photon polarizations in presence of either magnetic exchange fields with  $H_{\text{ex}} = 10 \text{ meV}$ , 20 meV, and 30 meV or tetragonal crystal fields with  $\Delta_{t2g} = 60 \text{ meV}$ , 120 meV, and 240 meV, respectively.

<span id="page-6-0"></span>

FIG. 7. Panels (a) and (b) show the temperature-dependent isotropic spectra of CoO<sub>6</sub> with Co 3d<sup>6</sup> electronic configuration for different magnetic exchange fields and tetragonal crystal fields, respectively. Panels (c)–(h) show the temperature-dependent absorption spectra for both *E*  $\parallel$  *c* and *E*  $\perp$  *c* polarizations in presence of either magnetic exchange field or tetragonal crystal field, as labeled in the corresponding panel.

spectral variations at different temperatures in the presence of tetragonal crystal fields. Therefore, temperature-dependent absorption measurements will separate the contribution from tetragonal field from magnetic exchange field. The small temperature dependence of  $\text{Co } 3d^6$  with different external  $H_{ex}$ suggests that the thermal effect is not dominant here. The simulated spectral variations in Figs.  $7(f)$ – $7(h)$  are mainly contributed by the modification of the ground and final states at different temperatures due to the tetragonal crystal fields. Further polarization-dependent simulations reveal that the temperature-dependent isotropic spectra at different  $\Delta_{i2g}$  = 60 meV, 120 meV, and 240 meV mainly originate from the temperature-dependent variations of  $E \perp c$  incoming photon polarization.

The simulated spectra for  $CoO<sub>6</sub>$  with  $Co3d<sup>5</sup>$  electronic configuration show similar spectral variations as  $CoO<sub>6</sub>$ with  $3d^7$  electronic configuration, i.e., the isotropic spectra show negligible temperature dependence, as shown in Figs. 8(a) and 8(b). Moreover, the polarization-dependent absorption spectra exhibit strong temperature dependence for  $H_{\text{ex}} = 10$  meV, 20 meV, and 30 meV, as shown in Figs.  $8(c) - 8(e)$ . Overall, temperature- and polarizationdependent absorption measurements can be used to separate

the contributions between tetragonal crystal field and magnetic exchange field as well as to understand the ground-state properties.

## **IV. CONCLUSIONS**

In summary, we have grown high-quality epitaxial  $ZnCo<sub>2</sub>O<sub>4</sub>$ ,  $CoAl<sub>2</sub>O<sub>4</sub>$ , and  $SrCrO<sub>3</sub>$  thin films by pulsed laser deposition technique. Using experimentally measured Co *L*23 edge absorption spectra as fingerprints, we carried out CI cluster calculations for Co and oxygen ions with local octahedral, tetrahedral, and tetragonal coordination environments. Crystal field splitting between the twofold *eg* orbitals and the threefold  $t_{2g}$  orbitals exhibits as one of the crucial parameters in determining the optoelectronic properties. Here, we focus on the detailed spectral variations with different octahedral crystal field  $\Delta_o$  and tetrahedral crystal field  $\Delta_t$ . The crystal field of a specified compound can be extracted from our simulations, which is important for understanding ground-state properties and is complementary to the results obtained in optical measurements as well as in other calculations. We notice that CI calculations have been intensively studied for  $CoO<sub>6</sub>$  clusters with local octahedral coordination, but much



FIG. 8. Panels (a) and (b) show the temperature-dependent isotropic spectra of Co  $3d^5$  at different magnetic exchange fields and different tetragonal crystal fields, respectively. Panels (c)–(h) show the temperature-dependent absorption spectra for both  $E \parallel c$  and  $E \perp c$  polarizations with the specified magnetic exchange or tetragonal crystal field in the corresponding panel.

<span id="page-7-0"></span>less for the tetrahedral case in literature. Through a linear combination of the CI simulated spectra with different valences and symmetries, the features of an experimentally measured spectrum of a spinel structure can be well captured. It can work properly for both integer and mixed valence state systems, which is favorable to understand the ground-state properties as well as to explore their multifunctional physical behaviors.

Later, the simulated spectra for  $CoO<sub>6</sub>$  clusters in tetragonal symmetry with different incoming photon polarizations revealed the natural linear dichroism. We further showed that the magnetic exchange field can also give rise to linear dichroism, which is necessary to be considered for Co ions with partially filled 3*d* shell and different possible spin states. To separate both contributions, we proposed detailed temperature- and polarization-dependent measurements, which show different spectral variations due to the specified modifications of the ground and final states at different temperatures. Our results offer theoretical guidance for understanding the multiplet structure at  $Co L_{23}$ -edge absorption spectra, obtaining the representative energy parameters for comparisons with other measurements or calculations, extracting the precise crystal field for Co oxides with versatile coordinations which determines the optoelectronic applications, and explaining the underlying mechanism of linear dichroism in cobalt oxides and their thin films.

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