Conductance quantization and shot noise of a double-layer quantum point contact

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The conductance quantization and shot noise below the first conductance plateau $G_0 = 2e^2/h$ are measured in a quantum point contact fabricated in a GaAs/AlGaAs tunnel-coupled double quantum well. From the conductance measurement, we observe a clear quantized conductance plateau at $0.5G_0$ and a small minimum in the transconductance at $0.7G_0$. Spectroscopic transconductance measurement reveals three maxima inside the first diamond, thus suggesting three minima in the dispersion relation for electric subbands. Shot noise measurement shows that the Fano factor behavior is consistent with this observation. We propose a model that relates these features to a wave-number directional split subband due to a strong Rashba spin-orbit interaction that is induced by the center barrier potential gradient of the double-layer sample.

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I. INTRODUCTION

In quantum point contacts (QPCs) on two-dimensional electron gas (2DEG) systems, nanometer-scale confinement embodies a quantum ballistic transport analogous to the transverse modes of optical waveguides. The transverse modes or subbands are well separated in energy; thus, the conductance through a QPC becomes quantized in a unit of $G_0 =$ $2e^2/h$ [1-3], where h denotes Planck's constant, e is the elementary charge, and the coefficient 2 expresses the spin degeneracy that is understood using the Landauer-Büttiker formalism [4-6]. Although many theoretical studies suggested the lifted spin degeneracy state ($0.5G_0$ plateau) at zero magnetic field [7–11], this degeneracy is typically not resolved. Instead, a small plateau appears at $0.7G_0$ [3], and it has attracted considerable interest (for a review, see [12]). The Landauer-Büttiker model has been tested by measuring shot noise, i.e., the discrete noise of the charge that is carried by particles in the probabilistic scattering process [13–19], in this system. Previous shot noise measurements for OPCs on 2DEGs have contributed significantly to the elucidation of basic physics and complemented the conductance results [20–27]. Furthermore, in addition to their fundamental physical importance, semiconductor nanostructures with a QPC offer electronic devices that can manipulate electron charges and spins; thus, they are feasible for spintronic devices [28,29] and quantum computation [30]. In particular, a QPC on a tunnel-coupled double layer (coupled quantum wire) is a candidate for implementing a qubit [31–33]. Hitherto, several studies [34–40] have been conducted that resolved the coupled wave-function modes of double-layer systems, and the obtained information is useful for quantum engineering. The resolution of spin degeneracy and the generation of spin currents with only electrical controls, such as using spin-orbit interactions (SOIs) [27,41–47], remain to be addressed in future studies. In addition, the shot noise for tunnel-coupled QPCs should be measured, because additional degrees of freedom are expected to affect many-body interactions in the nonequilibrium regime [48].

In this study, we fabricated a QPC in a double-layer 2DEG of a GaAs/AlGaAs double quantum well (DQW) sample, and we investigated the conductance quantization in this doublelayer QPC system. Here, we report the shot noise results when the conductance is below the first conductance plateau, G_0 . Previously, researchers have reported the coexistence of $0.5G_0$ and $\sim 0.7G_0$ plateaus [27,37,49–51]. Using a high mobility and low electron density double-layer sample, we observed a clear conductance plateau at $0.5G_0$, and transconductance minima at 0.5 and $\approx 0.7G_0$ at zero magnetic field and the lowest temperature available for the dilution refrigerator used in this experiment. Energy spectroscopy reveals a rich structure of subband edge (SBE) lines with three maxima inside the first SBE diamond, between the $0.5G_0$ and G_0 plateau region. They are dependent on the magnitude and direction of the magnetic fields, and consistent with the horizontal (in the wave-number direction) subband splitting model discussed herein. From the shot noise measurement, the Fano factor F, i.e., the current noise normalized to the noise of Poissonian transmission statistics, exhibits reductions at $0.5G_0$ and G_0 , and a small reduction at $0.7G_0$. In addition, we observe a difference in F with regard to the positive and negative biases that further suggests an SOI dispersion with Zeeman splitting. We hypothesize that this splitting is caused by the Rashba SOI

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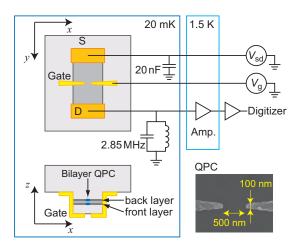


FIG. 1. Schematics of the sample and current noise measurement setup. The sample is placed upside down on the cold finger of the mixing chamber, as shown in the horizontal view in the bottom panel. Right inset: scanning electron microscopy image of the split gates.

[52] that is induced by a strong potential gradient of the center barrier and the high mobility of the sample. This study would invoke further investigations for spin-related physics and a quasiparticle's charge in the double-layer system.

The remainder of this paper is structured as follows: In Sec. II, we describe the sample of this experiment (Sec. II A), the experimental setups for conductance measurements (Sec. II B), and the shot noise measurements (Sec. II C). In Sec. III, we present the experimental results on the conductance measurement (Sec. III A) and shot noise measurement (Sec. III B). A discussion is presented in Sec. IV. After calculating the wave functions in the DQW at the QPC (Sec. IV A), we discuss the effect of the SOI for the conductance and shot noise (Sec. IV B). We present the conclusions in Sec. V, as well as a brief mention of future perspectives.

II. EXPERIMENT

A. Sample preparation

The sample used in this study was fabricated on a DQW heterostructure grown by molecular beam epitaxy on a GaAs (100) surface in the NTT Basic Research Laboratories. The wafer comprises two 20-nm-wide GaAs quantum wells separated by a 3-nm-wide AlAs barrier layer; thus, the centerto-center distance d is d = 23 nm. The DQW was located 600 nm below the surface, and it was doped from both sides using 1×10^{12} cm⁻² Si δ -dopings 200 nm away from both layers. The energy gap between the DQW symmetric and antisymmetric states Δ_{SAS} was measured to be 0.29 meV through the analysis of Shubnikov-de Haas (SdH) oscillation at low magnetic fields (see Appendix A). The total electron density is 1.20×10^{11} cm⁻², with 0.64×10^{11} cm⁻² in the symmetric state and 0.56×10^{11} cm⁻² in the antisymmetric state. The sample was processed in a shape of a standard Hall bar of width 50 μ m and four voltage probes separated by 180 μ m (see Fig. 1). Two of the probes were used in this experiment. Ohmic contacts were created using AuGe/Ni metals. They were contacted with both layers simultaneously.

Subsequently, a pair of split gates of width 500 nm and length 100 nm was created, under which a coupled double-layer QPC was formed. The scanning electron microscopy image of the split gates is shown in Fig. 1. In this setup, the conductance and current noise are the results of the transport measurement through this QPC. The low-temperature electron mobility is as high as $\approx 2.5 \times 10^6$ cm²/(V s), given the low electron density in the DQW. This value provides a mean free path of $\approx 14 \ \mu m$ and a momentum relaxation time of $\approx 95 \ ps$ from the Drude model. The sample was mounted on the cold finger of the mixing chamber of a dilution refrigerator with a base temperature of 20 mK. We determine the x-, y-, and z-directions with regard to the current flow direction through the QPC and the 2DEG plane: the x-direction is perpendicular to the current and in-plane to the 2DEG; the y-direction is parallel along the current and in-plane to the 2DEG; the z-direction is perpendicular to the 2DEG. Magnetic fields $\boldsymbol{B} = (B_x, B_y, B_z)$ were applied using a vector magnet, with maximum fields of $B_x = 3$, $B_y = 1$, and $B_z = 8$ T. We use B = |B| as the magnitude of the total magnetic fields; thus, B = 0 T represents $B_x = B_y = B_z = 0$ T.

B. Conductance measurement

We measured the two-terminal differential conductance $G = dI_{\rm sd}/dV_{\rm sd}$ ($I_{\rm sd}$ and $V_{\rm sd}$ denote the source-drain current and voltage, respectively) and the transconductance dG/dV_{g} $(V_g$ denotes the gate voltage applied to the split gates) simultaneously, using two lock-in amplifiers. First, G was measured using a standard lock-in technique with a frequency of 387 Hz and an amplitude of $V_{\rm sd}^{\rm ac} = 10 \ \mu \rm V \ rms$; simultaneously, a small ac gate modulation $V_{\sigma}^{ac} = 4$ mV rms was applied through the second lock-in amplifier with a frequency of 13 Hz. The output signal of the first lock-in amplifier, which includes the ac modulation signal from V_{α}^{ac} , was input to the second lock-in amplifier, whose ac modulation was referenced by itself. This method allows us to measure the transconductance directly; therefore, it is sensitive enough to detect a small change in the transconductance. A dc gate voltage V_{g}^{dc} was also applied to the sample; thus, the total voltage applied to the split gate V_g is $V_g = V_g^{dc} + V_g^{ac}$. In addition, a dc voltage V_{sd}^{S} was applied to the source to cancel the voltage arising from the Seebeck effect because the drain was grounded at the mixing chamber, and dc voltage V_{sd}^{dc} was applied to the source electrode. Thus, the total voltage applied to the source V_{sd} was $V_{sd} = V_{sd}^{ac} + V_{sd}^{dc} - V_{sd}^{S}$. For practical use in graphs and image plots, we ignored the ac component of $V_{\rm g}$ and $V_{\rm sd}$.

C. Shot noise measurement

The current noise, i.e., the current fluctuation around its average, was measured at 300 mK following Refs. [53–55]. The voltage fluctuation generated in the parallel circuit of the sample and a 2.85-MHz *LC* resonator was measured as an output signal of a homemade cryogenic amplifier [54] at a 1 K pot and a room-temperature amplifier, as shown schematically in Fig. 1. Subsequently, the time-domain noise signal acquired by a digitizer was converted to a power spectrum through fast Fourier transform (FFT). The current spectral density $S_{\rm I}$ was

TABLE I. Typical values of parameters for noise measurement.

A	$Z_0\left(\Omega ight)$	<i>C</i> (pF)	$S_{\rm V}^{\rm out}~({ m V}^2/{ m Hz})$	$S_{\rm I}^{\rm out}~({\rm A}^2/{\rm Hz})$
8.7×10^{5}	6.1×10^{4}	1.0×10^{2}	1.3×10^{-19}	6.0×10^{-28}

obtained by fitting the resonance peak P_0 that was described as a function of the sample differential resistance $R_d = 1/G$ at a finite V_{sd} ,

$$P_0 = A \left[S_{\rm V}^{\rm out} + \left(\frac{Z_0 R_{\rm d}}{Z_0 + R_{\rm d}} \right)^2 \left(S_{\rm I}^{\rm out} + S_{\rm I} \right) \right], \tag{1}$$

where A denotes the total gain of the cold and roomtemperature amplifiers, Z_0 denotes the impedance of the *LC* resonance circuit, and S_V^{out} and S_I^{out} denote the current and voltage noise of the amplifier, respectively. After a series of careful calibration procedures, we obtained the parameters as shown in Eq. (1). Their typical values are tabulated in Table I.

For a finite temperature, S_{I} is described by the following equation [18]:

$$S_{\rm I} = \frac{2F}{R_d} \left[eV \coth\left(\frac{eV}{2k_{\rm B}T_{\rm e}}\right) - 2k_{\rm B}T_{\rm e} \right] + \frac{4k_{\rm B}T_{\rm e}}{R_{\rm d}}, \quad (2)$$

where T_e denotes the electron temperature and F denotes the Fano factor. For high bias region ($|eV| > 2k_{\rm B}T_{\rm e}$), the equation above becomes simpler; $S_{\rm I}$ behaves linearly on $\langle I_{\rm sd} \rangle$ as

$$S_{\rm I} = 2eF \langle I_{\rm sd} \rangle. \tag{3}$$

We evaluated the Fano factor using this simpler form as it yielded more reliable values [55].

III. RESULTS

A. Results of the conductance measurement

Figure 2(a) shows G as a function of V_g at 2 K and 35 mK. Reflecting the property of double-layer systems at 2 K, G drops twice at $V_g \approx -1.0$ and -1.5 V (indicated by the downward arrows), corresponding to the depletion of the front and back 2DEGs under the split gate, respectively. Then at 35 mK, several conductance plateaus are observed for $V_g < -2.8$ V

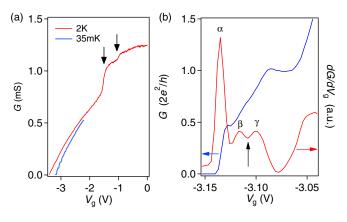


FIG. 2. (a) G as a function of V_g at 2 K and 35 mK at zero magnetic field B = 0 T. (b) G (left axis, in units of $G_0 = 2e^2/h$) and dG/dV_g (right axis, in arbitrary unit) as a function of V_g .

before the channel is pinched off at $V_g = -3.14$ V. Figure 2(b) shows detailed structures of G and dG/dV_g for $G < 1.5G_0$. The resistances of the leads and at the contacts are subtracted accordingly. We observe a clear $0.5G_0$ plateau in G and a local minimum in the dG/dV_g with a small plateau around $0.7G_0$ (indicated by the upper arrow). The simultaneous observation of these two features for B = 0 T has been reported in several experiments [27,37,49,51,56]. To the best of our knowledge, however, this has never been observed in a double-layer system before. To supplement the explanation, unlike the typical so-called "0.7 anomaly" in that a relatively higher temperature is required to observe a plateaulike feature [3], this minimum in dG/dV_g is clearly observed at extremely low temperatures such as $T \leq 35$ mK, indicating that it originates in a ground state. In addition, a 0.7 plateau is evolved into a clear 0.5 plateau by changing the electron density [8,36,37], or by increasing the in-plane magnetic field parallel to the channel [3]. Therefore, the concurrent observation of 0.5 and 0.7 plateaus is rather unusual. Physically, the peaks observed in dG/dV_g imply that the Fermi energy crosses the SBEs. In Fig. 2(b), three peaks are shown between the G = 0 and G_0 regions, suggesting that the Fermi energy crosses three SBEs in this region. We name these three peaks α , β , and γ from low to high $V_{\rm g}$.

Subsequently, the energy spectroscopy for the channel under the double-layer QPC was measured. Subband spacings of transverse modes at the QPC are observed in a spectroscopic measurement by controlling the Fermi energy E_F through $V_{\rm g}$ and the chemical potentials between the source and drain $\Delta \mu_{\rm sd} = \mu_{\rm s} - \mu_{\rm d} = eV_{\rm sd}$. Figure 3(a) shows the image plot of $dG/dV_{\rm g}$ as a function of $V_{\rm sd}$ and $V_{\rm g}$. The dark regions represent low dG/dV_g ; therefore, these regions indicate plateau regions in the conductance, whereas the brighter regions represent high $dG/dV_{\rm g}$, indicating that a Fermi energy passes through an SBE. It should be noted that the pinch-off voltage is different from that in Fig. 2 due probably to unexpectedly localized electric charges. As compared to ordinary monolayer QPC cases [57–61], or even several tunnel-coupled double-layer QPC cases [35,38,39], the data reveal a rich SBE structure, particularly inside the first (lowest) SBE diamond [see also Fig. 3(b), which is an enlarged image plot of Fig. 3(a) around the first SBE structure]. In Figs. 3(a) and 3(b), we draw the SBE lines by connecting the maxima in dG/dV_g on the image plot with the primary integer series in solid lines. The first large diamond appears from $V_{\rm g}\simeq -2.8~{
m V}$ and closes at $\simeq -2.7$ V, with a width of approximately 1.5 mV. As is well known, this width is to determine the subband spacing in the QPC. The electrostatic potential at the narrow constriction can be described as a saddle point model [62-64] given by

$$V(x, y) = V_0 - \frac{1}{2}m^*\omega_y^2 y^2 + \frac{1}{2}m^*\omega_x^2 x^2,$$
(4)

where V_0 is the electrostatic potential at the saddle, and the confinement potential curvatures are expressed in terms of the harmonic oscillation frequencies ω_x and ω_y . It should be noted that our coordinate is different from that used in Ref. [63], in which the propagation direction is *x*. The subband spacing in this diamond corresponds to $\hbar\omega_x = 0.75$ meV. The observed diamond shapes resemble slightly crushed rhombuses as compared to those in previous reports (e.g., [58]). Subsequently, we focus on the small structures by drawing split SBE lines in

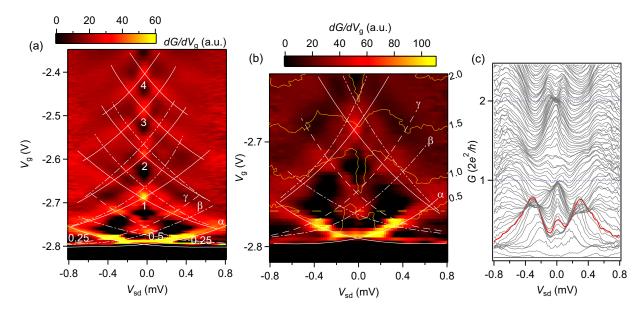


FIG. 3. (a) Image plot of dG/dV_g as a function of V_{sd} and V_g at T = 20 mK and B = 0 T with primary SBE lines (solid lines) and with full SBE splitting lines (dash-dotted lines and a broken line), which were drawn based on the dG/dV_g maxima. The numbers express the plateau values in the units of $G_0 = 2e^2/h$. (b) Enlarged image plot of dG/dV_g with contours of G in the units of G_0 (indicated by the slanted numbers near the right axis). The line profile at the dashed yellow line is shown later in Fig. 5(d). (c) G in units of G_0 as a function of V_{sd} for various V_g .

the dG/dV_g result, using dash-dotted lines and a broken line. An enlarged image plot focusing on the structure in the first diamond is shown in Fig. 3(b). From this experimental result, we observe three split SBE lines corresponding to the three peaks observed in Fig. 2(b) (α , β , and γ) for the first-integer SBE. We will demonstrate that this SBE splitting is supported by the in-plane magnetic fields dependence of dG/dV_g . Figure 3(c) shows the G profiles in units of G_0 as a function of $V_{\rm sd}$. As shown, the conductance is asymmetric with respect to the positive and negative sides of $V_{\rm sd}$. This asymmetry in G is large below $G < G_0$. As an example of the asymmetric behavior, we show a line profile of G at $V_{\rm g} = -2.766$ V [the horizontal broken yellow line in Fig. 3(b)] with a red curve in Fig. 3(c). This asymmetric behavior was observed previously [58] and explained in terms of self-gating effects. However, by analyzing the results of the shot noise measurements, which will be presented in Sec. III B, we inferred that this asymmetry has an intrinsic physical origin.

As we have explained in Sec. II, the in-plane components of the magnetic field, B_x and B_y , can be applied to the QPC independently. Figure 4 shows the image plots of dG/dV_{g} as functions of (a) V_g and B_x and (b) V_g and B_y . As B_x is increased with $B_v = 0$ T (fixed), each SBE except for the lowest SBE [marked with α in Fig. 4(a)] separates into two, then the upper branches move upward. Even the SBE between the 0.5 and 1 plateaus decouples into two (marked with β and γ). Therefore, the SBE under the G_0 plateau splits into three, which is consistent with the observed SBE lines in Fig. 3. The other SBEs show a Zeeman splitting similar to the cases of monolayer QPCs [65–67] as B_x increases. It is remarkable that the SBE splitting starts at approximately $B_x = 1$ T. However, as shown in Fig. 4(b), the SBEs indicate no clear dependences on B_{y} below 1 T; instead, they decrease slightly, particularly for higher SBEs. The lowest SBE shows no dependence of

 B_x and B_y . In addition, no clear onset of the second subladder (antisymmetric wave-function series) occurs for both in-plane fields below $G < 5G_0$, contrary to the previous double-layer QPC data [34,35,38].

Figures 5(a)-5(c) show the image plots of dG/dV_g for $B_x = 1.0$, 2.0 ($B_y = 0$ T), and $B_y = 1.0$ T ($B_x = 0$ T), respectively. As B_x increases, the structure in the first diamond (indicated by the white circles, SBE lines of β and γ in Figs. 3 and 4) shows an interesting change. The lower broad peak separates into two peaks gradually, in contrast to the upper peak that becomes a clear single peak. This is demonstrated in Fig. 5(b) ($B_x = 2.0$ T) as we indicate with three white arrows. Meanwhile, at $B_y = 1.0$ T, each of the lower and upper peak smears out and becomes a broad peak. In Fig. 5(d),

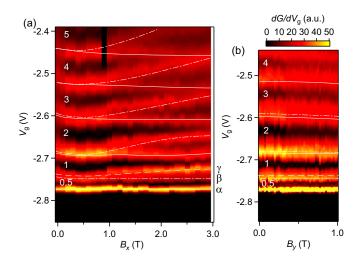


FIG. 4. Image plots of dG/dV_g as a function of (a) B_x and V_g at $B_y = 0$ T, and (b) B_y and V_g at $B_x = 0$ T.

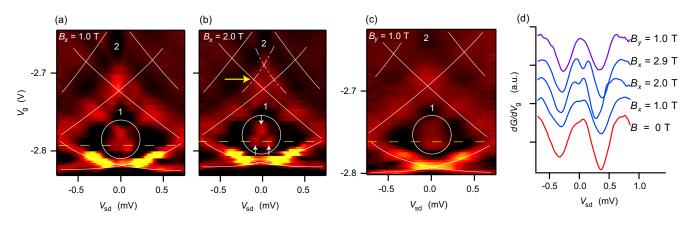


FIG. 5. Image plots of dG/dV_g as a function of V_{sd} and V_g at (a) $B_x = 1.0$, (b) $B_x = 2.0$, and (c) $B_y = 1.0$ T. Primary SBEs are indicated by the solid white lines. The three white arrows in (b) indicate three peaks inside the first diamond. In addition, the yellow arrow in (b) shows the Zeeman gap opening. (d) Line profiles of dG/dV_g at the lower peak in the first diamond [at the yellow broken lines in (a)–(c)] as a function of V_{sd} for B = 0, $B_x = 1.0$, $B_x = 2.0$, $B_x = 2.9$, and $B_y = 1.0$ T. For the $B_x = 2.9$ T data, see Fig. 14(c). Each trace is offset for clarity.

we plot the dG/dV_g profile of the lower peak at $V_g = 2.795$ V [indicated by yellow broken lines in Figs. 5(a)–5(c)] at B = 0, $B_x = 1$, $B_x = 2.0$, $B_x = 2.9$, and $B_y = 1$ T. At B = 0 T, a small shoulder appears on the left side of the center peak (at $V_{sd} = 0$ mV). However, we observe two peaks at $B_x = 2.0$ and 2.9 T clearly, and at $B_x = 1.0$ T slightly. Thus, the observed structure inside the first diamond shows a clear dependence on the magnitude of B_x . Meanwhile, the higher SBEs in Fig. 5(b) (indicated by the yellow horizontal arrow at $V_g = -2.705$ V) change differently; they exhibit a small diamond structure in accordance with the Zeeman gap opening as B_x increases (see also Fig. 14 in Appendix B).

In addition, we observe a result that is different from the previous results of the 0.7 anomaly. Figure 6 shows the image plots of dG/dV_g for several temperatures from 100 to 600 mK. Interestingly, the structure inside the first diamond smears out as *T* is increased, showing a broad vague peak at the center of the diamond. Therefore, it is clear that the structure observed in this study originates from the band dispersion of the

double-layer system. Conversely, the dG/dV_g minimum for the 0.5 G_0 plateau is robust. G forms a clear plateau at 0.5 G_0 ; after this plateau, it increases without forming additional clear plateaus.

B. Results of the shot noise measurement

To further obtain information on the phenomenon from a different aspect, we performed shot noise measurements. Figure 7(a) shows G as a function of V_g at 300 mK. The overshoot observed at the $0.5G_0$ plateau is more prominent at higher temperatures, resembling the one observed in [68]. We attribute the appearance of this overshoot to a resonance mode due to the superimposed transmission and reflection on the lowest SBE at the QPC region. Figure 7(b) shows S_I as a function of I_{sd} for $V_g = -2.88$, -2.85, and -2.83 V. S_I shows a parabolic behavior for $|eV_{\rm sd}| \lesssim 2k_{\rm B}T$, and then shows a linear dependence for $|eV_{sd}| \gtrsim 2k_BT$, which is a typical behavior of the shot noise with crossover from thermal noise to shot noise. We observe an asymmetric dependence between the positive and negative I_{sd} near $G = 0.7G_0$, which was also observed previously [22,58] and explained in terms of the self-gating effect in QPC. However, this asymmetry in $S_{\rm I}$ is observed

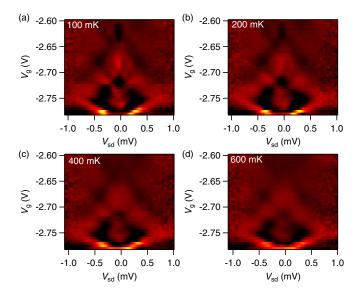


FIG. 6. Image plot of dG/dV_g as a function of V_{sd} and V_g at B = 0 T for T = (a) 100, (b) 200, (c) 400, and (d) 600 mK.

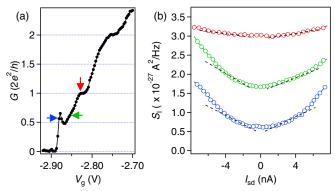


FIG. 7. (a) *G* as a function of V_g at T = 300 mK and B = 0 T for $V_{sd} = 0$ V. (b) S_I as a function of I_{sd} for $V_g = -2.88$, -2.85, and -2.83 V (from the bottom trace to the top). Each trace is offset for clarity. The colors of the traces correspond to the colors of the arrows in (a).

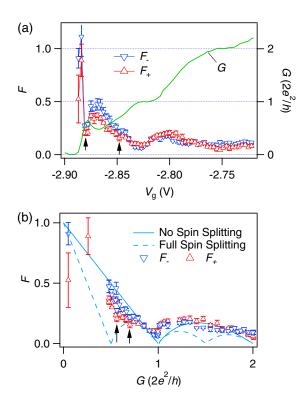


FIG. 8. (a) F_+ and F_- (left axis) and G (right axis) as a function of V_g at B = 0 T. (b) F_+ and F_- as a function of G. The solid lines and broken lines represent the theoretically expected values of the Fano factor for no spin splitting and full spin splitting, respectively. Fano factor reductions at $G = 0.5G_0$ and $0.7G_0$ are indicated by the upper arrows.

only for $-2.875 \leq V_g \leq -2.84$ V (for $0.5G_0 < G < G_0$), and it does not occur in other V_g values, thus suggesting other possibilities. Accordingly, the slope of S_I is always higher in the negative side of I_{sd} for $0.5G_0 < G < G_0$. As we have stated earlier, we derived the Fano factor from the slope of S_I as $F = S_I/(2e\langle I_{sd}\rangle)$. Due to the asymmetry between the positive and negative I_{sd} sides of the S_I , we used the Fano factor of the positive side F_+ and negative side F_- , and we plotted them as a function of V_g , as shown in Fig. 8(a). Further, the zero bias ($V_{sd} = 0$) conductance G is plotted on the right axis in Fig. 8(a). Consistent with the S_I result, F_- is larger than F_+ between the 0.5 G_0 and G_0 plateaus.

In a noninteracting scattering process, theory predicts [18]

$$F = \frac{\sum_{n} T_n (1 - T_n)}{\sum_{n} T_n},\tag{5}$$

where T_n denotes the transmission probability of the *n*th channel. We replot F_+ and F_- as a function of *G* in Fig. 8(b), along with the theoretical value of *F* when no spin splitting (the solid lines) and full spin splitting (the broken lines) occur. Both F_+ and F_- are suppressed at $G = G_0$ and $2G_0$, thus implying the formation of a single perfect conductance channel in the coupled DQW for the plateau region. Two important features of F_+ and F_- observed are (i) a clear suppression at $G = 0.5G_0$ and a rapid increase after this reduction as *G* is decreased, and (ii) a small reduction at $G \sim 0.7G_0$ [both reductions are indicated by the upper arrows

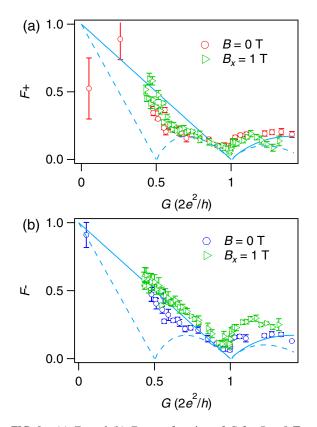


FIG. 9. (a) F_+ and (b) F_- as a function of G for B = 0 T and $B_x = 1$ T. The solid lines and broken lines represent the same as those in Fig. 8(b).

in Figs. 8(a) and 8(b)]. Regarding the first point, the decrease in the Fano factor indicates that $E_{\rm F}$ finishes crossing an SBE. After the suppression at $0.5G_0$, the Fano factor is increased even when the plateau of G is established. Generally, the increase in the Fano factor indicates that a new conduction channel opens as G increases from $G = 0.5G_0$. The second point suggests that, as shown previously [22,23,26] regarding the 0.7 anomaly, the existing channels' transmission probabilities contribute unequally to the conductance. This small reduction appears for both F_+ and F_- . The F values are larger than the theoretical values of F at the conductance plateau region. For the enhanced Fano factor, three possibilities can be considered: electron heating [55], channel mixing, and 1/f noise. However, the 1/f noise scarcely contributes to the enhancement in this experiment due to the noise measurement technique using a high resonant frequency LC circuit and double-high electron mobility transistor amplifier [54].

Furthermore, we measured the shot noise in the presence of in-plane magnetic fields. Figure 9 shows F_+ and F_- against G for B = 0 and $B_x = 1$ T. In the presence of in-plane magnetic fields, the Fano factor increases. At $B_x = 1$ T, the difference between F_+ and F_- becomes larger than the zero-field difference between the 0.5 and 1 plateau regions. As a notable difference, F_- obeys the theoretical dependence well.

IV. DISCUSSION

In this section, first we summarize our observations before presenting a discussion of the results. First, it is shown that three maxima exist inside the first diamond for the dG/dV_{g} result, especially in the presence of a large B_x . Next, G, dG/dV_g , and F exhibit an asymmetric dependence with respect to V_{sd} . However, in our results, an apparent beginning of the secondlayer SBE such as those observed in Refs. [34,35,38] is not observed, contrary to expectation. We cannot completely deny the possible effects from double-layer wave-function mixing on the issues above. Thus, we must specify whether our observation originated from double-layer wave functions. Hence, we conducted computer simulations using the NEXTNANO simulation software [69]. The simulation results do not support the formation of double-layer wave functions; thus, it is difficult to explain the results solely based on double-layer effects. Having obtained the simulation results, we propose a possible explanation for the experimental results above using the spin effect, i.e., the SOI-modified dispersion relation in particular.

A. Simulation results

Because the system contains two layers (front and back), we must consider two subladders for the wave functions and confinement potentials. We denote the wave function of the system as

$$\Psi_{l,m}(x, y, z) = u(y)\psi_{l,m}(x, z)$$
(6)

with direction y for propagating modes, and directions x and z for lateral and vertical (quantum-well) confinement, respectively. The envelope wave function can further be denoted as

$$\psi_{l,m}(x,z) = \chi_m(x)\phi_l^p(z),\tag{7}$$

where $\chi_m(x)$ denotes the *m*th lateral mode and $\phi_l^p(z)$ denotes the *l*th vertical wave function in the quantum well. For tunnel-coupled vertical modes,

$$\phi_l^p(z) = \alpha \varphi_l^{\rm f}(z) + \beta e^{i\theta} \varphi_l^{\rm b}(z), \quad \alpha^2 + \beta^2 = 1, \qquad (8)$$

where φ^{f} and φ^{b} denote the wave function in the front and back layers (subladder index), respectively, and θ denotes the interlayer phase difference. The index *p* uses S or AS: for *p* = S, $\theta = 0$ for the symmetric bonding state, and for *p* = AS, $\theta = \pi$ for the antisymmetric bonding state.

To confirm the SBEs in the first diamond, the wavefunction energies at the QPC were simulated using the selfconsistent Schrödinger-Poisson method with NEXTNANO. We first performed a one-dimensional (1D) simulation in the zdirection with reference to the characteristics of the bulk, i.e., the calculated Δ_{SAS} and V_g dependence of G to determine the simulation parameters (see Appendix C). Subsequently, we proceeded with two-dimensional (2D) simulations in the xzplane as a function of V_{g} . The SBE energies are calculated as the eigenvalues of the quantized wave functions in the xzplane under a lateral parabolic confinement potential. It is noteworthy that although the 2D simulation did not consider the y direction, we assume that the y-directional eigenenergies exhibit a qualitatively equivalent dependence on V_{g} in the QPC region. Thus, the lateral potential and width are determined based on the V_g value. Figure 10(a) shows the SBE energies as a function of V_g at the center of the QPC region. We found that the energy of the lowest antisymmetric wave

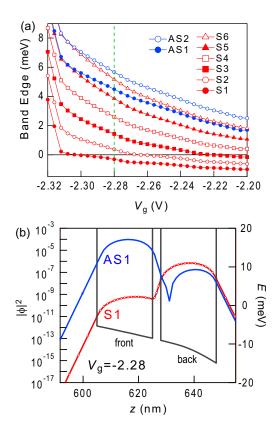


FIG. 10. (a) V_g dependence of the SBEs. S and AS denote symmetric and antisymmetric wave functions, respectively, and the number index represents the *m*th lateral mode. (b) $|\phi|^2$ for S1 and AS1 at $V_g = -2.28$ V [the dotted green line on the simulation result of (a)]. The black line represents the quantum-well potential V(z) for this gate voltage value. The origin of the *z*-axis starts from the sample surface.

function (l = 1, p = AS, m = 1) was higher than that of the fifth symmetric wave function (l = 1, p = S, m = 5), because the screening effect of the front layer was extremely strong to allow for the electrons to realize the antisymmetric wave function (hereafter, we denote the wave function using two indexes, p and m, such as AS1, because l is always 1). In Fig. 10(b), we show the $|\phi|^2$ of the lowest symmetric wave function (S1) and the antisymmetric wave function (AS1) at the first plateau region. The wave function shows a large imbalance between the front and back layers, indicating an extremely weak coupling between the two layers under an applied strong electric field of approximately $\sim 4 \text{ V}/(\mu \text{m})$. Hence, we expect electrons to exist primarily in the back layer and their wave function to permeate to the front laver: thus, the system behaves as a single-layer system with a large potential gradient toward the front layer.

B. Possible explanation with SOI-induced split dispersion relation

To explain the structure in the first diamond (indicated by the white circles in Fig. 5), the following simple relationship between the density of states (DOS) and conductivity can be useful. As is well known, the ballistic electron transport in a QPC shows the conductance that changes stepwise depending

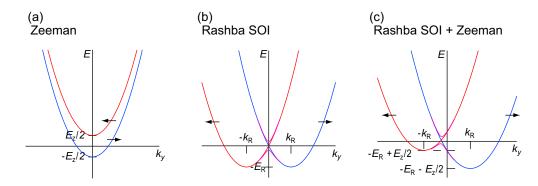


FIG. 11. Dispersion relations for (a) Zeeman splitting, (b) Rashba SOI splitting, and (c) Rashba SOI plus Zeeman splitting.

on the number of subbands below the Fermi level. Each subband carries the current

$$j = e^2 V_{\rm sd} n(E) v(E), \tag{9}$$

where $n(E) = \frac{1}{2\pi} \frac{\partial k}{\partial E}$ denotes the 1D unidirectional density of states, and $v = \frac{2\pi}{h} \frac{\partial E}{\partial k}$ denotes the group velocity. Therefore, cancellation between the DOS and the Fermi velocity causes the conductance quantization. Equation (9) describes the importance of the DOS, because the conductance is the result of the integral of the current divided by the applied voltage. Experimentally, a sudden DOS change results in a large conductance jump and a large transconductance peak. In our experiment, the brighter the SBE in the dG/dV_g plot, the larger are the DOS changes. Therefore, we observed three large DOS changes within the first diamond, as shown explicitly in Fig. 5(b).

For the candidate of the threefold DOS change, we suggest the dispersion relation that splits in the wave number k direction, such as the SOI-induced splitting [43,44,70] and the in-plane magnetic-field-induced splitting for tunnel-coupled double-layer systems [71], because three minima appear in the subbands. However, taking into account the simulation result, the possibility of realizing an in-plane magnetic-field-induced splitting is highly unlikely, because well-developed tunnelcoupled wave functions are a prerequisite for this to occur (we will discuss this in detail later). Regarding the SOI in this case, the space inversion symmetry is expected to be maintained for the x and y directions, but broken for the z direction. Thus, the Rashba SOI [52] with regard to the potential gradient in the zdirection and the current in the y direction $([0, 0, \partial V(z)/\partial z] \times$ $[0, k_v, 0] \parallel B_x$ is expected. The Hamiltonian regarding the Rashba SOI with this broken symmetry is

$$\mathcal{H} = \frac{\hbar^2 k_y^2}{2m^*} - \frac{\hbar^2}{4m^{*2}c^2} \sigma_x \frac{\partial V(z)}{\partial z} k_y \tag{10}$$

$$=\frac{\hbar^2 k_y^2}{2m^*} + \alpha_{\rm R} \sigma_x k_y, \tag{11}$$

where V(z) denotes the potential function of the DQW, σ_x denotes the *x* component of the Pauli matrix, and α_R is the so-called Rashba parameter. From Eq. (11) above, we can derive the dispersion relation with the Rashba SOI as

$$E^{\leftrightarrows}(k_y) = \frac{\hbar^2 k_y^2}{2m^*} \pm \alpha_{\rm R} k_y.$$
(12)

Then, the energy assumes a minimum value of $-\hbar^2 k_{\rm R}^2/(2m^*) = -E_{\rm R}$ at $k_y = \mp \frac{m^* \alpha_{\rm R}}{\hbar^2} = \mp k_{\rm R}$. Further, according to analysis [43,70], the *k*-directional split subbands are mixed; consequently, the subbands repel and open a gap into the upper and lower branches [see Fig. 11(b)]. Importantly, the lower branch contains two minima and the upper branch contains one minimum, at which the up- and down-spin DOSs are degenerated; hence, this SOI-modified dispersion exhibits three large DOS changes. Furthermore, in the presence of B_x , Eq. (12) is modified as follows:

$$E^{:=}(k_y) = \frac{\hbar^2 k_y^2}{2m^*} \pm \alpha'_{\rm R} k_y \pm \frac{1}{2} g^* \mu_{\rm B} B_x, \qquad (13)$$

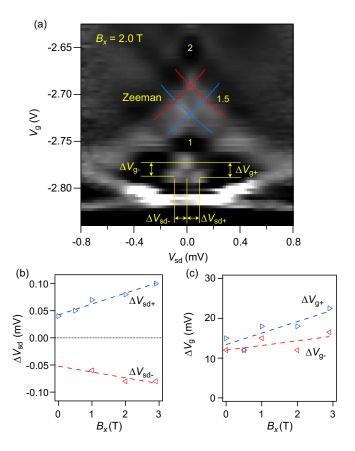


FIG. 12. (a) Enlarged image plot of dG/dV_g at $B_x = 2.0$ T. Two sets of Zeeman splitting SBE lines have been indicated. Plots of (b) ΔV_{sd} and (c) ΔV_g as a function of B_x .

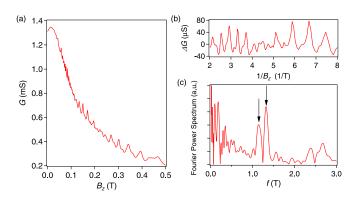


FIG. 13. (a) *G* as a function of B_z . (b) SdH oscillation extracted from (a). ΔG represents the conductance subtracted the background conductance change. (c) FFT power spectrum of the data in (b).

where μ_B denotes the Bohr magneton. The dispersion relations of the Zeeman splitting, Rashba SOI splitting, and Rashba SOI plus Zeeman splitting cases are illustrated in Fig. 11. The Rashba parameter should be modified because of an additional magnetic confinement potential created by B_x , $m^* \omega_{B_x}^2 z^2/2$ [35] ($\omega_{B_x} = eB_x/m^*$) in the yz plane, as follows:

$$\alpha'_{\rm R} = \frac{\hbar^2}{4m^{*2}c^2} \frac{\partial}{\partial z} \bigg[V(z) + \frac{1}{2}m^*\omega_{B_x}^2 z^2 \bigg].$$
(14)

Thus, the Rashba energy increases with the increase in B_x , which is a magnetic field parallel to the Rashba SOI field. This indicates that the two minima in the dispersion curves of Rashba SOI separate with the increase in B_x ; further, the crossing point and a side of a minimum separate vertically, whereas the other side approaches. As shown in Fig. 5, the lower two maxima inside the first diamond separate as B_x increases, and thus agree qualitatively to the behavior of minima in the dispersion curves of Rashba SOI.

We extract the positions of the lower two maxima as ΔV_{sd+} and $\Delta V_{\rm sd-}$. In addition, the separation of the center maximum and each lower maximum is extracted as ΔV_{g+} and ΔV_{g-} [see Fig. 12(a) for graphical illustration]. Figures 12(b) and 12(c) show the $\Delta V_{\rm sd}$ and the $\Delta V_{\rm g}$ values, respectively, as a function of B_x . Although ΔV_{g-} increases slightly, the overall changes correspond well to the three points in the dispersion curves of the Rashba SOI plus Zeeman splitting-the crossing point and the two minima. Therefore, the three maxima observed inside the first diamond can be attributed to these points. Considering that the Rashba SOI field is proportional to $\frac{\partial V(z)}{\partial z}p_y$, the principle behind the observed SOI is simple: the strong potential gradient and high mobility (or the large relaxation time [72]) of the sample. In our opinion, the center barrier in the DQW produces this strong potential gradient, as shown in the potential profile V(z) in Fig. 10(b).

Furthermore, the shot noise results support the conjecture above in that the SBE splitting originates from the SOI. As shown in Fig. 9, the additional B_x increases F_- to theoretical values. In addition, the difference between F_{-} and F_{+} becomes larger at $B_x = 1$ T. Given that B_x is in the same direction as that of the effective Rashba magnetic field $B_{\rm eff}$, when the current flows from the source to drain, $V_{sd} > 0$ (hence the electron momentum is in the opposite direction), a positive B_x supports $B_{\rm eff}$. However, the situation is completely different when V_{sd} is negative, because a positive B_x cancels B_{eff} as $B_{\rm eff}$ is induced to the negative x direction. Therefore, in the presence of the positive B_x , the separation by the Rashba SOI is enhanced for $V_{sd} > 0$ and decreased for $V_{sd} < 0$. Consequently, G is suppressed for $V_{sd} > 0$ and hence F_+ , and vice versa. As shown in Fig. 8, this anisotropic Fano factor is observed at 0 T. This is attributed to the effective Zeeman energy $g\mu_{\rm B}B_{\rm eff}$.

An alternative SOI-like dispersion splitting can be considered in a tunnel-coupled double-layer system. According to Ref. [71], an in-plane field induces the subband splitting in proportion to the magnitude of the in-plane field in the

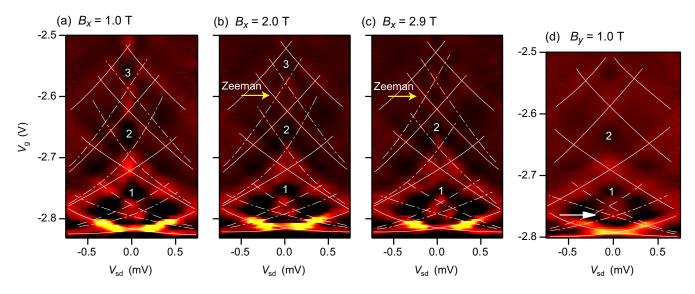


FIG. 14. Overall view of image plots of dG/dV_g as a function of V_{sd} and V_g at (a) $B_x = 1.0$, (b) $B_x = 2.0$, (c) $B_x = 2.9$, and (d) $B_y = 1.0$ T. The yellow arrows in (b) and (c) show subband openings due to the Zeeman splitting. (e) Line profiles of dG/dV_g at the white arrows in (a)–(d) as a function of V_{sd} for B = 0, $B_x = 1.0$, $B_x = 2.9$, and $B_y = 1.0$ T. Each trace is offset for clarity.

direction perpendicular to the in-plane field for 2DEG systems. Thus, B_x splits the subband in the k_y direction as $\Delta k_y = d/[\hbar/(eB_x)]$. However, the estimated separation for $B_x = 1$ T is $\Delta k_y = 3.5 \times 10^7 \text{ m}^{-1}$, thus yielding $\frac{(\hbar \Delta k_y)^2}{2m^*} = 0.69$ meV. Although the theory considers a double-layer 2DEG system, this value is significantly large, comparable to the observed first diamond splitting. Furthermore, we cannot explain the small split that is already observed at the zero magnetic field. In addition, a strong double-layer coupling is a prerequisite for this splitting. As shown in Fig. 10(b), the wave functions in the lower subbands are the highly unbalanced bonding state. Therefore, this cannot be the primary contribution to the horizontal splitting.

Finally, we would like to briefly discuss the reentrant conductance behavior that was observed in strong SOI systems in previous studies [43–45]. In this study, a small reentrant feature was confirmed as shown in Fig. 2(b), and in the conductance data in Figs. 7 and 8, although we interpreted them as a resonant mode. However, these features are not apparent compared with those in Refs. [43–45]. We attribute this to the band structure of the sample: the second lowest band exists immediately above the lowest band. This configuration suppresses "the helical gap" and obscures the reentrant behavior.

V. CONCLUDING REMARKS AND PERSPECTIVES

Herein we have revealed the SBE lines as a consequence of the wave-number direction subband splitting induced by a strong SOI. We have observed the coexistence of a $0.5G_0$ plateau and a structure at $0.7G_0$ in a double-layer QPC system. The structure observed in the dG/dV_g spectroscopy has revealed three maxima corresponding to the three minima in the dispersion relation of the wave-number-directional subband splitting. We attribute this splitting to a strong SOI due to the high potential gradient at the center barrier and the high mobility of the double-layer sample. The Fano factor obtained from the shot noise measurement has indicated an asymmetric transmission probability. This result further supports the SOImodified dispersion model and the asymmetry observed in the conductance measurement. However, multiple unanswered questions still exist that require theoretical considerations and additional experiments. This experiment includes useful information on spintronics and quantum engineering that would benefit applications. In particular, a strong SOI in a GaAs/AlGaAs sample invokes spintronic applications in this well-developed platform. In addition, we intend to perform shot noise measurements in the QHE region of this system in the future.

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APPENDIX A: SHUBNIKOV-DE HAAS OSCILLATION ANALYSIS

First, we measure the Shubnikov-de Haas (SdH) oscillation at zero bias ($V_{sd} = 0$) and zero split gate voltages ($V_g = 0$) in low magnetic fields at the lowest temperature available in this experiment to obtain the electron densities and tunnel coupling strength between the layers. Figure 13(a) shows G as a function of B_z . As a clear sign of the weak localization effect [73], positive magnetoconductance is observed initially. Subsequently, the difference in density between the symmetric state and the antisymmetric state results in a beating of the SdH oscillations in G [74]. This beating is resolved into two sharp peaks of a Fourier power spectrum from the fast Fourier transform analysis of the $1/B_z$ dependence of G, as shown in Fig. 13(c) by the arrows. The density ρ corresponding to each peak is, as we mentioned earlier, 0.64×10^{11} and 0.56×10^{11} cm⁻² from a well-known relation between the SdH frequency $f = \Delta B_z$ and ρ , $\rho = 2ef/h$, and the energy separation between the symmetric and antisymmetric states Δ_{SAS} is $\Delta_{\text{SAS}} = \pi \hbar^2 (\rho_{\text{S}} - \rho_{\text{AS}})/m^* = 0.29 \text{ meV}$, where $m^* = 0.067m_e$ in GaAs with m_e denoting the electron rest mass, and $\rho_{\rm S}$ and $\rho_{\rm AS}$ denote the electron density in the symmetric and antisymmetric states, respectively.

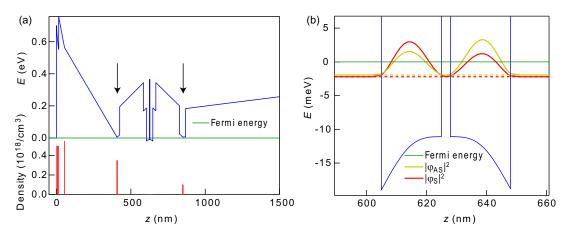


FIG. 15. (a) Potential distribution for the *z*-direction of the sample (upper) and the electron density profile (lower). The two downward arrows indicate the positions of δ -doping. (b) Probability densities for the lowest two energy wave functions (symmetric φ_S and antisymmetric φ_{AS} state) at the DQW confinement for the *z* direction.

TABLE II. Comparison of Δ_{SAS} between experiment and calculation.

	Experiment	Calculation
$\rho_{\rm S} \ (\times 10^{10} / {\rm cm}^2)$	6.4	6.2
$\rho_{\rm AS} (\times 10^{10}/{\rm cm}^2)$	5.6	5.5
$\Delta_{SAS} (mV)$	0.29	0.25

APPENDIX B: SUPPLEMENTAL dG/dV_{g} DATA

Figures 14(a)–14(d) show the overall view of the image plots of dG/dV_g as a function of V_{sd} and V_g for $B_x = 1.0$, 2.0, and 2.9 T and $B_y = 1.0$ T, respectively. For $B_x = 2.0$ and 2.9 T, the spin degeneracy is resolved for higher SBEs; consequently, we observe a minimum (dark region) corresponding to the 2.5G₀ plateau (indicated by yellow arrows). From this gap opening, the Zeeman splitting is ≈ 0.09 meV at $B_x =$ 2.0 T. Compared to the bare g-factor of GaAs (|g| = 0.44), the Zeeman energy, $|g|\mu_BB$, at this in-plane magnetic field is approximately twice that of the bare Zeeman splitting.

APPENDIX C: COMPUTER SIMULATION USING NEXTNANO SOFTWARE

To estimate the double-layer effects on the conductance, we must calculate the wave functions at the double-layer QPC under a strong electric field confinement. Hence, we used the electronic simulator software, NEXTNANO [69]. To supplement the main text, we provide the 1D simulation results of the Δ_{SAS} calculation and the V_g dependence of the wave functions. Figure 15(a) shows the potential profile for the z direction and the electron density profile. Due to our careful design, two Si δ -doping positions, indicated by the two downward arrows, render the DQW symmetric against the z direction successfully. Figure 15(b) shows the energy

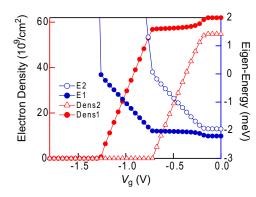


FIG. 16. 1D eigenenergies and electron densities for each layer as a function of V_g . E and Dens represent eigenenergies and electron densities, respectively; 1 and 2 correspond to the back layer and front layer, respectively.

of symmetric and antisymmetric wave functions and their probability density profiles at $V_g = 0$ V. The tunnel gap, Δ_{SAS} , is calculated as 0.25 meV, which is extremely close to the experimental value. We tabulate the measured and calculated values of Δ_{SAS} in Table II, along with the densities of the lowest symmetric and antisymmetric wave functions.

Figure 16 shows the calculated eigenenergies from the 1D simulation (*z*-direction) for the lowest wave function and the electron density for each layer as a function of V_g . As V_g increases in the negative direction, the potential of the front layer increases, the symmetric state electrons depopulate from the front layer, and the energy separation between the symmetric and antisymmetric wave functions becomes larger. As shown in Fig. 2(a), *G* drops twice at the two downward arrows. Although these two points represent two pinch-off points in the bulk 2DEGs of the front and back layers under the μ m-scale gate electrodes, we assume that the calculation results above correspond to this *G* behavior.

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