Influence of Pr substitution on the physical properties of the $Ce_{1-x}Pr_xCoGe_3$ system: Combined experimental and first-principles study

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We present the results of our investigations of physical properties for the novel $Ce_{1-x}Pr_xCoGe_3$ system performed with a number of experimental methods: magnetic susceptibility, specific heat, electrical resistivity, magnetoresistance, and thermoelectric power. Moreover, the electronic structure was studied by means of photoelectron spectroscopy measurements and first-principles calculations. All investigated compositions of the $Ce_{1-x}Pr_xCoGe_3$ series crystallize in the tetragonal BaNiSn₃-type structure. The lattice parameters and unit cell volumes decrease with increasing Pr concentration. On the basis of the measurements taken, a preliminary magnetic phase diagram was created. Continuous suppression of the long-range magnetic ordering was observed with an increase of Pr concentration. The critical Pr concentration for magnetic moment ordering was determined from linear extrapolation of the ordering temperature versus x to the lowest temperatures (T = 0 K) and is equal to about 0.66. Based on the first-principles calculations, we show how the substitution of Pr for Ce affects the electronic structure and magnetic properties of the considered alloys. Within a single model, we take into account the magnetic ordering, fully relativistic effects, and Hubbard U repulsion on Ce and Pr. The impact of Hubbard U on the results of calculations is also discussed. We present the valence band analysis, Mulliken electronic population analysis, and calculated electronic specific heat coefficients. For CeCoGe₃, it is found that the + + -- configuration of magnetic moments on Ce is slightly more stable than the + - +- one, and also that the calculated value of total magnetic moment on Ce (including spin and orbital parts) is in good agreement with the measurements.

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I. INTRODUCTION

Most of the interesting properties of the strongly correlated systems are connected with the presence of the felectrons. Extensive experimental and theoretical efforts focus on studying the unconventional superconductivity and other effects, like, for example, the heavy fermion state, deviations from the Fermi liquid behavior, and competition between the RKKY (Ruderman-Kittel-Kasuya-Yosida) and Kondo interactions [1-6]. In this work, we will focus on noncentrosymmetric structures that are of great scientific interest, because the lack of inversion symmetry is a key factor in the formation of unconventional superconductivity. One of widely studied crystal structures is BaNiSn₃-type (space group I4mm, No. 107). Many of compounds crystallizing in this structure are composited as RTX_3 , where R – rare-earth, T – transition metal, and X – Si, Ge or Al. The examples are EuTGe₃ (T = Co, Ni, Rh, Pd, Ir, Pd) [7], $RCoSi_3$ (R =Pr, Nd, Sm) [8], and NdCoGe₃ [9]. A wide group of compounds are those containing Ce. The exemplary compounds are: CeRhSi₃ [10], CeIrSi₃ [10], CeRhGe₃ [10], CeIrGe₃ [10], $CeCuAl_3$ [11], and $CeAuAl_3$ [12].

One of the most interesting RTX_3 compound is CeCoGe₃, with three magnetic phase transitions at $T_{N1} = 21$ K, $T_{N2} =$ 12 K, and $T_{N3} = 8$ K [13]. For this compound, three metamagnetic transitions at $\mu_0 H_{c1} = 0.19$ T, $\mu_0 H_{c2} = 0.84$ T, and $\mu_0 H_{c3} = 3.0$ T were observed for $H \parallel [001] [13]$. The electronic specific heat coefficient value for this compound is $\gamma = 32 \text{ mJ mol}^{-1} \text{ K}^{-2}$. The magnetic structure of each of the magnetic phases described by Smidman et al. by means of the neutron diffraction experiment [14]. CeCoGe₃ compound undergoes superconducting transition under the pressure $p_{sc} =$ 5.5 GPa at temperature $T_{sc} = 0.7$ K [15]. After substitution of Ge with Si the CeCoGe_{3-x}Si_x series exhibits a quantum critical point (QCP) for the critical concentration $x_c = 1.5$ [16,17]. Even more complicated evolution of magnetism occurs in the system $CeCo_{1-x}Fe_xGe_3$ [18–20], in which the predominant ferro- or antiferromagnetic contributions change as the Fe content increases.

Another interesting compound of BaNiSn₃-type structure is PrCoGe₃. It is a paramagnet with a low value of the electronic specific heat coefficient $\gamma = 6.1$ mJ mol⁻¹ K⁻² [9]. Analysis of magnetic susceptibility with the Curie-Weiss law indicated the Pr³⁺ ion state without Co and Ge contributions to the effective magnetic moment [9]. Moreover, theoretical calculations and de Haas-van Alphen experiment revealed identical Fermi surface topologies for PrCoGe₃ and LaCoGe₃

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compounds [21]. The authors suggest that the Pr f electrons do not contribute to the Fermi surface and increase the cyclotron mass, which is for PrCoGe₃ nearly twice as large as for LaCoGe₃. More interestingly, considering similarities to LaCoGe₃, the two Pr 4f electrons might be in a low-spin state caused by strong interactions with the crystal electric field (CEF). The metamagnetic transition observed at the magnetic field value of 50 T and 1.3 K changes the CEF scheme [9], which indicates possible metaorbital transition, which is predicted, for example, for CeCu₂Si₂ compound [22]. Therefore, the modification of the local surroundings of Pr ions might change their ground state, causing an increase in the hybridization of 4f electrons with the conduction band.

The aims of this paper are to investigate the effects of the substitution in the $Ce_{1-x}Pr_xCoGe_3$ system on the electronic structure and physical properties and to identify the role of the rare-earth elements in the magnetism of these alloys. Our experimental efforts are followed by first-principles calculations. In case of materials containing rare-earth elements, the simplest approaches based on density functional theory (DFT) are often insufficient. Even the simplest rare-earth materials, like α and γ Ce phases, are recently undergoing an in-depth study to determine the optimal approaches leading to the reliable results [23]. In our study, we will go beyond the generalized-gradient approximation (GGA) and apply the intra-atomic Hubbard U repulsion term (GGA + U). However, the application of GGA + U method for spin-polarized Ce systems raises a problem of an emergence of multiple solutions [23,24]. We will discuss how to find the ground-state solution anyway and how the value of Hubbard U parameters affects the results. In contrast to the previous theoretical works on CeCoGe₃ [20,25], the new model will include the antiferromagnetic ordering as observed at low temperatures. We will also present the DFT results for the terminal PrCoGe₃ composition and for the Ce_{0.5}Pr_{0.5}CoGe₃ alloy containing two types of rare-earth elements.

An important issue that has to be taken into consideration is the CEF on the Pr site in the temperature range of 10–30 K, which has been observed by many experimental methods [9]. It is known that the distribution of charge around an ion produces an electric field, which is experienced by the 4*f* electrons. The type of splitting of the ground state by the CEF depends in particular on the type of ion. It can provide additional contribution to the temperature dependencies of physical properties, e.g., specific heat. Usually, the contribution of Ce ions is observed in the range of 100–300 K. For example, for the CeCoGe₃ compound, the CEF energy levels of $\Delta_1 = 220$ K and $\Delta_2 = 315$ K have been determined by the use of the inelastic neutron scattering method [14].

II. METHODS

A. Experimental details

The polycrystalline samples were obtained by melting high purity elements several times in an arc furnace to ensure sample homogeneity. Final mass loss was less than 1%. Next, the sample ingots were wrapped in tantalum foil, encapsulated in evacuated quartz tubes, and annealed at 900 °C for 7 days. The crystal structure of prepared samples was investigated with x-ray diffraction (XRD) measurements performed on X'pert Pro PANalytical device with Cu K_{α} radiation source at room temperature. In order to test the physical properties of the $Ce_{1-x}Pr_xCoGe_3$ system, a number of experimental methods have been used. As the main measuring device we used a Quantum Design Physical Property Measurement System (QD PPMS) with appropriate options for specific measurements. Firstly, the zero field cooling (ZFC) and field cooling (FC) curves of magnetic susceptibility were measured with a vibrating sample magnetometer (VSM) module in the temperature range 2-300 K and at applied magnetic field value of 0.1 T. Hysteresis loops were measured at 2 K at magnetic field values up to 9 T. In the next step, specific heat measurements were performed in the temperature range 1.9-295 K without applied magnetic field and in the range of 1.9-40 K for various magnetic field values. Further investigations were focused on electrical resistivity and isothermal magnetoresistance, which were measured using the four probe method. The resistivity measurements were performed without applied magnetic field in the range of 2-300 K, while magnetoresistance was measured at magnetic field values up to 9 T for temperatures in the range of 2-30 K. Thermoelectric power data were collected using four probe method of the thermal transport option (TTO) in the temperature range 2-300 K. Finally, the x-ray photoelectron spectroscopy (XPS) measurements were performed with the use of PHI 5700/660 Physical Electronics spectrometer. The measured spectra were analyzed at room temperature using monochromatized Al K_{α} radiation (1486.6 eV). The clean surface of samples was obtained by in-situ fracturing. All procedures and measurements were performed in ultrahigh vacuum chamber (UHV) with base pressure of 10^{-10} Torr.

B. Computational details

We will present also the results of density functional theory (DFT) calculations. The models of CeCoGe₃, Ce_{0.5}Pr_{0.5}CoGe₃, and PrCoGe₃ are investigated using the fullpotential local-orbital scheme (FPLO version 18.00-52) [26]. The FPLO code is one of the DFT implementations characterized by the highest numerical accuracy [27]. Its precision comes, among the others, from the use of the full-potential approach, which does not introduce shape approximation to the crystalline potential and to the expansion of the extended states in terms of localized atomic-like basis orbitals [26,28]. The application of the full-potential method is particularly important for the 4f electron systems for which the results are strongly dependent on the quality of the potential [26]. Another crucial element of our approach is treating the relativistic effects in a full four-component formalism. The application of a fully relativistic (including spin-orbit coupling) approach significantly improves the description of 4f electrons, which are characterized by a high value of spin-orbit coupling. For the exchange-correlation potential, we choose the generalized-gradient approximation (GGA) in the Perdew-Burke-Ernzerhof form (PBE) [29]. For elements with an open 4f shell, like Ce or Pr, it is important to further improve the utilized approximation by applying Hubbard U intra-atomic repulsion term to the energy functional, resulting in LSDA + U (local spin density approximation) or GGA + U method

TABLE I. The lattice parameters of $Ce_{1-x}Pr_xCoGe_3$ compounds used for first-principles calculations.

Composition	<i>a</i> (Å)	<i>c</i> (Å)	Reference
CeCoGe ₃	4.320	9.835	[35]
PrCoGe ₃	4.308	9.829	[21]
Ce _{0.5} Pr _{0.5} CoGe ₃	4.314	9.832	interpolated

[30]. In this work, we used the fully localized limit of the LSDA+U (GGA+U) functional introduced by Czyżyk and Sawatzky [31], sometimes referred also as an atomic limit. The magnitude of Hubbard U repulsion introduced to the Ce 4f and Pr 4f orbitals has been set at 6 eV, which value has been previously calculated for Ce [32], whereas the J parameter was set to zero. The issue of choice of the parameter U will be discussed in more detail in Appendix **B**. We have also checked that the effect of the on-site repulsion U on the Co 3d orbitals is weak, so in the case of $Ce_{1-x}Pr_xCoGe_3$ system, the U_{3d} corrections can be neglected. A similar firstprinciples approach has been taken, for example, for fcc Ce [23] and PrO_2 [33]. However, some authors argue that for Ce compounds with transition metals (TM) the application of Hubbard U correction for Ce 4f electrons is not necessary because, as a result of strong hybridization between the Ce 4fand TM 3d electrons, the bonding bands are filled earlier than in the case of localized 4 f electrons of pure Ce for which one should use the corrections like, for example, Hubbard U [34].

CeCoGe₃ and PrCoGe₃ crystallize in a tetragonal noncentrosymmetric structure of the BaNiSn₃-type (space group *I4mm*), in which Ce and Pr atoms occupy one position, Co atoms another one, and Ge atoms the two nonequivalent positions [21,35,36]. In our models, we used the experimental lattice parameters [21,35] and atomic positions [21,36], see Table I and Fig. 1. The intermediate composition Ce_{0.5}Pr_{0.5}CoGe₃ was modeled as an ordered compound [37] with one Ce and one Pr atom per unit cell containing two



FIG. 1. The crystal structure models of CeCoGe₃ (a) and $Ce_{0.5}Pr_{0.5}CoGe_3$ (b) compositions. They crystallize in a tetragonal noncentrosymmetric structure of the BaNiSn₃-type, space group *I*4*mm*.



FIG. 2. The exemplary x-ray diffraction pattern of the $Ce_{0.8}Pr_{0.2}CoGe_3$ sample. The bottom solid line shows the difference between the measured and calculated patterns. Vertical bars indicate the positions of structural reflections. Miller indices are presented for the most pronounced peaks.

formula units, see Fig. 1(b). The antiferromagnetic configurations (+ + -- and + - +-) were constructed on the basis of the double unit cells, see Appendix B. For calculations based on the single unit cell (nonmagnetic solutions), we used k meshes equal to $20 \times 20 \times 20$ and energy convergence criterion equal to 2.72×10^{-6} eV (10^{-7} Hartree). For calculations based on the double unit cell (magnetic solutions) we used k-meshes equal to $20 \times 20 \times 6$ and charge convergence criterion equal to 10^{-6} which simultaneously led to the energy convergence of about 10^{-6} eV or better. To visualize crystal structures, we used the VESTA code [38].

Based on the band-structure results, we calculated the valence band x-ray photoelectron spectra. The densities of states (DOS) of individual orbitals have been convoluted by the Gaussian function with a full width at half maximum parameter δ equal to 0.3 eV. The aim of convolution was to imitate the experimental broadening resulting from the apparatus resolution, lifetime of the hole states, and thermal effects. Subsequently, the partial DOS were multiplied by the appropriate photoionization cross-sections [39]. The above method of determining theoretical x-ray photoelectron spectra we used previously for the Zr-Pd alloys [40].

III. RESULTS AND DISCUSSION

A. Crystal structure

The crystal structure of the prepared samples was examined by XRD measurements at room temperature. The results were analyzed using the FULLPROF [41] program (an exemplary refinement is shown in Fig. 2), which revealed that all samples have the desired single-phase noncentrosymmetric tetragonal BaNiSn₃-type structure. The evolution of crystal lattice parameters with Pr concentration is presented in Fig. 3. Values of the parameters *a* and *c* decrease with the addition of Pr as the alloying ion has smaller radius than the Ce ion. The



FIG. 3. Parameters *a* and *c* of the crystal lattice (a), the primitive cell volume *V*, and the c/a ratio (b) as function of Pr concentration *x* for the series Ce_{1-x}Pr_xCoGe₃.

c/a ratio presents small growth of values with increasing Pr content. For the parent compounds, the obtained values of the lattice parameters are in good agreement with those known from the literature [21,35].

B. Magnetic properties

Figure 4 presents temperature dependencies of magnetic susceptibility measured at low temperatures. In Fig. 4(a), the results for sample with Pr concentration x = 0.2 are shown. We have defined the phase transition temperatures as T_i (i = 1, 2, 3), because the nature of the magnetic order varies depending on the extent of substitution. The magnetic phase transitions for the sample with Pr concentration x = 0.2 take the values $T_1 = 11.4(2)$ K, $T_2 = 7.8(2)$ K, and $T_3 = 5.2(2)$ K, which are shifted towards lower temperatures in comparison to the temperatures of magnetic phase transitions of the parent compound CeCoGe₃ [13]. Like for the previously studied $CeCo_{1-x}Fe_xGe_3$ system [42], a small amount of the substituted element results in the enhancement of the ferromagnetic correlations. However, a metamagnetic transition is still visible in Fig. 5 for the magnetization curves of the samples with Pr content x = 0.2 and 0.4. This may suggest that magnetic structure is preserved after the change from antiferromagnetic to ferrimagnetic and only enhancement of the ferromagnetic contribution occurs. This change might be caused by a small difference in cell parameters, which changes the RKKY interaction into a ferromagnetic type, or by magnetic disorder, which has a noticeable contribution visible by the large discrepancy between the ZFC and FC curves. In this case, as a



FIG. 4. Zero field cooling (ZFC) and field cooling (FC) curves of magnetic susceptibility for samples $Ce_{0.8}Pr_{0.2}CoGe_3$ (a), $Ce_{0.6}Pr_{0.4}CoGe_3$ (b), $Ce_{0.4}Pr_{0.6}CoGe_3$ (c), and $PrCoGe_3$ (d) of the series $Ce_{1-x}Pr_xCoGe_3$ at $\mu_0H = 0.1$ T. Inset of (d) shows the inverse magnetic susceptibility fitted with the Curie-Weiss law.

magnetic disorder we can interpret disruption of the magnetic structure by noninteractive Pr ions.

For the sample with Pr concentration x = 0.4, the splitting between ZFC and FC curves occurs at $T_1 = 7.6(2)$ K, which can be assigned to the phase transition, whereas the next transition is at $T_2 = 4.8(2)$ K, see Fig. 4. A broad peak in the temperature range 10-20 K is associated with CEF of Pr and it is also visible for samples with $x \ge 0.6$. The splitting



FIG. 5. The first quarters of the hysteresis loops for the series $Ce_{1-x}Pr_xCoGe_3$ at temperature of 2 K.

TABLE II. The effective magnetic moment m_{eff} , the paramagnetic Curie temperature θ_{P} , and the effective magnetic moment of Pr m_{Pr} obtained from fitting magnetic susceptibility with the Curie-Weiss law [Eq. (1)] for the Ce_{1-x}Pr_xCoGe₃ series. Values of m_{Pr} were calculated with Eq. (2) with assumption of the free Ce³⁺ ion effective magnetic moment value $m_{\text{Ce}} = 2.54 \ \mu_{\text{B}}$.

$\overline{x_{\mathrm{Pr}}}$	$m_{ m eff}~(\mu_{ m B})$	$\theta_{\rm P}$ (K)	$m_{ m Pr}~(\mu_{ m B})$
0.0	2.542(2)	-63.7(2)	-
0.2	2.757(7)	-36.6(6)	3.493(7)
0.4	3.035(13)	-24.8(7)	3.653(13)
0.6	3.115(6)	-16.2(3)	3.445(6)
0.8	3.345(13)	-7.7(4)	3.517(13)
1.0	3.519(9)	-10.3(4)	3.519(9)

between ZFC and FC curves also suggests a high disorder in the magnetic structure. In Fig. 5, for sample with x = 0.4, there is a small hysteresis with metamagnetic transition also at the magnetic field value of 5 T.

The sample with Pr content x = 0.6 also exhibits splitting between ZFC and FC curves. A small hump at 2.2(2) K implies a possibility of phase transition. Additionally, for this sample the hysteresis is not visible in Fig. 5. Alloy with the Pr concentration x = 0.8 presents no anomalies in magnetic susceptibility at low temperatures (not shown in this work) and no magnetic hysteresis (Fig. 5), which indicates possible paramagnetism. The parent compound PrCoGe₃ shows expected paramagnetic behavior with noticeable contribution originating from the CEF excitation, see Fig. 4. Moreover, it also does not exhibit hysteresis, see Fig. 5.

The Curie-Weiss law allowed to determine the valence state of Pr in the $Ce_{1-x}Pr_xCoGe_3$ series. We used the formula for a magnetic susceptibility temperature dependence:

$$\chi(T) = \chi_0 + \frac{N_{\rm A} m_{\rm eff}^2}{3k_{\rm B}(T - \theta_{\rm P})},\tag{1}$$

where χ_0 is the temperature independent magnetic susceptibility, N_A is the Avogadro's number, m_{eff} is the effective magnetic moment, k_B is the Boltzmann constant, and θ_P is the paramagnetic Curie temperature. If we assume that the Co and Ge contribution is negligible, the magnetic susceptibility is a sum of the Ce and Pr contributions with appropriate proportions depending on the stoichiometry of a sample. Hence, to calculate the effective magnetic moment of Pr, m_{Pr} , we used the formula [43]

$$m_{\rm eff}^2 = x m_{\rm Pr}^2 + (1-x) m_{\rm Ce}^2,$$
 (2)

with assumption of the free Ce³⁺ ion effective magnetic moment value $m_{Ce} = 2.54 \ \mu_B$, according to previous reports that in this crystal structure Ce has the effective magnetic moment close to 2.50 μ_B [36,42,44]. The data resulting from the fitting of the Curie-Weiss law are presented in Table II. For all samples, the Pr part of effective moment is around 3.50 μ_B , which is close to the Pr³⁺ ion value 3.58 μ_B . The θ_P shows a tendency to decrease with increasing Pr concentration. This indicates a decrease in the collectivity of magnetism and strength of Kondo interaction, which finally leads to paramagnetic state in the parent compound PrCoGe₃.



FIG. 6. Magnetic entropy change $\Delta S_{\rm M}$ as a function of temperature *T* for Pr concentration x = 0.2 (a) and 0.4 (b) of the Ce_{1-x}Pr_xCoGe₃ series. The vertical lines indicate the detected phase transitions and anomalies.

Temperatures of magnetic phase transitions determined from magnetic susceptibility might be inaccurate, because of the overlapping Pr CEF contribution. Therefore, the phase transition temperatures were additionally estimated employing magnetocaloric effect (MCE). We calculated the magnetic entropy change $\Delta S_{\rm M}$ with the formula [45]:

$$\Delta S_{\rm M} \approx \frac{\mu_0}{\Delta T} \bigg[\int_0^{H_{\rm max}} M(T + \Delta T, H) \mathrm{d}H - \int_0^{H_{\rm max}} M(T, H) \mathrm{d}H \bigg],$$
(3)

where μ_0 is the magnetic permeability of vacuum, H_{max} is the maximum magnetic field for determined ΔS_M , ΔT is the temperature interval between subsequent isotherms, and M(T, H) and $M(T + \Delta T, H)$ correspond to magnetization for specific magnetic field value and temperatures T and $T + \Delta T$. Observation of the maxima and minima of ΔS_M can indicate dominating magnetic ordering in the considered samples [42,46]. The plots of ΔS_M as a function of temperature are presented in Fig. 6. For the sample with Pr concentration x = 0.2 [Fig. 6(a)], a wide peak is visible at 11.5(5) K for the



FIG. 7. Arrott plots for samples with Pr concentration x = 0.2 (a) and 0.4 (b) of the Ce_{1-x}Pr_xCoGe₃ series.

lowest magnetic field values, which corresponds to T_1 from the magnetic susceptibility results [Fig. 4(a)]. Small hump at temperature 6.5(5) K and small minimum at 4.5(5) K for magnetic field values of 1 T might correspond to temperatures of phase transitions T_2 and T_3 denoted from magnetic susceptibility curves. For the sample with x = 0.4 [Fig. 6(b)], there is also maximum with metamagnetic transition at $T_1 = 8.5(5)$ K, which corresponds to the observed anomaly in the magnetic susceptibility. A wide peak indicates $T_2 = 4.5(5)$ K.

The Arrott plots for samples with Pr concentration x = 0.2and 0.4 are presented in Fig. 7. For both samples there is a negative curvature below the temperature T_1 . This suggests a first order metamagnetic transition according to the Banerjee criterion [47].

Based on the evolution of the phase transitions temperatures with the Pr concentration x a magnetic phase diagram is constructed, see Fig. 8. Linear extrapolation of the magnetic ordering temperature T_1 to 0 K gives a critical Pr concentration equal to $x_{c1} = 0.66(8)$, while for T_2 it is equal to $x_{c2} =$ 0.60(1), and for T_3 it is equal to $x_{c3} = 0.53(1)$. Similarly as in the CeCo_{1-x}Fe_xGe₃ system [42], we observed a suppression of the magnetism, but the evolution of the magnetic behavior with the concentration of Pr is different. Alongside with a



FIG. 8. Magnetic phase diagram for the Ce_{1-x}Pr_xCoGe₃ system. Data were obtained from the results of magnetic susceptibility. Solid lines are a linear extrapolation of specific phase transitions to a temperature of 0 K. Critical concentrations obtained for specific phase transitions are: $x_{c1} = 0.66(8)$ for T_1 , $x_{c2} = 0.60(1)$ for T_2 , and $x_{c3} = 0.53(1)$ for T_3 . Results for CeCoGe₃ are taken from Ref. [42].

decrease of T_1 , the system exhibits a decrease in the strength of Kondo interaction. In terms of the Doniach diagram [48], we can assume that the system is approaching the low energy region of RKKY and Kondo interactions. It is the opposite situation to the QCP region, therefore, in our case, any possible non-Fermi liquid (NFL) behavior between concentration of x = 0.6 and 0.8 would be connected with the formation of the Griffiths phase instead of the occurrence of the QCP. A possible explanation for the reduction of energy of RKKY and Kondo interactions may be related to the interference of both interactions due to the substitution of Pr for Ce in the crystal structure - noninteractive Pr ions disrupt collectiveness of the magnetic structure and also coherence of the Kondo lattice, as the Pr ions separate the interacting Ce ions. Consequently, in the sample volume, statistically RKKY and Kondo interactions are further reduced with a higher Pr content.

C. Specific heat

Temperature dependencies of the specific heat in the range 1.9–40 K for exemplary samples and different values of the applied magnetic field are presented in Fig. 9. The increase in magnetic field values for samples with Pr concentration x = 0.2, 0.4, and 0.6 shifts the main peaks related to the magnetic phase transition T_1 towards lower temperatures, which suggests ferrimagnetic or antiferromagnetic type of ordering. In addition, if we consider the results of magnetic susceptibility and isothermal magnetization measurements, we can assume that the ferrimagnetic ordering scenario is more probable for these samples.

The sample with Pr content x = 0.4 presents the suppression of the main phase transition T_1 with the increase of the magnetic field values. For the sample with Pr concentration x = 0.6, the transition peak is around 2 K, what can be seen thanks to the influence of magnetic field on the C_p/T



FIG. 9. Temperature dependencies of the specific heat of samples $Ce_{0.8}Pr_{0.2}CoGe_3$ (a), $Ce_{0.6}Pr_{0.4}CoGe_3$ (b), $Ce_{0.4}Pr_{0.6}CoGe_3$ (c), and $PrCoGe_3$ (d) of the series $Ce_{1-x}Pr_xCoGe_3$ presented in the form of C_p/T vs $log_{10} T$ measured in various magnetic field.

versus $\log_{10} T$ curves. The results for PrCoGe₃ are similar to those reported earlier [9], with no visible changes due to increased magnetic field values. For these three samples the CEF contribution connected with Pr is visible as a wide peak appearing in the temperature range of 10-30 K. In addition, the increase in Pr concentration leads to the distinction of the CEF part. Due to the CEF peak and the magnetic contribution, it is difficult to determine the γ parameter values, because the correct temperature range cannot be chosen for applying the formula $C_p/T = \gamma + \beta T^2$. However, we can observe the trend of the γ values at 2 K. For the samples with x = 0.2 and 0.4 (x = 0.6 has a phase transition at T = 2.2 K and it cannot be considered in the analysis), it can be noticed that higher Pr content results in higher γ values, which may be related to the increase in disorder. For parent compounds denoted γ values are in good agreement with 32 mJ mol⁻¹ K⁻² for CeCoGe₃ and 6.1 mJ mol⁻¹ K⁻² for PrCoGe₃ from previous reports [9,13].

D. Resistivity

The results of the measurements of the temperature dependence of resistivity ρ in the range of 2–300 K are shown in Fig. 10. With increasing concentration of Pr we can observe a clear reduction of the Ce CEF contribution (broad peak around 100 K) in favor of the Pr CEF contribution (around 30 K). This is especially important as we can assume that there are two separate CEF contributions, which are modified



FIG. 10. Temperature dependencies of the electrical resistivity for the series $Ce_{1-x}Pr_xCoGe_3$.

by the stoichiometry of the alloy. It is necessary to consider this information in further investigation of the CEF levels for particular alloys of the system $Ce_{1-x}Pr_xCoGe_3$. In Fig. 10, one can also notice anomalies in the low temperature region for samples with Pr content x = 0.2, 0.4, and 0.6, which are related to the phase transitions at T_1 . For sample with x = 0.8there is an upturn in the lowest temperatures, which might be connected with a single ion Kondo effect. This is expected as the concentration of Ce is significantly reduced. The threshold between the Kondo lattice and the Kondo impurity effect is between 0.6 < x < 0.8, where also the magnetism is suppressed.

Similarly as for specific heat results, where CEF contribution of Pr and magnetism in the lowest temperatures prevented the systematic estimation of the γ parameter, the same issues do not allow to extract the values of residual resistivity ρ_0 . However, we can observe some tendencies, which can provide a few rough conclusions. It is noticeable that the overall ρ values for alloys at the lowest temperatures increase with the addition of Pr, suggesting a growing chemical disorder (except for the sample with x = 0.8 which cannot be considered in the analysis as it presents the Kondo impurity effect). For the parent compound PrCoGe₃, we observe a metallic type behavior with a significant CEF contribution in the temperature range of 10–30 K. Additionally, the parameter RRR = 81 (residual resistivity ratio) of PrCoGe₃ has a rather high value for a polycrystalline sample and was reproduced for two different pieces of the sample. Due to the high degree of disorder observed over the whole concentration range (excluding parent compounds), the values of the RRR parameter are only of the order of 1-2.

E. Magnetoresistance

In order to extend the characterization of the magnetic properties of the studied alloys, we carried out isothermal measurements of the resistivity as a function of the magnetic field. In Fig. 11, we show magnetoresistance (MR) plotted as $MR = [\rho(H, T) - \rho(0, T)]/\rho(0, T)$, where $\rho(0, T)$ and



FIG. 11. The magnetoresistance (*MR*) isotherms measured in the temperature range 2–30 K for Pr concentration x = 0.2 (a), 0.4 (b), 0.6 (c), and 1.0 (d) of the Ce_{1-x}Pr_xCoGe₃ series.

 $\rho(H, T)$ correspond to resistivity values for specific temperature without and with applied magnetic field. For the sample with x = 0.2, there is a metamagnetic transition reflected as a change from positive to negative values of MR at temperatures below 12 K and at magnetic field of about 5 T. This confirms the maintenance of the magnetic structure of CeCoGe3 for Ce_{0.8}Pr_{0.2}CoGe₃. Similar behavior can be observed for the sample with Pr content x = 0.4, but the metamagnetic peak is in the region of negative MR values, which may suggest a ferrimagnetic ordering with a larger ferromagnetic contribution than in the case of x = 0.2. For higher temperatures, above 18 K for x = 0.2, magnetoresistance reveals a wide positive peak, which can be interpreted as the effect of CEF [49]. It is also visible at lower temperatures for samples with x = 0.4and 0.6. Although the CEF contribution increases with the Pr content, it does not coincide with the magnetic part because the magnetic transitions take place at much lower temperatures than the CEF effects. Further increase of temperature causes disappearance of the peak, as we are moving out from the CEF region and a linear, metalic-type form of the positive MR is revealed.

A more complicated situation is presented in Fig. 11(d), where the parent compound PrCoGe₃ shows a typical metallic-type MR, but with high values of up to 250%. While metallic behavior is expected, the high MR value observed is not so obvious. At first glance, this may be related to the MRformula and low values of $\rho(0, T)$. Looking at the results for other samples and the contribution of the CEF part to the MR, this contribution is not evident in the case of PrCoGe₃. Instead, the CEF part is entirely covered by a metallic contribution, unlike for sample with Pr concentration x = 0.2, where the magnetic contribution overlaps the CEF part. Previously, the explanation of the giant MR in Tb₂Ni₃Si₅ and Sm₂Ni₃Si₅ has been connected with the layered magnetic structure [50]. Additionally, for PrNiGe₃ compound [51], the authors have suggested the influence of the magnetic field on the mobility of conduction electrons and magnetic ordering. Since the high values of MR in intermetallic compounds are still not fully explained, we think that in our case the interpretation related to the modification of electron mobility might be possible. For LaCoGe₃ [52], the results of MR are similar to the results for PrCoGe₃. This is expected because Pr behaves as La in these compounds, providing similar influence on the band structure, as it has been reported by Kawai et al. [21]. This may be an indication that the giant MR for PrCoGe₃ compound is associated with the band structure and the mentioned modification of the mobility of the conduction electrons.

F. Seebeck coefficient

In Fig. 12(a), the values of the Seebeck coefficient S as a function of temperature are presented. A wide peak around 100 K is observed for all samples containing Ce, which is connected with the Ce CEF contribution. The highest value $S = 43.4(2) \ \mu V K^{-1}$ was found for Ce_{0.8}Pr_{0.2}CoGe₃ at 95 K. Using electrical resistivity values, the thermoelectric power factor $PF = S^2/\rho$ can be calculated. For the sample with x = 0.2, *PF* reaches 7.1(1) × 10⁻³ W m⁻¹ K⁻² at 95 K. The observed decrease in maximum values is associated with the decreasing Ce content, whereas the Pr CEF contribution visible in range of 10-30 K becomes more pronounced with increasing Pr content. For PrCoGe₃, very low S values are observed. However, if we consider the formula $S = AT + BT^3$, the linear character of the curve suggests the dominance of the electron diffusion part with almost no contribution of the phonon drag part. In this case, in low temperature regime the value of one is expected for the Behnia ratio [53]:

$$q = \frac{S}{T} \frac{N_A e}{\gamma}.$$
 (4)

We estimated the S/T values for samples with x = 0.6, 0.8, and 1.0 using C_p/T values at T = 2 K and assuming q = 1. The results are 2.48, 1.37, and 0.09 μ V K⁻², respectively, which can be compared to the data in Fig. 12(b). Good agreement (considering that we do not know exact values of S/T and C_p/T at 0 K) between the thermoelectric power and specific heat results confirms the domination of the electronic contribution in low temperature properties of alloys with Pr concentration $x \ge 0.6$. Therefore, the drop of the *S* values with increasing *x* can be connected with decreasing density of electronic states at the Fermi level due to the reduction of the Ce content.

Figure 12(b) shows the S/T versus $\log_{10} T$ curves for all samples. Peaks at 12, 7, and 3 K for Pr content *x* equal to 0.2, 0.4, and 0.6, respectively, are connected with the magnetic phase transitions. However, the increase in S/T values with decreasing temperature occurs for the concentration of



FIG. 12. Temperature dependencies of the Seebeck coefficient *S* of the Ce_{1-x}Pr_xCoGe₃ samples plotted in two different representations: *S* vs *T* (a) and S/T vs log₁₀ *T* (b).

x = 0.6, which is partially overlapped by the phase transition peak. This is also observed for the Pr concentration of x = 0.8, where the Kondo impurity effect is involved. Observation of this trend may suggest the possibility of NFL behavior for a very small range of Pr concentration between regions with magnetic ordering and Kondo impurity. However, there are no signs of NFL temperature dependencies in other experimental results.

G. X-ray photoelectron spectroscopy

Exemplary x-ray photoelectron spectra of $Ce_{1-x}Pr_xCoGe_3$ alloys collected in a wide binding energy (BE) range up to 1400 eV with the identification of core levels and Auger lines are shown in Fig. 13. For all samples, we observe low content of oxygen and carbon, suggesting good quality of the samples received.

In BE region from 90 to 140 eV [Fig. 14(a)], we observed three sets of spin-orbit splitted peaks related to Ce 4*d*, Pr 4*d*, and Ge 3*p* states. The positions of the peaks are in good agreement with the ones published for similar systems [54–56] and calculated positions presented in Fig. 18. Additionally, a broad



FIG. 13. XPS survey spectra of $Ce_{1-x}Pr_xCoGe_3$ series for selected samples with x = 0.4 and 0.8.

peak assigned to Co 3s state is present at 101.0 eV. Due to the overlapping of the Ce 4d spectrum with the Pr 4d and Ge 3p states, the evaluation of the Ce oxidation state is not possible. While the relative intensity of the peaks associated with Ge is constant for all samples, the intensity of the peaks related to Pr and Ce varies significantly for different samples.

The Co 2p XPS spectra for selected samples from Ce_{1-x}Pr_xCoGe₃ series are shown in Fig. 14(b). The positions of the Co $2p_{1/2}$ and $2p_{3/2}$ core levels in all investigated samples are around 793.4 and 778.3 eV, respectively, with the spin-orbit splitting value of 15.1 eV. The values obtained are practically the same as for pure metallic Co [57]. The lack of additional satellite peaks suggests that there are no Co oxides and that the charge transfer can be neglected in this system. Therefore, the oxidation state of Co in the Ce_{1-x}Pr_xCoGe₃ series is equal to zero. The Ge 2p spectra, presented in Fig. 14(c), show the strong peak positions at 1248.3 eV and 1217.3 eV, which correspond to the Ge $2p_{1/2}$ and Ge $2p_{3/2}$ core levels, respectively. Spin-orbit splitting is equal in this case to 31.0 eV. In addition to these two sharp peaks, two more



FIG. 14. XPS spectra of Ge 3p, Ce 4d, and Pr 4d (a), Co 2p (b), and Ge 2p (c) core levels for the Ce_{1-x}Pr_xCoGe₃ samples.



FIG. 15. The Ce 3*d* XPS spectra for the selected Ce_{1-x}Pr_xCoGe₃ samples. The spectra intensities are normalized to the intensity of the Ce $3d_{5/2}$ peak. For selected sample, Ce_{0.8}Pr_{0.2}CoGe₃, the deconvolution of Ce 3*d* states is presented (lines) together with levels diagrams. Open symbols correspond to the experimental spectrum.

wide satellites have been registered towards higher BE values. These structures probably originate from Ge oxide [58].

Figures 15 and 16 present 3d states of Ce and Pr for selected samples of the $Ce_{1-x}Pr_xCoGe_3$ series. In all cases, we observed a set of two broad peaks, which originate from spin-orbit splitting of the 3d states equal to 18.7 eV and 20.4 eV for Ce and Pr, respectively. The resulting spectra for Pr look very similar to those published for pure Pr and other compounds containing Pr [59–61]. No visible changes in the Ce and Pr 3d spectra have been observed with the change of Pr concentration. Analysis of XPS spectra for 3d states of Ce and Pr with Gunnarsson-Schönhammer theory can provide useful information about valence state and hybridization strength [62,63]. The exemplary analysis of the Ce 3d states for the sample Ce_{0.8}Pr_{0.2}CoGe₃ is presented in Fig. 15, and for the Pr 3d states of Ce_{0.6}Pr_{0.4}CoGe₃ in Fig. 16. To model the background, the Tougaard algorithm was used [64]. Relatively small values of the intensity ratio $r_2 = I(f^2)/[I(f^1) + I(f^2)]$, where $I(f^1)$ and $I(f^2)$ are intensities of specific states, suggest weak hybridization of the 4f and conduction electrons. Moreover, according to the ratio $r_0 = I(f^0)/[I(f^0) + I(f^1) +$ $I(f^2)$], where $I(f^0)$ is the intensity of the f^0 state, the absence of distinctive peaks of the Ce $4f^0$ states indicates a full occupancy of the f^1 state. In order to get the best possible fits, it was necessary to include additional peaks (dotted lines in



FIG. 16. The Pr 3*d* XPS spectra for the selected $Ce_{1-x}Pr_xCoGe_3$ samples. The spectra intensities are normalized to the intensity of the Pr $3d_{5/2}$ peak. For selected sample, $Ce_{0.6}Pr_{0.4}CoGe_3$, the deconvolution of Pr 3*d* states is presented (lines) together with levels diagrams. Open symbols correspond to the experimental spectrum.

Figs. 15 and 16). In the case of Ce 3*d* states, we considered two additional peaks at BE \approx 892 eV and BE \approx 916 eV, while for Pr 3*d* spectra additional peak at BE \approx 955 eV was added. Those additional structures may originate from various excitations, such as plasmon energy loss [65].

For all studied samples, the XPS valence bands (VBs) in the energy range 0–12 eV are presented in Fig. 17. In this BE range, we observed three broad structures. The broad peak closest to the Fermi level (BE ≈ 2.0 eV) is formed by the Pr/Ce (5d, 6s), Co 3d, and Ge 4p states. Small hump close to the Fermi level is related to the Ce 4f¹ state and its intensity decreases with the increasing Pr concentration. The middle peak (BE ≈ 4.0 eV) is mainly due to the Pr 4f¹ and Ce 4f⁰ states [66]. Therefore, the position and relative intensity of this peak changes with the change of Ce/Pr concentration. That interpretation is further supported by our DFT results presented in Sec. III H. The last structure, broad band of small intensity near 8.0 eV, originates from Ge 4s states.

H. First-principles calculations

1. Relativistic atomic energies

We start the theoretical analysis by presenting the electronic structure of CeCoGe₃ for a wide range of energies,



FIG. 17. XPS valence band spectra of the $Ce_{1-x}Pr_xCoGe_3$ series.

including core states. Figure 18 shows the relativistic atomic energies in three successively decreasing ranges. Where the scale allows for it, the atomic energies are attributed to particular orbitals. The spectrum starts with the strongest bonded



FIG. 18. The relativistic atomic energies for CeCoGe₃ calculated with FPL018 in fully relativistic approach and applying PBE.

electron Ce 1s at about -40 keV. As the presented atomic energies are calculated in the beginning of the self-consistent cycle, some of the energy levels can shift after the system converge. Nevertheless, we observe a good agreement between the calculated energy levels presented in the middle panel and the measured XPS survey spectrum shown before, see for example the spin-orbit splitted spectra for Ge 2*p* (below -1210 eV), Ce 3*d* (at about -900 eV), and Co 2*p* (at about -790 eV) in Figs. 14 and 15. The spin-orbit doublets measured for Ge 3*p* and Ce 4*d* in a range between -130and -110 eV [Fig. 14(a)], can be identified in the bottom panel of Fig. 18. However, the XPS spectra closest to the Fermi level are better interpreted on the basis of band structure calculations.

2. Valence band x-ray photoelectron spectra

After a general introduction to the electronic structure of CeCoGe₃, we will now focus on a valence band covering a range of only several eVs around the Fermi level. A detailed analysis of the valence band allows us to predict many physical properties of the materials tested, whereas the primary purpose of our first-principles calculations is the interpretation of the measured XPS spectra and investigations of magnetic properties. In our previous work on $CeCo_{1-x}Fe_xGe_3$ alloys [20] we presented the XPS spectra calculated without on-site repulsion term *U*. Because, in contrast to the CeCoGe₃ case, the Hubbard *U* applied to Pr 4*f* orbitals significantly affects the valence band below Fermi level, in this work we decided to consequently present all the calculated XPS spectra including on-site repulsion term U_{4f} equal to 6 eV, see Fig. 19.

A comparison of the XPS spectra calculated for CeCoGe₃, Ce_{0.5}Pr_{0.5}CoGe₃, and PrCoGe₃ shows that the energy bands located between 0 and 6 eV binding energy consist mainly of Co 3d contribution and a much smaller Ge 4p share. With increasing Pr concentration, the new maximum for Pr 4f is formed and develops at about 4 eV, and at the same time, the Ce 4f contribution observed at Fermi level disappears. The main features of the calculated XPS spectra are in good agreement with the experimental results shown in Fig. 17.

3. Antiferromagnetic solutions for CeCoGe₃

Our magnetic measurements for CeCoGe₃ (Fig. 8), confirmed the appearance of three magnetic phase transitions at 21, 12, and 8 K observed previously [13]. Those results have been interpreted as the transitions between paramagnetic, ferrimagnetic, and antiferromagnetic configurations [36]. Pecharsky et al. [36] deduced from magnetization isotherms that in temperature below 16 K (a magnetic ground state in their understanding) the Ce magnetic moments are primarily antiferromagnetically ordered in the ab plane, but canted along the c axis. The canting order is + - + -, i.e., a colinear antiferromagnetic ordering along the c axis [36]. The total longitudinal moment at 3 K has been deduced by those authors to be equal to 0.37 $\mu_{\rm B}$ [36]. However, the refinement of the integrated intensities of single crystal neutron diffraction, presented by Smidman group, suggests a two-up, two-down magnetic structure (++--) below 8 K, with magnetic moments of 0.405 $\mu_{\rm B}/{\rm Ce}$ atom along the c axis [14]. As the Hund's rule value of the ground-state magnetic



FIG. 19. The valence band x-ray photoelectron spectra calculated with FPL018 in fully relativistic approach applying PBE + U ($U_{4f} = 6 \text{ eV}$) and assuming lack of spin polarization. (a) Comparison of the results for CeCoGe₃, Ce_{0.5}Pr_{0.5}CoGe₃ and PrCoGe₃. [(b)–(d)] The most important contributions from individual orbitals compared to the total XPS spectra.

moment (gJ) for Ce³⁺ ion ($M_J = 5/2$, J = 5/2) is 2.14 μ_B , the experimental moment for CeCoGe₃ is clearly reduced against this theoretical value. However, such reduction is a well-recognized characteristic of the Ce intermetallic compounds, where, for example, the measured magnetic moments on Ce are about 0.5 μ_B for CeFe₂ [67], 1.0 μ_B for CeB₆ [68], and 1.47 μ_B for CeSi [69]. In addition to measuring the magnetic moment on Ce at 2 K, Smidman's group also determined the CEF scheme for CeCoGe₃ [14]. The predicted CEF ground-state wave function ψ_1 [$\Gamma_6(1)$] corresponds to the Ce magnetic moment of 1.01 μ_B along the *c* axis [14]. Smidman and coworkers conclude that the lower value of the measured moment on Ce (0.405 μ_B) compared to the deduced value of the CEF ground-state results from a hybridization between the ground-state and conduction electrons [14].

In order to examine the magnetic properties of CeCoGe₃, we decided to extend the non-spin-polarized first-principles investigations into the spin-polarized procedure. Since CeCoGe₃ in its ground state is an antiferromagnet with a non-trivial configuration of magnetic moments extending beyond a single elementary cell, it is necessary to pay special attention to preparing a suitable model. At the same time, in case of describing the Ce 4*f* electrons it is necessary to go beyond the LDA/GGA. The procedure for preparing such a model is not standard and therefore it is described in the Appendix B. We show there how we have dealt with the problem of emergence of multiple solutions within the proposed model combining



FIG. 20. The densities of states (DOS) of CeCoGe₃. The model is based on a double unit cell with antiparallel configuration of magnetic moments on Ce sites (+ + --) and quantization axis [100]. The total DOS is presented together with the most significant contributions of individual orbitals (Ce 4*f*, Co 3*d*, and Ge 4*p*). The results are obtained with FPL018 in fully relativistic approach and applying PBE + $U(U_{4f} = 6 \text{ eV})$.

the LDA/GGA + U approach with description of the magnetic properties of Ce systems. We discuss the influence of the value of the Hubbard U parameter on the obtained values of magnetic moments and the DOS of the valence band and we conclude that the results are not very sensitive to the value of U in a range from about 3 to 6 eV. Finally, in Appendix B we present the models of the most probable collinear antiferromagnetic configurations (+ + - - and + - + -) deduced from experiments. We find that the ++-- configuration oriented along the [100] direction is the ground state and the +-+- [100] one is slightly less stable. In all cases, the spin magnetic moment on Ce is close to 1.00 $\mu_{\rm B}$, which is related to a localization of the occupied 4f orbitals. The utilized fully relativistic approach allows us to calculate also the orbital contributions to the magnetic moments, which in the case of f electron systems are often substantial [70]. In our case, the opposite orbital magnetic moment on Ce is equal to about $-0.57 \ \mu_{\rm B}$ and significantly reduces the resultant total magnetic moment equal to about 0.43 $\mu_{\rm B}$. The latter result stays in a good agreement with the experimental value 0.405 $\mu_{\rm B}/{\rm Ce}$ deduced from single crystal neutron diffraction below 8 K [14] and with another experimental result suggesting the magnetic moment of about 0.37 $\mu_{\rm B}/{\rm Ce}$ at 3 K [36]. Additionally, the calculated moments on Co are below 0.04 $\mu_{\rm B}$ /atom and are opposite to the moments on Ce, whereas the moments on Ge are below 0.005 $\mu_{\rm B}/{
m atom}$ and parallel with Ce.

Figure 20 shows the spin-polarized DOS for CeCoGe₃ with the ground-state antiparallel configuration + + -- [100] of magnetic moments on Ce sites, whereas the magnetic configuration sketch is presented in Fig. 25(f) of Appendix B. The observed hybridization between the Co 3d and Ge 4p orbitals in a whole region below the Fermi level confirms the formation of the 3d-4p covalent bonds. As we have already discussed, the position of 4f bands depends on the selected value of the Hubbard U. Hence, for U_{4f} equal to 6 eV, the occupied 4f states form the lower Hubbard band at about -3 eV

and upper Hubbard band centered at about 4 eV, which stay in decent agreement with experimental values for γ Ce (-2 and 4 eV [71,72]). The lower Hubbard band is not hybridized with other bands, which indicates localization of the occupied Ce 4f orbital. What is characteristic to the antiferromagnetic solution, the result consists of two types of Ce contributions with an antiparallel orientation of magnetic moments, which are denoted as Ce \uparrow and Ce \downarrow and marked in different colors on the plot. These two results are symmetric, and each consists of majority spin channel occupied with about one electron (1.09 from Mulliken analysis) and another channel nearly empty (about 0.09 e). This polarization of 4f band leads to the local spin magnetic moment on Ce equal to 1.00 $\mu_{\rm B}$, see also Table V of Appendix B. The main difference between the presented nonmagnetic and antiferromagnetic solutions is a shift of the 4f occupied band from the Fermi level to the position of -3 eV below Fermi level, compare with Fig. 19(b).

The density of states at the Fermi level equal to 1.8 states eV^{-1} f.u.⁻¹ consists mainly of contributions from Co 3*d* and Ge 4*p* orbitals forming the valence band. This rather low value corresponds to the electronic specific heat coefficient γ equal to 4.3 mJ mol⁻¹ K⁻² in qualitative agreement with γ equal to 32 mJ mol⁻¹ K⁻² measured for CeCoGe₃ [13].

The excess electron number (resultant charge) of CeCoGe₃ calculated for magnetic configuration + + -- [100] is the same as obtained for a nonmagnetic case. Just like in the nonmagnetic case, the charge taken from Ce sites (-1.23) is transferred to the Co (+0.17) and Ge (+0.47, +0.30) sites. However, the occupation of particular Ce orbitals is slightly different. While for nonmagnetic solution we had occupation Ce $5p^{5.82}$ $6s^{0.19}$ $5d^{1.59}$ $6p^{0.14}$ $4f^{0.98}$, for configuration + + -- [100] we have Ce $5p^{5.85}$ $6s^{0.18}$ $5d^{1.49}$ $6p^{0.13}$ $4f^{1.09}$, which differs primarily by a charge 0.1 transferred from Ce 5d to Ce 4f orbital.

4. Antiferromagnetic solution for Ce_{0.5}Pr_{0.5}CoGe₃

For the composition $Ce_{0.5}Pr_{0.5}CoGe_3$ we do not perform as extended analysis as for CeCoGe₃. Instead, we present a model based on a double unit cell, with the antiparallel configuration of magnetic moments Ce(+) Pr(+) Ce(-)Pr(-) along the *c* axis, and with the energetically preferred quantization axis [001]. The DOS of Ce_{0.5}Pr_{0.5}CoGe₃ and CeCoGe₃ are very similar, see Figs. 20 and 21. The main difference between the occupied parts below the Fermi level is the contribution of Pr 4f states located at about -5 eV. Additionally, in $Ce_{0.5}Pr_{0.5}CoGe_3$ the Ce 4f are depopulated due to the lower concentration of Ce in the alloy. The Mulliken analysis shows that the charges taken from Ce (-1.21) and Pr (-1.14) sites are transferred to Co (+0.18, +0.16) and Ge (+0.47, +0.43, +0.28) sites. The occupation of Pr valence orbitals $(5p^{5.74} \ 6s^{0.25} \ 5d^{1.50} \ 6p^{0.23} \ 4f^{2.14})$ is most different from the Ce counterparts $(5p^{5.85} \ 6s^{0.18} \ 5d^{1.49} \ 6p^{0.13} \ 4f^{1.09})$ for 4f orbital, which for Pr is close to two instead of one for Ce. The occupation of spin-polarized Pr 4 f orbital is reflected as a high peak in the DOS and also in the Pr spin magnetic moment equal to 2.08 $\mu_{\rm B}$. Taking into account an orbital moment equal to $-1.45 \ \mu_{\rm B}$ leads to the total magnetic moment on Pr equal to 0.63 $\mu_{\rm B}$, while the calculated magnetic moments on Ce sites stay the same as for CeCoGe₃ ($m_s = 1.00$ and



FIG. 21. The densities of states (DOS) of $Ce_{0.5}Pr_{0.5}CoGe_3$ ordered compound. The model is based on a double unit cell with the antiparallel configuration of magnetic moments Ce(+) Pr(+) Ce(-)Pr(-) along the *c* axis and with the quantization axis [001] (in the previous section, it was [100] that was energetically preferred). The total DOS is presented together with the most significant contributions of individual orbitals (Ce 4*f*, Pr 4*f*, Co 3*d*, and Ge 4*p*). The results are obtained with FPL018 in fully relativistic approach and applying PBE + *U* ($U_{4f} = 6$ eV on Ce and Pr sites).

 $m_l = 0.56\mu_B$). Similar like for the antiferromagnetic solution of CeCoGe₃, the calculated value of DOS at the Fermi level for Ce_{0.5}Pr_{0.5}CoGe₃ is equal to 1.8 states eV⁻¹ f.u.⁻¹, which corresponds to the γ coefficient equal to 4.3 mJ mol⁻¹ K⁻², with regard to the γ equal to 32 and 6.1 mJ mol⁻¹ K⁻² measured for CeCoGe₃ and PrCoGe₃, respectively [9,13].

5. Nonmagnetic solution for PrCoGe₃

Because $PrCoGe_3$ does not order magnetically, we decided to present only the nonmagnetic DOS for this system, see Fig. 22, which we previously used to get the XPS spectra, see Fig. 19(d). We notice that even in the nonmagnetic state the



FIG. 22. The densities of states (DOS) of $PrCoGe_3$ in the nonmagnetic state. The total DOS is presented together with the most significant contributions of individual orbitals (Pr 4*f*, Co 3*d*, and Ge 4*p*). The results are obtained with FPL018 in fully relativistic approach and applying PBE + U ($U_{4f} = 6 \text{ eV}$).

occupied Pr 4f states form the lower Hubbard band at about -4 eV below the Fermi level, when for the nonmagnetic solution of CeCoGe₃ we observed much wider 4f peak located directly at Fermi level [20]. The main contributions of Co 3d and Ge 4p orbitals do not change qualitatively in comparison to the previously discussed CeCoGe₃ and Ce_{0.5}Pr_{0.5}CoGe₃ results. Like it was discussed before, the charge taken from Pr (-1.14) sites is transferred to the Co (+0.18) and Ge (+0.45; +0.26) sites. The occupations of particular Pr orbitals are $5p^{5.74}$ $6s^{0.25}$ $5d^{1.51}$ $6p^{0.23}$ $4f^{2.15}$, with regard to the ground-state electronic configuration of a neutral Pr atom ([Xe] $4f^3 6s^2$). Similar like for the antiferromagnetic solutions of CeCoGe₃ and Ce_{0.5}Pr_{0.5}CoGe₃, the DOS at the Fermi level for $PrCoGe_3$ is equal to 1.8 states eV^{-1} f.u.⁻¹, which corresponds to the γ coefficient equal to 4.3 mJ mol⁻¹ K⁻², in fair agreement with the γ measured for PrCoGe₃ equal to $6.1 \text{ mJ mol}^{-1} \text{ K}^{-2}$ [9].

6. Summary of the first-principles calculations

Investigation of the $Ce_{1-x}Pr_xCoGe_3$ system (where x =0.0, 0.5, and 1.0) by first-principles calculations allowed to observe the evolution of the electronic structure with increasing Pr concentration. The growth of the number of electrons in the system due to a higher proportion of the element with a higher atomic number ($Z_{Ce} = 58$ and $Z_{Pr} = 59$) is realized mainly by increasing the occupation of the narrow 4fband located several eVs below the Fermi level, remaining the part of the valence band in the vicinity of the Fermi level almost intact. Moreover, even though we are able to suggest the ground-state ordered magnetic configuration for CeCoGe₃, the applied methods are insufficient to model the antiferromagnetic-paramagnetic transition and to indicate the critical concentration. For example, the paramagnetic state of PrCoGe₃ could be better investigated with the disordered local moments approach (DLM) based on the coherent potential approximation (CPA), but in FPLO this option is incompatible with the fully relativistic PBE + U approach.

IV. CONCLUSIONS

We have presented results of our studies of various physical properties for the $Ce_{1-x}Pr_xCoGe_3$ system, which shows the suppression of magnetic ordering with increasing Pr concentration x in isostructural transformation. From the magnetic hysteresis and magnetoresistance measurements, we deduced that the magnetic structure of the parent compound CeCoGe₃ is preserved for a low content of Pr ($x \leq 0.4$). In all presented experimental results, there is a significant crystal electric field contribution of Pr in the temperature range of 10-30 K, which is separated from a Ce contribution visible in the temperature of 100 K. The Pr CEF contribution may have a strong impact on the Pr state. In the studied alloys Pr behaves as La with two additional noninteractive f electrons. More interestingly, the parent compound PrCoGe₃ shows giant magnetoresistance, which is probably connected with the observed reduction of electrons mobility with the applied magnetic field.

The constructed magnetic phase diagram reveals that the ordering temperature decreases monotonically with increasing Pr concentration x and the extrapolation to 0 K provides

TABLE III. Excess electron number (resultant charge) for CeCoGe₃ and PrCoGe₃ compounds calculated with FPL018 in fully relativistic approach applying PBE + U ($U_{4f} = 6$ eV) and without spin polarization. The nonequivalent crystallographic sites are based on the Refs. [21,36]. Unlike the other sites, the multiplicity for Ge2 per formula unit is two instead of one.

Formula\site	Ce/Pr	Co	Gel	Ge2
CeCoGe ₃	-1.23	0.17	0.47	0.30
PrCoGe ₃	-1.16	0.18	0.43	0.27

the critical concentration $x_{c1} = 0.66(8)$ for the phase transition at T_1 . The possibility of appearance of the non-Fermi liquid behavior is very low, as the quantum critical point scenario is excluded due to the reduction of energy of RKKY and Kondo interactions.

X-ray photoelectron spectroscopy measurements confirmed the successful synthesis of good quality samples of solid solutions for the $Ce_{1-x}Pr_xCoGe_3$ series. The Co 2pspectra demonstrate the absence of contribution of Co oxides and a close similarity with metallic Co. The analysis of the Pr/Ce 3d and 4d XPS spectra suggests weak hybridization between the Pr/Ce 4f and remaining valence band electrons in the studied materials. The stable Pr^{3+} and Ce^{3+} ions are consistent with magnetic susceptibility measurements.

From the point of view of possible applications, the materials tested, like most of similar compounds based on Ce, show small values of magnetic entropy change $(\Delta S_{\rm M} = 0.9 \,\mathrm{J \, kg^{-1} \, K^{-1}}$ at 15 K for 9 T for x = 0.2) and thermoelectric power factor ($PF = 7.1(1) \times 10^{-3} \,\mathrm{W \, m^{-1} \, K^{-2}}$ at 95 K for x = 0.2), which does not augur well for their wide application in industry.

We have also presented the results of first-principles calculations for CeCoGe₃, Ce_{0.5}Pr_{0.5}CoGe₃, and PrCoGe₃

TABLE IV. The Mulliken electronic population analysis for CeCoGe₃ and PrCoGe₃ compounds calculated with FPL018 in fully relativistic approach applying PBE + U ($U_{4f} = 6 \text{ eV}$) and without spin polarization. The nonequivalent crystallographic sites are based on the Refs. [21,36]. Results for several almost empty valence orbitals are not provided, although they were included in the calculation.

	Site	5 <i>p</i>	6 <i>s</i>	5 <i>d</i>	6 <i>p</i>	4f
CeCoGe ₃	Ce	5.82	0.19	1.59	0.14	0.98
PrCoGe ₃	Pr	5.73	0.25	1.50	0.22	2.15
	Site	4 <i>s</i>	3 <i>d</i>	4 <i>d</i>	4 <i>p</i>	
CeCoGe ₃	Со	0.52	7.91	0.19	0.53	
PrCoGe ₃	Co	0.52	7.92	0.19	0.54	
	Site	4 <i>s</i>	4 <i>p</i>	4 <i>d</i>		
CeCoGe ₃	Ge1	1.60	2.71	0.16		
PrCoGe ₃	Ge1	1.59	2.53	0.17		
	Site	4 <i>s</i>	4 <i>p</i>	4d		
CeCoGe ₃	Ge2	1.60	2.55	0.17		
PrCoGe ₃	Ge2	1.60	2.53	0.17		



FIG. 23. Spin and orbital magnetic moment on Ce sites as a function of on-site repulsion U_{4f} calculated for CeCoGe₃ with antiparallel configuration + + -- of magnetic moments on Ce sites. Calculations are carried out with FPL018 in fully relativistic approach applying PBE + U and for quantization axis [001]. While orbital moments are oriented against spin moments, the graph shows orbital moments multiplied by minus one $(-m_l)$. For U = 0, spin and orbital magnetic moments are equal to 0.06 and $-0.07 \mu_B$, respectively.

compositions. We considered non-spin-polarized models as the basis for XPS spectra and spin-polarized models to investigate magnetic properties. We have shown that the substitution of Pr for Ce significantly affects the electronic structure of the alloys. The main conclusions of the calculations are as follows.

(1) The calculations explain the evolution of the measured $Ce_{1-x}Pr_xCoGe_3$ XPS spectra mainly as a change in the position and magnitude of the 4*f* contributions.

(2) Mulliken electronic population analysis indicates electronic states of f electron atoms as close to Ce f^1 and Pr f^2 .

(3) The charge analysis and calculated densities of states indicate that the chemical bonds in $Ce_{1-x}Pr_xCoGe_3$ alloys are formed mainly by the Ce/Pr 5*d*, Co 3*d*, Ge 4*p*, and Ge 4*s* orbitals.



FIG. 24. The densities of states of Ce \uparrow 4*f* orbitals as a function of on-site repulsion U_{4f} calculated for CeCoGe₃ with antiparallel configuration + + -- of magnetic moments on Ce sites. Calculations are carried out with FPL018 in fully relativistic approach applying PBE + U and for quantization axis [001].

(4) The calculated electronic specific heat coefficient γ is low and remains almost constant as the Pr concentration increases.

(5) The charge transfer mainly occurs from the 4f elements (Ce and Pr) towards Ge and Co.

(6) Of the considered magnetic configurations of $CeCoGe_3$, the more stable are the ones with [100] magnetization direction.

(7) The most stable configuration of CeCoGe₃ is the antiferromagnetic + + --, but it has only slightly lower energy than the + - +- one.

(8) The selection of the on-site repulsion term U_{4f} in the range from about 3 to 6 eV does not change qualitatively the calculated densities of states for antiferromagnetic CeCoGe₃.

(9) The calculated total magnetic moment on Ce (0.43 $\mu_{\rm B}$) for CeCoGe₃ is consistent with the experimental values determined at low temperatures.

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APPENDIX A: MULLIKEN ELECTRONIC POPULATION ANALYSIS

The analysis of the valence band can be extended by an estimation of the partial atomic charges based on the Mulliken approach [73]. Tables III and IV present the results of the Mulliken electronic population analysis for CeCoGe₃ and PrCoGe₃. The Mulliken approach is possible to apply as the utilized FPLO code is based on the linear combination of atomic orbitals method. For CeCoGe₃, we observe that the charge taken from Ce sites (-1.23) is transferred to the Co (+0.17) and Ge (+0.47, +0.30) sites. A similar picture we see also for PrCoGe₃. For both compounds, the chemical bonds result mainly from the interaction of Ce/Pr 5d, Co 3d, and Ge 4p and 4s orbitals. For Ce and Pr sites, we observe a slight depopulation of 5p orbitals and a low occupation of 6s and 6p orbitals. A significant difference between the Ce and Pr electronic configurations is found for 4f orbitals (0.98) versus 2.15) and stems directly from the distinction in atomic numbers of the elements under consideration ($Z_{Ce} = 58$ and $Z_{Pr} = 59$). The calculated occupations of Ce/Pr 4*f* orbitals ($f^{0.98}$ and $f^{2.15}$) are in fair agreement with the main contributions identified from analysis of Ce 3d and Pr 3d spectra coming from f^1 and f^2 states, see Figs. 15 and 16. In the case of Co sites, with regard to the ground-state electronic configuration of a neutral Co atom $(3d^7 4s^2)$, we observe depopulation of the 4s orbitals and increase in the occupation of the 3d orbital. In addition, the Co 4d and 4p orbitals become partially occupied. The latter so-called polarization states are not taken into account in the basic electronic configurations of the neutral atoms or ions. In the case of Ge sites, with regard to the ground-state electronic configuration of a neutral Ge atom



FIG. 25. The colinear magnetic configurations of CeCoGe₃ based on the double unit cell model. [(a) and (b)] Ferromagnetic, [(c) and (d)] antiferromagnetic + - + -, and [(e) and (f)] antiferromagnetic + + - - configurations of spin magnetic moments on Ce sites. Fully relativistic calculations will allow the quantization axes ([001] and [100]) to be considered.

 $(3d^{10} 4s^2 4p^2)$, we observe accumulation of charge on 4p and 4d orbitals and a partial depopulation of 4s orbitals.

APPENDIX B: DETAILS OF ANTIFERROMAGNETIC SOLUTIONS FOR CeCoGe₃

Tran *et al.* have summarized that the theoretical approaches most often used to investigate the prototype α and γ Ce phases are LDA/GGA, LDA/GGA + U, self-interaction corrected LDA (SIC-LDA), and LDA plus dynamic mean-field theory (LDA + DMFT), for more details see Ref. [23]. As it is well-known that the LDA/GGA alone does not reproduce the properties of Ce compounds well, we will go beyond the GGA and apply the intra-atomic Hubbard U repulsion term (GGA + U), which is often used to model f electron systems. We choose the U_{4f} to be equal to 6 eV – a value previously calculated for Ce [32]. Furthermore, we take into account the antiferromagnetic configurations + - +- and + + -suggested by the experiments [14,36].

Among many difficulties related to the LDA/GGA + U description of the magnetic properties of Ce systems, the most important seems to be the emergence of multiple solutions [23,24]. If the applied potential is orbital-dependent, as for the LDA/GGA + U functional, the resultant occupation of

f orbitals strongly depends on the occupation used to run the self-consistent calculations [23]. Different solutions can also be obtained starting from different parameters, like for example the value of initial spin splitting, the value of *U*, or starting the calculation with the spin-orbit coupling enabled. In our calculations for antiferromagnetic (+ + --) configuration of CeCoGe₃, we have found several distinct solutions characterized by different values of magnetic moments. The three characteristic solutions were (1) highly magnetic (spin magnetic moment m_s on Ce atoms equal to about 0.97 μ_B and orbital magnetic moment m_l on Ce atoms equal to about $-1.96 \mu_B$), (2) medium magnetic ($m_s = 1.00 \mu_B; m_l =$ $-0.57 \mu_B$), and nonmagnetic ($m_s = m_l = 0$). The comparison of total energies indicated the ground-state solution with the orbital magnetic moment m_l equal to about $-0.57 \mu_B$.

The Hartree-Fock interaction energy and the doublecounting term of the LDA/GGA + *U* functionals depend on the occupation matrix $n_{m,m'}$, where *m*, *m'* means orbital quantum numbers, for orbital *f* (*l* = 3) taking 7 values (2*l* + 1) from -3 to 3 [23]. The occupation matrix can be used, in some approaches even in a fully controlled manner, to define the occupation of given sets of *d* or *f* orbitals on given sites [74]. The occupation matrix of majority-spin Ce 4*f* orbital of our solutions with $m_l \approx -0.57 \mu_{\rm B}$ is

ſ	0.01	-0.04	0.01	0.00	-0.01	0.04	ך 0.00
	-0.04	0.48	-0.06	0.00	0.06	-0.48	0.04
	0.01	-0.06	0.01	0.00	-0.01	0.06	-0.01
	0.00	0.00	0.00	0.01	0.00	0.00	0.00,
	-0.01	0.06	-0.01	0.00	0.01	-0.06	0.01
	0.04	-0.48	0.06	0.00	-0.06	0.48	-0.04
l	0.00	0.04	-0.01	0.00	0.01	-0.04	0.01

whereas the minority-spin states of Ce 4*f* occupation matrix are nearly empty. A roughly equal amount of $m_l = 2$ and -2in this state corresponds (approximately since the solution is fully relativistic and includes spin-orbit coupling) to the orbital composed as a superposition of spherical harmonics: $f_{xyz} = (Y_3^2 - Y_3^{-2})/(i\sqrt{2})$. Our solution also correlates to the

one called *FM1* obtained for ferromagnetic fcc Ce within the PBE + U approach (U = 4.3 eV) [23] characterized by a very similar magnetic state [$m_s = 1.2 \mu_B$; $m_l = -0.5 \mu_B$ (inside muffin-tin sphere)]. It is worth noting that the compared solutions were obtained using two DFT implementations based on different basis sets, namely local orbitals in the case of FPLO and plane waves in the case of WIEN2K. The magnetic solutions (ferro- and antiferromagnetic) discussed further in this section are very similar to the one which has been just described.

The next issue we will discuss is an impact of the value of the Hubbard U parameter. For this purpose, we will use a representative model of CeCoGe₃ with antiparallel configuration ++-- of magnetic moments on Ce sites. Other considered magnetic configurations will be discussed in details later. While it is known that the application of on-site Hubbard repulsion term to the Ce 4f orbitals qualitatively change the results of the LDA/PBE calculations for Ce-based systems [23,24], a selection of a specific value of U for a given system is sometimes problematic. We decided to set the value of Uequal to 6 eV as calculated for Ce within DFT [32]. However, for example, Tran et al. used for bcc Ce the value of U equal to 4.3 eV, which is the average of two values of U calculated with constrained RPA method for α and γ Ce phases [75]. To better understand how our results are affected by the magnitude of Uvalue, we solve the set of cases with U equal from 0 to 6 eV. In Fig. 23, we see that the value of magnetic moment on Ce changes significantly after applying on-site Hubbard repulsion to the Ce 4f orbitals. At the same time we see that the results are not very sensitive to the value of U in a range from about 3 to 6 eV.

The antiferromagnetic solution for CeCoGe₃ consists of two types of Ce contributions with antiparallel orientation of magnetic moments denoted as Ce \uparrow and Ce \downarrow . Figure 24 shows how the value of U affects the densities of states of Ce \uparrow 4f orbitals, compare with Ref. [24]. For $U_{4f} = 0$, the 4f band is located at Fermi level, similar like in nonmagnetic case with $U_{4f} = 6$ eV, see Fig. 19(b). With an increase in the value of U, the 4f band splits, and the distance between occupied and unoccupied parts grows. For U = 6 eV, the lower Hubbard band is located at about -3 eV, while the upper band is at about 4 eV above the Fermi level. For comparison, a photoelectron spectroscopy of Ce γ phase indicates lower and upper Hubbard bands at -2 and 4 eV, respectively [71,72]. The analysis carried out helps to better understand the effect of U on the results and suggests that 6 eV is one of the reasonable values of U_{4f} for Ce.

As our DFT results present in principle the ground state at 0 K, we are interested in proper modeling of the ground-state magnetic configuration. In the case of CeCoGe₃, low-temperature measurements suggest antiferromagnetic ground state. However, as we have already presented, there is no agreement on the details of the magnetic configuration. Pecharsky *et al.* suggest + - + - ordering [36], whereas Smidman *et al.* deduced + + - - configuration at 2 K [14]. The next question to which the calculations can provide answers is the direction of local magnetic moments on Ce, however, here our method is limited to consider only colinear solutions. Looking for an answer, we prepared the models with antiferromagnetic (+ - + - and + + - -) and ferro-

TABLE V. Spin (m_s) and orbital (m_l) magnetic moments $(\mu_B \text{ (atom or f.u.)}^{-1})$ on Ce sites calculated for considered colinear magnetic configurations of CeCoGe₃, see Fig. 25. Magnetic moments are calculated with FPL018 in relativistic approach applying PBE + $U (U_{4f} = 6 \text{ eV})$. Two slightly different values of m_s for + + -- configuration are present within single solution.

	FM (++++)		AFM (+ - +-)		AFM (++)	
axis	m _s	m_{l}	m _s	$m_{\rm l}$	m _s	$m_{\rm l}$
001	1.001	-0.563	1.003	-0.561	1.000/1.004	-0.562
100	1.001	-0.571	1.004	-0.572	1.001/1.004	-0.571

magnetic configurations of spin magnetic moments on Ce sites, see Fig. 25. To construct the + + -- configuration we had to double the unit cell and reduce the symmetry according to magnetic ordering. To be able to accurately compare the total energies between the + + -- configuration and other solutions, the remaining models (+ - +- and ferromagnetic) have been prepared within the same double cell approach, even though in these cases in principle it would be possible to use a single unit cell. In addition, we consider cases with magnetization pointing towards [001] and [100] direction.

The calculated magnetic moments on Ce sites for considered colinear magnetic configurations are presented in Table V.

The comparison of total energies (Fig. 26), indicates that in each case the [100] magnetization direction is energetically more stable than the [001], which means that the magnetic moments prefer to order in *ab* plane than along *c* axis. The similar orientation of magnetic moments in the ground-state magnetic configuration has been suggested from experiment [36]. However, in our model, we do not consider the small canting of magnetic moments suggested by the same experimental results [36]. In all our cases, the energy difference between [100] and [001] solutions is about 0.1 meV f.u.⁻¹ (about 0.2 MJ m⁻³) which is comparable to the values of magnetocrystalline anisotropy obtained for semi-hard ferromagnets [76]. A further comparison of all cases shows that the lower energies have been determined for antiferromagnetic solutions, with the lowest energy being calculated for



FIG. 26. The energy distance to the antiferromagnetic + + --[100] configuration (E_0). The considered colinear magnetic configurations of CeCoGe₃ are based on the double unit cell model, see Fig. 25. Total energies are calculated with FPL018 in fully relativistic approach and applying PBE + U ($U_{4f} = 6 \text{ eV}$).

+ + -- [100] configuration, which we since now will consider as the ground-state solution (from among the considered colinear cases). Although the whole set of the obtained results indicates + + -- solution as the ground state, the energy

- distance between + + -- [100] and + +- [100] solution is very small (about 0.01 meV f.u.⁻¹) and lies at the limit of
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