High-order minibands and interband Landau level reconstruction in graphene moiré superlattices

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The propagation of Dirac fermions in graphene through a long-period periodic potential would result in a [band folding together with the emergence of a series of cloned Dirac points \(DPs\) \[C.-H. Park](https://doi.org/10.1038/nphys890) *et al.*, Nat. Phys. **4**, 213 (2008); Phys. Rev. Lett. **101**[, 126804 \(2008\)\]](https://doi.org/10.1103/PhysRevLett.101.126804). In highly aligned graphene/hexagonal boron nitride (G/hBN) heterostructures, the lattice mismatch between the two atomic crystals generates a unique kind of periodic structure known as a moiré superlattice. Of particular interest is the emergent phenomena related to [the reconstructed band-structure of graphene, such as the Hofstadter butterfly \[L. A. Ponomarenko](https://doi.org/10.1038/nature12187) *et al.*, Nature (London) **497**, 594 (2013); B. Hunt *et al.*, Science **340**[, 1427 \(2013\);](https://doi.org/10.1126/science.1237240) C. R. Dean *et al.*, Nature(London) **497**, [598 \(2013\)\], topological currents \[R. V Gorbachev](https://doi.org/10.1038/nature12186) *et al.*, Science **346**[, 448 \(2014\)\]](https://doi.org/10.1126/science.1254966), gate-dependent pseudospin mixing [Z. Shi *et al.*, Nat. Phys. **10**[, 743 \(2014\)\]](https://doi.org/10.1038/nphys3075), and ballistic miniband conduction [M. Lee *et al.*, Science **353**, [1526 \(2016\)\]. However, most studies so far have been limited to the lower-order minibands, e.g., the first and](https://doi.org/10.1126/science.aaf1095) second minibands counted from charge neutrality, and consequently the fundamental nature of the reconstructed higher-order miniband spectra still remains largely unknown. Here we report on probing the higher-order minibands of precisely aligned graphene moiré superlattices by transport spectroscopy. Using dual electrostatic gating, the edges of these high-order minibands, i.e., the third and fourth minibands, can be reached. Interestingly, we have observed interband Landau level (LL) crossing inducing gap closures in a multiband magnetotransport regime, which originates from band overlap between the second and third minibands. As observed, high-order minibands and LL reconstruction qualitatively match our simulated results.

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The quantum nature of electrons in a spatially periodic lattice generates a band structure. Similarly, electrons in crystalline solids moving through longer-period superlattice develop a finer energy spectrum consisting of discrete minibands. Manipulating electronic states by superlattices to overcome the constraints of the original materials has been a remarkable route for band engineering [\[1,2\]](#page-4-0). The moiré superlattice of graphene/hexagonal boron nitride (G/hBN) has emerged recently as a model two- dimensional (2D) system, which can effectively fold the band spectrum without destroying the original honeycomb lattice of graphene [\[3–7\]](#page-4-0). In contrast to conventional mesoscale scalar potentials, the moiré potential arises from atomic scale potentials in hBN and should be described by a two-by-two tensor [\[8,9\]](#page-4-0), leading to a much more complicated band spectrum. According to previous simulations [\[9\]](#page-4-0), different minibands can overlap with each other and obscure the presence of extra Dirac points. So far, most attention has been focused on the second-generation Dirac cones (between the first and second minibands). However, the exploration of higher-order minibands has been much more limited. Hence, the study of high-order minibands in G/hBN moiré superlattice is crucial to fully understand the emergent quantum behavior of Dirac fermions in a periodic spinor potential.

Probing high-order minibands of G/hBN moiré superlattice has been experimentally challenging. The modulation of the chemical potential by electrostatic gating is usually not sufficient to reach the edges of high-order minibands due to the breakdown of conventional solid gate dielectrics $(hBN/SiO₂)$. Also, the band spectrum of the moiré superlattice depends very sensitively on the twist angle between graphene and hBN [\[9,10\]](#page-4-0). The density of electron states of each completely filled miniband can be described as $n_0 = 1/A$ (if not counting spin-valley degeneracy), where $A = \sqrt{3}\lambda^2/2$ is the area of a single moiré unit cell and λ is the moiré wavelength. When

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FIG. 1. Dual-gated G/hBN moiré superlattice device. (a) Schematic cross-sectional view of device. Inset is a high-resolution AFM image of precisely aligned G/hBN moiré superlattices, showing a well-defined moiré pattern with a period of ∼15 nm. The scale bar is 20 nm. (b), (c) Conductance of two independent devices as a function of top gate voltage V_{TG} at different bottom gate voltage V_{BG} with different minibands edges indicated by dashed lines. Curves at different V_{BG} have been off-set for clarity. Inset in (b) shows an optical microscopy image of an as fabricated device with scale bar 10 um. (d) Color plot of dG/dV_{TG} as a function of V_{TG} and V_{BG} measured from devices D1. All measurements are done at a base temperature of 1.5 K.

two crystals are precisely aligned, it gives the maximum moiré wavelength $\lambda = \sim 15$ nm [\[11–13\]](#page-4-0). When the twist angle increases, λ decreases drastically, resulting in a rapid increase of the carrier capacity for each miniband. As a result, the perfectly aligned G/hBN moiré superlattice has lowest carrier density for each filled miniband and is an ideal system for probing high-order minibands.

In this study, we present magnetotransport studies of zero-twisted G/hBN moiré superlattices. Figure 1(a) shows a schematic of the device structure in which dual-gate geometry is adopted. Samples were prepared by a van der Waals epitaxy technique [\[12\]](#page-4-0), followed by stacking of another hBN flake on top of it (by dry-transfer technique) as top gate dielectric. A high resolution atomic force microscopy (AFM) image of the epitaxial graphene on hBN is displayed in Fig. $1(a)$ (inset), showing a well-defined moiré pattern with a period of $\lambda = \sim 15$ nm. Cr/Pd/Au (1 nm/10 nm/100 nm) was then deposited for contacts and gate electrodes. Figures $1(b)$ and $1(c)$ show the typical top gate dependent conductance measured from two independent devices at different bottom gate values. Original Dirac point (DP) and second-generation DP (SDP) are reflect on the minimums of conductance which are marked by onsets of the first miniband (first MB) and the second miniband (second MB), respectively. Interestingly, at higher carrier density we find two more conductivity minimums,

most likely originated from high-order minibands. Figure $2(d)$ shows the numerical derivative of the conductance dG/dV_{TG} as a function of V_{TG} and V_{BG} . The minimums of conductivity are further resolved in Fig. $2(d)$ (red lines). Some other features at $V_{BG} = 45 \text{ V}$, 5 V and -35 V are also observed and expected to come from non-top-gated area of graphene, since they are independent of *V*_{TG}. Considering the spin and valley degeneracy in graphene, the capacity of each miniband is $4n_0$. According to previous studies, SDPs are always located at a carrier density of $n = 4n_0$ where n_0 only depends on the twist angle. For precisely aligned G/hBN moiré superlattices [\[12,13\]](#page-4-0), that is, $4n_0 = 1.85 \times 10^{12}$ cm⁻². Thus, by employing the parallel plate capacitor model, we can deduce the carrier density at any gate voltages. To keep simplicity, we use to *n*₀ normalize the carrier density below $(0, -4n_0, -6.5n_0)$ and $-11.2 n_0$ are the normalized onset carrier density of the first MB, second MB, third MB, and fourth MB, respectively). Note that, both two devices with top layer hBN randomly stacked show same features at same carrier density which can be normalized by that of SDP, thus ruling out the possibility of super moiré induced by top layer hBN.

To gain a better understanding of these results, we thus calculated the band structure of a precisely aligned G/hBN moiré superlattice using the general symmetry-based approach described in a previous work $[9,14]$. The superlattice

FIG. 2. High order minibands (MBs) in G/hBN moiré superlattices. (a) Calculated band spectrum in the SBZ, with different minibands indicated by different color. (b) Calculated energy dispersions along the $K-M-K'\Gamma$ - $M-K$ directions of SBZ shown in the inset figure inset. (c) Calculated density of states (DOS). Positions corresponding to four different DPs are indicated by black arrows.

parameters were extracted from Ref. $[14]$. Figure $2(a)$ displays the band spectrum in the superlattice Brillouin zone (SBZ) with different minibands rendered with different colors. The points of contact between different minibands occur at SDPs [\[11\]](#page-4-0), tertiary Dirac points (TDPs) [\[15\]](#page-4-0), and quaternary Dirac points (QDPs), all found at the edges of the SBZ. Figure $2(b)$ shows the energy dispersion along the *K-M -K --M-K* direction in the SBZ from which the four generations of DPs can also be identified. The SDP is located at the K' point of the SBZ at energy −170 meV relative to the original DP, which is consistent with the angle-resolved photoemission spectroscopy results [\[16\]](#page-4-0). TDPs and QDPs are also marked in Figs. $2(a)$ and $2(b)$. According to the simulated dispersions, TDPs are located at the K point in the SBZ at energy −210 meV below the original DP while the QDPs are located at the M' points and -300 meV. Figure $2(c)$ shows the density of state (DOS) plotted against normalized carrier densities. When the carrier density is gradually tuned to $-6.5 n_0$, the Fermi surface starts to touch the TDP which is also the onset point of the third miniband. An observed increase of sample resistivity can thus be attributed to the abrupt decrease of the DOS as well as the opening of an additional interband scattering channel $[17–19]$. Similarly, when the carrier density is further tuned to $-11.2 n₀$, the Fermi surface starts to touch QDPs and results in another abrupt increase of resistivity.

Under a magnetic field, the energy spectrum of a graphene superlattice is reconstructed into sequences of magnetic Bloch bands and Landau level (LLs) [\[20,21\]](#page-4-0). The plot of the correspondingly reconstructed carrier density against the magnetic field, known as a Wannier diagram, has its incompressible states described by the following Diophantine relation [\[21\]](#page-4-0):

$$
(n/n_0) = t(\Phi/\Phi_0) + s,
$$

where n is the carrier density; n_0 is the density of electron states of each Bloch band; Φ is the magnetic flux per moiré unit cell; $\Phi_0 = h/e$ is the magnetic flux quantum; t is the LL filling index and s is Bloch band filling index. Here both t and s should be an integer.

Figures $3(a)$ and $3(b)$ show the differential conductivity dG/dn as a function of normalized carrier densities n/n_0 and the magnetic field B with bottom gate voltage V_{BG} set at -60 and 60 V, respectively. Landau fans tracing from the DPs and SDPs strictly follow the rule described in the Diophantine relation. For LLs fanning out from Dirac point, $s = 0$ and $t = 4(N + 1/2)$ where $N = 0, \pm 1, \pm 2$ etc, shows features of the typical half integer quantum Hall effect in monolayer graphene. For LLs fanning out from SDPs $(n = \pm 4n_0)$, fitting of the Diophantine relation gives $s = 4$ and $t = 4(N + 1/2)$ where $N = 0, \pm 1, \pm 2$, etc. Here, both Bloch bands and Landau levels are four fold degenerated due to spin and valley degrees of freedom. Interestingly, at higher carrier densities,

FIG. 3. Anomalous quantum Hall states in G/hBN moiré superlattice. (a), (b) dG/dn as a function of normalized carrier density n/n_0 and magnetic field *B* with V_{BG} set at (c) −60 V and (d) 60 V, respectively. Data is measured from device D1.

FIG. 4. Interband LL reconstruction induced gap closing. (a) Schematic showing interband LL crossing induced gap closing. (b) Numerically calculated LL spectrum on the hole side. A region of crossing LLs is indicated with red shading. (c) Calculated Wannier diagram of a precisely aligned graphene moiré superlattice with color rendering corresponding to the different gap sizes. The red dashed lines indicate the areas of LL crossing induced gap closing.

we observed extra sets of fan diagrams, which are marked by red dashed lines in Figs. $3(a)$ and $3(b)$. As we can see, the fan diagrams are no longer symmetric and only features tracing to one side are observable. We note that in nonperfectly aligned G/hBN moiré superlattice, the LL-like signatures fanning out from TDP hosts a degeneracy of 12, which was attributed to a $\sqrt{3} \times \sqrt{3}$ R 30° hidden superstructure [\[15\]](#page-4-0). Here we also find the spacing between adjacent features faning out from TDP is much larger than those found for the DP and SDP, however, still smaller than 12 (close to eight). On the electron side, the LL-like features are not even straight. The asobserved features cannot be well described by the Diophantine relation and are most likely induced by interband LLs crossing.

In a multiband transport regime, LLs from overlapping minibands with different effective electron masses cross with each other at some finite magnetic field, leading to a reconstructed energy spectrum $[22]$. As shown in Fig. $4(a)$, the gap between two neighboring LLs, e.g., *L*² and *L*3, from miniband $A(M_A)$ is filled by L_1 from miniband $B(M_B)$. As a result, the sample will be conductive even without edge state when the Fermi surface is tuned inside the gap between L_2 and L_3 in M_A . According to Fig. [2\(b\),](#page-2-0) there will be a transition from single-band transport to multiband transport in precisely aligned G/hBN moiré superlattice when the Fermi surface is tuned to TDP at ∼−210 meV and thus makes it possible to observe the induced gap closing due to interband LLs crossing in a multiband transport regime.

Figure 4(b) displays the calculated the energy spectrum in magnetic field, which is focused on the hole side. LLs traced to two overlapping minibands produce a criss-crossed pattern which is visible in the area marked by the red shading.

To investigate these LL crossing features, we further calculated the density-magnetic field diagram in which different colors are used to display the different gap sizes [Fig. $4(c)$]. In a single particle picture, LL gaps in the n-B plain always trace back to an integer miniband filling factor at $B = 0$ (e.g., $n = 0, \pm 4n_0, \pm 8n_0, \ldots$ [\[23\]](#page-4-0), which is also clearly shown in Fig. 4(c). Qualitatively consistent with experimental the results, interband LL crossing in a multiband transport regime, leads to sequences of gap closures [indicated by the red dashed lines in Fig. $4(c)$], which are traced to noninteger band filling at $B = 0$. The winding features on the electron side [indicated by red dashed lines in Fig. $2(b)$] are also clearly resolved.

According to our simulated results, the interband LL crossing induced gap closing in hole side is only visible at low magnetic fields $B < 2T$. The value is lower compared experimental value (∼4 T). Meanwhile, the calculation cannot well interpret the spacing between adjacent features (almost two times of the spacing for fourfold LLs) fanning out from TDP on the hole side. These discrepancies may come from the non-negligible role of interactions in the moiré system, especially at high carrier densities.

In conclusion, we carried out transport measurements to probe the minibands of precisely aligned graphene moiré superlattices at high carrier densities. We observed TDPs and QDPs at carrier densities of ~ 6.5 n₀ and ~ 11.2 n₀, respectively, which manifest as an abrupt increase of sample resistivity. Gap closing induced by the interband LL crossing is observed and can be explained by a multiband transport mechanism. Our results reveal a clear picture of the band structure of perfectly aligned G/hBN moiré superlattices and indicate the important role of the synergistic effect of minibands in transport.

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G.Z. and X.L. designed the research; X.L. and J.T. performed the growth, structural characterization, device fabrication, and electrical transport measurements; J.W. and V.F. performed the calculation. K.W. and T.T. synthesized h-BN crystals. X.L., J.W., G.Z. and V. F. analyzed data and wrote the manuscript, and all authors discussed and commented on the paper.

The authors declare no competing financial interest.

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