# Strain-induced switching between noncollinear and collinear spin configuration in magnetic Mn<sub>5</sub>Ge<sub>3</sub> films

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We report the temperature-dependent magnetic and structural properties of epitaxial  $Mn_5Ge_3$  thin films grown on Ge substrates. Utilizing density-functional theory (DFT) calculations and various experimental methods, we reveal mechanisms governing the switching between collinear and noncollinear spin configuration in  $Mn_5Ge_3$ . The Mn atoms in  $Mn_5Ge_3$  occupy two distinct Wyckoff positions with fourfold ( $Mn_1$ ) and sixfold ( $Mn_2$ ) multiplicity. The DFT calculations reveal that below a critical distance of approximately 3.002 Å the coupling between  $Mn_2$  atoms is antiferromagnetic (AFM) while ferromagnetic (FM) above that critical distance. The FM coupling between  $Mn_1$  atoms is weakly affected by the strain. The observed noncollinear spin configuration is due to the coexistence of AFM and FM coupling at low temperatures. The findings give insight in developing strain-controlled spintronic devices.

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# I. INTRODUCTION

Spintronic offers lower power dissipation and processing capabilities much beyond the current complementary metal oxide semiconductor technology [1,2]. However, it is very challenging to find a ferromagnetic semiconductor material with high Curie temperature  $(T_C)$  and compatible with Si technology. Ferromagnetic Mn<sub>5</sub>Ge<sub>3</sub> films fabricated by epitaxial solid-state reaction on Ge substrates exhibit a  $T_C$  of about 283 K [3], a considerable spin polarization [4,5], a sharp interface between the ferromagnetic layer and Ge substrates [6,7], all of which are essential to achieve efficient spin injection and manipulation within semiconductors prepared by alreadyexisting silicon-based technologies. Furthermore, the  $T_C$  of Mn<sub>5</sub>Ge<sub>3</sub> was shifted much above room temperature by applying strain engineering ( $\sim$ 320 K) [8], quantum confinement  $(\sim 400 \text{ K})$  [9], or codoping with carbon  $(\sim 430 \text{ K})$  [10,11]. The fundamental properties of Mn<sub>5</sub>Ge<sub>3</sub>, especially the magnetic structure, have been investigated in detail [12-14]. Mn<sub>5</sub>Ge<sub>3</sub> possesses a hexagonal D88-type crystal structure with space

group  $P6_3/mcm$  whose unit cell contains 6 Ge and 10 Mn atoms. The Mn atoms occupy two different sublattices where Mn<sub>1</sub> is located at the Wyckoff 4*d* site and Mn<sub>2</sub> at the 6*g* site with x = 0.2397 [14]. In the relaxed unit cell, the magnetic moment of Mn<sub>1</sub> is  $1.96 \mu_B/Mn$  and that of Mn<sub>2</sub> is  $3.23 \mu_B/Mn$  [14]. The magnetic moment direction of Mn<sub>1</sub> and Mn<sub>2</sub> atoms has been demonstrated to be parallel to the *c* axis of the hexagonal structure from 77 K to  $T_C$ . The distinguished magnetic coupling between two different sublattices leads to an anisotropic exchange and complex magnetic ordering in different temperature regimes.

Ab initio pseudopotential calculations have demonstrated that  $Mn_5Ge_3$  has two competing phases with collinear and noncollinear spin configurations [15]. The interaction  $(J_1)$ between the nearest neighbors  $Mn_1$ - $Mn_1$  is ferromagnetic and weakly depends on the distance  $(d_1)$  between the  $Mn_1$ atoms, and it is much stronger than the interaction between the  $Mn_1$ - $Mn_2$  and  $Mn_2$ - $Mn_2$  atoms [16]. In contrast, the interaction  $(J_3)$  between the nearest neighbors  $Mn_2$ - $Mn_2$  strongly depends on the related atomic distance  $(d_3)$ . The neighboring  $Mn_2$  atoms are ferromagnetically (FM) coupled in the fully relaxed unit cell where  $d_3 = 3.017$  Å [based on density-functional theory (DFT) calculation]. By applying compressive strain,  $d_3$  decreases and the corresponding FM

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coupling is suppressed, then transformed into antiferromagnetic (AFM) coupling. In theoretical calculations presented by Slipukhina *et al.* [16], when  $d_3 = 2.974$  Å, the neighbor Mn<sub>2</sub> atoms are AFM coupled. The competing interactions between the AFM coupling between Mn<sub>2</sub> and the FM coupling between Mn<sub>1</sub> atoms stabilize noncollinear spin configurations [17,18]. The transition temperature from collinear to non-collinear magnetism in Mn<sub>5</sub>Ge<sub>3</sub> is 70 ± 5 K [19,20] which is usually explained by similar lattice distortions observed in Mn<sub>5</sub>Si<sub>3</sub> [21–23]. Yet there is no convincing explanation why the noncollinear spin configuration appears in nanostructured Mn<sub>5</sub>Ge<sub>3</sub> but not in bulk materials [16,19,20].

To gain insight into the complex physical properties of ferromagnetic Mn<sub>5</sub>Ge<sub>3</sub> thin films, we have performed systematically experimental investigation using temperature and angular-dependent magnetoresistance, temperaturedependent x-ray diffraction (TDXRD) as well as theoretical calculations using DFT [24-26]. According to our theoretical calculations the exchange constant  $J_3$  becomes negative and the nearest-neighboring Mn<sub>2</sub>-Mn<sub>2</sub> atoms are AFM coupled for a  $d^{\text{DFT}}_{3}$ -value on the order of 3.002 Å or smaller. The relative distance  $d^{exp}_3$  between two neighbor Mn<sub>2</sub> atoms, extracted experimentally from TDXRD, shrinks from  $3.012 \pm 0.002$  Å at room temperature down to 2.999  $\pm$ 0.002 Å at 5 K. The critical distance for the neighboring Mn<sub>2</sub> atoms ( $d_3$  smaller than 3.002 Å) at which magnetic coupling changes from FM to AFM is achieved at the temperature of  $150 \pm 10$  K. This means that at low temperatures the AFM coupling of Mn<sub>2</sub> atoms coexists with FM coupling of Mn1 atoms. At higher temperatures, all coupling interaction between Mn atoms is ferromagnetic. The temperature-dependent anisotropic magnetoresistance (AMR) reveals a well-visible transition from twofold to multifold symmetry with increasing temperature. This work provides experimental and theoretical evidence that both the switching between noncollinear and collinear spin configurations and the intriguing behavior of AMR are caused by the change of the magnetic coupling between Mn<sub>2</sub> atoms occupying 6g positions in the Mn<sub>5</sub>Ge<sub>3</sub> sublattice.

## **II. RESULTS AND DISCUSSION**

#### A. Magnetotransport results

In this work, (100)-orientated Mn<sub>5</sub>Ge<sub>3</sub> epitaxial films were fabricated on (001) Ge substrates by ms-range solid-state reaction (see the inset in Fig. 1) [3]. Figure 1 shows the temperature-dependent resistivity ( $\rho - T$ ) and the related first derivative curve of the Mn<sub>5</sub>Ge<sub>3</sub> thin film. In the  $d\rho/dT$  curve, a clear transition from positive to negative near 283 K is observed, which mainly ascribed to the transition from ferromagnetic to paramagnetic state [3,6,7,27]. The observed  $T_C$ corresponds well to the value obtained by superconducting quantum interference device-vibrating-sample magnetometer measurements (see Fig. S1 in Supplemental Material [28]). Below  $T_C$  (283 K) the resistivity decreases with decreasing temperature, showing typical metallic behavior [16,29,30]. Below  $T_C$ , the carrier-magnon scattering must be taken into account as well since the electron-magnon scattering dominates the electrical transport properties in strong ferromagnetic films.



FIG. 1. Temperature dependence of the resistivity for a (100)oriented  $Mn_5Ge_3$  film grown on Ge (001) substrate (red circles) and the corresponding first derivative (yellow curve). The inset shows the schematic alignment of the  $Mn_5Ge_3$  and Ge unit cells where the hexagonal  $Mn_5Ge_3$  (100) is twisted with respect to the (110) of cubic Ge (001). Here, we only show one case where the *c* axis of  $Mn_5Ge_3$ is roughly oriented along the [110] direction of Ge.

It is worth noting there is another small deformation (kind of cusp) in the  $d\rho/dT$  curve at  $T_I \sim 72$  K beside the wellvisible transition at  $T_C$ . Such a cusp is commonly observed in Mn<sub>5</sub>Ge<sub>3</sub> thin films and nanostructures but has not been shown in bulk crystals [19,20,31]. The appearance of such a cusp in the  $d\rho/dT$  curve is often related to the emergence of a new magnetic ordering. Zeng et al. reported that the cusp is due to the coexistence of two magnetic sublattices (Mn<sub>1</sub> and Mn<sub>2</sub>) with different magnetocrystalline anisotropies and exchange coupling constants [19]. The change of the magnetic coupling between Mn atoms was concluded by an analogy to the antiferromagnetic Mn<sub>5</sub>Si<sub>3</sub> where noncollinear spin states exist at lower temperatures [21,23,32]. The nontrivial spin arrangements at lower temperatures were demonstrated to induce the topological Hall effect [23,33]. To date, no further interpretation has been proposed to understand the underlying mechanism why the noncollinear spin configuration exists in Mn<sub>5</sub>Ge<sub>3</sub> films.

The AMR is a response of the electronic structure in magnetic materials to the variation of the magnetization direction. In traditional AMR theory of ferromagnetic metals [34,35], the magnetoresistance exhibits maximum value when the current is parallel to the magnetization direction, in which carriers moving along the magnetized direction are experiencing the strongest scattering potential among all Fermi surface states, whereas it shows a minimum when the current flow is perpendicular to the magnetization direction. This theory is valid for polycrystalline and amorphous ferromagnets in which the AMR only depends on the relative orientation of magnetization and current. However, in the case of epitaxial or strongly textured crystalline ferromagnetic films, such as Mn<sub>5</sub>Ge<sub>3</sub> grown on Ge, the AMR depends also on the orientation of magnetization with respect to the crystalline axes. The AMR can be decomposed into two parts, noncrystalline and crystalline terms [28,36–39]. For the noncrystalline component the AMR depends on the angle between the cur-



FIG. 2. (a) Schematic representation of the angular-dependent magnetoresistance measurements geometry. The electric current *I* flows parallel to the [110] direction of Ge and the magnetic field was rotated in the surface plane (001) of Ge. The angular-dependent magnetoresistance  $\rho_{AM}$  with in-plane magnetic field of 5 T as a function of the angle ( $\varphi$ ) between magnetic field and current were measured at (b) 5 K, (c) 170 K, and (d) 250 K.  $\rho_{AM}$  is defined as [( $\rho(\varphi) - \rho_{min}$ )/ $\rho_{min}$ ] × 100%.

rent and magnetization, but is independent of the orientation of magnetization with respect to the crystalline axes. On the other hand, the crystalline component relies on the symmetry of the crystal structure and is independent of the current direction.

Magnetotransport measurements were performed using four-wire contacts designed in a row [see Fig. 2(a)]. Figures 2(b)-2(d) show the angle  $(\varphi)$ -dependent anisotropic magnetoresistance  $\rho_{AM}$  measured at various temperatures with magnetic field applied in-plane sample surface. As shown in Fig. S2, the AMR maxima and minima of (100)oriented Mn<sub>5</sub>Ge<sub>3</sub> are almost independent of the current flow direction but strongly dependent on the crystalline axis, which indicates dominating crystalline AMR. Therefore, the observed evolution of anisotropy in magnetoresistance can be tentatively attributed to the crystalline component of the AMR. The magnitude of the  $\rho_{AM}$  and its dependence on  $\varphi$  are quite diverse with temperature rising from 5 to 300 K. At 5 K [see Fig. 2(b)],  $\rho_{AM}$  has a large modulation (2.24%) as a function of  $\varphi$  that accurately follows a typical  $\cos^2 \varphi$  dependence. It exhibits twofold symmetry [AMR(I)] with global minimum values at about 110° and 290° while global maximum values are observed at about 20° and 200°. The current is injected along the [110] lattice plane of Ge while the AMR response at 5 K is originated from the ferromagnetic Mn<sub>5</sub>Ge<sub>3</sub> layer. As shown in the inset of Fig. 1, the out-of-plane [210]<sub>H</sub> direction of  $Mn_5Ge_3$  is parallel to the [001]<sub>C</sub> direction of Ge substrate (the subscript indexes H and C denote the hexagonal and cubic unit cells, respectively) [3]. The  $[001]_{H}$  direction of Mn<sub>5</sub>Ge<sub>3</sub> lies in the surface plane of the Ge (001) substrate, and is roughly oriented along the  $\langle 110 \rangle_{\rm C}$  direction of Ge. Due to the relatively large lattice mismatch between Mn<sub>5</sub>Ge<sub>3</sub> and Ge the unit cell of the ferromagnetic film is misoriented in all directions, resulting in the tilt of the (100) net planes and a twist in the basal plane. The tilt/rotation of the Mn<sub>5</sub>Ge<sub>3</sub> layer with respect to the Ge substrate is likely related to the shift of the twofold symmetry global maximum in the AMR signal with respect to the injected current, consistent with our finding of dominating crystalline AMR. The AMR symmetry changes with increasing temperature. Most probably, this is mainly due to the change of the magnetic coupling between Mn<sub>2</sub> atoms with increasing interatomic distance between them. The twofold AMR contributed from Mn1 atoms becomes weaker while the additional AMR component with new symmetries contributed from Mn<sub>2</sub> becomes stronger with increasing temperature. With increasing temperature, the Mn<sub>2</sub> atoms in the 6g site become FM coupled, which changes the distribution of the local magnetic moments and results in a multifold symmetry in the AMR signal [schematically marked with blue dashed lines in Fig. 2(d)]. At this temperature, the multifold symmetry coexists with the Mn<sub>1</sub>-related twofold symmetry as schematically shown in Fig. 2(d).

Now we discuss the AMR evolution in detail. Firstly, with increasing temperature from 5 to 150 K, the magnitude of  $\rho_{\rm AM}$  reduces from 2.24 to 0.38%, but still shows the identical twofold AMR [Figs. S3(a)-S3(c)] [28]. At 170 K [see Fig. 2(c)], besides the AMR(I) component with twofold symmetry, additional local peaks emerge along several specific angular directions (i.e.,  $\varphi = 70^\circ$ ,  $115^\circ$ ,  $160^\circ$ ,  $250^\circ$ ,  $295^\circ$ , and 340°). At 250 K [see Fig. 2(d)], the magnitude of inherent twofold AMR(I) is strongly suppressed (reduced to 0.07%), while the newly emerged AMR(II) component becomes stronger and new global maxima appear at  $\varphi = 75^{\circ}$ , 125°, 175°, 255°, 305°, and 355°. At 250 K the AMR(II) increases up to 0.12% for the global maximum at 125°. With increasing temperature from 170 to 250 K the angle interval between maxima in AMR(II) changes from 45° to 50°. The position of the global maximum changes with increasing temperature. Most probably, the rotation of the global maximum is due to the structural deformation of the Mn<sub>5</sub>Ge<sub>3</sub> unit cell with temperature causing a change in the spatial position of the Mn atoms. At 300 K, the Mn<sub>5</sub>Ge<sub>3</sub> is paramagnetic and the related  $\rho_{AM}$  curve exhibits a twofold symmetry again (see Fig. S4) [28].

To explain the transition of spin configurations at 72 K and the diverse AMR symmetries observed at different temperature regimes, the magnetotransport properties of  $Mn_5Ge_3$  are further discussed in terms of structural evolutions and corresponding DFT calculations.

#### **B.** Structural analysis

Figures 3(a) and 3(b) show the distances  $d_3$  and  $d_1$  between the nearest-neighboring atoms in Mn<sub>2</sub> and Mn<sub>1</sub> sublattices extracted from the TDXRD results (see Fig. S5) [28,40,41], respectively. Upon cooling, both  $d_3$  and  $d_1$  distinctly shrink with decreasing the temperature. At 150 K,  $d_3$  reduces to 3.002 Å. Here, for the calculation of  $d_3$  we assumed an identical change of the  $d_3$  for all Mn<sub>2</sub> atoms in the basal configuration and a constant parameter of the 6g Wyckoff position. In fact, while the basal configuration of the Mn<sub>2</sub> unit in relaxed Mn<sub>5</sub>Ge<sub>3</sub> is an equilateral triangle, only one side is aligned along the out-of-plane direction in our film geometry. Nevertheless, the assumptions made here are sufficient to present qualitatively the influence of the temperaturedependent strain and the unit-cell deformation on the AMR and spin configuration. It is important to note that the decreasing of  $d_3$  is much faster than  $d_1$ . This is due to the different thermal expansion coefficient ( $\alpha$ ) for the semimetallic Mn<sub>5</sub>Ge<sub>3</sub> film (the average  $\alpha = 2.6 \times 10^{-5} \text{ K}^{-1}$ ) and for semiconducting Ge ( $\alpha = 6.1 \times 10^{-6} \text{ K}^{-1}$ ) [8]. For the Mn<sub>5</sub>Ge<sub>3</sub> film, the change of the out-of-plane lattice parameter is about four times larger than the change of the in-plane lattice parameter that depends on the Ge substrate. As a result, the hexagonal unit cell is flattened and distorted at lower temperatures, where the  $Mn_5Ge_3$  unit cell has the large c/a ratio.

## C. Density-functional theory (DFT) calculations

To understand the roles of accumulated strains on the magnetotransport properties of experimental samples, we carried out the computations [42–46] assuming the relative change



FIG. 3. (a), (b) Temperature-dependent distances  $d_3$  and  $d_1$  between the nearest-neighbor atoms in Mn<sub>2</sub> and Mn<sub>1</sub> sublattices as deduced from TDXRD and tabulated lattice spacing at room temperature ( $d_3^0 = 3.017 \text{ Å}$ ,  $d_1^0 = 2.518 \text{ Å}$ ) [14], respectively. Error bars are shown for the measured atomic distances  $d_3$  and  $d_1$  while the error in the temperature is within the size of the used data symbols. The insets in (a) and (b) show the schematic picture of the crystal structure. The Mn<sub>1</sub>, Mn<sub>2</sub>, and Ge atoms are shown with green, blue, and gray circles, respectively.

of the lattice values obtained from the experiments. In order to gain insight into macroscopic magnetism revealed in the experimental samples, it is crucial to examine the microscopic picture. Note that the macroscopic magnetism originates from short-range exchange couplings that constitute the microscopic magnetic model. Moreover, any microscopic magnetic model is apparently related to the geometrical features of the underlying crystal structure, in particular, the mutual arrangements of the magnetic atoms. Thus, it is crucial to consider the distances between the nearest-neighboring Mn ions in each of two sublattices for the magnetic ground state ( $M_1$  configuration in Fig. S6) [28]. Mn<sub>5</sub>Ge<sub>3</sub> films invariably present ferromagnetic behavior with the exertion of experimental strain, in accordance with previously reported results [15,16].

Furthermore, we examine the impact of the elastic strains on the exchange interactions between the Mn spins (shown in Fig. 4), by considering an effective classical spin Hamiltonian [46]. The details of these calculations along with derived equations are presented in Supplemental Material [28] (see Figs. S6–S8).

Note that the nearest-neighbor interaction between the  $Mn_1-Mn_1$  exhibits FM exchange coupling  $J_1$ , which dominates over the remaining interactions. See Table I. The negligible changes in  $J_1$  are reflected by the very small changes of  $d_1$  distances, which are approximately 0.003 Å between 300 and 5 K. In the case of the  $Mn_2$  sublattice the AFM coupling appears under the compressive strain. The AFM interaction is more favorable for the  $Mn_2$  sublattice when the  $d_3$  distance is getting shortened, in agreement with



FIG. 4. Schematic picture of the crystal structure and exchange couplings. Different colors indicate various Mn-Mn distances and the corresponding exchange couplings. The thin black lines denote the size of the unit cell. The  $Mn_1$  and  $Mn_2$  atoms in the sublattices with fourfold and sixfold positions are marked with green and blue color. The Ge atoms are not shown here and the unit cell is shifted to (0.5, 0.5, 0).

previously reported calculations [16]. However, note that in Ref. [16] the authors reported a larger change of  $J_3$  [from -2.04 (rigid) to 1.80 meV (relaxed)] which corresponds to a larger shortening of the  $d_3$  distance (0.083 Å presented in Ref. [16] vs 0.017 Å obtained in this work). The latter is probably a consequence of different and larger strain used in comparison to our simulations, not directly stated in Ref. [16]. According to our DFT calculation, for  $d_3$  larger than 3.002 Å the Mn<sub>2</sub> sublattice exhibits ferromagnetism. However, the Mn atoms in the Mn<sub>2</sub> sublattice are AFM coupled for the  $d_3$  smaller than 3.002 Å.

## **D.** Discussion

Finally, we propose a scenario for the noncollinear to collinear switching and anomalous AMR behavior as a function of temperature. During the cooling process,  $d_3$  becomes smaller than 3.002 Å at a temperature below 150 K (see Fig. 3). Furthermore, the FM coexists with AFM states at low temperatures in Mn<sub>5</sub>Ge<sub>3</sub> films. Since the AFM coupling in the Mn<sub>2</sub> sublattice induces the change of local spin ordering, it would exert different influence on the AMR. In addition, it has been reported that the electronic properties of Mn<sub>5</sub>Ge<sub>3</sub> depend strongly on the atomic distance and atomic environment of Mn atoms [28]. In this case, the magnetoresistance below 150 K with a twofold symmetry can be related to the interaction between conduction electrons and FM spin ordering in the Mn<sub>1</sub> sublattice. In the temperature range from 150 to 280 K

TABLE I. Exchange couplings for the strained  $Mn_5Ge_3$  samples at 5 K and unstrained  $Mn_5Ge_3$ . Negative and positive  $J_{ij}$  values denote AFM and FM couplings, respectively. The changes in distances are given in respect to the FM ground state.

$\overline{J_{ij}(d_{ij}) \text{ (meV)}}$	Strained at 5 K	Unstrained
$\overline{J_1^{\text{Mn1-Mn1}}(\Delta d_1)}$	33.2 (0.003 Å)	33.6
$J_2^{\text{Mn1-Mn2}}$	6.9	8.4
$J_3^{Mn2-Mn2}(\Delta d_3)$	−0.2 (0.017 Å)	1.0
$J_4^{\text{Mn2-Mn2}}$	5.7	5.7
$J_5^{\text{Mn1-Mn1}}$	8.2	8.5
$J_6^{Mn2-Mn2}$	4.8	4.8

the AMR shows combination of both twofold and multifold symmetry. We infer that the twofold symmetry is caused by FM coupling between Mn atoms with fourfold position in the  $Mn_1$  sublattice. The multifold symmetry is probably associated with the FM coupling between  $Mn_2$  atoms with sixfold position in the  $Mn_2$  sublattice.

In addition, the coexistence of AFM and FM coupling observed at low temperatures probably contributes to a low-temperatures noncollinear spin configuration which is commonly observed in Mn<sub>5</sub>Ge<sub>3</sub> thin films. With temperature decreasing below 150 K, the AFM coupling between Mn<sub>2</sub> atoms is increasing. So, the magnetic state depends on the distance between the Mn atoms, and spins will rotate to adjust to the new positions of the atoms with temperature decreasing. Upon cooling to 70 K, the strong enough AFM coupling can compete with FM coupling, and thus it is highly plausible to result in the noncollinear spin state. Moreover, Stroppa and Peressi have shown that the noncollinear spin configuration in  $Mn_5Ge_3$  is stabilized at a higher c/a ratio [15]. In our work,  $Mn_5Ge_3$  exhibits a larger c/a ratio with decreasing temperature, which additionally justifies the existence of noncollinear spin configuration below 70 K. The experimental error in the presented atomic distances might also contribute to the discrepancy between these two identified characteristic temperatures.

# **III. CONCLUSION**

In summary, the ferromagnetic  $Mn_5Ge_3$  films grown on Ge substrates show anomalous temperature-dependent AMR and switching from noncollinear to collinear spin configuration. Using different experimental techniques combined with DFT calculations, we have proposed a physical scenario responsible for both anomalous AMR and the switch of the spin configuration. The low-temperature noncollinear spin configuration very probably arises from the coexistence of AFM and FM coupling between Mn atoms in the Mn<sub>2</sub> and Mn<sub>1</sub> sublattices. The change of the magnetic coupling between Mn atoms in the Mn<sub>2</sub> sublattice from AFM to FM is proposed as an explanation for the anomalous AMR behavior as a function of temperature. Our results would stimulate further investigations to understand the intriguing magnetic properties in Mn<sub>5</sub>Ge<sub>3</sub> films.

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magnetoresistance measurements. P.D. and D.K. performed the temperature-dependent XRD measurements. M.B. performed the DFT calculations and related analyses. J.G. contributed to the discussion about structural analyses.

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