

**Spin transport in different oxide phases of copper**Rongxin Sha<sup>1,2</sup>, Qinxin Liu<sup>3</sup>, Mengyi Wang<sup>1,2</sup>, Min Liu<sup>4</sup>, Yibo Peng<sup>4</sup>, Ziyang Zhang<sup>1,2</sup>, Ailiang Zou<sup>1,2</sup>, Yuekui Xu<sup>1,2</sup>, Xue Jiang<sup>3,\*</sup> and Zhiyong Qiu<sup>1,2,†</sup><sup>1</sup>Key Laboratory of Materials Modification by Laser, Ion, and Electron Beams (Ministry of Education), School of Materials Science and Engineering, Dalian University of Technology, Dalian, 116024 Liaoning, China<sup>2</sup>Key Laboratory of Energy Materials and Devices (Liaoning Province), School of Materials Science and Engineering, Dalian University of Technology, Dalian, 116024 Liaoning, China<sup>3</sup>School of Physics, Dalian University of Technology, Dalian, 116024 Liaoning, China<sup>4</sup>School of Mechanical Engineering, Dalian Jiaotong University, Dalian, 116024 Liaoning, China

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In this study, spin transport was directly compared in two types of copper oxides: The first is antiferromagnetic CuO, in which  $\text{Cu}^{2+}$  has one unpaired spin in the  $3d$  orbital; the second is diamagnetic  $\text{Cu}_2\text{O}$  with a  $\text{Cu}^+$  ion having a fully filled  $3d$  orbital. The results indicate that CuO exhibits good spin conductivity, whereas  $\text{Cu}_2\text{O}$  is a spin insulator. This indicates that possessing unpaired spins may be an important characteristic of good spin conductors and that copper oxides may have the potential to be spin manipulators.

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Spin can be transported via an insulator even in the absence of free electron motion, implying that it is not affected by the Joule heating problem [1]. Since Kajiwara *et al.* demonstrated spin transport in insulating yttrium iron garnet (YIG) [2], electrical spin in insulators, rather than electrical charge, has been considered to serve as the carrier of information and energy in spin-based devices [3]. It has been observed that spin can be transported in various insulators [4–8], some of which may even enhance its efficiency [9–11]. The study of spin transport in insulators is important for developing insulating spin-based devices and is a central topic in spintronics [4,12,13]. Therefore, one of the most important challenges in spintronics is to understand the mechanisms and dominant characteristics of spin transport in insulating systems.

Spin transport has been actively investigated and discussed in the context of various insulating systems [4–17]. For nonmagnetic insulators, spin transport follows the tunneling mechanism by which most nonmagnetic insulators are spin insulators [15]. For magnetic insulators, the magnetic excitations can act as spin carriers; thus, many magnetic insulators exhibit good spin conductivities [3,18]. Furthermore, spin transport has been found to be sensitive to specific properties of magnetic materials. Spin susceptibility, for example, was found to be a governing factor for spin transport efficiency in an antiferromagnetic insulator [8,9]. The Néel vector is another explicit factor concerning spin transport in an antiferromagnetic insulator that has a definite uniaxial Néel vector and strong anisotropy energy [19]. However, the relationship between spin transport and intrinsic characteristics of the ambient material, such as phase, structure, defects, and even electronic configuration of the ions, is still rarely investigated.

In the present study, we focus on the influence of electronic configurations of ions on the spin transport efficiency in materials. Two types of copper oxides were selected in this study; although both of them are composed of copper and oxygen, the copper ions have different electronic configurations [20]. In CuO, the  $\text{Cu}^{2+}$  ion has one unpaired spin in the  $3d$  orbital [Fig. 1(a)] [20], whereas in  $\text{Cu}_2\text{O}$ , the  $\text{Cu}^+$  ion has a fully filled  $3d$  orbital [Fig. 1(b)] [20]. It is well known that electronic configuration cannot be separated from the other materials characteristics, such as magnetic property and crystal structure. Thus, CuO and  $\text{Cu}_2\text{O}$  demonstrate different characteristics, where monoclinic CuO [21,22] is antiferromagnetic [23] while cubic  $\text{Cu}_2\text{O}$  [21] is diamagnetic [24]. By comparing the spin transport in these two oxides, it is possible to obtain information about the influence of metallic ions having different electronic configurations on spin transport.

A trilayer spin pumping structure [25] was used to study spin transport, wherein the copper oxide layer was sandwiched between a YIG layer and a heavy-metal (Pt) layer [Fig. 2(a)]. Within this structure, the YIG layer acted as a spin generator while the Pt layer acted as a spin detector [8,26]. Our results show that spin currents can be conducted through a 5 nm thick CuO film [Fig. 1(c)], which indicates that CuO is a good spin conductor. Contrarily, the spin currents were completely blocked by a 5 nm thick  $\text{Cu}_2\text{O}$  film [Fig. 1(d)], indicating that  $\text{Cu}_2\text{O}$  is a spin insulator. The different spin conducting properties between CuO and  $\text{Cu}_2\text{O}$  can thus be attributed to the electronic configurations of their copper ions, which can also be related to their magnetic properties and crystal structures.

**II. EXPERIMENT**

YIG/CuO/Pt and YIG/ $\text{Cu}_2\text{O}$ /Pt trilayer devices were developed as the target samples [Figs. 1(c) and 1(d)], and a fundamental YIG/Pt bilayer device was prepared as the control sample. Single-crystal YIG was grown on a  $\text{Gd}_3\text{Ga}_5\text{O}_{12}$

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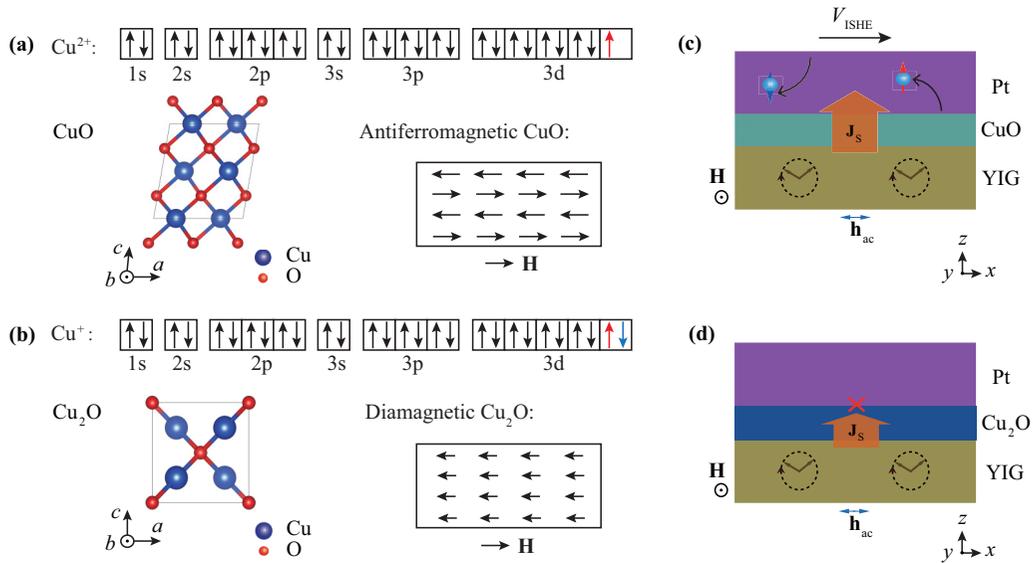


FIG. 1. (a) The electronic structure, crystal structure, and magnetic property of CuO. (b) The electronic structure, crystal structure, and magnetic property of  $\text{Cu}_2\text{O}$ . (c) The concept of the spin transport in the YIG/CuO/Pt trilayer device.  $\mathbf{J}_s$  denotes spin currents injected from the YIG layer into the Pt layer through the CuO layer by spin pumping, which is detected as a voltage signal  $V_{\text{ISHE}}$  via the inverse spin Hall effect in the Pt layer. (d) The concept of the spin transport in the YIG/ $\text{Cu}_2\text{O}$ /Pt trilayer device.

substrate by a liquid-phase epitaxy method. The YIG substrates of all the samples were cut from the same wafer to minimize differences among the samples. Copper oxide films of 5 nm thickness were deposited on the YIG layer from a metallic copper target in a mixture of Ar and  $\text{O}_2$  gases using

a reactive magnetron sputtering system at room temperature. The total pressure of the mixed gas was set to 3 Pa, in which  $p(\text{O}_2)/p(\text{O}_2 + \text{Ar})$  was 33%. A post-annealing process was employed to modify the chemical valences of the copper ions, by which CuO was obtained at 500 °C after 1 h whereas  $\text{Cu}_2\text{O}$  was generated at 700 °C after 1 h. Both these films were annealed in the Ar and  $\text{O}_2$  gas mixture under 3 Pa for CuO and  $5 \times 10^{-5}$  Pa for  $\text{Cu}_2\text{O}$ ; a 10 nm thick Pt film was then deposited on both samples in the same sputtering chamber.

CuO and  $\text{Cu}_2\text{O}$  were then identified using x-ray diffraction measurements [Fig. 2(b)]. The monoclinic CuO film shows a single sharp (11-1) pattern, and the cubic  $\text{Cu}_2\text{O}$  film shows both the (111) and (200) patterns, suggesting that the CuO film exhibits a preferred orientation whereas the  $\text{Cu}_2\text{O}$  film exhibits random orientation. As the full width at half maximum of CuO and  $\text{Cu}_2\text{O}$  films are almost the same, their nominal grain sizes should be similar. Therefore, the discrepancy of peak intensity between the films can mainly be attributed to the different orientations.

Spin transport in different devices were studied using a spin pumping setup [Fig. 2(a)] [8,26]. The trilayer device was placed at the end of a short-end coplanar waveguide, using which microwaves were applied at a frequency of 6 GHz [Fig. 2(a)]. The microwaves and an external magnetic field  $H$  thus excited ferromagnetic resonance (FMR) in the YIG layer. Then, spin currents were generated and injected into the copper oxide layers by the spin pumping effect [25]. The spin currents that are conducted through the middle oxide layer will be detected as voltage signals via the inverse spin Hall effect (ISHE) in the Pt layer [27].

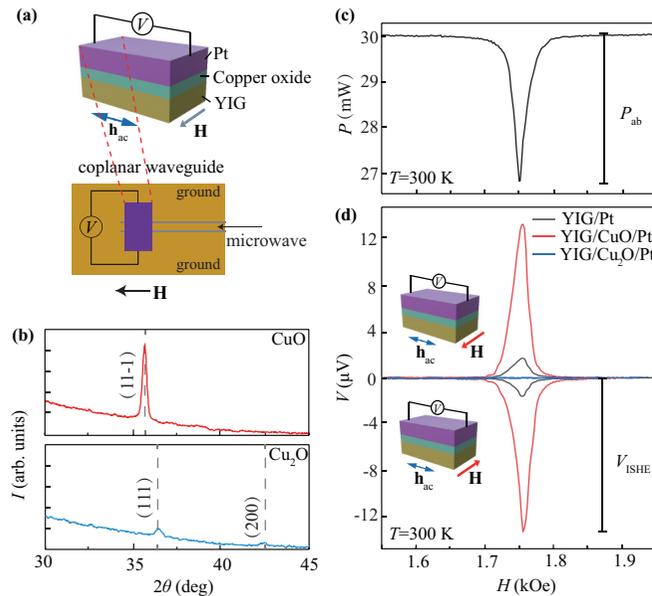


FIG. 2. (a) The schematic of sample and experimental setup of spin pumping effect. (b) The x-ray diffraction patterns of the CuO and  $\text{Cu}_2\text{O}$  films displayed on a linear scale. (c) Magnetic field ( $H$ ) dependence of microwave absorption spectrum for the YIG/Pt, YIG/CuO (5 nm)/Pt, and YIG/ $\text{Cu}_2\text{O}$  (5 nm)/Pt devices at  $T = 300$  K. (d) Magnetic field ( $H$ ) dependence of electric voltage ( $V$ ) detected in the YIG/Pt, YIG/CuO (5 nm)/Pt, and YIG/ $\text{Cu}_2\text{O}$  (5 nm)/Pt devices at  $T = 300$  K.

### III. RESULTS AND DISCUSSION

A typical microwave absorption spectrum is shown in Fig. 2(c), where the microwave absorption peak can be

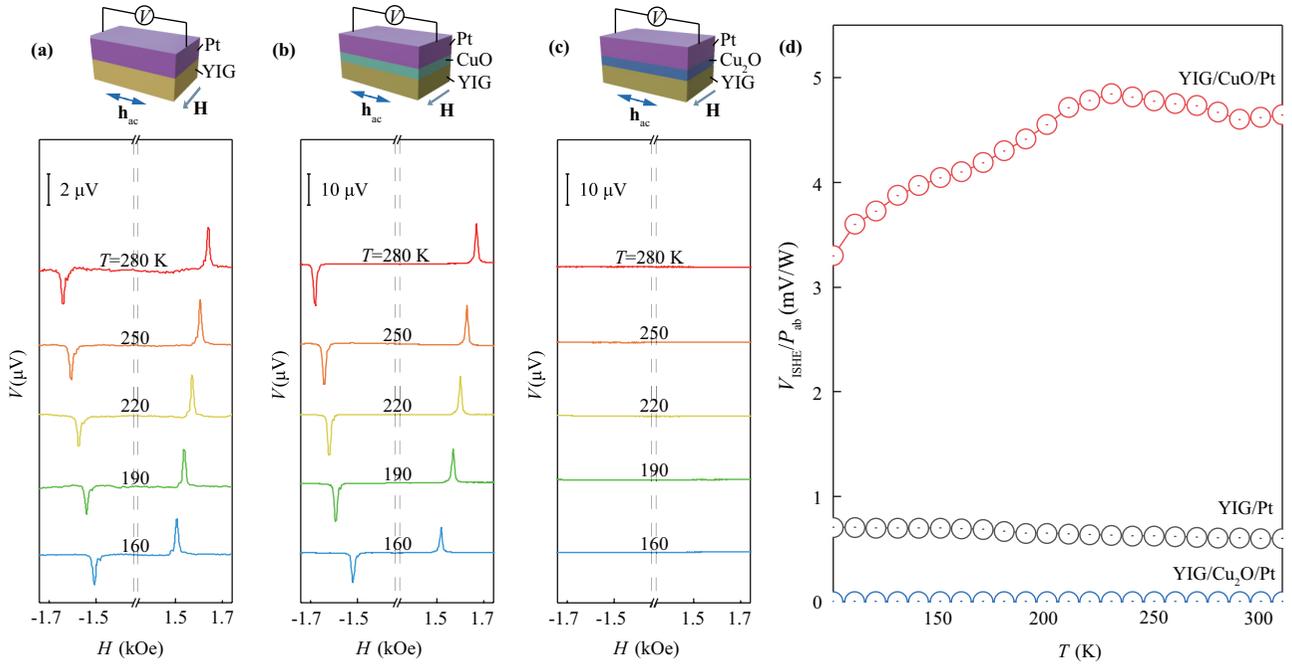


FIG. 3. (a)–(c) Magnetic field ( $H$ ) dependence of electric voltage ( $V$ ) detected in the YIG/Pt, YIG/CuO (5 nm)/Pt, and YIG/Cu<sub>2</sub>O (5 nm)/Pt devices at various temperatures with evenly spaced offset in vertical axis. (d) Temperature dependence of  $V_{\text{ISHE}}/P_{\text{ab}}$  for the YIG/Pt, YIG/CuO (5 nm)/Pt, and YIG/Cu<sub>2</sub>O (5 nm)/Pt devices.

observed at  $H_{\text{FMR}} = 1.76$  kOe when  $T = 300$  K; here,  $H_{\text{FMR}}$  corresponds to the FMR of the YIG layer. The microwave absorption power  $P_{\text{ab}}$  was defined as the height of the microwave absorption peak [Fig. 2(c)]. For all samples, the positions and heights of the microwave absorption peaks are almost similar because the YIG substrates were cut from the same wafer. Therefore, the YIG substrates can be considered as stable spin generators in all samples. With regard to the magnetic field ( $H$ ) dependence of electric voltage ( $V$ ), the voltage peaks were obtained at the same  $H_{\text{FMR}}$  [Fig. 2(d)]. Here, the electric voltage  $V$  was set to zero where the FMR was not excited (see Supplemental Material Fig. 1 [28]); this is a commonly practiced data processing method for spin pumping [8,9]. The signs of the voltage peaks were reversed when the external magnetic field was reversed, suggesting that the voltage peaks are the induced ISHE signals in the Pt layer by spin currents pumped from the YIG layer. Herein, we define the height of the voltage peak as the magnitude of the spin pumping signal  $V_{\text{ISHE}}$  [Fig. 2(d)].

CuO, with one unpaired spin in  $\text{Cu}^{2+}$ , exhibits spin conductive behavior. The  $V_{\text{ISHE}}$  of the YIG/CuO/Pt trilayer device is approximately  $12 \mu\text{V}$  at  $T = 300$  K [Fig. 2(d)]. This indicates that spin currents are conducted through the 5 nm thick CuO film. Furthermore, the  $V_{\text{ISHE}}$  of the YIG/CuO/Pt trilayer device is almost six times the magnitude of that of the YIG/Pt bilayer device, thereby implying that the CuO middle layer enhanced the spin transport efficiency at the YIG/Pt interface. Spin transport enhancement similar to the CuO middle layer in this study was also reported for a NiO middle layer in a previous work [9]. Currently, this enhancement phenomenon cannot be explained using existing theories and needs further investigation by researchers. In contrast to CuO, Cu<sub>2</sub>O without the unpaired spin in  $\text{Cu}^+$  acts as a spin insulator because

no voltage peaks are observed in the YIG/Cu<sub>2</sub>O/Pt trilayer device. It is possible that the magnitudes of any existing voltage peaks might be less than the 30 nV noise level of our experiment, indicating that such spin currents were blocked by the 5 nm thick Cu<sub>2</sub>O layer.

The magnetic field  $H$  dependence of the electric voltage  $V$  was measured at various temperatures for the YIG/Pt, YIG/CuO/Pt, and YIG/Cu<sub>2</sub>O/Pt devices [Figs. 3(a), 3(b), and 3(c), respectively]. Voltage peaks can be observed in both the YIG/Pt and YIG/CuO/Pt devices at all temperatures. The positions of these peaks shift toward the direction of low magnetic field with decreasing temperatures, which corresponds to the dependence of the temperature dependence on the FMR condition in the YIG layer [8,29]. Furthermore, the signs of these voltage peaks are reversed by reversing the applied magnetic field, thereby confirming that the voltage peaks are related to the spin currents generated from the YIG layer via the spin pumping effect. On the contrary, no voltage peaks were observed in the YIG/Cu<sub>2</sub>O/Pt trilayer device at any temperature.

The temperature dependences of spin pumping signals  $V_{\text{ISHE}}$  of the YIG/Pt, YIG/CuO/Pt, and YIG/Cu<sub>2</sub>O/Pt devices are shown in Fig. 3(d). Here,  $V_{\text{ISHE}}$  is normalized by the microwave absorption power  $P_{\text{ab}}$  as  $V_{\text{ISHE}}/P_{\text{ab}}$ . In the YIG/Pt bilayer device, the  $V_{\text{ISHE}}/P_{\text{ab}}$  is almost constant over the entire range of temperatures, which is consistent with trends noted in other published reports [2,30]. However, by inserting a 5 nm thick CuO layer between the YIG and Pt layers, a clear peak of  $V_{\text{ISHE}}/P_{\text{ab}}$  was observed at  $T = 230$  K, which is approximately equal to the Néel temperature of CuO. The observation that spin transport efficiency is maximized at the Néel temperature is consistent with that reported in previous studies [8,10]. Meanwhile,  $V_{\text{ISHE}}$  is suppressed on both sides of the

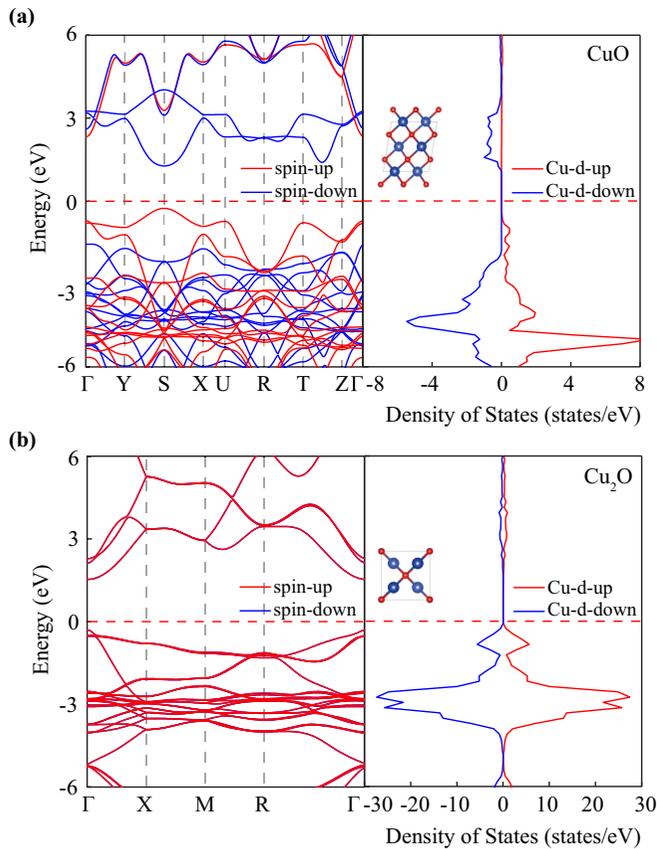


FIG. 4. (a) The band structure and density of states for CuO. (b) The band structure and density of states for Cu<sub>2</sub>O. The red dashed lines indicate the Fermi level.

Néel temperature, which may be because the main carriers of spins are the thermally excited magnons in antiferromagnets [8]. Conversely, spin currents are blocked by the 5 nm thick Cu<sub>2</sub>O layer at all temperatures.

CuO and Cu<sub>2</sub>O exhibit different magnetic properties and structures owing to the electrical configurations of their ions. As seen from the calculated band structures using the HSE06 functional [31] in Fig. 4, both CuO and Cu<sub>2</sub>O are typical electrical insulating materials with band gaps of 2.59 eV and 1.83 eV, respectively. In CuO, the spin-up and spin-down band

structures are different around the Fermi level. By comparing the energies of several typical types of magnetic ordering, we prove that the Cu atoms in CuO prefer the antiferromagnetic ordering. The antiferromagnetic ground state can be explained as a consequence of the unpaired spin in the  $d_{x^2-y^2}$  orbital of the Cu<sup>2+</sup> ion. On the contrary, Cu<sub>2</sub>O exhibits diamagnetic properties. The spin-up and spin-down band structures are almost identical, and the spin band gap of Cu<sub>2</sub>O is equivalent to its electron band gap. As a result, the spins are decoupled from each other in Cu<sub>2</sub>O.

We attribute the different spin transport properties of CuO and Cu<sub>2</sub>O to their different electronic configurations of copper ions. In CuO, the unpaired spins couple with each other, and the collective excitation acts as the carrier for the transported spins. Spin transport in such antiferromagnetic systems has been reported in several existing studies [4,8]. In Cu<sub>2</sub>O, the spins are decoupled from each other, which prevents coherent excitation. As a result, the diamagnetic Cu<sub>2</sub>O exhibits spin insulativity. Our study experimentally shows that unpaired spins are an important prerequisite for a good spin conductor. The observation that spin transport is affected by the electronic configuration of the ions offers a unique approach to realizing a new type of spin-current switch for a spin current transistor or memory.

#### IV. SUMMARY

In summary, our study found that possessing unpaired spins may be an important characteristic of a spin conductor. We compared spin transport in two different oxide phases of copper and found that CuO was a good spin conductor whereas Cu<sub>2</sub>O was a spin insulator, which confirmed that spin transport was sensitive to electronic configurations of the constituent ions. Our results show the physical mechanism of spin transport in insulators and provide an approach for the manipulation of spin-based devices.

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