

## Suppression of indirect exchange and symmetry breaking in the antiferromagnetic metal HoB<sub>12</sub> with dynamic charge stripes

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Precise angle-resolved magnetoresistance (ARM) measurements are applied to reveal the origin of symmetry lowering in electron transport and the emergence of a huge number of magnetic phases in the ground state of the antiferromagnetic metal HoB<sub>12</sub> with *fcc* crystal structure. By analyzing the polar  $H$ - $\theta$ - $\varphi$  magnetic phase diagrams of this compound reconstructed from the experimental ARM data, we argue that nonequilibrium electron density oscillations (dynamic charge stripes) are responsible for the suppression of the indirect Ruderman-Kittel-Kasuya-Yosida exchange along the  $\langle 110 \rangle$  directions between the nearest neighboring magnetic moments of Ho<sup>3+</sup> ions in this strongly correlated electron system.

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### I. INTRODUCTION

The concurrence between different simultaneously active charge, spin, lattice, and orbital interactions is believed to play a key role in the formation of a rich variety of magnetic structures in phase diagrams of strongly correlated electron systems (SCES) [1]. A well-known example are the manganites with colossal magnetoresistance that demonstrate an enormous number of different states including ferro- and antiferromagnetic (AF) long-range ordering, magnetic short-range correlations, charge and spin density waves, and diversity of structural transitions [1–3]. In the family of cuprates, the competition of high temperature superconductivity with AF ordering is complemented by spin and charge ordering, pseudogap states, and the unusual “strange metal” phase with non-Fermi-liquid behavior at intermediate temperatures [4–6]. Very complicated phase diagrams have been also found in ruthenates [7], organic charge-transfer salts [8], superconducting iron-based pnictides and chalcogenides [9,10], and in Ce-based heavy fermion metals [11], where electron nematic phases were detected. The contention of various states leads often to nanoscale phase separation and spatially inhomogeneous phases that is extremely useful for practical applications due to giant responses to weak enough external perturbations. Unfortunately, the common features of the effects arising in most of these SCES cannot be easily analyzed since these compounds possess a complex chemical composition with a low symmetry crystal structure.

It was recently demonstrated that Ho<sub>x</sub>Lu<sub>1-x</sub>B<sub>12</sub> dodecaborides with a face-centered-cubic (*fcc*) crystal structure may be treated as model SCES, which show electronic phase separation [dynamic charge stripes along the  $\langle 110 \rangle$  axis,

Fig. 1(a)] in combination with dynamic Jahn-Teller instability and a frustrated AF ground state with Néel temperature  $T_N \leq 7.4$  K [12–15]. In these compounds, the competition between Ruderman-Kittel-Kasuya-Yosida (RKKY) oscillations of the electron spin density [indirect exchange interaction, Fig. 1(b)] and quantum oscillations of the electron density (dynamic charge stripes) is shown to result in an extremely complicated and anisotropic magnetic phase diagram, which has a form of Maltese cross with a huge number of various magnetic phases [14–16]. Since the arrangement of magnetic phases depends dramatically both on the magnitude and direction of external magnetic field, high precision studies of charge transport were performed here to reconstruct the three-dimensional (3D)  $H$ - $\varphi$ - $\theta$  magnetic phase diagram of HoB<sub>12</sub>. As a result, we argue that nonequilibrium electron density oscillations (stripes) seem to be responsible for the suppression of the indirect exchange interaction along the  $\langle 110 \rangle$  directions and lead to symmetry breaking in this strongly correlated electron system.

### II. RESULTS AND DISCUSSION

Detailed studies of heat capacity, magnetization, and magnetoresistance were performed on high-quality single-domain and isotopically enriched (<sup>11</sup>B) single crystals of Ho<sup>11</sup>B<sub>12</sub> ( $T_N \approx 7.4$  K). The related experimental details are shown in the Supplemental Material [17]. The  $H$ - $T$  magnetic phase diagrams were reconstructed for three principal directions  $\mathbf{H}||[100]$ ,  $\mathbf{H}||[110]$ , and  $\mathbf{H}||[111]$  displaying numerous magnetic phases and phase transitions [Figs. 1(c)–1(e)]. It is worth noting that in contrast to the nearly isotropic AF-P transition (P is the paramagnetic state) in the  $H$ - $T$  diagram, the location

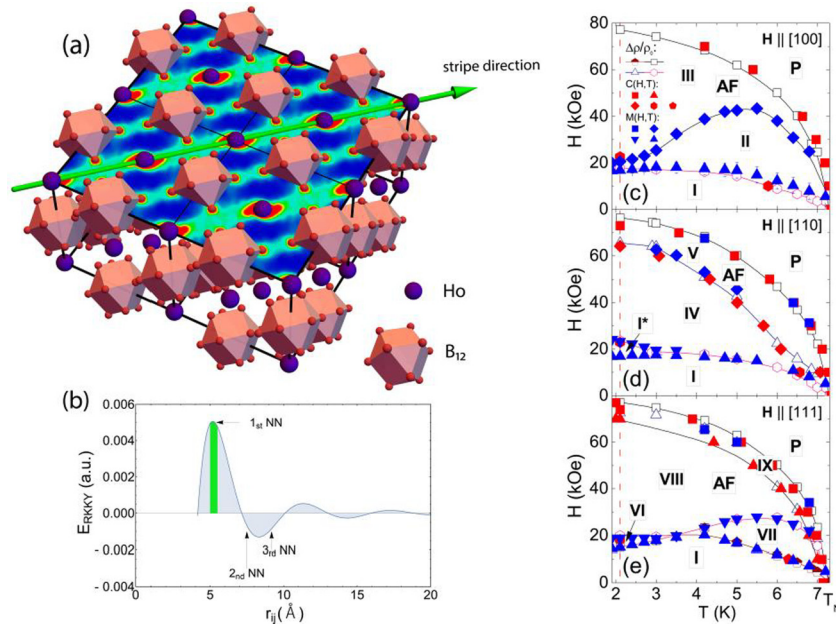


FIG. 1. (a) Crystal structure of  $RB_{12}$ . The color plane shows the distribution of the electron density in the dynamic charge stripes (green bands) along with  $[110]$  direction [12]. (b) RKKY exchange interaction function in  $RB_{12}$ . The vertical green band marks the distance where the dynamic charge stripes destroy the indirect magnetic exchange. Arrows show the position of first ( $1_{\text{st}}$  NN), second ( $2_{\text{nd}}$  NN) and third ( $3_{\text{rd}}$  NN) nearest neighbor magnetic ions in the *fcc* lattice. (c)–(e)  $H$ - $T$  magnetic phase diagrams of  $\text{Ho}^{11}\text{B}_{12}$  obtained from magnetoresistance  $\Delta\rho/\rho_0$ , heat capacity  $C(T, H)$  and magnetization  $M(T, H)$  measurements [see legend in panel (c)] for three principal directions  $H \parallel [100]$ ,  $H \parallel [110]$ , and  $H \parallel [111]$  [panels (c), (d), and (e), respectively]. Roman numerals indicate different AF phases, P denotes the paramagnetic state. The red dotted vertical line indicates the temperature  $T = 2.1$  K where the measurements leading to the  $3D$  ( $H$ - $\varphi$ - $\theta$ ) diagram were performed.

of phase boundaries inside the AF phase is considerably different for various  $H$  directions [Figs. 1(c)–1(e)]. The results of our precise measurements allowed us to refine the  $H$ - $T$  diagrams detected previously in Refs. [16,18,19]. Besides, we show below that despite the high symmetry of the crystal lattice are the magnetic phases for the principal field directions separated by radial phase boundaries and, hence, these phases are completely different, and that only one low-field AF state (marked as I in Fig. 1) exists for any magnetic field orientation.

To clarify the location of phase boundaries in the AF state in external magnetic field up to 80 kOe, angle-resolved magnetoresistance (ARM) was investigated at fixed temperature  $T = 2.1$  K [see vertical dotted line in Figs. 1(c)–1(e)] in four experiments with sample rotating around excitation current directions (i)  $I \parallel [100]$ , (ii)  $I \parallel [1\bar{1}0]$ , (iii)  $I \parallel [111]$ , and (iv)  $I \parallel [112]$ . For example, the experimental data obtained with rotating around  $I \parallel [100]$  [see case (i) above] are presented in Fig. 2. Results of these experiments may be summarized as follows. Firstly, only a slight cosine-like  $\rho(\varphi) \sim \cos(2\varphi)$  modulation is detected when the magnitude of  $H$  does not exceed  $\sim 20$  kOe [the phase boundary position, which restricts the “I” phase, see Figs. 1(c)–1(e)]. Secondly, the increase of magnetic field above  $\sim 25$  kOe leads to two additional features (sharp peaks in the neighborhood of  $\langle 110 \rangle$  directions and “horns” that are symmetrical to the  $\langle 100 \rangle$  axis) appear and become broader with  $H$  increase. Thirdly, the cosine-like behavior is restored above the Néel field ( $H_N \sim 76$  kOe) with two additional features, different from the low-field data: (a) the phase of cosine is shifted by 45 degrees and (b) a narrow local minimum of tiny amplitude appears near the  $\langle 001 \rangle$  direction.

It is worth noting that abrupt anomalies in the AF phase observed in the wide neighborhood of  $\langle 100 \rangle$  directions may be associated with magnetic phase transitions between states with different magnetic order [13,14]. Besides, the unusual behavior of sharp peaks in the vicinity of  $\langle 110 \rangle$  directions is

suggested to be induced by the dynamic charge stripes along  $\langle 110 \rangle$  axis [see Fig. 1(a)].

The same features can be easily resolved on magnetic field dependences of resistivity measured at the same configura-

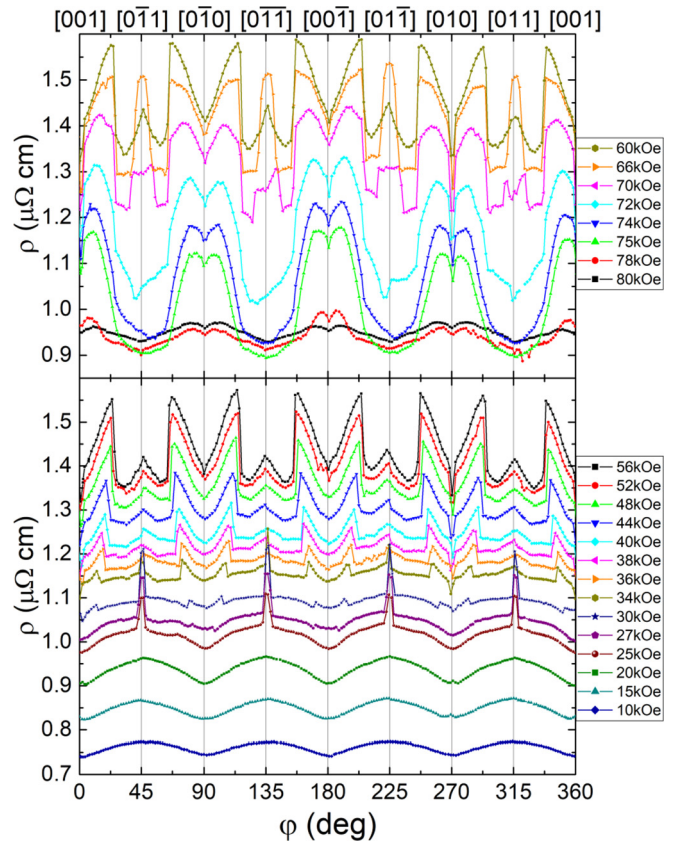


FIG. 2. Angular dependences of  $\text{Ho}^{11}\text{B}_{12}$  resistivity for the various magnetic field at  $T = 2.1$  K. The rotation was performed around the axis  $I \parallel [100]$ . Vertical lines indicate the positions when the magnetic field  $H$  is aligned with principal axes.



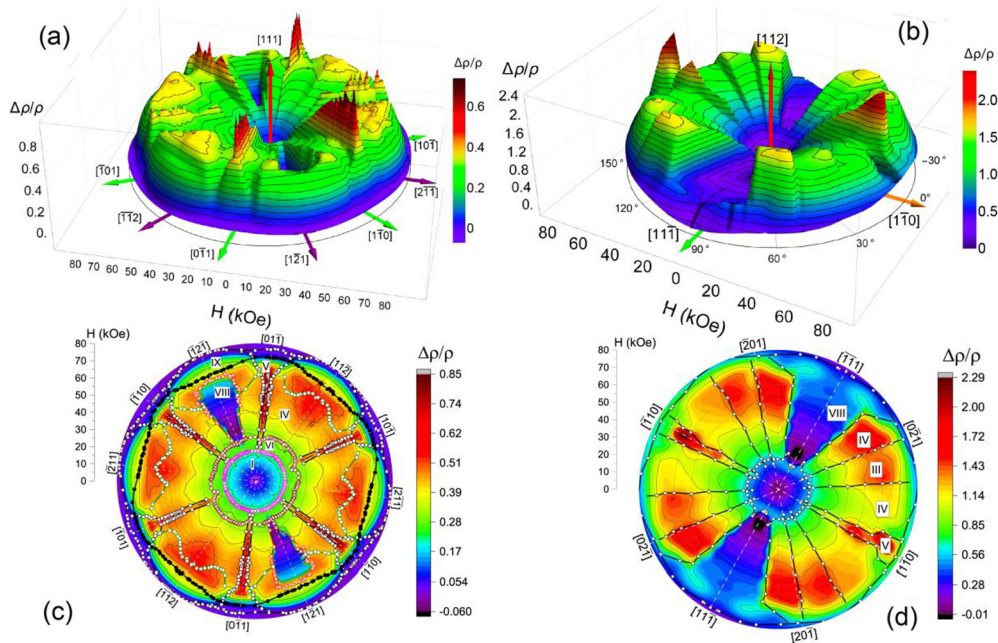


FIG. 5. Magnetoresistance  $\Delta\rho/\rho = f(H, \varphi)$  of the  $\text{Ho}^{11}\text{B}_{12}$  in cylindrical coordinates for the current direction  $I||[111]$  (a) and  $I||[112]$  (b) and its projection onto (111) and (112) planes (c) and (d), respectively at  $T = 2.1$  K. Roman numerals show different magnetic phases in the AF state.

with a radius of  $H \sim 20$  kOe; (2) the area in the wide neighborhood of [100] direction where the maximum MR values are achieved; (3) the region with the minimum MR values around [111] direction; (4) the zone with positive MR that is symmetrical concerning the direction of dynamic charge stripes  $\mathbf{H}||[110]$ .

Note, that the edges of these plane  $H$ - $\varphi$  diagrams [Figs. 4(c), 4(d), 5(c), and 5(d)] provide important information related to the arrangement of four different sections of the spherical  $H$ - $\varphi$ - $\theta$  (3D) magnetic phase diagram in cases when the  $\mathbf{H}$  vector lies in planes perpendicular to the measuring current axes. Figure 6(a) shows the combined  $H$ - $\varphi$  planes for measuring current directions  $I||[100]$  and  $I||[1\bar{1}0]$  [see Figs. 4(c)–4(d)] for  $\text{Ho}^{11}\text{B}_{12}$  at  $T = 2.1$  K and presents also schematic views of the main regions [phases I, III, IV, and VIII in Figs. 4(c)–4(d)] in the 3D  $H$ - $\varphi$ - $\theta$  space constructed with the help of two more sets of experimental data (iii)  $I||[111]$  and (iv)  $I||[112]$  [see Figs. 5(c) and 5(d)]. Since these four  $H$ - $\varphi$  planes for various measuring current directions were obtained on different samples cut from one single crystal ( $\mathbf{n}||[110]$

plate) of  $\text{Ho}^{11}\text{B}_{12}$ , we can compare rather the behavior of MR than the absolute values of MR amplitude. However, it can be seen that the phase boundaries obtained from these experiments with different rotational axes coincide very well. One more schematic view (the projection on the spherical surface) of three basic high-field phases (III, IV, and VIII) is shown in Fig. 6(b). It is worth noting that these three segments corresponding to three different types of magnetic phases [III, IV, and VIII, see Figs. 4, 5, and 6(a)] in combination with the low-field spherical area [phase I, Figs. 4(c), 4(d), 5(c), 5(d), and 6(a)] fill almost completely the space inside the AF region in the 3D  $H$ - $\varphi$ - $\theta$  phase diagram. The dashed lines in Fig. 6(b) indicate the angular  $\varphi = (\mathbf{n}, \mathbf{H})$  trajectories in these four experiments: (i) A-B-A corresponds to rotation from  $\mathbf{H}||[010]$  to  $\mathbf{H}||[001]$  [see Fig. 4(c)]; (ii) A-C-B corresponds to rotation from  $\mathbf{H}||[001]$  to  $\mathbf{H}||[110]$  [see Fig. 4(d)]; (iii) B-c-B corresponds to rotation from  $\mathbf{H}||[011]$  to  $\mathbf{H}||[110]$  [see Fig. 5(c)], and (iv) B-a-b-C corresponds to rotation from  $\mathbf{H}||[011]$  to  $\mathbf{H}||[111]$  [see Fig. 5(d)]. Thus, it is obvious that despite the partial similarity of the borders in  $H$ - $T$  phase diagrams of

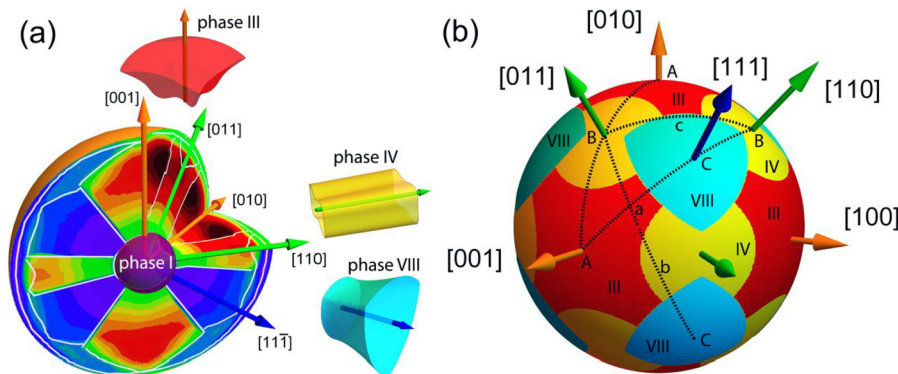


FIG. 6. (a)  $H$ - $\varphi$  phase diagrams of  $\text{HoB}_{12}$  for current directions  $I||[100]$  and  $I||[1\bar{1}0]$  combined into one 3D  $H$ - $\varphi$ - $\theta$  phase diagram. Purple, cyan, yellow, and red shapes show four key segments (phases I, VIII, IV, and III, correspondingly) in the center and in the vicinity of principal axes that determine the anisotropy of the phase diagram. (b) Schematic view of the projection on the spherical surface at  $H \sim 60$  kOe of three basic high-field phases (III, IV, and VIII) in the  $H$ - $\varphi$ - $\theta$  phase diagram. The dashed lines in panel (b) indicate the trajectories of angle  $\varphi$  variation in four experiments with sample rotation (see text for details).

$\text{Ho}^{11}\text{B}_{12}$  for various magnetic field directions [Figs. 1(c)–1(e)], the set of phases in three principal directions is almost completely different. Such a pronounced anisotropy of charge carriers scattering and of the magnetic phase diagram should be associated with the interaction of the external magnetic field with the dynamic charge stripe structure in  $\text{Ho}^{11}\text{B}_{12}$ . Note that the observed effects cannot be related to the Fermi surface (FS) topology of the  $\text{RB}_{12}$  compound. The main sheet of the FS of  $\text{RB}_{12}$  has the form of a “monster” [20–22] with open orbit directions along the  $\langle 111 \rangle$  axis. Despite the highly anisotropic hole sheet, the electron FS sheet is quite isotropic. Moreover, taking into account the small enough mean free path of electrons/holes, the low-field regime  $\mu_H H \ll 1$  of charge transport is valid even in the nonmagnetic reference compound  $\text{LuB}_{12}$ , so it seems natural that the obtained complex magnetic phase diagram cannot be associated with the FS anisotropy. Besides, if considering the stripes as the main factor to be responsible for a strong renormalization of the indirect RKKY exchange interaction, one needs to expect a huge suppression of the nearest neighbor exchange ( $J_1$ ) in this model AF metal. Indeed, the long-range RKKY magnetic interaction between localized magnetic moments of  $d$ , or  $f$  orbitals in metals is transmitted by spin density oscillations of conduction electrons [see Fig. 1(b)], and these are suppressed dramatically in the presence of dynamic charge stripes (fast quantum vibrations of the nonequilibrium charge density with a frequency of  $\sim 200$  GHz [23]) directed along the  $\langle 110 \rangle$  axes. Thus, the stripe direction corresponds to the location of neighboring magnetic ions [Figs. 1(a), the Ho-Ho distance is about 5.3 Å] and destroys totally the nearest neighbor RKKY interaction (Fig. 1).

To support these ARM experimental findings an independent estimate of the nearest neighbor ( $J_1$ ) and next-nearest neighbor ( $J_2$ ) interactions was undertaken [24]. With this purpose, the magnon dispersion data in  $\text{HoB}_{12}$  [19] were compared with the results of classical Monte Carlo (MC) simulation. The full version of the MC study will be published elsewhere [25]. It is worth noting here that the deduced very small  $J_1$  value detected in the MC simulations confirm the suppression of RKKY exchange interaction between the nearest Ho ions in the model antiferromagnet.

### III. CONCLUSION

In summary, the model SCES  $\text{Ho}^{11}\text{B}_{12}$  compound with incommensurate AF structure, cooperative Jahn-Teller instability of boron network, and dynamic charge stripes was studied in detail by ARM measurements at liquid helium temperature. For this nonequilibrium AF metal, strongly anisotropic polar  $H$ - $\varphi$ - $\theta$  magnetic phase diagrams were reconstructed. It is shown that they consist of four basic sectors: a spherical low-field region and three variously complicated cone-shaped segments detected in the vicinity of principal directions: (a) along ( $\mathbf{H} \parallel [110]$ ) and (b) transverse to ( $\mathbf{H} \parallel [001]$ ) the dynamic charge stripes, and (c) parallel to the axis of magnetic structure ( $\mathbf{H} \parallel [111]$ ) in the  $fcc$  lattice. We argue that *the strong anisotropy* both of the phase diagram and the charge transport *is a fingerprint of the electron instability* related to the formation of a filamentary structure (fluctuating charge carrier channels along  $[110]$  direction) of nonequilibrium electrons. As a result, *the indirect RKKY exchange interaction* between the nearest neighbor magnetic ions located at the distance of  $\sim 5.3$  Å in  $\langle 110 \rangle$  directions *is dramatically destroyed providing magnetic symmetry lowering* and leading to field-angular phase diagrams with a huge number of magnetic phases and phase transitions.

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