Observation of a molecular muonium polaron and its application to probing magnetic and electronic states

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Muonium is a combination of first- and second-generation matter formed by the electrostatic interaction between an electron and an antimuon (μ^+). Although a well-known physical system, their ability to form collective excitations in molecules had not been observed. Here, we give evidence for the detection of a muonium state that propagates in a molecular semiconductor lattice via thermally activated dynamics: a muonium polaron. By measuring the temperature dependence of the depolarization of the muonium state in C_{60}, we observe a thermal narrowing of the hyperfine distribution that we attribute to the dynamics of the muonium between molecular sites. As a result of the time scale for muonium decay, the energies involved, charge and spin selectivity, this quasiparticle is a widely applicable experimental tool. It is an excellent probe of emerging electronic, dynamic, and magnetic states at interfaces and in low dimensional systems, where direct spatial probing is an experimental challenge owing to the buried interface, nanoscale elements providing the functionality localization and small magnitude of the effects.

I. INTRODUCTION

The ability to map in a multilayered thin film electronic, vibrational and spin order in thin films is key to many chemical, engineering and physical applications, in particular for compounds involving nanocarbon and molecular materials [1,2]. Yet, the direct spatial probing of spin ordering and electronic properties is an experimental challenge, owing to the nm-scale localization and small magnitude of the effects. Magnetic proximity, spin accumulation and spontaneous spin order in non-magnetic metals can lead to localized magnetic phenomena that are at the lower limit of sensitivity of laboratory-based and synchrotron magnetometry techniques [3–6]. Mapping charge distribution is also an essential challenge to, e.g., solid-state (thin-film) batteries and fullerene hybrid photovoltaics [7,8]. In the past, bulk muon spin rotation (μSR) has been used extensively to study various properties of the fullerenes including, but not limited to: rotational dynamics [9,10], superconducting properties of the alkali-doped fullerene complexes [11], and spin ordering in the TDAE-C_{60} charge-transfer complex [12].

Low-energy muon spin rotation (LE-μSR) is also a powerful tool in characterizing interfacial and thin film spin phenomena for a multitude of systems [13–16]. Here, LE-μSR is used first to show the presence of low frequency endohedral muonium in C_{60}, coupled to the vibrational states of the molecule at all temperatures. The depolarization of this state is linked to the dynamics of the molecular cages, as two distinct dynamical phases can be seen in the temperature dependence of this state. This muonium polaron is a highly sensitive probe to local electronic, vibrational and spin states. Here, we use it to probe changes in electron density at metal interfaces and emergent magnetism down to $\sim$10s of μT via Zeeman splitting of the hyperfine interaction. The principle for this probing technique is shown in Fig. 1(a).

II. METHODS

For all measured samples, metal films were deposited by DC magnetron sputtering and C_{60} films were sublimated in a high vacuum system with a 10^{-8} mbar base pressure. Sputtering was undertaken in a 3.3×10^{-3} mbar Ar atmosphere at ambient temperature unless otherwise specified. The growth rate of each material was calibrated against samples

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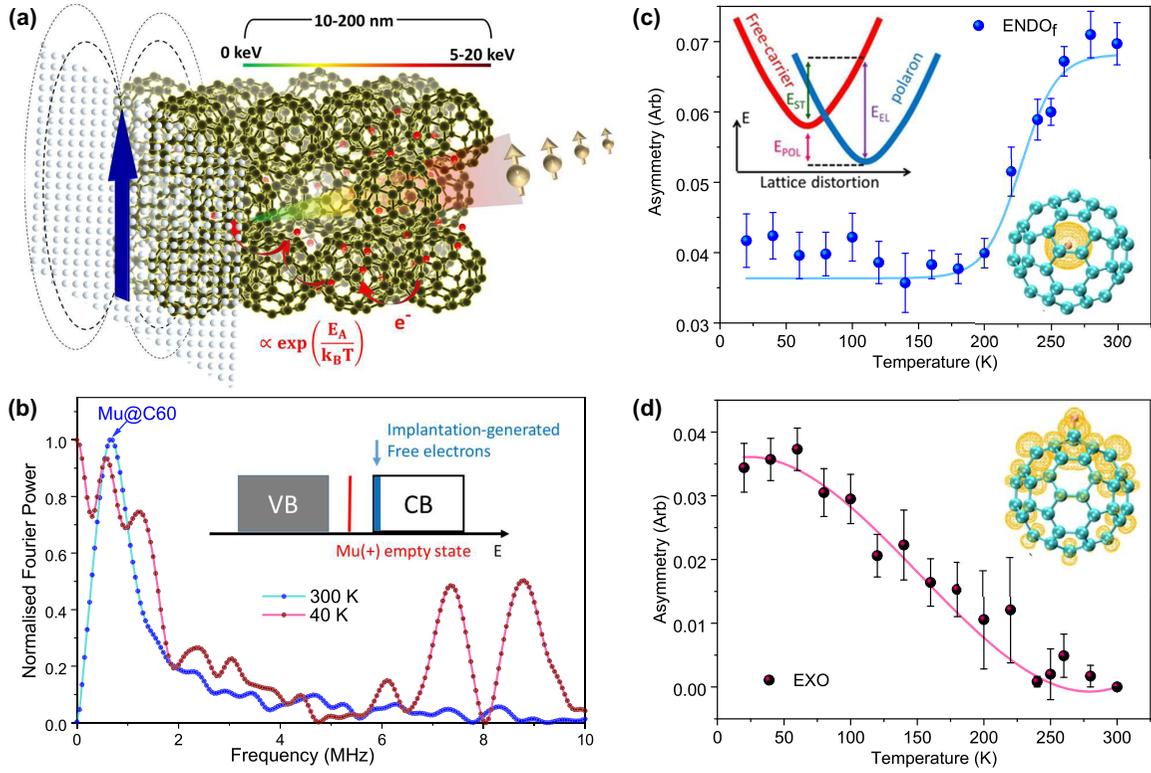
FIG. 1. (a) Schematic of the $ENDO_f$ formation via ionization, charge hopping, and trapping then coupled with molecular rotations. Its oscillation frequency is sensitive to, e.g., the electron transfer and emergent magnetism at interfaces. (b) Fourier transform of the time domain asymmetry data at ZF for a 210-nm- thick amorphous C_{60} film on a thermally oxidized Si substrate. The EXO muonium at 1.2, 7.4, and 8.6 MHz is observable at 40 K. At 300 K, only the $ENDO_f$ muonium is observed. Inset: (∼keV) muon-beam generated free carriers remain delocalized in the conduction band (CB) of the C_{60} film, leaving the e-acceptor state of the μ^+ empty. (c) The temperature dependence of the asymmetry attributed to the low-frequency $ENDO_f$ together with the calculated spin-density using the PBE exchange-correlation (XC) functional (yellow: $10^{-6}\,\mu_B\,\text{Å}^{-3}$). A semiempirical model has been used to fit the temperature dependence leading to an activation energy (equivalent to $-E_{POL}$) for $ENDO_f$ of $E_A = 300 \pm 100$ meV [30]. (d) Temperature dependence of the EXO signal fraction, also with the calculated PBE spin-density (yellow: $10^{-6}\,\mu_B\,\text{Å}^{-3}$). The EXO state becomes more apparent as we cool the system through the glass transition and the molecular rotations are frozen.

grown in the same vacuum cycle whose thickness was determined via the fitting of Kiessig fringes produced by x-ray reflectivity measurements.

LE-μSR measurements were performed on the μE4 beamline at the Paul Scherrer Institute, where a moderator technique allows for the implantation energy of nearly 100% spin polarized epithermal muons to be tuned via an acceleration electric field [17,18]. Thus, low-energy muons allow for the depth profile of magnetic texture to be obtained. The energies required to probe the Cu/C_{60} were determined through the use of Monte Carlo simulations performed within TRIM.SP software [19]. The muon is an unstable spin ½ particle with charge $+e$ and a lifetime of $\tau_\mu \sim 2.2\,\mu$s. Following implantation, the muon will rapidly thermalize. In a system which lacks sufficient carrier concentration to screen the μ^+ charge, such as insulating and semiconducting systems, the muon is expected to generate a hydrogenlike bound state known as muonium (Mu = μ^+e^-). In a metallic system, one would observe the Larmour spin precession of the μ^+ particle about a local field B_{loc}. In a system where the muonium formation dominates the signal, we directly probe transitions between spin configurations of the μ^+ and e^- spin, governed by the Hamiltonian which describes the hyperfine interaction. This

is given, in terms of angular frequency, as

$$\frac{H_{HF}}{\hbar} = -\gamma_\mu S^\mu \cdot B + \gamma_e S^e \cdot B + S^\mu \cdot A \cdot S^e, \quad (1)$$

where S^μ and S^e are the respective muon and electron spin operators, γ_μ and γ_e are the gyromagnetic ratios for the electron and muon, A is the hyperfine coupling tensor, and B is the magnetic field [20,35]. For an isotropic hyperfine tensor ($A_{xx} = A_{yy} = A_{zz}$), two states exist in zero-field: a singlet and a degenerate triplet state. The application of a magnetic field lifts the degeneracy of the triplet state and then transitions between energy levels can be observed as an oscillation frequency ν_{ij} which is equal to the splitting between energy levels $(E_i - E_j)/\hbar$. The splitting between the ZF states is equal to the hyperfine coupling constant $A_H = 2\pi \times 4463$ MHz. This frequency would be unobservable in a typical μSR experiment. Therefore, it is expected that no oscillation should be observed in the isotropic hyperfine case. If, however, some axial anisotropy is introduced into the hyperfine tensor, the degeneracy of the triplet state is lifted and a single frequency can now be expected in the absence of magnetic field. The μSR data were analyzed using the program MUSRFIT [21,41].

III. OBSERVATION OF THE FLOATING ENDOHEDRAL MUONIUM POLARON IN C_{60} (ENDO$_f$)

The zero-field (ZF) muonium oscillation data for an amorphous, thick ($\sim$200 nm) C_{60} film has been fitted using a multiple frequency model, where an individual precession frequency ν_i has a contribution to the muon polarization, $P(t)$, given by

$$P(t) = \sum_{i=1}^{4} A_i \cos\left(2\pi \nu_i t\right) e^{(-\lambda_i t)}, \qquad (2)$$

where λ_i is the depolarization rate of the oscillating muonium. The asymmetry, A_i, is then the fraction of signal attributed to a given oscillation; see the Supplemental Material [22].

At room temperature, C_{60} crystals form a face-centered-cubic (fcc) structure where the individual molecules are orientationally disordered and freely rotate between degenerate configurations via a ratcheting mechanism [23]. Below 260 K, C_{60} molecules lose two rotational degrees of freedom. Due to inequivalent molecular orientations on the Bravais sites of the fcc lattice, crystalline C_{60} undergoes a first-order phase transition to a simple cubic structure. Below $\sim$120 K, the time scale of the molecular rotation (τ_r) is longer than the measurement time scale for μSR ($\tau_m \sim 2.2\,\mu$s), and the rotational degrees of freedom appear frozen [24,25]. As shown in Fig. 1(b), at low temperatures, oscillations at 1.2, 7.4, and 8.6 MHz are visible. These frequencies are well understood and are attributed to the completely anisotropic hyperfine interaction of the exohedral radical muonium state (EXO) [26,27], but can only be detected when $\tau_r > \tau_m$.

In addition to the MuC$_{60}$ radical precession, we observe an additional low-frequency precession that persists up to room temperature. This room-temperature oscillation has not been reported in the various studies of bulk crystalline C_{60} [27,28]. However, it is seen in all the thin fullerene films grown throughout this study, with stronger signals in the more disordered films. This high temperature muonium state has been shown to be sensitive to magnetic surface states [3,4]. The presence of the sub-MHz oscillation infers some intrinsic distortion of the fullerene cages and a precession decoupled from the molecular dynamics. Density functional theory (DFT) simulations of muon and muonium species in different crystalline C_{60} films [22], identifies the endohedral muonium polaron (ENDO$_f$) state as the energetically most favored product of electron trapping at μ^+ sites in the presence of free-carriers in the conduction band of the C_{60} film ([22] Fig. S13 and Table S5), as produced by the μ^+ keV implantation. This polaronic state, with a formation energy of about -0.72 eV, is characterized by a floating geometry for the μ^+ inside the C_{60} (ENDO$_f$), slightly offset from the center of mass of the C_{60} and at a distance of $\sim$3 Å from the closest C-atom ([22] Fig. S7). As shown by the absence of μ^+-C stretching vibrational modes (Table S3), this geometry presents no chemical bonding between muonium and C_{60}, leading to an electron spin-density localized around the μ^+ sites ([22] Fig. S11).

The low-frequency oscillation is due to an axially symmetric hyperfine interaction for ENDO$_f$. Its frequency depends on film quality, charge state and the local magnetic field. It varies between 0.1 MHz for a highly crystalline, pristine and de-

gaussed system, to 0.8 MHz for an amorphous, non-degaussed and/or charged film, e.g., at metallic interfaces. This is in good agreement with the predicted value of $\sim$0.45 MHz for a system with 25% C_{60} vacancies (see Table S7 [22]). Experimentally, the formation energy of the ENDO$_f$ polaron is 300 ± 100 meV [Figs. 1(c)–1(d)]. This is a factor two smaller than in the calculations (Table S5 [22]). The difference is probably due to impurities and defects up to 0.9 eV above the top of the valance band [29], limitations in the simulations and the overestimated concentration of μ^+ in simulations with respect to the experiment, where only one μ^+ is present in the $\sim$$10^{-4}$ cm^3 sample at a time. The overestimated concentration induces unscreened, artificial electrostatic (multipolar) interactions between periodic replicas of the simulation cell that in turn overstabilize the polaronic solution with respect to the delocalized state [Fig. 1(c)].

IV. DYNAMICS OF THE ENDO$_f$ MUONIUM POLARON

Molecules in C_{60} films undergo a glass transition at $T_g \sim$ 120 K. Below this temperature, the rotational degrees of freedom for the fullerene cages are completely frozen. Above T_g, a uniaxial ratcheting mechanism between different molecular orientations takes place until around 260 K, where the cages undergo continuous rotational diffusion [31]. Additionally, Born-Oppenheimer, DFT molecular dynamics (BOMD) simulations of different endohedral and exohedral μ^+ and muonium species confirm the ENDO$_f$ state as the only system uncorrelated to the C_{60} rotational dynamics. This makes ENDO$_f$ the only detectable oscillation at 250 K, regardless of the C_{60} free rotation. Path integral MD (PIMD) simulations of the ENDO$_f$ state at 50 and 300 K confirm its localization around, but not exactly at, the center of mass of the C_{60}. There is no quantum tunneling through the C_{60} cage observed during the (finite) timespan of the simulations [Fig. 2(c)].

The depolarization rate λ of the low-frequency oscillation was studied as a function of temperature T. We assume Arrhenius dynamics, with a decoherence period τ such that [32]

$$\lambda \sim \frac{1}{\tau} = A e^{\frac{E_A}{k_B T}}, \qquad (3)$$

where E_A is the activation energy, k_B is the Boltzmanns constant, and A is a fitting factor. Although the ENDO$_f$ state appears decoupled from the molecular rotations in the ps scale [see Figs. 2(a)–2(c)], we expect some effect of the ratcheting on the muonium spin direction over the longer decay time scale of 2.2 μs. The dynamics may have an effect in the temperature-dependent slowing of the decoherence.

The spin depolarization of the ENDO$_f$ polaron state undergoes thermal changes with characteristic activation energies of the order of 15 meV above T_g and 1 meV below T_g [Fig. 2(d)]. This observation resembles the temperature dependent, motional line-narrowing experienced in NMR experiments, where the increased motion of a sampling environment due to molecular dynamics causes areas of varying magnetic field to become more homogeneous, reducing the depolarization of the nuclear spin [33,34]. The depolarization above T_g is therefore conditioned by the molecular rotations. Below T_g, the activation energy corresponds to the dynamic barrier for the movement and rotation of the muonium in-

FIG. 2. Muonium dynamics and activation energies. (a) Time evolution of the Mu- and C- rotational dynamics in ENDO$_f$, as calculated by the angles between the instantaneous Mu (closest C-atom) radial distance from the C$_{60}$'s center of mass and the x(θ_x), y(θ_y) and z(θ_z) axes. The C-trace reports the rotational evolution of the C-atom closest ($\sim$3 Å) to the Mu at the start of the BOMD trajectory. (b) As in a, but for the EXO muonium state. The C-atom closest to the Mu does not change during the whole BOMD trajectory. Note that for the ENDO$_f$ state the dynamics of molecule and muonium are decoupled, whereas in the EXO state the muonium follows the molecular rotation. (c) *Ab initio* path integral molecular dynamics (AI-PIMD) distribution of the muon particle in the ENDO$_f$ at 50 and 300 K. For each of the 16 beads used in the simulations, 1000 frames (2 fs apart) were extracted from the production run and superimposed in the same image. The initial position of the C$_{60}$ is used to provide a better visualization of the quantum spread of the muonium inside the molecule. C: cyan, Mu: pink. (d) Temperature dependence of the depolarization rate associated with ENDO$_f$ state, showing the two thermal activation regimes above (red line fit) and below (blue) the glass transition T$_g$.

V. LOW MAGNETIC FIELD DETECTION IN A CRYSTALLINE SAMPLE

The dependence of the muonium hyperfine transition frequency with a magnetic field was studied using a crystalline C$_{60}$ film grown at a substrate temperature of 473 K onto a [110] oriented Nb layer sputtered at 1073 K onto *c*-plane Al$_2$O$_3$ x-ray diffraction spectrum in Fig. S1. When comparing the crystalline C$_{60}$ to the disordered film grown on SiO$_2$ at room temperature, we note that muonium formation is 30% of the implanted muons, demonstrating the diamagnetic behavior of the uncoupled μ^+ particle. The difference suggests a role of the molecular crystal structure to the formation of the muonium polaron, as observed in the calculated vibrational density of states of C$_{60}$ for crystalline and disordered films. This probably explains the discrepancy between these measurements and past studies on fullerite single crystals. Figures 3 and

Fig. S3 [22] demonstrate that at 250 K, in fields up to 8 G, there is only a single frequency line, increasing linearly at 1.402 $\pm$ 0.003 MHz G^{-1} [35]. This is in line with the standard theoretical predictions for a strongly coupled muon-electron system. Simultaneously, there is axial anisotropy leading to a zero-field frequency of 0.50 $\pm$ 0.02 MHz. At 20 K, ν_{ZF} reduces to 0.15 $\pm$ 0.03 MHz with the slope reducing to 0.74 $\pm$ 0.05 MHz G^{-1} [Fig. 3(b)]. This slope cannot be explained by a simple strong coupling approximation, which predicts the behavior seen in Fig. 3(a). It appears instead in the case of isotropic coupling on the same order of magnitude as the applied field, which suggests a small Fermi contact term for this site; see the Supplemental Material for further detail [22].

VI. PROBING EMERGENT LOCAL MOMENTS AND ELECTRONIC STATES AT METALLOMOLECULAR HETEROSTRUCTURES

We use the ENDO$_f$ state to detect small spin-electronic changes at a metallomolecular interface. The sample structure is [Si(Sub)/Ta(3)/Cu(5)/C$_{60}$(114)/Cu(5)/Au(14)], where

FIG. 3. The magnetic field dependence of the ENDO_f and EXO muonium oscillation frequencies as measured in the crystalline sample. (a) Observed experimental frequencies (circles) vs simulations (color map) for ENDO_f at 250 K. (b) 20 K experiments (circles) and simulations (color map) for the ENDO_f state, modeled with a hyperfine isotropic coupling $A_{\text{iso}} = 9.65\,\text{MHz}$. (c) Observed experimental frequencies (circles, squares, and triangles) vs simulated intensities (color map) for the EXO state. The dipolar part of the tensor was chosen to match the observations at zero field and the Fermi contact term is in the high limit ($A_{\text{iso}} \gg 100\,\text{MHz}$). Since the middle peaks become very broad and low at high field, the color map here is logarithmic in order to enhance their visibility. This decay with field is observed experimentally [22].

the thicknesses in brackets are in nm. Here, the Ta layer seeds the [111] growth of the Cu film. The thickness of the Au layer was chosen to provide adequate moderation of the muon beam, while also protecting the sample against oxidation. Measurements were taken at 250 K, where the time scale of the rotation of the molecule is short enough that the EXO muonium does not contribute to the observed signal. The sample was grown in a forming field of 20 mT. The sample was first measured in ZF before any other magnetic field was applied. The time-dependent polarization of the muonium state in ZF has been fitted with a single frequency model with the addition of an A_{tail} decay term which accounts for the slow depolarization of diamagnetic μ^+ particles within the metal layers:

$$P(t) = A_{Mu} \cos{(2\pi \upsilon_{Mu} t)} e^{(-\lambda_{Mu} t)} + A_{\text{tail}} e^{(-\lambda_{\text{tail}} t)}. \quad (4)$$

This yields the ENDO_f oscillation frequency, υ_{Mu}. The depolarization rate, λ_{Mu}, is also obtained. λ_{Mu} characterizes the distribution of hyperfine oscillations contributing towards

the signal at any given implantation energy. Figure 4(b) shows the dependence of the percentage change in ENDO_f frequency, $\Delta\upsilon_{Mu}$, as a function of implantation depth. The average implantation depth has been calculated from the simulated stopping profiles shown in Fig. 4(a). $\Delta\upsilon_{Mu}$ has been calculated relative to the frequency at 12 keV; the implantation energy that captures the center-most region. In the initial, as-grown measurement, a curved profile of muonium frequency is observed with depth. υ_{Mu} is higher at the top and bottom interfaces by $14 \pm 5\%$ and $25 \pm 5\%$, respectively. From this measurement alone, it is clear that towards the C_{60}/Cu interfaces, there is a change in the hyperfine splitting between ENDO_f spin configurations. Orbital rehybridization, lattice reconstruction, and Fermi level matching, lead to charge-transfer from the metal into the first fullerene monolayer [36–39]. As the neutral C_{60} lowest unoccupied molecular orbital is triply degenerate, the addition of charge is accompanied by a molecular distortion to break the degeneracy through the Jahn-Teller effect [40]. The reduced symmetry due to the molecular distortion imparts anisotropy onto the hyperfine
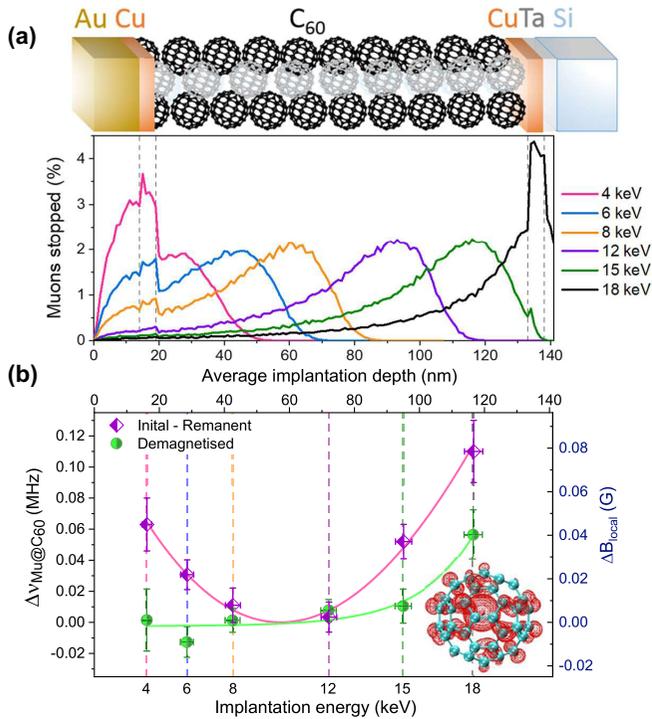
FIG. 4. ZF-LE-μSR measurements of the Mu@C_{60} frequency, υ_{Mu}, and depth profile in a thin film heterostructure. (a) The simulated implantation profile for a structure of [Si(Sub)/Ta(3)/Cu(5)/C_{60}(114)/ Cu(5)/Au(14)], where the thicknesses in brackets are in nm. At the 4 and 18 keV implantation energies, a considerable percentage (57% and 34%, respectively) of muons stop in the metal layers. As the measurement was performed in ZF, these are not expected to contribute to the oscillating signal. (b) The obtained depth dependence of the relative change in the ENDO$_f$ oscillation frequency, $\Delta\upsilon_{Mu}$, for the initial state measurement and following a degauss; lines are a guide for the eye. The corresponding change in the local field, ΔB_{Local}, calculated from the measured calibration curve in the crystalline C_{60} sample is also shown. Inset shows the highly anisotropic spin density (red: 10^{-6} μ_B Å^{-3}) for the endohedral muonium polaron state with an additional electron ENDO$_f$(-) calculated using screened-hybrid DFT (HSE06, see Supplemental Material).

coupling tensor, which describes the energy splitting in zero-field of the triplet muonium spin configurations. This is the cause of the observable 0.7 MHz ZF oscillation in the oblate molecule, C_{70} [9,10,41].

To examine the origin of the frequency shifts at the metallo-molecular interfaces, we compare the as-grown state with the signal after the sample is degaussed in a damped alternating field starting at 300 G. Following this degauss procedure, the depth profile of the muonium frequency dramatically changes. As shown in Fig. 4(b), υ_{Mu} now remains almost constant throughout the molecular layer. The increased υ_{Mu} frequency at both metal interfaces before degauss is therefore a consequence of Zeeman splitting of the muonium hyperfine levels due to small stray fields, of the order of 20–80 mG, originating at the Cu/C_{60} interface. After degauss, the remaining $9 \pm 3\%$ frequency shift at the depth closest to the bottom Cu/C_{60} interface can be attributed to metal-to-molecule electron trans-

fer at the interface and the presence of negatively charged ENDO$_f$(−). This state has a more anisotropic spin density, leading to higher oscillation frequency [inset in Fig. 4(b) and Supplemental Material Fig. S11]. The fact that there is no change in υ_{Mu} at the top Cu/C_{60} interface after degauss suggests a lower coupling and damage of the molecular layer with the metal layer sputtered on top as compared to the bottom interface, where the molecules were evaporated on the metal.

VII. CONCLUSION

We have presented LE-μSR data that characterizes the dynamics of the endohedral floating muonium polaronic state in C_{60} layers. The hyperfine frequencies of this state map the emergent magnetism formed at a Cu/C_{60} interface via the Zeeman splitting of the muonium hyperfine coupling. DFT calculations were used to model the charge, spin density, and dynamics of this muonium state, confirming it as the only system being detectable for temperatures >260 K as observed in the experiments. The polaron state causes a small anisotropy in the hyperfine coupling of the endohedral muonium, which allows us to observe a ZF precession of a few hundred kHz. This precession is very sensitive to any deviation from ZF and therefore is highly sensitive to weak stray magnetic fields of weak or dilute magnetic moments. For a nonpolaronic, isotropic muonium state, to measure a precession we need to apply a magnetic field. X-ray-based synchrotron techniques have been used to observe magnetic moments in Cu as small as 10^{-5} μ_B, which is roughly equivalent to local fields of 0.1 G [5,6]. The ENDO$_f$ polaronic state can detect local magnetic fields of ~0.01 Gauss and the charge transfer at a metallo-molecular interface [Fig. 4(b)]. When x-ray techniques are element sensitive, the muonium polaron offers the possibility to map the depth profile of the magnetization and the distribution of free charge in, e.g., magnetic multilayers, hybrid batteries or photovoltaic devices. C_{60} or other compounds forming muon polaron states such as crystalline semiconductors or oxides [42] are part of, or can be added, to the device structure [7,8]. For example, fullerene layers can be evaporated *in situ* on top of candidates to two-dimensional magnetism or ferroelectric materials to study weak surface effects such as magnetic monopoles [14].

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