## Collective excitations in the tetravalent lanthanide honeycomb antiferromagnet Na<sub>2</sub>PrO<sub>3</sub>

M. J. Daum,<sup>1,\*</sup> A. Ramanathan<sup>(a)</sup>,<sup>2,\*</sup> A. I. Kolesnikov<sup>(a)</sup>,<sup>3</sup> S. Calder,<sup>3</sup> M. Mourigal,<sup>1,†</sup> and H. S. La Pierre<sup>(a)</sup>,<sup>4,‡</sup>

<sup>2</sup>School of Chemistry and Biochemistry, Georgia Institute of Technology, Atlanta, Georgia 30332, USA

<sup>4</sup>Nuclear and Radiological Engineering and Medical Physics Program, School of Mechanical Engineering,

Georgia Institute of Technology, Atlanta, Georgia 30332, USA

(Received 13 October 2020; accepted 22 February 2021; published 12 March 2021)

Thermomagnetic and inelastic neutron-scattering measurements on Na<sub>2</sub>PrO<sub>3</sub> are reported. This material is an antiferromagnetic honeycomb magnet based on the tetravalent lanthanide Pr<sup>4+</sup> and has been proposed to host dominant antiferromagnetic Kitaev interactions. These measurements reveal magnetic fluctuations in Na<sub>2</sub>PrO<sub>3</sub> below an energy of 2 meV as well as crystal-field excitations around 230 meV. The latter energy is comparable to the scale of the spin-orbit interaction and explains both the very small effective moment of around 1.0  $\mu_{\rm B}$  per Pr<sup>4+</sup> and the difficulty to uncover any static magnetic scattering below the ordering transition at  $T_{\rm N} = 4.6$  K. By comparing the low-energy magnetic excitations in Na<sub>2</sub>PrO<sub>3</sub> to those of the isostructural spin-only compound, Na<sub>2</sub>TbO<sub>3</sub>, a microscopic model of exchange interactions is developed that implicates dominant and surprisingly large Heisenberg exchange interactions  $J \approx 1.1(1)$  meV. Although antiferromagnetic Kitaev interactions with  $K \leq 0.2J$  cannot be excluded, the inelastic neutron-scattering data of Na<sub>2</sub>PrO<sub>3</sub> is best explained with a  $\Delta = 1.22$  easy-axis XXZ exchange anisotropy.

DOI: 10.1103/PhysRevB.103.L121109

Frustrated quantum magnets have been proposed as a platform to realize quantum spin-liquids (QSLs) and other exotic forms of magnetic matter [1,2]. In OSLs, quantum fluctuations are so strong that spins remain disordered for temperatures well below the average interaction scale between spins and become entangled. Geometrically frustrated lattices featuring lanthanide ions have gained much recent attention, including the triangular, kagome, and pyrochlore systems [3-8]. An alternative realization of a QSL (with an exact solution) was proposed by Kitaev based on S =1/2 moments on a honeycomb lattice with bond-dependent Ising-like interactions [9]. While the honeycomb lattice is not inherently frustrated, anisotropic interactions, parametrized by the Kitaev term (K) give rise to frustration between the competing orthogonal anisotropy axes. However, in real materials, the Kitaev interactions are often perturbed by Heisenberg interactions (J) giving rise to the strongly frustrated Heisenberg-Kitaev (*J*-*K*) model [10,11].

Bond-dependent interactions stem from strong spin-orbit coupling (SOC) in magnetic insulators. Hence heavy 4*d* and 5*d* transition metal ions have been proposed as a paradigm to realize a Kitaev QSL [12,13]. Spin-orbit  $J_{\text{eff}} = 1/2$  Mott insulators comprising low-spin  $d^5$  and  $d^7$  transition metal ions such as Na<sub>2</sub>IrO<sub>3</sub>, H<sub>3</sub>LiIr<sub>2</sub>O<sub>6</sub>, Li<sub>2</sub>IrO<sub>3</sub>, and RuCl<sub>3</sub> have been extensively studied to search for Kitaev physics [14–20]. An alternative approach is to explore  $J_{\text{eff}} = 1/2$  magnetic

moments from *f*-element ions, which exhibit significant anisotropy [21,22]. In the 4*f* electron manifold, several electron configurations can host  $J_{eff} = 1/2$  magnetic moments, with the one electron/one hole  $(4f^{1}/4f^{13})$  configurations as the most desirable. The one-hole case is realized by the  $J_{eff} = 1/2$  honeycomb material YbCl<sub>3</sub>, the collective behavior of which was recently shown to be best described from the Heisenberg limit [23]. The one-electron case leads to the 4*f*<sup>1</sup> ions Ce<sup>3+</sup> or Pr<sup>4+</sup> including Na<sub>2</sub>PrO<sub>3</sub>, a material with edgesharing PrO<sub>6</sub> octahedra forming a honeycomb network similar to the iridates and was recently proposed to exhibit dominant antiferromagnetic Kitaev interactions, contrasting with 4*d* and 5*d* systems [24].

In this work, the magnetic properties of Na<sub>2</sub>PrO<sub>3</sub> are investigated using a combination of thermomagnetic and neutron-scattering measurements on powder samples. These studies uncover spin-wave-like excitations at energies below 2 meV. A comparison to the isostructural compounds Na<sub>2</sub>TbO<sub>3</sub> and Na<sub>2</sub>CeO<sub>3</sub>, which represent spin-only magneticmoment and nonmagnetic analogs of the title compound, respectively, yields deeper insights into the effective magnetic Hamiltonian of Na<sub>2</sub>PrO<sub>3</sub>. Although no magnetic Bragg peaks are observed within experimental sensitivity below the  $T_{\rm N} \approx$ 4.6 K transition seen in thermomagnetic probes, dynamic correlations in Na<sub>2</sub>PrO<sub>3</sub> are well explained by a model including antiferromagnetic nearest-neighbor interactions and a easy-axis XXZ exchange anisotropy. The inelastic data do not support the presence of a sizable Kitaev term K. These studies also reveal an unusually small effective magnetic moment for the Pr<sup>4+</sup> ions which is explained by the increased crystal-field splitting in comparison to trivalent lanthanides [25,26].

<sup>&</sup>lt;sup>1</sup>School of Physics, Georgia Institute of Technology, Atlanta, Georgia 30332, USA

<sup>&</sup>lt;sup>3</sup>Neutron Scattering Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA

<sup>&</sup>lt;sup>\*</sup>These authors contributed equally to this work.

<sup>&</sup>lt;sup>†</sup>mourigal@gatech.edu

<sup>\*</sup>hsl@gatech.edu



FIG. 1. (a) Monoclinic crystal structure of Na<sub>2</sub>PrO<sub>3</sub> showing the honeycomb layers of Pr<sup>4+</sup> ions and the resulting nearest-neighbor and out-of-plane magnetic exchange pathways. (b) Comparison of the expected splitting of the  ${}^{2}F_{5/2}$  free-ion ground-state of Pr<sup>4+</sup> by SOC and a  $O_h$  CEF environment in LS and intermediate coupling. (c) Comparison between low momentum-transfer  $Q \leq 6$  Å<sup>-1</sup> inelastic neutron-scattering spectra measured with  $E_i = 800$  meV for Na<sub>2</sub>LnO<sub>3</sub> (Ln = Ce, Pr, Tb) at T = 1.8 K. (d) Momentum-transfer dependence of the E = 233(1) meV excitation at T = 14 K compared to phonon background at comparable energies. (e) The inverse magnetic susceptibility  $1/(\chi(T) - \chi_0)$  and susceptibility  $\chi(T)$  of  $Na_2PrO_3$  in a 0.1 T field and  $\chi_0 = 1.09 \times 10^{-3} \text{ emu/mol}^{-1}$ . The bold solid line (purple) is the CEF comparison to the data with the parameters in (f). The black and red traces in the inset correspond to FC and ZFC measurements, respectively. (f) Isothermal magnetization M(H) at T = 5 K and obtained CEF parameters.

Polycrystalline samples of Na<sub>2</sub> Ln<sup>4+</sup>O<sub>3</sub> with Ln = Ce  $(4f^0)$ , Pr  $(4f^1)$ , Tb  $(4f^7)$  were synthesized by solid-state reactions and structurally characterized by synchrotron x-ray diffraction (see Ref. [27], Sec. S1 and Ref. [28]). Na<sub>2</sub>PrO<sub>3</sub> contains layers of PrO<sub>6</sub> octahedra forming distorted honeycomb networks separated by layers of Na ions, with two intraplane Pr–Pr distances, d = 3.407(3) Å and d' = 3.487(6) Å, and an interplane distance of  $d_{\perp} \approx 5.8$  Å at T = 100 K [Fig. 1(a)]. The ABC stacking sequence in the C2/c space group originates from symmetry-breaking displacements of the Na atoms which also lead to evident-stacking faults in diffraction patterns. Na<sub>2</sub>CeO<sub>3</sub> and Na<sub>2</sub>TbO<sub>3</sub> are isostructural to Na<sub>2</sub>PrO<sub>3</sub> [28]. Given the air sensitivity of these samples, all synthesis and measurement operations were performed in an inert-gas atmosphere.

To understand the single-ion properties of  $Na_2PrO_3$ , broadband inelastic neutron-scattering measurements on the fineresolution Fermi chopper spectrometer (SEQUOIA) [29,30] were performed at the Spallation Neutron Source (SNS), Oak Ridge National Laboratory (ORNL). Experiments were performed on (m = 8 g) polycrystalline samples loaded in annular Al powder cans and inserted into a liquid <sup>4</sup>He cryostat reaching a base temperature of T = 1.5 K. The data were reduced in MANTID [31] to yield the neutron-scattering intensity I(Q, E)as a function of momentum-transfer Q and energy-transfer E. We used a series of incoming energies to probe possible crystal electric field (CEF) excitations of our samples up to an energy transfer of  $E \approx 800$  meV (see Ref. [27], Sec. S2, and Refs. [32,33]).

 $Pr^{4+}$  is a  $4f^1$  Kramers ion, isoelectronic to  $Ce^{3+}$ , with a  ${}^{2}F_{5/2}$  free-ion ground-state. For an octahedral oxygen environment with  $O_h$  symmetry, the CEF splitting leads to a Kramers doublet ground-state  $(\Gamma_7)$  and an excited quartet  $(\Gamma_8)$  which we expect to split into two doublets given the lower  $D_{2d}$  site symmetry of  $Pr^{4+}$  in Na<sub>2</sub>PrO<sub>3</sub> [Fig. 1(b)]. The energy dependence of the neutron-scattering intensity at low-momentum-transfer  $I(Q \leq 6 \text{ Å}^{-1}, E)$  was used to search for these CEF excitations. The comparison of different  $E_i$ s and samples (Fig. 1(c) and Supplemental Material, Ref. [27], Sec. S2) reveals a strong excitation at E = 233(1) meV. The intensity of the excitation increases at low Q as expected for magnetic scattering [Fig. 1(d)]. The excitation found in Na<sub>2</sub>PrO<sub>3</sub> compares well to the 260 meV  $\Gamma_7$  to  $\Gamma_8$  splitting observed for BaPrO<sub>3</sub> [34] which comprises  $Pr^{4+}$  ions in an ideal  $O_h$  environment. Since no other CEF excitations are observed below 500 meV, the E = 233 meV mode is associated with the two quasidegenerate  $\Gamma_8$  doublets see Ref. [27], Sec. S2).

Given the axial distortion of the PrO<sub>6</sub> octahedra (see Ref. [27], Sec. S3 and Refs. [35–37]), the CEF Hamiltonian can be written using the Wybourne tensor operators [36] as  $\hat{\mathcal{H}}_{CEF} = B_0^2 \hat{C}_0^2 + B_0^4 \hat{C}_0^4 + B_4^4 \hat{C}_4^4 + B_0^6 \hat{C}_0^6 + B_4^6 \hat{C}_4^6$ . The large CEF energy scale in Na<sub>2</sub>PrO<sub>3</sub> has been observed indirectly by O *K*-edge x-ray absorption near edge spectroscopy studies of PrO<sub>2</sub> [26] and is similar in magnitude to the spin-orbit interaction  $\lambda \approx 100$  meV resulting in a  $\approx 360$  meV separation between  ${}^2F_{5/2}$  and  ${}^2F_{7/2}$  for a free Pr<sup>4+</sup> ion [38]. As a result, a mixing of the  ${}^2F_{5/2}$  and  ${}^2F_{7/2}$  electronic manifolds is expected and the above Hamiltonian must be diagonalized using the complete set of intermediate-coupling basis states using SPECTRE [39].

Given the number of CEF parameters, it is not possible to constrain the Hamiltonian solely using the observed excitation. To progress, it is possible to additionally match the temperature dependence of the magnetic susceptibility for  $\mu_0 H = 0.1$  T [Fig. 1(e)] and  $T \ge 60$  K using the set of CEF parameters of Fig. 1(f) and a temperature-independent term  $\chi_0 = 1.09 \times 10^{-3} \text{ emu/mol}^{-1}$ , although the CEF parameters remain underconstrained. The value of  $\chi_0$  is in reasonable agreement with the estimated value [40]  $\chi_0 \approx \frac{8}{3\lambda} \mu_B^2 N_A = 0.8 \times 10^{-3} \text{ emu/mol}^{-1}$  for a Pr<sup>4+</sup> ion and with observations for the related compound BaPrO<sub>3</sub> [41]. We note that a constrained form of the Hamiltonian preserving the proximate  $O_h$  crystal field symmetry with axial distortion as a perturbation does not allow us to match the magnetic susceptibility (see Ref. [27], Sec. S4). This choice of CEF parameters yields a ground-state doublet dominated by  $|{}^{2}F_{5/2} \pm 3/2\rangle$  and  $|{}^{2}F_{7/2} \pm 5/2\rangle$  states and predicts several higher-energy doublets beyond the 800 meV reach of our experiments (see Ref. [27], Sec. S2). This also yields a



FIG. 2. (a) Heat capacity measurements of our Na<sub>2</sub> $Ln^{4+}O_3$  samples measured using the relaxation method above T = 2 K. For Na<sub>2</sub>PrO<sub>3</sub>, measurements down to T = 100 mK were carried out using a dilution refrigerator insert on pressed pellets mixed with Ag. The change in magnetic entropy for Na<sub>2</sub>PrO<sub>3</sub> and Na<sub>2</sub>TbO<sub>3</sub> is obtained after subtracting the (scaled) lattice contribution from Na<sub>2</sub>CeO<sub>3</sub>. (b) Neutron diffraction measurements on Na<sub>2</sub>PrO<sub>3</sub> at T = 1.6 K using  $\lambda = 2.4$  Å. The red line is the result from a Rietveld refinement. (c) Comparison at low-angle diffraction between T = 1.6 K and T = 55 K.

calculated powder-averaged g=0.98 for effective  $J_{\rm eff} = 1/2$ . The effective moment  $\mu_{\rm CEF}^{\rm eff} = 0.84 \ \mu_{\rm B}/{\rm Pr}$  is unusually small given the free-ion value is  $\mu_{\rm eff}^{\rm free} = 2.54 \ \mu_{\rm B}/{\rm Pr}$ . The small g tensor is evident from the experimental isothermal magnetization at T = 5 K, which is linear and reaches only  $\approx 0.12 \ \mu_{\rm B}/{\rm Pr}$  at  $\mu_0 H = 14$  T, far short of saturation [Fig. 1(f)].

Below  $T \approx 40$  K, the susceptibility of Na<sub>2</sub>PrO<sub>3</sub> deviates from the single-ion form and culminates in a magnetic transition at  $T_N$ =4.6 K, consistent with Ref. [42], with a clear splitting between field-cooled (FC) and zero-field-cooled (ZFC) traces but no visible frequency dependence in ac susceptibility (see Ref. [27], Sec. S4). Thus, this sharp peak is interpreted as magnetic ordering preceded by short-range order [Fig. 1(e)]. It is difficult to find an adequate regime for a Curie-Weiss analysis: A fit limited to  $40 \leq T \leq 60$  K yields an antiferromagnetic Weiss constant  $\Theta_{W} = -30.4(1) K$  and  $\mu_{CW}^{\text{eff}} = 1.19(1)\mu_{\text{B}}/\text{Pr}$ , comparable to  $\mu_{CEF}^{\text{eff}}$ . Heat capacity measurements (see Ref. [27], Sec. S5 and Refs. [43,44]) corroborate this picture [Fig. 2(a)]. An additional upturn is observed below T = 0.3 K, which is associated with nuclear spins. Subtracting the lattice contribution reveals an entropy change  $\Delta S \approx 0.76R \ln 2$  between 0.1 K and 40 K, corroborating the  $J_{\rm eff} = 1/2$  picture for  $Pr^{4+}$  and revealing some missing entropy.

To understand the ground-state of Na<sub>2</sub>PrO<sub>3</sub> below the transition, neutron powder diffraction experiments were performed on the HB2A diffractometer [47] at the High Flux Isotope Reactor (HFIR), ORNL. No additional Bragg peaks are observed beyond the C2/c nuclear structure [Fig. 2(b)], even after subtracting a T = 55 K background [Fig. 2(c)]. Given the high incoherent scattering background from the sample see Ref. [27], Sec. S2), the small effective moment of Pr<sup>4+</sup>, the stacking faults in the crystal structure, and the likelihood of a  $k_m = 0$  propagation vector, this result is not entirely surprising. To get an estimate on any ordered moment  $\langle \mu^z \rangle$ , the hyperfine coupling in the nuclear specific heat was modeled using a Schottky form. Assuming the entire upturn is nuclear yields a static electronic moment  $\langle \mu^z_{hyp} \rangle = 0.41 \ \mu_B$ 

at the timescale of the nuclear-lattice relaxation [4], which is comparable to  $\langle \mu_{\rm CEF}^z \rangle = 0.49 \mu_{\rm B}$  estimated from CEF calculations.

In the absence of visible magnetic Bragg peaks in Na<sub>2</sub>PrO<sub>3</sub>, low-energy inelastic neutron scattering  $(E_i = 8,$ 20 meV) was employed to search for magnetic fluctuations. It is instructive to compare these results to the isostructural spinonly compound, Na<sub>2</sub>TbO<sub>3</sub> [Figs. 3(a)-3(e)]. Na<sub>2</sub>TbO<sub>3</sub> orders at  $T'_{\rm N} = 38.2$  K and develops structured spin-wave excitations below  $T'_{\rm N}$  [Figs. 3(a) and 3(b)] with a band top of 5 meV and a  $\approx 1$  meV gap. Subtracting T = 55 K data from T = 20 K, the elastic line shows evidence of intense magnetic Bragg peaks, show evidence of intense magnetic Bragg peaks indexed by a  $k_{\rm m} = 0$  propagation vector [Fig. 3(d)]. Representation analysis in SARAH [48] yields four possible magnetic structures, only one of which yields a good fit following a Rietveld refinement in FULLPROF [49] (see Ref. [27], Sec. S6). Spins in the resulting Néel ordered structure lie in the ac-plane, essentially along c. Spin-wave excitations in Na<sub>2</sub>TbO<sub>3</sub> are very intense given S = 7/2 [Fig. 3(e)] and can be efficiently modeled using linear spin-wave theory [50] in SPINW [51]. A spin Hamiltonian  $\mathcal{H} = \mathcal{H}_{ex} + D \sum_i (S_i^z)^2$  with Heisenberg exchange interactions  $J_1$  and  $J'_1$  for the split nearest-neighbor pairs (d and d'),  $J_{\perp}$  between inequivalent lanthanide sites in two adjacent honeycomb planes, and a single-ion anisotropy term D are considered. The calculated powder-averaged intensity is in excellent agreement with the data [Fig. 3(c)] with parameters obtained after a grid calculation and subsequent search for a minimal  $\chi^2$  (see Ref. [27], Sec. S7). These parameters,  $J_1 = 0.50$  meV,  $J'_1 = 0.85J_1$ ,  $J_\perp = -0.02J_1$ , and  $D = -0.001 J_1$  indicate that the observed band-top dispersion [Figs. 3(a) and 3(b)] is induced by the splitting of  $J_1$  and  $J'_1$ , and that the small spin gap is the combined effect of ferromagnetic  $J_{\perp}$  and easy-axis D.

This foregoing analysis facilitates the description of the magnetic fluctuations in Na<sub>2</sub>PrO<sub>3</sub> at T = 1.5 K [Figs. 3(f)-3(i)], which resemble the spin-wave excitations in Na<sub>2</sub>TbO<sub>3</sub> [Fig. 3(a)], but with a reduced band top of 2 meV [Fig. 3(f)] and a scattering intensity decreased by a factor  $\approx 30$  [Figs. 3(b) and 3(f)]. Thus, a high-temperature subtraction (T = 55 K) was utilized [Fig. 3(f)]. Given that no static magnetic scattering is observed, an incipient  $k_{\rm m} = 0$  order is assumed by analogy with Na<sub>2</sub>TbO<sub>3</sub>. Given the  $J_{eff} = 1/2$  magnetic moments, several models are adopted to incorporate exchange anisotropies (scaled to the corresponding primary exchange) on  $J_1$  and  $J'_1$  bonds, with spin-wave theory calculations performed in SPINW (see Ref. [27], Sec. S8). Including a diagonal exchange anisotropy (XXZ), e.g.,  $\mathcal{H}_{ex} \equiv J \sum_{ij} (S_i^x S_j^x +$  $S_i^y S_i^y + \Delta S_i^z S_i^z$ ), opens a gap in the spectrum and yields an excellent agreement with the data for  $J_1 = J'_1 = 1.06$  meV and  $\Delta = 1.22$  [Fig. 3(g)]. Allowing  $J'_1$  to vary independently slightly broadens the bandwidth but does not significantly improve the agreement between data and calculations [Fig. 3(h)]. Introducing a Kitaev term K in the Hamiltonian yields an overall agreement with the data for  $J_1 = 1.1 \text{ meV} (J'_1 = J_1)$  and an antiferromagnetic  $K=0.18J_1$ , but introduces a weak doublegap feature at the band bottom that is clearly not observed in the experiment [Fig. 3(i)]. A cut through the low-energy part of the data and the corresponding spin-wave calculations



FIG. 3. (a)–(e) Inelastic neutron-scattering intensity I(Q, E) from Na<sub>2</sub>TbO<sub>3</sub> at T = 1.5 K using (a)  $E_i = 8$  meV or (b)  $E_i = 20$  meV, where (b) is normalized to absolute units using the nuclear elastic scattering intensity see Ref. [27], Sec. S9 and Refs. [45,46]). (c) Comparison with powder-averaged linear spin-wave theory calculations for optimized parameters including the magnetic form factor of Tb<sup>3+</sup> and a constant energy energy broadening factor of 0.2 meV. The intensity in (a) was multiplied by a factor 0.25 to match the scale of (b)–(c). (d) Elastic magnetic scattering  $-0.5 \le E \le 0.5$  meV of Na<sub>2</sub>TbO<sub>3</sub> obtained by subtracting T = 55 K data from T = 20 K (black dots). The red line and vertical black ticks are the result of a Rietveld refinement using a  $k_m = 0$  propagation vector. (e) Momentum dependence of the low-energy inelastic signal  $0.9 \le E \le 4$  meV (black dots) and comparison to linear spin-wave-theory predictions for optimized parameters (red line). (f)–(j) Inelastic neutron-scattering results from Na<sub>2</sub>PrO<sub>3</sub> at T = 1.5 K using (f)  $E_i = 8$  meV, T = 55 K subtracted, and normalized to the absolute units. Comparison to linear spin-wave-theory predictions with optimized parameters for (g) a  $J_1$  XXZ model with  $\Delta = 1.22$  ( $J_1 = 1.06$ meV), (h) a  $J_1-J'_1$  XXZ model with  $\Delta = 1.26$  and  $J'_1 = 0.85J_1$  ( $J_1 = 1.1$  meV), and (i) a  $J_1-K$  model with  $K = 0.18J_1$  ( $J_1 = 1.1$  meV). (i) Momentum dependence of the low-energy inelastic signal  $0.9 \le E \le 1.4$  meV (black dots) and comparison to linear spin-wave-theory predictions for optimized parameters from the  $J_1-J'_1$  XXZ (solid red line) and  $J_1-K$  models (dashed blue line). To avoid oversubtraction, the cut is taken from empty cryostat subtracted data while (f) shows a temperature-subtracted spectrum.

[Fig. 3(j)] shows overall agreement, except between Q = 0.25 Å<sup>-1</sup> and 1 Å<sup>-1</sup> where background contributions are large. All models fail to account for the apparent continuum at the top of the band (see Ref. [27], Sec. S8), which we attribute to the presence of quantum fluctuations given recent studies on the honeycomb magnets YbCl<sub>3</sub> and YbBr<sub>3</sub> [23,52], although single-crystal studies will be necessary to determine the relative importance of these terms in detail.

In conclusion, the 1.1(1) meV energy scale of the Heisenberg exchange interaction in Na<sub>2</sub>PrO<sub>3</sub> is surprisingly large for a lanthanide system that is reflected in the unusually large 230 -meV scale of the CEF and the necessity to employ an intermediate-coupling scheme to explain the small effective moment per  $Pr^{4+}$ . Comparable CEF and SOC energy scales have also been proposed for KCeO<sub>2</sub> [53] and observed in RuCl<sub>3</sub> under pressure [54] where the impact of intermediate coupling on exchange was shown to favor antiferromagnetic Heisenberg interactions. Similar effects can hypothesized to be the origin of the considerably weaker antiferromagnetic Kitaev interaction, extracted by modeling the magnetic fluctuations of Na<sub>2</sub>PrO<sub>3</sub> when compared to theoretical and *ab initio* calculations [24]. The absence of visible magnetic Bragg

peaks in Na<sub>2</sub>PrO<sub>3</sub> as well as the missing entropy of around  $0.3R \ln 2$  are two avenues for future inquiry. In particular, the observed low moment for the Pr<sup>4+</sup> ion has important implications for the understanding and application of high-valence lanthanide ions in magnetic materials, since, akin to observations in high-valence actinides, this moment is derived from competition between SOC and CEF and necessitates the use of an intermediate coupling scheme to capture the observed temperature dependence [55,56].

We thank Zhiling Dun for numerous helpful discussions and are indebted to Andrew Boothroyd for refining the definition of the Wybourne operators in an initial version of this paper. The work of A.R. and H.S.L. at Georgia Tech was supported by the Beckman Foundation as part of a Beckman Young Investigator Award to H.S.L. The work of M.D. and M.M. at Georgia Tech was supported by the National Science Foundation through Grant No. NSF-DMR-1750186. This research used resources at the High Flux Isotope Reactor and the Spallation Neutron Source, a DOE Office of Science User Facility operated by the Oak Ridge National Laboratory.

- [2] C. Broholm, R. Cava, S. Kivelson, D. Nocera, M. Norman, and T. Senthil, Science 367, eaay0668 (2020).
- [3] R. Sibille, E. Lhotel, V. Pomjakushin, C. Baines, T. Fennell, and M. Kenzelmann, Phys. Rev. Lett. 115, 097202 (2015).
- [4] K. Kimura, S. Nakatsuji, J. Wen, C. Broholm, M. Stone, E. Nishibori, and H. Sawa, Nat. Commun. 4, 1934 (2013).
- [5] J. A. M. Paddison, M. Daum, Z. Dun, G. Ehlers, Y. Liu, M. B. Stone, H. Zhou, and M. Mourigal, Nat. Phys. 13, 117 (2017).
- [6] M. M. Bordelon, E. Kenney, C. Liu, T. Hogan, L. Posthuma, M. Kavand, Y. Lyu, M. Sherwin, N. P. Butch, C. Brown, M. J. Graf, L. Balents, and S. D. Wilson, Nat. Phys. 15, 1058 (2019).
- [7] Z. Dun, X. Bai, J. A. M. Paddison, E. Hollingworth, N. P. Butch, C. D. Cruz, M. B. Stone, T. Hong, F. Demmel, M. Mourigal, and H. Zhou, Phys. Rev. X 10, 031069 (2020).
- [8] R. Sibille, N. Gauthier, E. Lhotel, V. Porée, V. Pomjakushin, R. A. Ewings, T. G. Perring, J. Ollivier, A. Wildes, C. Ritter, T. C. Hansen, D. A. Keen, G. J. Nilsen, L. Keller, S. Petit, and T. Fennell, Nat. Phys. 16, 546 (2020).
- [9] A. Kitaev, Ann. Phys. **321**, 2 (2006).
- [10] J. Chaloupka, G. Jackeli, and G. Khaliullin, Phys. Rev. Lett 105, 027204 (2010).
- [11] Y. Singh, S. Manni, J. Reuther, T. Berlijn, R. Thomale, W. Ku, S. Trebst, and P. Gegenwart, Phys. Rev. Lett. 108, 127203 (2012).
- [12] Y. Motome, R. Sano, S. Jang, Y. Sugita, and Y. Kato, J. Phys.: Condens. Matter. 32, 404001 (2020).
- [13] H. Takagi, T. Takayama, G. Jackeli, G. Khaliullin, and S. E. Nagler, Nat. Rev. Phys. 1, 264 (2019).
- [14] A. Banerjee, C. Bridges, J.-Q. Yan, A. Aczel, L. Li, M. Stone, G. Granroth, M. Lumsden, Y. Yiu, and J. Knolle, Nat. Mater. 15, 733 (2016).
- [15] A. Banerjee, J. Yan, J. Knolle, C. A. Bridges, M. B. Stone, M. D. Lumsden, D. G. Mandrus, D. A. Tennant, R. Moessner, and S. E. Nagler, Science 356, 1055 (2017).
- [16] S. K. Choi, R. Coldea, A. N. Kolmogorov, T. Lancaster, I. I. Mazin, S. J. Blundell, P. G. Radaelli, Y. Singh, P. Gegenwart, K. R. Choi, S. -W. Cheong, P. J. Baker, C. Stock, and J. Taylor, Phys. Rev. Lett 108, 127204 (2012).
- [17] K. Kitagawa, T. Takayama, Y. Matsumoto, A. Kato, R. Takano, Y. Kishimoto, S. Bette, R. Dinnebier, G. Jackeli, and H. Takagi, Nature 554, 341 (2018).
- [18] T. Takayama, A. Kato, R. Dinnebier, J. Nuss, H. Kono, L. S. I. Veiga, G. Fabbris, D. Haskel, and H. Takagi, Phys. Rev. Lett. 114, 077202 (2015).
- [19] R. Sano, Y. Kato, and Y. Motome, Phys. Rev. B 97, 014408 (2018).
- [20] H. Liu and G. Khaliullin, Phys. Rev. B 97, 014407 (2018).
- [21] F.-Y. Li, Y.-D. Li, Y. Yu, A. Paramekanti, and G. Chen, Phys. Rev. B 95, 085132 (2017).
- [22] J. G. Rau and M. J. P. Gingras, Phys. Rev. B 98, 054408 (2018).
- [23] G. Sala, M. B. Stone, B. K. Rai, A. F. May, P. Laurell, V. O. Garlea, N. P. Butch, M. D. Lumsden, G. Ehlers, G. Pokharel, A. Podlesnyak, D. Mandrus, D. S. Parker, S. Okamoto, B. G. Halasz, and A. D. Christianson, Nat. Commun. 12, 1 (2021).
- [24] S.-H. Jang, R. Sano, Y. Kato, and Y. Motome, Phys. Rev. B 99, 241106(R) (2019).
- [25] T. P. Gompa, A. Ramanathan, N. T. Rice, and H. S. La Pierre, Dalton Trans. 49, 15945 (2020).

[26] S. G. Minasian, E. R. Batista, C. H. Booth, D. L. Clark, J. M.

PHYSICAL REVIEW B 103, L121109 (2021)

- Keith, S. A. Kozimor, W. W. Lukens, R. L. Martin, D. K. Shuh, S. C. E. Stieber, T. Tylisczcak, and X.-d. Wen, J. Am. Chem. Soc. **139**, 18052 (2017).
- [27] See Supplemental Material at http://link.aps.org/supplemental/ 10.1103/PhysRevB.103.L121109 for sample preparation, INS, ac susceptibility, specific heat and spin wave analysis.
- [28] A. Ramanathan, J. E. Leisen, and H. S. La Pierre, Inorg. Chem. 60, 1398 (2021).
- [29] G. E. Granroth, A. I. Kolesnikov, T. E. Sherline, J. P. Clancy, K. A. Ross, J. P. C. Ruff, B. D. Gaulin, and S. E. Nagler, J. Phys.: Conf. Series 251, 012058 (2010).
- [30] M. B. Stone, J. L. Niedziela, D. L. Abernathy, L. DeBeer-Schmitt, G. Ehlers, O. Garlea, G. E. Granroth, M. Graves-Brook, A. I. Kolesnikov, A. Podlesnyak, and B. Winn, Rev. Sci. Instrum. 85, 045113 (2014).
- [31] O. Arnold, J. Bilheux, J. Borreguero, A. Buts, S. Campbell, L. Chapon, M. Doucet, N. Draper, R. F. Leal, M. Gigg, V. Lynch, A. Markvardsen, D. Mikkelson, R. Mikkelson, R. Miller, K. Palmen, P. Parker, G. Passos, T. Perring, P. Peterson, S. Ren, M. Reuter, A. Savici, J. Taylor, R. Taylor, R. Tolchenov, W. Zhou, and J. Zikovsky, Nucl. Instrum. Methods A 764, 156 (2014).
- [32] C.-K. Loong, L. Iton, and M. Ozawa, Physica B **213**, 640 (1995).
- [33] R. Senesi, D. Flammini, A. I. Kolesnikov, É. D. Murray, G. Galli, and C. Andreani, J. Chem. Phys. 139, 074504 (2013).
- [34] S. Kern, C.-K. Loong, and G. H. Lander, Phys. Rev. B 32, 3051 (1985).
- [35] U. Walter, J. Phys. Chem. Solids 45, 401 (1984).
- [36] B. G. Wybourne, Spectroscopic Properties of Rare Earths (Interscience, New York, 1965).
- [37] V. Kaufman and J. Sugar, J. Nat. Bu. Stand. Sect. A 71A, 583 (1967).
- [38] Y. Hinatsu and N. Edelstein, J. Solid State Chem. **112**, 53 (1994).
- [39] A. Boothroyd, Spectre, a program for calculating spectroscopic properties of rare earth ions in crystals (1990–2014).
- [40] J. Chaloupka, G. Jackeli, and G. Khaliullin, Phys. Rev. Lett 110, 097204 (2013).
- [41] M. Bickel, G. Goodman, L. Soderholm, and B. Kanellakopulos, J. Solid State Chem. 76, 178 (1988).
- [42] Y. Hinatsu and Y. Doi, J. Alloys Compd. 418, 155 (2006).
- [43] B. Bleaney, HPCRE 11, 323 (1988).
- [44] R. J. Elliott and K. Stevens, Proc. R. Soc. Lond. A. Math. Phys. Sci. 218, 553 (1953).
- [45] J. A. M. Paddison, H. S. Ong, J. O. Hamp, P. Mukherjee, X. Bai, M. G. Tucker, N. P. Butch, C. Castelnovo, M. Mourigal, and S. Dutton, Nat. Commun. 7, 13842 (2016).
- [46] M. Mourigal, W. T. Fuhrman, J. P. Sheckelton, A. Wartelle, J. A. Rodriguez-Rivera, D. L. Abernathy, T. M. McQueen, and C. L. Broholm, Phys. Rev. Lett 112, 027202 (2014).
- [47] V. O. Garlea, B. C. Chakoumakos, S. A. Moore, G. B. Taylor, T. Chae, R. G. Maples, R. A. Riedel, G. W. Lynn, and D. L. Selby, Appl. Phys. A 99, 531 (2010).
- [48] A. S. Wills, Physica B (Amsterdam, Neth.) **276**, 680 (2000).
- [49] J. Rodríguez-Carvajal, Physica B (Amsterdam, Neth.) 192, 55 (1993).

- [50] S. Petit, Collection SFN 12, 105 (2011).
- [51] S. Toth and B. Lake, J. Phys: Condens. Matter 27, 166002 (2015).
- [52] C. Wessler, B. Roessli, K. W. Krämer, B. Delley, O. Waldmann, L. Keller, D. Cheptiakov, H. B. Braun, and M. Kenzelmann, npj Quant. Mater. 5, 85 (2020).
- [53] M. S. Eldeeb, T. Petersen, L. Hozoi, V. Yushankhai, and U. K. Rößler, Phys. Rev. Mater. 4, 124001 (2020).
- [54] G. Bastien, G. Garbarino, R. Yadav, F. J. Martinez-Casado, R. Beltrán Rodríguez, Q. Stahl, M. Kusch, S. P. Limandri, R. Ray, P. Lampen-Kelley, D. G. Mandrus, S. E. Nagler, M. Roslova, A. Isaeva, T. Doert, L. Hozoi, A. U. B. Wolter, B. Büchner, J. Geck, and J. van den Brink, Phys. Rev. B 97, 241108(R) (2018).
- [55] N. Magnani, P. Santini, G. Amoretti, and R. Caciuffo, Phys. Rev. B 71, 054405 (2005).
- [56] L. Escalera-Moreno, J. J. Baldoví, A. Gaita-Ariño, and E. Coronado, Inorg. Chem. 58, 11883 (2019).