Hidden magnetic order in the triangular-lattice magnet Li₂MnTeO₆

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The manganese tellurate Li₂MnTeO₆ consists of trigonal spin lattices made up of Mn⁴⁺ (d^3 , S = 3/2) ions. The magnetic properties of this compound were characterized by several experimental techniques, which include magnetic susceptibility, specific-heat, dielectric permittivity, electron-spin-resonance, nuclear magnetic resonance (NMR), and neutron powder-diffraction measurements, and by density functional theory calculations. The magnetic susceptibility $\chi(T)$ demonstrates very unusual behavior. It is described by the Curie-Weiss law at high temperature with Curie-Weiss temperature of $\Theta = -74$ K and exhibits no obvious anomaly indicative of a long-range magnetic ordering at low magnetic fields. At high magnetic fields, however, the character of $\chi(T)$ changes showing a maximum at about 9 K. That this maximum of $\chi(T)$ reflects the onset of an antiferromagnetic order was confirmed by specific-heat measurements, which exhibit a clear λ -type anomaly at $T_N \approx 8.5$ K even at zero magnetic field, and by ⁷Li NMR and dielectric permittivity measurements. The magnetic structure of Li₂MnTeO₆, determined by neutron powder-diffraction measurements at 1.6 K, is described by the 120° noncollinear spin structure with the propagation vector $\mathbf{k} = (1/3, 1/3, 0)$. Consistent with this finding, the spin-exchange interactions evaluated for Li_2MnTeO_6 by density functional calculations are dominated by the nearest-neighbor antiferromagnetic exchange within each triangular spin lattice. This spin lattice is strongly spin frustrated with $f = |\Theta|/T_N \approx 8$ and exhibits a two-dimensional magnetic character in a broad temperature range above T_N .

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I. INTRODUCTION

Systems staying in a disordered spin-liquid-like state down to lowest temperatures are of great interest as candidates in which to discover quantum phenomena [1–4]. The most promising candidates are low-dimensional frustrated magnets, which are prevented from achieving a long-range order (LRO) by Mermin-Wagner theorem [5]. Though rare, there occurs an exotic situation in which a system undergoes a long-range ordering but its observation is hampered [6–8]. In this case, the standard macroscopic magnetic techniques such as magnetic susceptibility, specific heat, or even neutron-scattering measurements are insufficient for gaining insight into the ground state of a magnetically ordered solid, particularly if it exhibits

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a short-range order or nearly random order. Systems possessing this type of hidden magnetic order have not been well studied, and studies on such systems can lead to interesting results.

Historically, the heavy Fermion material URu₂Si₂ was an early compound for which a hidden (i.e., not observable by standard techniques) magnetic order was discovered [9,10]. Numerous experimental efforts have been made to uncover the true nature of this phenomenon with tiny magnetic moments below a transition temperature. One of the recent explanations includes the formation of a nontrivial magnetic dotriacontapole (rank 5) moment as the order parameter [7]. The cause for the violation of the Stoner criteria in actinides is thought to arise from a strong spin-orbit coupling. In contrast to conventional magnets, therefore, the Fermisurface nesting stabilizes staggered multipole moments, which can be viewed as an unconventional density wave (UDW) [6,7,11].

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FIG. 1. Polyhedral view of the layered crystal structure of $\text{Li}_2\text{MnTeO}_6$ ($P\bar{3}1c$ space group): (a) A perspective view of layers. (b) A projection of the layer of magnetic ions along the *c* direction, in which the MnO₆ and TeO₆ octahedra alternate sharing their edges. The green and blue octahedra represent the MnO₆ and TeO₆, respectively. The Li and O atoms are represented by yellow spheres and black balls, respectively.

In ferropnictide superconductors, the magnetic moments on iron cancel out below the quantum critical point. The hidden magnetic order behind this observation was related to a weak Hund's rule coupling, in contrast to a commensurate spin-density wave (cSDW), which occurs at a strong Hund's rule coupling [12]. It was assumed that injected mobile holes can account for the nature of low-energy single-particle excitations in the hidden magnetic order states in ferropnictide materials.

There are a few remarkable examples of hidden magnetic order in low-dimensional magnets. In particular, an intricate magnetic transition around 70 K has been observed for quasione-dimensional (1D) spin-lattice semiconducting magnet CuNCN [8]. Despite the lack of specific-heat anomaly as well as the missing magnetic scattering in the neutron-diffraction data, the antiferromagnetic (AFM) LRO was evidenced by a bending in the temperature dependence of the magnetic susceptibility and clearly established by the spectroscopic techniques like Muon spin rotation, relaxation and resonance (μ SR), electron-spin resonance (ESR), and NMR [13]. It has been shown that the experimental observation of the LRO has been impeded by strong quantum fluctuations that reduce the Néel temperature and the ordered moment.

The coexistence of two spin sublattices with mixed dimensionalities [e.g., 1D and two-dimensional (2D)] and energy scales was believed to be the reason for the hidden magnetic order in another Cu-based compound CuP₂O₆ [14]. The ordering weakly manifests itself in the magnetic susceptibility but has not been seen by neutron diffraction, while ESR data confirm the LRO onset with low net moment indicating substantial fluctuations that persist even below T_N .

An unusual hidden magnetic ordering occurs in an insulating oxide Sr_2VO_4 at low temperature [15–19], for which several possible scenarios have been mentioned including an orbital ordering triggered by Jahn-Teller distortion [15], an unconventional magnetic octupolar ordering [20], and a Néel order with muted order parameter of $0.06 \,\mu_B$ (compared to $1 \,\mu_B$ in a classical spin-1/2 system) [16,19]. A direct confirmation of the LRO and inhomogeneous magnetic state was obtained by μ SR studies [17], while recent theoretical calculations predict the single-stripe magnetic ordering [18]. In the present paper, we examine the properties of a quasi-2D triangular lattice compound Li_2MnTeO_6 , which belongs to the A_2MnTeO_6 (A = Li, Na, Ag, Tl) structural family of frustrated low-dimensional magnets [21], to find that the magnetic properties of Li_2MnTeO_6 are similar to those magnets possessing unusual hidden magnetic order.

II. EXPERIMENT

Powder samples of Li₂MnTeO₆ were prepared by a moltensalt ion exchange reaction of the isostructural Na₂MnTeO₆, as reported previously [21]. Li₂MnTeO₆ crystallizes in the space group $P\bar{3}1c$. The Mn⁴⁺ and Te⁶⁺ cations of Li₂MnTeO₆ form magnetic honeycomb layers, which alternate with nonmagnetic layers of Li⁺ cations. Each individual (MnTeO₆)²⁻ layer is essentially ordered such that the magnetic Mn⁴⁺ ions form a triangular network consisting of weak spin-exchange paths Mn-O-Te-O-Mn (Fig. 1). Thus, the crystal structure provides the conditions necessary for low-dimensional frustrated magnetic interactions.

The temperature-dependent magnetic susceptibilities were measured at the magnetic field B = 0.1, 1, 3, 6, and 9 Tin the temperature range 2-300 K by means of a Quantum Design physical property measurement system (PPMS) using a vibrating-sample magnetometer Teflon capsule with 34 mg of powder sample. Specific-heat measurements were carried out by a relaxation method using a Quantum Design PPMS system on a cold-pressed 5.03-mg sample. The data were collected at zero magnetic field as well as under applied fields of 3, 6, and 9 T in the temperature range 2-300 K. The dielectric constant was measured on a Quantum Design magnetic property measurement system (MPMS) XL-7 system using a custom-made insert and Andeen-Hagerling 2700A capacitive bridge. The measurements were performed at various frequencies in the 1-20-kHz range at temperatures from 2 to 300 K in zero magnetic field. The resolution of the Andeen-Hagerling 2700A bridge is 2.4-16 aF depending on the frequency. In addition, the device can measure the loss tangent up to 1.5×10^{-8} , the conductivity down to 3×10^{-16} S, or the resistance up to 1.7×10^{15} Ohm, with the operating voltage of 15 V. The duration of one measurement is from 30 ms to 0.4 s. The sample for dielectric permittivity

measurements was a plane-parallel disk with a diameter of up to 6 mm and a thickness of up to 3 mm. A silver paste, "LietSilber," was applied to both sides of the disk, resulting in a capacitor. The sample was mounted in the measuring insert for the MPMS XL-7 system, which was used to control the temperature and external magnetic field.

Electron spin resonance (ESR) studies were carried out using an X-band ESR spectrometer CMS 8400 (ADANI) ($f \approx$ 9.4 GHz, $B \leq 0.7$ T) equipped with a low-temperature mount, operating in the 6–270-K range. The effective g factor of our sample was calculated with respect to an external reference for the resonance field. We used a g-bisdiphenyline-bphenylallyl (BDPA) ($g_{et} = 2.00359$) as a reference material. Nuclear magnetic resonance (NMR) measurements were carried out for ⁷Li nuclei (spin I = 3/2, gyromagnetic ratio $\gamma_n =$ 16.55 MHz/T) at constant frequencies 13.0 and 116.56 MHz in the temperature range 4.2-100 K. The data were collected using a Tecmag Redstone pulse solid-state NMR spectrometer. For recording the spectra, we used a solid-echo sequence as the main experimental technique. The magnetic field varied in the range of 0.59–0.99 T and 6.87–7.22 T with a step from 0.01 to 0.0005 T depending on the measurement temperature. The relaxation rates were measured by the saturation recovery method. The nuclear magnetization M versus the pulse delay time τ was fitted to a single exponential function $M(\tau) = M0\{1 - f \exp[-(\tau/T_1)^b]\}$ with 0.7 < f < 0.9 (f = 1 for ideal saturation). The constant b = 1 at T > 10 K but decreases slightly at low temperatures indicating the growth of electron-spin system anisotropy. In principle, the main line of spin = 3/2 nuclei is described by a double-exponential dependence. In the present case, however, a single-exponential dependence describes the experiment more correctly, since the line shows a strong inhomogeneous broadening and since quadrupole satellites are not resolved. Dynamic studies (ESR and NMR) were carried out using powder samples of 38 and 43 mg, respectively.

NPD measurements were carried out at the spallation neutron source SINQ at PSI Villigen using the two instruments, DMC (cold neutron powder diffractometer) and HRPT (high-resolution powder diffractometer for thermal neutrons). The HRPT diffractometer uses thermal neutrons with $\lambda = 1.886$ Å, monochromatized by a focusing singlecrystal germanium monochromator with Ge (335) reflection. The fixed take-off monochromator angle was 120°. Neutrondiffraction patterns were collected in the 2θ diffraction angle range of 3.55° –164.50° with steps of 0.05°. The sample was placed into a thin-walled cylindrical vanadium container with dimensions $6 \text{ mm} \times 50 \text{ mm}$. HRPT measurements at room temperature were carried out to verify the quality of the sample and refine the crystal structure. The latter is possible due to the high resolution of the diffractometer. Measurements at the lowest achieved temperature, T = 1.6 K, were carried out to record magnetic neutron scattering associated with a long-range magnetic order. This allows one to construct and describe the spin structure in the ground state.

To analyze the temperature evolution of the magnetic scattering, neutron-diffraction patterns were measured on a high intensity DMC powder diffractometer using cold neutrons monochromatized with a graphite monochromator. The measurements were carried out at a wavelength $\lambda = 2.4575$ Å of



FIG. 2. Refined neutron-diffraction pattern of Li_2MnTeO_6 measured on the HRPT diffractometer at T = 300 K. The red dots represent the experimental data, the black line shows the calculated intensity, the green ticks indicate the position of the Bragg reflections, and the blue line shows the difference between experimental and calculated data, plotted at the bottom for convenience.

the neutron beam incident on the sample in the angular range of 5.0° -86.7° with a step of 0.1°. The neutron-diffraction patterns were recorded at temperatures T = 1.6, 2.5, 4, 6, 10, 20 K. All diffraction patterns from HRPT and DMC were treated with the Rietveld method using the FULLPROF suite [22].

III. RESULTS AND DISCUSSION

A. Sample characterization

The neutron-diffraction pattern measured on the HRPT at room temperature and the results of its Rietveld refinement are presented in Fig. 2. It clearly demonstrates the high quality of the sample under study and the absence of any meaningful impurities. All diffraction peaks, even low-intensity ones, are well described in terms of the space group $P\bar{3}1c$ [$a = b = 5.017 \ 10(6)$ Å, c = 9.5267(2) Å at T = 300 K]. The narrow and symmetrical shapes of the diffraction maxima indicate a high crystallinity of the sample. A microstructural analysis using the Rietveld refinement has slightly improved the quality of the fit due to the introduction of microstrains.

There is a significant difference in magnitude and even sign in the neutron-scattering lengths of the elements constituting the compound (i.e., $b_{\text{Li}} = -0.19 \times 10^{-12} \text{ cm}, b_{\text{Mn}} = -0.37 \times 10^{-12} \text{ cm}, b_{\text{Te}} = 0.82 \times 10^{-12} \text{ cm}, \text{ and } b_{\text{O}} = 0.58 \times 10^{-12} \text{ cm}$). Thus, neutron-diffraction measurements are especially important for the analysis of the possible substitutional defects, which often happen in similar layered oxides.

B. Static magnetic properties and dielectric permittivity

The temperature dependence of the magnetic susceptibility $\chi = M/B$ of Li₂MnTeO₆, measured in the field B = 0.1 T, is



FIG. 3. The temperature dependence of the magnetic susceptibility $\chi = M/B$ for Li₂MnTeO₆ at B = 0.1 T in both FC and ZFC modes (upper panel) and the integrated ESR intensity (green symbols). The inset to this panel represents the M/B(T) curves for the Li₂MnTeO₆ at various external magnetic fields. The solid red curve represents the Curie-Weiss law. The temperature dependence of the Curie constant $C = (\chi - \chi_0)(T - \Theta)$ is shown in the lower panel along with the inverse magnetic susceptibility $1/\chi$. The dashed line represents the limiting value C = 1.84 emu/(mol K).

shown in Fig. 3. The zero-field-cooled (ZFC) and field-cooled (FC) susceptibilities do not show noticeable divergence indicating the absence of impurities and spin-glass effects. This is in good agreement with the neutron data, which indicate a high purity of the sample. In weak magnetic fields, the behavior is almost a Curie-Weiss type without any clear anomaly that can be associated with a long-range magnetic order. It is found, however, that an increase in the probe magnetic field strength leads to significant changes in the behavior of the temperature dependence of the susceptibility with the appearance of a maximum of M(T) at approximately $T_{\text{max}} \approx 9.2$ K (inset in Fig. 3). In the paramagnetic state, the $\chi(T)$ can be approximated by a modified Curie-Weiss law with $\chi =$ $\chi_0 + C/(T - \Theta)$, where χ_0 is the temperature-independent term, *C* is the Curie constant, and Θ is the Weiss temperature.

The diamagnetic contribution χ_{dia} was determined by summing up the Pascal constants [23] and was fixed to reduce the number of variable parameters in the fitting analysis, which yields C = 1.84 emu K/mol and $\Theta = -74 \pm 1 \text{ K}$. The obtained Curie constant *C* gives the value of the effective magnetic moment as $\mu_{\text{eff}} = \sqrt{8C} \mu_{\text{B}} = 3.84 \mu_{\text{B}}$, which is in good agreement with theoretical estimation $\mu_{\text{theor}} = \sqrt{g^2 S(S+1)} \mu_{\text{B}} = 3.87 \mu_{\text{B}}$ for Mn⁴⁺ (S = 3/2). The Curie-Weiss temperature Θ is negative and relatively large in comparison with the $T_{\text{max}}(\approx 9.2 \text{ K})$, indicating the presence of dominant antiferromagnetic exchange interactions. With the frustration index $f = |\Theta|/T_{\text{N}} \approx 8$, the extent of spin



FIG. 4. The specific heat of Li_2MnTeO_6 (filled symbols) and that of nonmagnetic isostructural analog Na₂GeTeO₆ (open circles) under zero magnetic field. The upper inset shows the magnetic specific heat $C_m(T)$ (green symbols) and the magnetic entropy $S_m(T)$ (violet symbols). The red line is the result of the spin-wave theory. The lower inset shows $C_p(T)$ under various magnetic fields, where the data were shifted upwards for clarity.

frustration in the spin lattice is appreciable. In addition, at temperatures below ~ 150 K, a noticeable deviation of the $\chi(T)$ from the Curie-Weiss law is observed. This indicates the occurrence of strong short-range exchange interactions and a nontrivial ground state (lower panel of Fig. 3).

Despite the absence of a sharp anomaly in the magnetic susceptibility in weak magnetic fields, the low-temperature data on the specific heat unambiguously indicate the onset of a long-range magnetic order in Li₂MnTeO₆. The data on the specific heat $C_p(T)$ in a zero magnetic field exhibit a distinct λ -type anomaly, which obviously corresponds to a long-range ordering transition (Fig. 4). The Néel temperature found from the specific-heat data is $T_N = 8.5$ K.

This value is slightly smaller than T_{max} determined from the M(T), which is typical of antiferromagnets with short-range interactions [24,25]. Under magnetic fields, the position of the λ -type anomaly in $C_p(T)$ shifts very slowly towards lower temperatures with increasing the field strength (the lower right inset of Fig. 4).

In order to clarify the nature of the magnetic phase transition and evaluate its effect on the specific heat and entropy, the temperature dependence of specific heat $C_p(T)$ was also measured for the isostructural nonmagnetic compound Na₂GeTeO₆. The Debye temperatures are estimated as $\Theta_D^{\text{nonmag}} = 421 \pm 5 \text{ K}$ for Na₂GeTeO₆ and $\Theta_D^{\text{mag}} = 470 \pm 5 \text{ K}$ for Li₂MnTeO₆, after taking into account the molar mass differences between Li and Na and between Mn and Ge [26]. The standard scaling procedure [27] was applied to the $C_p(T)$ data for Li₂MnTeO₆ and Na₂GeTeO₆ to estimate the lattice phonon contribution $C_{ph}(T)$. We observe the specificheat jump $\Delta C_m = 8.3 \text{ J/(mol K)}$, which is lower than the value expected from the mean field (MF) theory because for the high-spin state of manganese Mn⁴⁺ (S = 3/2), $\Delta C_{\text{theor}} = 5RS(S + 1)/[S^2 + (S + 1)^2] = 18.3 \text{ J/(mol K)}$. The magnetic



FIG. 5. The magnetic phase diagram for Li_2MnTeO_6 . The inset shows the arrangement of magnetic sublattice.

entropy $\Delta S_{\rm m}$, released below $T_{\rm N}$ is less than 50% of the total one expected from the mean-field theory for a S = 3/2 spin system, i.e., $\Delta S_{\rm m} = R \ln(2S + 1) = 11.52 \text{ J/(mol K)}$ [26].

An analysis of $C_{\rm m}(T)$ below $T_{\rm N}$ in terms of the spin-wave (SW) approach shows that, at low temperature, it should follow the $C_{\rm m} \approx T^{\rm d/n}$ power law for magnons [28,29], where the constant *d* stands for the dimensionality of the magnetic lattice, and *n* is the exponent of the dispersion relation $\omega \approx \kappa^n$. For Li₂MnTeO₆, the least-squares fitting of the data below $T_{\rm N}$ (the red solid line in the upper inset of Fig. 4) leads to the values of $d = 2 \pm 0.1$ and $n = 0.99 \pm 0.1$, which indicates the presence of 2D AFM magnons at low temperatures.

The magnetic phase diagram can be constructed from our magnetic and thermodynamic data as depicted in Fig. 5. The long-range ordering into an AFM phase occurs at 8.5 K. This phase boundary is shifted slightly towards lower temperatures by magnetic field. As shown by the neutron-diffraction studies and density functional theory (DFT) calculations (see below), the magnetic structure is a 120° noncollinear spin arrangement expected for a triangular spin lattice with nearest-neighbor AFM spin exchanges (see below).

The results of our dielectric measurements for Li_2MnTeO_6 reveals the presence of an additional anomaly in the vicinity of the ordering temperature as can be seen from Fig. 6, where the real part of dielectric permittivity is compared with specific-heat and NMR data. Although this effect is weak, its presence is reproduced for all frequencies studied from 1 to 10 kHz. This fact may reflect the coupling of dielectric and magnetic subsystems in Li_2MnTeO_6 similar to that observed in triangular lattice antiferromagnets with noncollinear magnetic structure [30–33].

C. Dynamic magnetic properties

Evolution of the ESR spectra with a temperature variation for powder sample of Li_2MnTeO_6 is shown in Fig. 7(a). In the entire range of temperature investigated, a relatively wide Lorentz-type line is observed, apparently corresponding to the



FIG. 6. Temperature dependence of the specific heat at zero magnetic field (upper panel), the real part ε' of the permittivity recorded at frequency f = 20 kHz (middle panel), and the relaxation rate obtained at 116.56 MHz (lower panel), where the yellow area highlights the ordering transition region.

signal from Mn⁴⁺ ions. The integrated ESR intensity χ_{ESR} , obtained by the double integration of the first derivative absorption line, was shown in the upper panel of Fig. 2 along with static magnetic susceptibility. The shape of the line can be accounted for by fitting with a Lorentzian profile. Since the absorption line is relatively wide, we used the fitting expression that includes two circulating components of a linearly polarized high-frequency field [34]:

$$\frac{dP}{dB} \propto \frac{d}{dB} \left[\frac{\Delta B}{\Delta B^2 + (B - B_r)^2} + \frac{\Delta B}{\Delta B^2 + (B + B_r)^2} \right], \quad (1)$$

where P is the power absorbed in the ESR experiment, B is the magnetic field, B_r is the resonant field, and ΔB is the linewidth. The representative result of the fitting is shown by the red solid curve in the inset on Fig. 7(a). The effective g factor and the ESR linewidth ΔB obtained from this approximation are collected in Fig. 7(b). It is clearly seen that the line is noticeably broadened with decreasing temperature, and the effective g factor deviates from a constant value below \sim 150 K, indicating an extended range of the short-rangeorder correlations, which is typical for low-dimensional and frustrated systems [29]. In order to characterize the divergence of the temperature dependence of the linewidth, we have analyzed it in terms of the Dormann and Jaccarino [35] model and the classical critical behavior that, as the critical temperature is approached from above, the ΔB increases due to the slowing down of spin fluctuations [36-38]. In the paramagnetic regime far above the critical regions associated with the magnetic transition, where any critical contribution to $\Delta B(T)$ as well as spin-lattice relaxation can be neglected, the



FIG. 7. (a) The temperature-dependent ESR spectra of Li_2MnTeO_6 . The inset shows a representative ESR spectrum, where the Lorentzian fitting profile is given by the red solid line. (b)The temperature dependence of the effective *g* factor (green symbols) and the width of the ESR line (navy symbols). The solid orange curve corresponds to the temperature dependence of the linewidth within the framework of classical critical behavior and the magenta dashed line represents the prediction of Eq. (2).

temperature variation of the ESR linewidth can be described by the expression of Dormann and Jaccarino [35]:

$$\Delta B(T) = \Delta B_0 \left[\frac{\chi_0(T)}{\chi(T)} \right], \tag{2}$$

where $\chi_0 = C/T$ is the free single-ion susceptibility with *C* the Curie constant of the uncoupled paramagnetic system, while $\chi(T)$ is the static susceptibility of the coupled

system and ΔB_0 describes the temperature-independent high-temperature limit of the linewidth associated with the contribution of anisotropic spin-spin interactions. We have calculated the temperature variation of ΔB using the measured dc susceptibility $\chi(T)$, the Curie constant C = $N_A g^2 \mu_B 2S(S + 1)/3k_B = 1.84 \text{ emu/K}$ of Li₂MnTeO₆ (with S = 3/2 and experimental g = 1.97 for Mn⁴⁺ ions), as well as the constant value $\Delta B_0 \approx 90 \text{ mT}$ estimated in the hightemperature limit. As can be seen, the static susceptibility may roughly account for the temperature evolution of the ΔB [magenta dashed curves in Fig. 7(b)]. As temperature decreases, however, appreciable deviation occurs from the experimental points.

In the Kawasaki-Mori-Huber theory [36–38], the temperature variation of ΔB can be described as $\Delta B(T) = \Delta B^* + A[T_N^{\text{ESR}}/(T - T_N^{\text{ESR}})]^{\beta}$. Here A is an empirical parameter, ΔB^* is the high-temperature limiting value of the linewidth, T_N^{ESR} is the temperature of the order-disorder transition, and β is a critical exponent. A least-squares fitting of the experimental data [the orange line in Fig. 7(b)] reveals that the value of $T_N^{\text{ESR}} = 11 \pm 2 \text{ K}$ is close to the Néel temperature T_N obtained from the measurement of the specific heat. The critical exponent $\beta = 0.90 \pm 0.05 \text{ K}$ indicates the 2D nature [36] of the exchange correlations in Li₂MnTeO₆.

At high temperatures, the ⁷Li NMR spectrum has a powder profile with unresolved quadrupole satellites. With decreasing temperature, the line shifts toward a lower field, and its width slightly increases. The local magnetic fields $H_{\rm loc}$ cause a shift of the NMR line from the Larmor frequency $\omega_{\rm L} = (\gamma_{\rm n}/2\pi)H_0$, so the local electron-spin susceptibility can be directly extracted from this shift. The shift is defined as $K = (\omega - \omega_L)/\omega_L \times 100\%$, and consists of two terms, namely, $K(T) = K_{sp}(T) + K_0$, where K_0 is the temperatureindependent part of the shift related to the Van Vleck susceptibility and the second-order quadrupolar effects, which are very weakly dependent on temperature [Fig. 8(a)]. K_{sp} is the spin part of the shift, caused by interactions $\mathcal{H}_s = \vec{l}_i A_{hf}^{ij} \vec{S}_J$ between a nuclear spin \vec{I}_i and an electron spin \vec{S}_J . It consists of three contributions, $K_s = K_{dip} + K_{contact} + K_{core}$, where the Fermi contact term K_{contact} and the core polarization term K_{core} contribute to the isotropic part of the NMR shift while the dipolar term K_{dip} depends on the relative orientation of the



FIG. 8. (a) Line shift and (b) linewidth of the 7 Li NMR signal at 13.05 MHz as a function of the static magnetic susceptibility. The dashed lines show a linear dependence of the local counterpart from the bulk static susceptibility.



FIG. 9. (a) Temperature dependence of the relaxation rate obtained at 13.05 MHz (black solid circles) and 116.56 MHz (red open circles). The solid lines are guide for the eye. The inset shows high-temperature region at 13.05 MHz. (b) A log-log plot of the normalized $(1/^{7}T_{1})/(1/^{7}T_{1\infty})$ against the reduced temperature $|T-T_{N}^{NMR}|/T_{N}^{NMR}$ for both frequencies $(T_{N}^{NMR} = 6.7 \text{ K})$. The dashed line represents Eq. (5) with the critical exponent of p = 1.12. (c) Example of an inversion recovery measurement on 13.05 MHz at T = 15 K. Red line shows a fit by single exponent law (see text in Sec. II).

crystal axes to the external magnetic field and is therefore anisotropic. In the paramagnetic regime \vec{S}_J can be replaced by its expectation value $\langle S \rangle = \chi_s H_0$, and K is related to $\chi_{sp}(T)$ as

$$K_{\rm sp}(T) = A_{\rm hf} \chi_{\rm sp}(T) / N_{\rm A} \mu_{\rm B}, \qquad (3)$$

where $A_{\rm hf}$ is the hyperfine coupling constant, $N_{\rm A}$ is the Avogadro number, $\chi_{\rm sp}$ is the static spin susceptibility, and $\mu_{\rm B}$ is the Bohr magneton. Here we neglect the effect of the shape of the magnetic particles in the external field [39], which is much smaller than the transferred hyperfine field since the powder particles are almost spherical. The inhomogeneous linewidth is determined by the distribution of the local magnetic fields $H_{\rm loc}$, so in the paramagnetic regime its temperature change is also proportional to the static spin susceptibility $\chi_{\rm sp}$.

The shift and width of the line obtained at $H_0 \approx 0.789 \,\mathrm{T}$ depend linearly on the bulk static susceptibility $\chi(T)$ obtained at 1 T in the temperature range 15–100 K [Fig. 8(b)]. The hyperfine interaction constant $A_{\rm hf}$ is determined to be 0.123 \pm $0.009 \,\mathrm{kOe}/\mu_{\rm B}$. It is quite small compared to the compounds with three-dimensional (3D) magnetic lattice (see for example $A_{\rm hf} = 1.01 \, \rm kOe/\mu_B$ in spinel LiMn₂O₄ [40]). It is interesting that the obtained $A_{\rm hf}$ value is similar to, or even smaller than, the parameter $A_{ax} = 0.24 \pm 0.007 \,\text{kOe}/\mu_{\text{B}}$, which is estimated using the point moment model of dipole-dipole interaction within the coordination radius of 6.5 Å. This suggests that, in layered compound Li₂MnTeO₆, the interplanar exchange interaction associated with the hybridization of orbitals and the transfer of spin density is very weak and partially compensates for the local dipole field on the lithium nuclei due to the contact part of the hyperfine interaction. Below 15 K the line shift as well as the linewidth deviate strongly from the bulk static susceptibility. It means that the relation $\tau_e^{-1} \gg \omega_L$ is not satisfied (τ_e is a correlation time of electron spins), and \vec{S}_J cannot be replaced any more by $\langle S \rangle$. This indicates the development of anisotropic electron correlations in the vicinity of the Néel phase-transition temperature $T_N^{\text{NMR}} \approx 7 \text{ K}$. The NMR measurements are carried out in magnetic fields of several T, therefore the Néel temperature according to NMR is a bit lower than the one deduced from the zero-field specific heat data.

The dynamics of the electron-spin system was probed by the nuclear relaxation measurements. In the temperature range of 17-100 K the relaxation rate changes very slightly. Below 15 K, it grows sharply and has a peak at 6.7 K indicating



FIG. 10. The plot of $(T_1TK)^{-1}$ vs *T*, where $(T_1T)^{-1}$ represents the local dynamic susceptibility, and *K* is the local static susceptibility. The shaded area marks the region where this ratio is a constant, which corresponds to the pure paramagnetic regime.

	d	ν	Z	η	$p = v(z - \eta)$
MF	3	0.5 [42]	1 [42]	0 [42]	0.5
3D Heisenberg	3	0.71 [43]	3/2 [44]	0.037 [43]	1.039
3D Ising	3	0.63 [45]	2.025 [45]	0.036 [45]	1.253
			1.964 [<mark>46</mark>]		1.237
2D Ising	2	1 [47]	2.18 [45]	0.25 [47]	1.93
			1.75 [45]		1.5

TABLE I. Values of the critical exponents v, z, and η as well as the parameter p expected for various spin models.

the transition to an ordered state (Fig. 9). The temperature dependence of the spin-lattice relaxation observed in 7.045 T also shows a pronounced peak at 7 K. The relaxation process is dominated by the fluctuations of the local field arising from the local electron-spin dynamics. The nuclear relaxation rate is related to the imaginary part of the dynamic spin susceptibility $\chi''_{\perp}(\vec{q}, \omega_L)$ [40],

$$\frac{1}{T_1 T} \propto \gamma_n^2 \sum_{\vec{q}} |A_\perp(\vec{q})|^2 \frac{\chi''_\perp(\vec{q}, \omega_L)}{\omega_L}, \qquad (4)$$

where A_{\perp} is the *q*-dependent transverse component of the hyperfine coupling, \vec{q} is the wave vector, and $\omega_{\rm L}$ is the Larmor frequency. Thus, the $(T_1T)^{-1}$ can be considered as a measure for the local dynamic part of the local susceptibility. In a purely paramagnetic regime, there is no dependency of the susceptibility on the *q* vector, and the electron-spin fluctuation rate is much higher than the Larmor frequency. Therefore, the temperature dependence of the local dynamic and static susceptibility is the same, and $(T_1TK)^{-1} = \text{constant}$, where *K* is the line shift. The deviation of $(T_1TK)^{-1}$ from a constant value below 15 K manifests the development of electron-spin fluctuations (Fig. 10).

The temperature dependence of the relaxation rate in the critical regime slightly above $T_{\rm N}^{\rm NMR}$ can be described by the



FIG. 11. The ⁷Li spectrum of Li₂MnTeO₆ at 4.2 K at two different frequencies (i.e., external fields). The blue lines correspond to the AF powder profiles as described by Eq. (6), the red dashed lines to the impurity contribution (see the text), and the black dashed lines to the Larmor field $H_{\rm L}$.

formula

$$T_1^{-1} \propto \left(T - T_N^{NMR}\right)^{-p},\tag{5}$$

where the fitting parameters p and $T_{\rm N}^{\rm NMR}$ are found to be 1.12 ± 0.09 and $T_{\rm N}^{\rm NMR} = 6.7 \pm 1$ K, respectively. Using $p = v(z - \eta)$ [41] as well as the critical exponents v, z, and η listed in Table I, we can conclude that the critical behavior of the relaxation fits well by a 3D Heisenberg or a 3D Ising model.

In contrast to the Mn⁴⁺ ESR that probes the intralayer correlations, the NMR of the Li⁺ ions located in between the layers should be sensitive mostly to the interlayer interaction and consequently to a 3D order. Thus, using a combination of two local techniques, we can clearly distinguish the temperature regions for the 2D correlations (<150 K) and 3D correlations (15–6.7 K). Below T_N^{NMR} , the relaxation rate as well as the shape and the width of the spectrum change dramatically (see Fig. 11). The width consists of two contributions, namely, a rectangular shape with quadrupolar broadened wings and a relatively narrow Gaussian shape. The main part of the spectrum with rectangular shape is typical of powder samples of antiferromagnets [48]. Such a line shape can be described by the equation

$$f(H, H_A, H_0) = \frac{1}{4H_A} \left| 1 + \frac{H_0^2 - H_A^2}{H^2} \right|$$
(6)



FIG. 12. Temperature dependence of the intensity of the NPD maxima measured on the DMC diffractometer at low temperatures. The indices of the most intense magnetic reflections are marked.



FIG. 13. Refinement of the neutron-diffraction pattern of $\text{Li}_2\text{MnTeO}_6$ measured on the HRPT diffractometer at T = 1.6 K. The red dots represent the experimental data, the black line shows the calculated intensity, the green ticks indicate the positions of the nuclear and magnetic Bragg reflections, and the blue line shows the difference between experimental and calculated data, plotted at the bottom for convenience. The inset shows a small-angle portion of the neutron-diffraction pattern with an additional blue line showing calculated scattering from a magnetic phase.

for $|H_0 - H_A| \leq H \leq H_0 + H_A$. Here, H_A is an absolute value of the internal magnetic field created by ion moments in the ordered phase, $H_0 = \omega_L/(\gamma_n/2\pi)$ is the external field, ω_L is a Larmor frequency, and γ_n is the nuclear gyromagnetic ratio. We calculated the internal field on different lithium positions using the dipole point moment model and the magnetic structure proposed by neutron-diffraction study (see the next section). This model is approximate, but allows us to estimate the symmetry and a possible amount of magnetically

nonequivalent lithium positions in an ordered state. Our modeling results in three magnetically nonequivalent positions of lithium, so one can expect three components in the spectrum. The direction of the internal field at these positions varies by an angle of 120°, but its absolute values remain the same for all three cases. For this reason, only one rectangle is observed in the powder spectrum and the internal field value obtained from the experiment corresponds to the value of $H_{\rm A} = 1100$ Oe. Comparing this value with the one resulting from the approximate model of the dipole field from pointwise spins, we can estimate the magnitude of the effective magnetic moment on the Mn4+ ions in the ordered state to be $1.78 \,\mu_{\rm B} \pm 0.06 \,\mu_{\rm B}$, which is reasonable for S = 3/2 and $(T - T_{\rm N}^{\rm NMR})/T_{\rm N}^{\rm NMR} = 0.6$. It is interesting that the value of the internal field on Li⁺ changes insignificantly when the external field varies from 0.78 to 7.05 T. This suggests that the external field affects mostly the in-plane components of Mn⁴⁺ spins because, in this case, the additional magnetic fields at Li⁺ ions from two adjacent layers of Mn⁴⁺ ions almost cancel each other out. The second relatively narrow spectral component has a low intensity and almost vanishing line shift, which grows linearly with the external field as well as the linewidth. This contribution, probably from a small amount of nonmagnetic impurity, has long transverse and longitudinal relaxation times. Therefore, in the paramagnetic temperature region, where the time delays in the measuring sequence are short and the spectrum of the main sample is rather narrow, the relative intensity of the parasitic contribution to both the spectrum and the relaxation curves is small. At low temperatures, when the width of the main spectrum in the ordered state increases, the parasitic contribution becomes noticeable.

D. Neutron powder diffraction

Figure 12 shows NPD patterns measured on the DMC diffractometer at several low temperatures. The appearance of magnetic neutron scattering and its temperature evolution are visually demonstrated. Down to 10 K, the NPD pattern contains only nuclear reflections from the crystal lattice of the



FIG. 14. Magnetic structure of Li₂MnTeO₆: (a) An extended projection view on the *ab* plane of the 120° noncollinear spin arrangements of two adjacent trigonal layers (at z = 0.25 and 0.75). (b) A perspective view of the 120° noncollinear spin arrangements of two adjacent trigonal layers. The two triangles at z = 0.25 and 0.75 have a staggered arrangement. The thin black lines denote the crystallographic unit cells formed by the unit vectors **a** and **b**. The thick green lines highlight the Shubnikov magnetic unit cell formed by the unit vectors **A** and **B**. The relation between the parent crystal unit cell and the magnetic unit cell is determined by $\mathbf{A} = 2\mathbf{a} + \mathbf{b}$, $\mathbf{B} = -\mathbf{a} + \mathbf{b}$. [a = b = 5.0114(2) Å, c = 9.4915(9) Å at T = 1.6 K].



FIG. 15. Spin-exchange paths J_1 and J_2 in Li₂MnTeO₆. The blue circles represent the Mn⁴⁺ ions.

paramagnetic phase. At T = 6 K, we can observe the appearance of additional reflections, including the diffraction angles smaller than the position of the first nuclear (002) reflection. The first, most intense magnetic reflections (100)-k and (101)-k are marked in Fig. 12. Their appearance unambiguously indicates the AFM nature of the emerging long-range spin ordering.

The value of T_N estimated from the temperature dependence of the magnitude of the magnetic moment is inconsistent with that determined from the thermodynamic measurements. The data indicate a phase transition from the paramagnetic to the AFM state with decreasing temperature without any significant structural transformations. The low-temperature neutron-diffraction pattern from the HRPT allowed us to construct a magnetic structure in a magnetically ordered state. Figure 13 represents the results of the Rietveld refinement of the experimental neutron-diffraction pattern measured at T = 1.6 K. The appearance of the magnetic peaks is clearly seen from the inset of Fig. 13 in the 2Θ angle range between 10° and 45° . It is also worthwhile to mention that these data unambiguously demonstrate the absence of any magnetic impurity phases. The latter can manifest themselves in magnetic scattering even if these impurities are not detected by nuclear scattering due to their very low concentration.

The symmetry analysis of the seven most intensive magnetic reflections using the BasIreps program (in the FULL-PROF suite) shows that the observed magnetic reflections of Li₂MnTeO₆ are described by the propagation vector $\mathbf{k} = (1/3, 1/3, 0)$. This vector corresponds to a commensurate

magnetic structure, and the magnetic cell is tripled along two basic crystallographic directions a and b in the layer. The magnetic structure of Li₂MnTeO₆ obtained from the Rietveld analysis is shown in Fig. 14. There are two antiferromagnetically ordered manganese ions per unit cell in the positions (2/3, 1/3, 1/4) and (1/3, 2/3, 3/4). In a projection view of the crystallographic unit cell on the *ab* plane, shown in Fig. 15, two manganese ions are located with their spin moments lying in the *ab* plane and making the angle of 120° between them to forma 120° noncollinear spin arrangement in each magnetoactive MnTeO₆ layer with spin moment equal to $1.16 \,\mu_{\rm B}/{\rm Mn}$ $[m_x = 0.68(2) \mu_B/Mn, m_y = 1.38(3) \mu_B/Mn]$ [Fig. 14(a)]. This value of the magnetic moment was obtained as a result of the full-profile processing of the neutron-diffraction pattern measured at T = 1.6 K. This moment is three times smaller than the effective magnetic moment calculated from the magnetic susceptibility data (Sec. III B) and expected for Mn⁴⁺ ions. This reduction of the magnetic moment is very unusual. The spins in one spin triangle of one layer are pointed along the directions toward, or away from, the center of the triangle. Each triangle with spins pointed toward the center in one trigonal layer lie above and below the triangles with spins pointed away from the center [Fig. 14(b)].

The symmetry analysis performed with the ISODISTORT software tool [49] has shown that this magnetic structure corresponds to the maximal symmetry magnetic Shubnikov space group $P\bar{3}1c$ (165.1.1322 [50]). The group is generated by irreducible representation mK1, with special order parameter P1 (*a*,0), according to the international nomenclature given in Ref. [49], with the basis transformation (2,1,0), (-1,1,0), and (0,0,1). The Mn atom is at the position 6f (x,0,1/4) with x = 1/3 and the magnetic moment direction [u,0,0].

E. Theoretical calculations of exchange interactions

We evaluate the spin-exchange interactions of Li₂MnTeO₆ by performing energy-mapping analysis based on DFT calculations [51–53]. A perspective view of the arrangement of the magnetic ions Mn⁴⁺ in Li₂MnTeO₆ is presented in Fig. 15, which has two triangular layers of Mn⁴⁺ (d^3 , S = 3/2) ions in a unit cell. For our analysis, we consider the nearest-neighbor spin-exchange path J_1 within each triangular layer and the spin exchange path J_2 between adjacent triangular layers. For



FIG. 16. Spin ordered arrangements of (a) FM, (b) AF1, and (c) AF2 states, where the gray and white circles represent the up and down spin sites, respectively.

TABLE II. Relative energies (in meV/FU) of the three spin ordered states, the spin-exchange parameters (in K), and the Curie-Weiss temperature (in K) of Li_2MnTeO_6 determined from the generalized gradient approximation + U calculations with $U^{eff} = 2$, 3, and 4 eV

<i>U</i> (eV)	2	3	4	
E _{FM}	6.15	4.04	2.51	
$E_{\rm AF1}$	5.98	4.17	2.91	
E_{AF2}	0	0	0	
$J_1/k_{\rm B}$	-7.85	-5.26	-3.41	
$J_2/k_{\rm B}$	-0.15	0.12	0.34	
θ (K)	-60	-39	-23	

the evaluation of J_1 and J_2 , spin-polarized DFT calculations were carried out for Li₂MnTeO₆ using the (2*a*, *b*, *c*) supercell containing four formula units (FUs) and three ordered spin states (FM, AF1, AF2) defined in Fig. 16. Spin-polarized DFT calculations were carried out by using the Vienna ab Initio Simulation Package (VASP) [54,55], the projector augmented wave (PAW) method [56], and the Perdew-Burke-Ernzerhof exchange-correlation functionals [57]. The electron correlation associated with the 3*d* state of Mn was taken into consideration by performing the DFT + *U* calculations [58] with the effective on-site repulsion $U^{\text{eff}} = U-J$. All our DFT + *U* calculations used the plane-wave cutoff energy of 450 eV, the threshold of 10^{-6} eV for self-consistent-field energy convergence and the *k* points of the (6 × 6 × 3) set.

Using the spin Hamiltonian,

$$H_{\rm spin} = -\sum_{i < j} J_{ij} \vec{S}_i \cdot \vec{S}_j, \tag{7}$$

where \vec{S}_i and \vec{S}_j are the spins at magnetic ion sites *i* and *j*, respectively, with the spin exchange constant $J_{ij} = J_1, J_2$, the total spin exchange energies per four FUs of the three ordered spin states are written as

$$E_{\rm FM} = (-12J_1 - 12J_2)S^2,$$

$$E_{\rm AF1} = (-12J_1 + 12J_2)S^2,$$

$$E_{\rm AF2} = (4J_1 - 4J_2)S^2,$$
(8)

where S = 3/2, i.e., the spin of Mn⁴⁺. The relative energies of the three ordered spin states determined by DFT + U(with $U^{\text{eff}} = 2, 3, \text{ and } 4 \text{ eV}$) calculations are summarized in Table II. Thus, by mapping the relative energies onto the corresponding ones in terms of the total spin-exchange energies, we obtain the values of J_1 and J_2 listed in Table II. The latter reveals that the intralayer exchange J_1 is AFM and dominates over the interlayer exchange J_2 in magnitude. The latter is very weakly AFM with $U^{\text{eff}} = 2 \text{ eV}$ and becomes very weakly ferromagnetic (FM) with $U^{\text{eff}} = 3$ and 4 eV. The Curie-Weiss temperatures θ_{cal} calculated on the basis of the calculated spin exchanges J_1 and J_2 using the mean-field approximation [59] are also listed in Table II. The θ_{cal} values calculated with $U^{\text{eff}} = 2$ and 3 eV (-60 and -39 K, respectively) agree reasonably well with the experimental value of -51 ± 1 K. To a first approximation, therefore, our calculations show that the magnetic structure can be described by a triangular

spin lattice with the nearest-neighbor AFM spin exchange J_1 . The long-range magnetic order expected for a triangular spin lattice with nearest-neighbor AFM spin exchange is a 120° noncollinear spin arrangement. Therefore, our calculations are in support of our discussions presented in the previous sections.

IV. CONCLUSION

In summary, the magnetic susceptibility $\chi(T)$ of the layered triangular-lattice tellurate Li₂MnTeO₆ reveals an unusual behavior under external magnetic field. Although $\chi(T)$ shows no obvious anomaly indicative of a long-range magnetic ordering at low magnetic fields, its character changes radically showing a maximum at about 9 K at high magnetic fields. The specific-heat data exhibit a clear λ -type anomaly at $T_{\rm N} \approx$ 8.5 K even at zero magnetic field, unambiguously confirming that the maximum of $\chi(T)$ at high magnetic fields reflects the onset of an AFM order. This conclusion is also consistent with both ⁷Li NMR data and dielectric permittivity measurements, which indicate the presence of an AFM state below 7 K. Our DFT calculations suggest that the spins of each trigonal layer will have a 120° noncollinear spin arrangement, and that the 3D AFM ordering takes place when the interlayer spin arrangements become ordered. These suggestions are consistent with the magnetic structure determined by neutron-diffraction measurements. The 3D magnetic ordering temperature $T_{\rm N} \approx 8.5$ K is noticeably lower than the absolute value of the Curie-Weiss temperature $\Theta = -74 \pm 1 \text{ K}$ (frustration index $f = |\Theta|/T_N \approx 8$) showing the presence of strong spin frustration in each triangular spin lattice of Li₂MnTeO₆. Our ESR and NMR data show a 2D magnetic character in a broad temperature range above T_N . Support for the 2D magnetism picture in Li₂MnTeO₆ was also obtained from the magnetic specific heat and the critical divergence of the ESR linewidth.

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