




Large spin Hall effect in Si at room temperature

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(Received 13 December 2019; revised manuscript received 4 March 2020; accepted 9 March 2020; published 31 March 2020)

Silicon's weak intrinsic spin-orbit coupling and centrosymmetric crystal structure are a critical bottleneck to the development of Si spintronics, because they lead to an insignificant spin Hall effect (spin current generation) and inverse spin Hall effect (spin current detection). Here, we undertake current, magnetic field, crystallography dependent magnetoresistance, and magnetothermal transport measurements to study the spin transport behavior in freestanding Si thin films. We observe a large spin Hall magnetoresistance in both *p*-Si and *n*-Si at room temperature and it is an order of magnitude larger than that of Pt. One explanation of the unexpectedly large and efficient spin Hall effect is spin-phonon coupling instead of spin-orbit coupling. The macroscopic origin of the spin-phonon coupling can be large strain gradients that can exist in the freestanding Si films. This discovery in a light, earth abundant and centrosymmetric material opens a new path of strain engineering to achieve spin dependent properties in technologically highly developed materials.

DOI: [10.1103/PhysRevB.101.094435](https://doi.org/10.1103/PhysRevB.101.094435)

I. INTRODUCTION

The spin Hall effect (SHE) [1,2] and its reciprocal is an efficient mechanism of generation and detection of spin current, which arises in materials with large intrinsic spin-orbit coupling (SOC). However, large SOC can also arise due to broken inversion symmetry. In the case of centrosymmetric materials, the symmetry can be altered using an inhomogeneous strain [2–6]. The broken symmetry in centrosymmetric materials will give rise to a flexoelectric polarization due to an inhomogeneous strain field as shown in Fig. 1(a) [7]. Recently, the flexoelectric effect [8–11] due to a strain gradient has been experimentally observed in centrosymmetric Si [12], which provides a foundation for this study. Based on the flexoelectric coefficient reported for Si [13], the strain and strain gradient mediated Rashba-Dresselhaus SOC may lead to SHE in Si with a magnitude similar to that of GaAs (Supplemental Material A [14], and see, also, Refs. [3,9,13,15–20] therein). Traditionally, strain gradient experiments involve bending thin films on soft substrates [12]. Alternatively, a freestanding beam will buckle automatically due to residual stresses. The stresses and, as a consequence, the buckling can be controlled using thermal expansion. Within this framework, we perform experimental measurements of SHE in Si (*p*-doped and *n*-doped) free-standing thin films. Using spin Hall magnetoresistance (SMR), magnetoresistance (MR) as a function of crystallographic direction and magnetothermal transport measurements, we report an unexpectedly large SHE that is comparable to or larger than those found in Pt.

II. EXPERIMENTAL SETUP

Using standard micro/nanofabrication techniques (Supplemental Material B [14]), we fabricated a freestanding, multilayer thin film structure with a four-probe longitudinal resistance setup as shown in Figs. 1(b) and 1(c). The false color scanning electron micrograph in Fig. 1(c) shows the fabricated experimental device geometry [21,22]. The length and width of the suspended beam are 160 and 12 μm , respectively. The materials and thicknesses of the multilayer thin film are Pd (1 nm)/Ni₈₀Fe₂₀(25 nm)/MgO(1.8 nm)/*p*-Si(2 μm).

There are two contributions to the strain and strain gradient in a freestanding thin film, residual thermal expansion strain due to the thin film processing and buckling strain due to the removal of the substrate. The strain profile in the specimen will be a superposition of a uniform normal strain due to thermal expansion and a strain gradient due to buckling as shown in Fig. 1(b). Residual stresses in thin films on a substrate may cause strain gradients, but they are not controlled. However, the buckling of a freestanding thin film will change with an increase in applied current mediated by Joule heating. If strain is a primary driving mechanism, the spin transport behavior will change as a function of current. In an all-metal system, the out-of-plane anisotropic magnetoresistance (OP-AMR) and SMR were shown to be functions of temperature [23] with a crossover occurring below room temperature. Thus, Joule heating can result in pure temperature effects combined with temperature driven strain effects.

To estimate the strain in the Si near the interface, we made a similar device with a longer 600- μm Si beam so that we could measure the buckling deformation (Supplemental Material Fig. S1) and estimate the residual stresses

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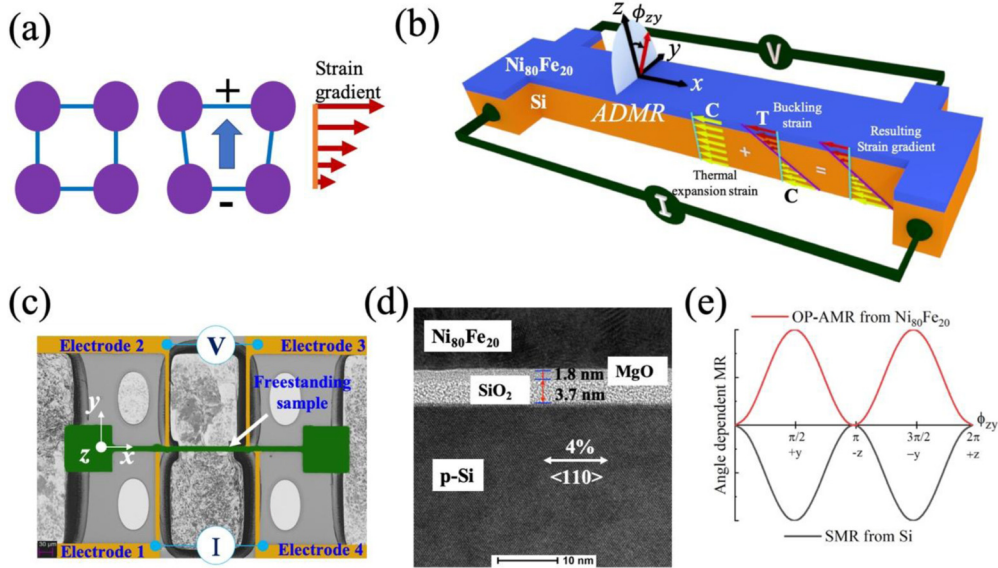


FIG. 1. Illustration of the test device, the effect of strain, and competing magnetoresistance effects. (a) Flexoelectric polarization due to a strain gradient. (b) Device schematic and experimental setup for angle dependent magnetoresistance measurements in the yz plane. The strain gradient due to thermal expansion and buckling is also shown. C denotes compression and T denotes tension. (c) A false color SEM micrograph showing the representative experimental device with freestanding channel, (d) high resolution transmission electron micrograph showing the thin film structure at the Si interface and the estimated strain in the $\langle 110 \rangle$ direction. (e) Expected symmetry behavior of the magnetoresistance corresponding to OP-AMR and SMR.

(Supplemental Material C [14]). From high resolution transmission electron microscope (HRTEM) diffraction along $\langle 110 \rangle$ and $\langle 111 \rangle$ directions, we estimate 4% tensile strain near the interface as shown in Fig. 1(d) and Supplemental Material Fig. S2. This calculated stress is less than the fracture stress of single crystal Si [24]. The strain is estimated for a very small region of the thin film, but the symmetry of the beam bending helps us in estimating the strain gradient. It is noted that the HRTEM sample preparation may release some of the stresses leading to underestimation of strain. The HRTEM image also shows the presence of a native oxide (~ 3.7 nm) despite Ar milling. However, the oxygen deficient native oxide will have dangling bonds and pin-holes that allow spin dependent electron tunneling and indirect exchange interactions required for spin transport studies. HRTEM imaging is complemented by energy-dispersive x-ray spectroscopy elemental mapping, which shows absence of any Ni or Fe diffusion in Si layer as shown in Supplemental Material Fig. S3 (Supplemental Material D [14]).

III. RESULTS

A. SMR measurement in p -Si thin film

SMR is a widely used characterization technique to identify SHE [25–27]. For SMR characterization, an angle dependent magnetoresistance (ADMR) measurement is carried out on a bilayer specimen that consists of a ferromagnetic (FM) layer and a normal layer. In our case, the normal layer is the Si layer. If SHE exists in the Si layer, the spin current absorption and reflection at the FM interface depends on the angle of the externally applied magnetic field. The spin absorption and reflection at the FM interface then modulates the longitudinal resistance of the Si through the inverse SHE.

The SMR behavior is identified by field rotation in the yz plane (field perpendicular to the direction of current) as shown in Fig. 1(b).

The $\text{Ni}_{80}\text{Fe}_{20}$ thin film exhibits OP-AMR [28] in the yz plane due to dimensional confinement. Hence, the total MR of the multilayer film will be a superposition of SMR from the Si layer and OP-AMR from the $\text{Ni}_{80}\text{Fe}_{20}$ as shown in Fig. 1(e). The angular resistance modulation (in the yz plane) due to OP-AMR and SMR can be written as

$$R = R_0 + (\Delta R_{\text{OP-AMR}} - \Delta R_{\text{SMR}})m_y^2, \quad (1)$$

where R_0 is the base resistance, $\Delta R_{\text{OP-AMR}}$ is the modulation in resistance due to OP-AMR, ΔR_{SMR} is modulation in resistance due to SMR, and m_y is the magnetic moment projection along the y axis defined in Figs. 1(b) and 1(c). Using ADMR measurements in the yz plane, the SHE behavior can be distinguished from the OP-AMR contribution due to their opposite symmetries as shown in Fig. 1(e).

The ADMR measurements are performed at a constant magnetic field of 4 T and as a function of applied current from 100 μA to 2 mA as shown in Fig. 2(a). The p -Si layer in the suspended structure is oriented along the $\langle 110 \rangle$ direction. At 100 μA , we observe an ADMR behavior having a polarity similar to OP-AMR as shown in Figs. 1(e) and 2(a). At 500 μA , the MR behavior is minimal and a further increase in current to 2 mA leads to a change in polarity that can be attributed to the contribution from SMR dominating the OP-AMR. Due to competition between OP-AMR and SMR, the measured ADMR values are small and are reaching the limit of instrumental resolution as observed in Fig. 2(a). However, the results presented in Fig. 2(a) are not artifacts due to instrumental resolution since they are supported by further measurements presented in this study.

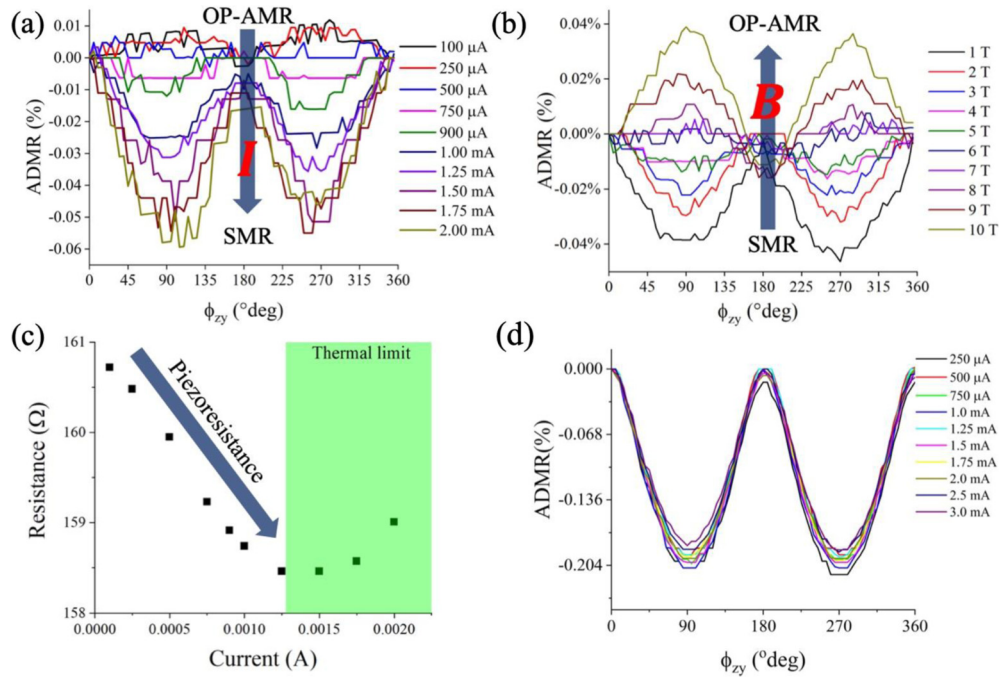


FIG. 2. The magnetotransport characterization of Si thin film samples. The angle dependent magnetoresistance as a function of rotation in the zy plane for Pd/Ni₈₀Fe₂₀/MgO/ p -Si thin film system aligned along the $\langle 110 \rangle$ direction (a) as a function of current showing transition from weak OP-AMR behavior to SMR at higher currents and (b) as a function of magnetic field showing transition from SMR at low fields to AMR at higher fields. The large arrow indicates the direction of current and magnetic field change. (c) The electrical resistance as a function of current at 300 K showing decrease attributed to piezoresistance in p -Si along $\langle 110 \rangle$ increasing compressive strain and (d) The angle dependent magnetoresistance as a function of rotation in zy plane for Pd/Ni₈₀Fe₂₀/MgO/ n -Si thin film system aligned along $\langle 110 \rangle$ direction showing SMR behavior as a function of current for an applied magnetic field of 3 T.

To ensure that observed behavior is due to interlayer spin dependent interactions, we measured the MR of the specimen as a function of magnetic field applied along y axis and z axis as shown in Supplemental Material Fig. S4 and magnetic hysteresis measurement as shown in Supplemental Material Fig. S5 (Supplemental Material E [14] and see, also, Refs. [29–31]). The measurement clearly shows a spin valve behavior due to spin dependent interactions across the layers despite the thick oxide layer.

To demonstrate the competition between SMR and OP-AMR, the ADMR measurement is carried out by keeping the current constant at 900 μ A while increasing the magnetic field from 1 to 10 T, as shown in Fig. 2(b). At low fields, the ADMR behavior displays polarity similar to SMR, indicating that magnitude of SMR is larger than OP-AMR. The ADMR is minimal at 6 T and changes polarity with further increase in strength of applied magnetic field to 10 T. The OP-AMR is a function of magnetic field due to magnon MR, while SMR is not. The magnetic field dependence of the ADMR is consistent with the picture of the two competing mechanisms of OP-AMR and SMR. To further support our argument, we measured the MR as a function of magnetic field from 14 to -14 T as shown in Supplemental Material Fig. S6 (Supplemental Material E [14] and see, also, Refs. [29–31]). The measurement shows a transition from SMR to OP-AMR behavior around 6 T, which supports ADMR measurement. This behavior arises due to diverging slopes of high field magnon MR [31] for a field applied along the y axis and z axis. Since the slope of magnon MR in the z axis is

larger, it supports our assertion that interlayer spin dependent interactions are responsible for SMR symmetry observed in ADMR measurements.

The observed SMR behavior can be quantified using thickness dependent measurements. However, unlike a deposited thin film, a single crystal Si layer makes thickness dependent measurements difficult. For quantitative estimation of the SMR, we calculate the maximum amplitude of the ADMR at each current using a sine square curve fit. The Ni₈₀Fe₂₀ resistance ($\rho_{\text{Ni}_{80}\text{Fe}_{20}} = 5.43 \times 10^{-7} \Omega\text{m}$) is measured from a control specimen and the resistance ($\rho_{p\text{-Si}} = 5.25 \times 10^{-5} \Omega\text{m}$) of the p -Si layer is estimated using a parallel resistor model. This value is consistent with the bulk SOI wafer resistivity of 0.001–0.005 Ωcm . With these resistivity values, 56% of the current flows in the Ni₈₀Fe₂₀ layer and 44% flows in the p -Si layer. Then, we measured ADMR in a Ni₈₀Fe₂₀ control sample as shown in Supplemental Material Fig. S7 to evaluate the OP-AMR contribution. The OP-AMR measurement in the Ni₈₀Fe₂₀ control specimen clearly shows that nonlinear effects due to high field are not the cause of SMR like symmetry behavior in a p -Si sample. We fabricated a second control sample with 25 nm of SiO₂ in between the Ni₈₀Fe₂₀ and p -Si layers. The ADMR measurement on this sample also displays OP-AMR response as shown in Supplemental Material Fig. S8. To further support our work, we fabricated a third control sample with Ni₈₀Fe₂₀ (25 nm) on a freestanding oxide membrane. This sample also exhibits an OP-AMR response as shown in Supplemental Material Fig. S9. These control experiments clearly show that the observed SMR behavior

arises due to the p -Si layer (Supplemental Material Section F [14]). From OP-AMR measurements on a $\text{Ni}_{80}\text{Fe}_{20}$ control specimen, we estimate the OP-AMR to be 0.125% at 4 T for the multilayer structure. Using this value for the OP-AMR, the magnitude of the SMR is 1.15×10^{-3} at 1.25 mA. It is an order of magnitude larger than that of Pt [25], and it is of the same order as the SMR reported in some topological insulators [32,33]. To approximate the spin Hall angle (Θ_{SH}), we utilize the SMR equations for a bimetallic [26] structure (the full expression is given in Supplemental Material H [14] and see, also, Ref. [34]). For our geometry and materials, it simplifies to

$$\frac{\Delta R_{xx}^{\text{SMR}}}{R_{xx}^0} \approx -\Theta_{SH}^2 \frac{\lambda_N}{d} \frac{2 * \tanh^2\left(\frac{d}{2\lambda_N}\right)}{(1 + \xi)\coth\left(\frac{d}{\lambda_N}\right)} \approx -\Theta_{SH}^2 \frac{2\lambda_N}{(1 + \xi)d}. \quad (2)$$

For the measured values of $\frac{\Delta R_{xx}^{\text{SMR}}}{R_{xx}^0} = 7.88 \times 10^{-4} - 0.00115$, a p -Si spin diffusion length of $\lambda_N = 310$ nm [35], a Si layer thickness of $d = 2 \mu\text{m}$, and a current shunting parameter $\xi = 1.21$, the spin Hall angle is $\Theta_{SH} = 0.075-0.096$. This value is three orders of magnitude larger than $\Theta_{SH} = 10^{-4}$ reported previously for p -Si [36] and it is of same order as the spin Hall angle of Pt ($\Theta_{SH} = 0.055 - 0.1$) [25,37]. 310 nm is one of the largest values of spin diffusion length reported for p -Si, and it results in a lower bound on the spin Hall angle. Shikoh *et al.* [38] reported a spin diffusion length of 148 nm in p -Si whereas Weng *et al.* [39] reported a value of 40 nm. Using these values increases the estimated spin Hall angles to 0.26. Hence, the extracted values of the spin Hall angle for p -Si in our samples can be in the range of 0.075–0.26. These values are two orders of magnitude larger than GaAs, and are not expected to arise due to strain gradient only (Supplemental Material A [14]). However, the strain may be the underlying cause of the large variance in reported spin Hall angle values.

B. Piezoresistive effects in p -Si

Similar to SMR, the longitudinal resistance of the specimen (R_{xx}^0), estimated from ADMR measurements, is also a function of applied current, as shown in Fig. 2(c). The resistance decreases as the applied electric current is increased from 100 μA to 1.25 mA, and then it increases after 1.25 mA. The Joule heating due to the current leads to an increase in the sample temperature, which consequently causes thermal expansion induced stresses. p -Si [40], $\text{Ni}_{80}\text{Fe}_{20}$, and the composite multilayer [30] have positive temperature coefficients of resistance. We measured the resistance of the specimen as a function of chamber temperature from 300 to 350 K as shown in Supplemental Material Fig. S10, which clearly shows an increase in resistance as a function of temperature. The rise in chamber temperature does not increase the buckling stresses significantly since the substrate is also expanding. In contrast, an increase in current causes thermal expansion of the sample structure only since the substrate (heat sink) temperature is not changing. Hence, the resistance of the multilayer thin film should not decrease due to Joule heating. However, thermal expansion induced compressive stresses along the Si $\langle 110 \rangle$

direction leads to a decrease in the resistance attributed to piezoresistance [41–43]. For the freestanding structure in this study, the decrease in resistance from piezoresistance is larger than the increase in resistance due to the temperature rise for applied currents less than 1.25 mA. From the parallel resistor model, we estimate that the electrical resistance of the p -Si layer changes from ~ 360.5 to $\sim 349.3 \Omega$. The bulk piezoresistance coefficient for p -Si (110) is $71.8 \times 10^{-11} \text{ m}^2/\text{N}$ [42,43] and it changes by a factor of ~ 0.4 [42] for doping concentrations above 10^{19} cm^{-3} . Using the piezoresistance coefficients, we estimate the change in compressive stress due to 1.25 mA of heating current is ~ 107 MPa in addition to residual stresses prior to Joule heating. The change in compressive stress of 107 MPa is larger than the estimated buckling stress (~ 20 MPa) of the specimen, which will enhance the existing strain gradient due to residual stresses. This analysis shows that strain and strain gradient is the underlying reason for increase in the magnitude of SMR observed in the current dependent ADMR measurements shown in Fig. 2(a).

C. SMR measurement in n -Si thin film

We attribute the SMR behavior in p -Si to spatially varying strain. Hence, strain effects should be observed in n -Si specimens as well. To verify it, we fabricated a Pd (1 nm)/ $\text{Ni}_{80}\text{Fe}_{20}$ (75 nm)/MgO (1.8 nm)/ n -Si ($2 \mu\text{m}$) freestanding structure in the same four-probe measurement geometry as shown in Figs. 1(b) and 1(c). The thickness of the $\text{Ni}_{80}\text{Fe}_{20}$ layer is increased, since the n -Si is more conductive ($\rho_{n\text{-Si}} 1.94 \times 10^{-5} \Omega\text{m}$) than the p -Si. Thicker $\text{Ni}_{80}\text{Fe}_{20}$ thin films do not exhibit OP-AMR behavior leading to simplified SMR estimates. The n -Si layer in the free-standing structure is oriented along Si $\langle 110 \rangle$ similar to p -Si. ADMR measurements as a function of current from 250 μA to 3 mA were taken as shown in Supplemental Material Fig. S11. The resistance of the specimen increases with increasing current in contrast to that of the p -Si sample. The sign of the piezoresistance coefficient for n -Si is opposite to that of p -Si. Hence, the compressive stress leads to an increase in resistance in the n -Si due to the piezoresistive effect. The measured SMR is 0.192% and shows a small decrease when the applied current is increased as shown in Fig. 2(d) unlike the p -Si sample. The magnitude of SMR is approximately twice as large as that of p -Si, which itself is larger than that of Pt. Assuming a spin diffusion length of $2 \mu\text{m}$ [44] for n -Si, we calculate the spin Hall angle to be 0.119 (Supplemental Material H [14]), which is larger than the calculated spin Hall angle for the p -Si sample. The SMR behavior as a function of current in n -Si suggests that the strain dependent behavior of the n -Si sample is different from p -Si sample. The residual stresses evolve during Si and SiO_2 etching and other processing steps. The $\text{Ni}_{80}\text{Fe}_{20}$ layer is three times thicker in the case of n -Si and the resulting residual stresses in n -Si after processing could be sufficient for the observation of the SMR behavior. In addition, the thin film structure can buckle to have either a convex or concave curvature, which will give rise to different signs for the strain gradient. However, further change in stresses (strain) due to thermal expansion may be relatively small to cause a significant change in the SMR behavior in case of n -Si.

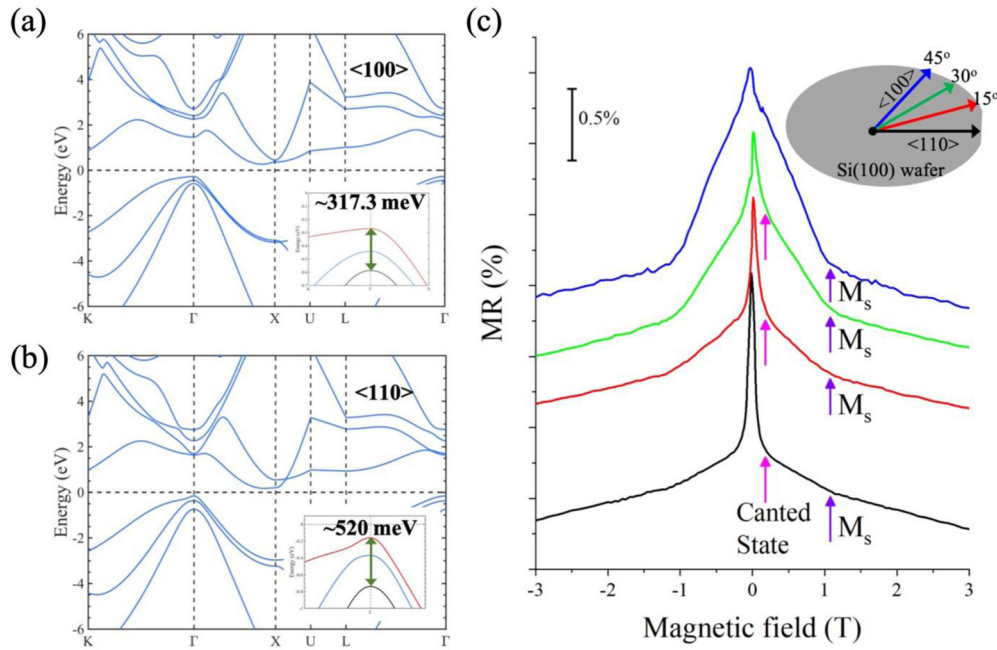


FIG. 3. Crystallographic behavior. (a) the band structure of Si for 4% tensile strain applied along $\langle 100 \rangle$ and inset showing the energy splitting at the peak of valence band, (b) the band structure of Si for 4% tensile strain applied along $\langle 110 \rangle$ and inset showing the energy splitting at the peak of valence band and (c) the magnetoresistance for an applied out of plane magnetic field for current applied along $\langle 110 \rangle$ direction or along the flat of the Si(100) wafer, at 15° to the $\langle 110 \rangle$ direction, at 30° to the $\langle 110 \rangle$ direction and along $\langle 100 \rangle$ direction. Arrows showing saturation magnetization and possible canted states and its transition as a function of orientation.

D. Crystallography dependent MR in p -Si

The next step is to understand the effect of a $\sim 4\%$ tensile strain near the interface. We performed density functional theory (DFT) calculations of the band structure of Si with an applied strain along the $\langle 001 \rangle$ and $\langle 110 \rangle$ directions. (Supplemental Material I [14] and see, also, Refs. [45–50]). The applied strain lifts the degeneracy of the valence band maxima resulting in a strain mediated valence band splitting. A 4% tensile strain applied along $\langle 001 \rangle$ direction leads to an energy splitting of 317 meV in the valence band as shown in Fig. 3(a) and for compressive strain, the splitting increases to 412 meV as shown in Supplemental Material Fig. S12 (d). Similarly, along $\langle 110 \rangle$, an applied 4% tensile or compressive strain leads to valence band splitting of ~ 520 or 600 meV respectively as shown in Fig. 3(b) and Supplemental Material Fig. S12(a) and S12(b), respectively. Applied strain has a significantly larger effect on the valence bands than on the conduction bands as shown in Supplemental Material Figs. S12(c) and S12(d). The fact that the SMR in p -Si (n -Si) has a strong (weak) dependence on the current is consistent with the picture of the SMR driven by temperature-controlled strain.

From DFT simulations, we observed that the valence band splitting due to strain in the $\langle 110 \rangle$ direction is different from that due to strain in the $\langle 100 \rangle$ direction. The symmetry of $\langle 110 \rangle$ strained Si will be lower than the $\langle 100 \rangle$ strained Si [51], which will give rise to a crystallographic dependent behavior. To ascertain the crystallographic direction dependent behavior, we fabricated a set of $\text{Ni}_{80}\text{Fe}_{20}(25\text{ nm})/\text{MgO}(1\text{ nm})/p\text{-Si}(2\ \mu\text{m})$ multilayer structures with the longitudinal direction of the Si layer

lying along $\langle 110 \rangle$, and at 15° , 30° , and 45° with respect to $\langle 110 \rangle$ as shown in Fig. 3(c). The negative MR for the Si channel oriented along $\langle 110 \rangle$ has two kinks due to changes in slope indicated by the arrows. The kink at higher magnetic field ($\sim 1.1\text{ T}$) corresponds to the change in slope at the saturation magnetization (M_s). The kink at low field ($\sim 0.2\text{ T}$) is not expected for a $\text{Ni}_{80}\text{Fe}_{20}$ thin film hard axis magnetization. This kink can only arise due to spin dependent tunneling across the oxide barrier. The low field kink disappears for measurement along $\langle 100 \rangle$ direction or at 45° from $\langle 110 \rangle$, which indicates the changes in the spin dependent interactions between the $\text{Ni}_{80}\text{Fe}_{20}$ and the Si layers. The negative MR behavior arises from polycrystalline $\text{Ni}_{80}\text{Fe}_{20}$ thin film. And, the observed correlation of the MR with the Si layer crystallographic direction will not arise if there are no spin dependent tunneling and interactions. This measurement gives additional proof that exchange interactions are taking place in spite of thick oxide layer (MgO and SiO_2). We have also demonstrated that the spin dependent interactions are function of crystallographic direction of p -Si layer.

IV. DISCUSSION

There are various mechanisms that can give rise to SMR behavior in Si. From experimental transport measurements, we demonstrate that inhomogeneous strain is the macroscopic cause of the SMR response in n - and p -doped Si. Microscopically, inhomogeneous strain can be modeled as Rashba-Dresselhaus SOC (Supplemental Material A [14]), which can give rise to SMR behavior. However, the spin Hall angle is larger than the one expected according to flexoelectric

coefficients (Supplemental Material A [14]). Alternatively, inhomogeneous strain will give rise to internal effective magnetic field, which arises due to coupling of electron spin to the off diagonal elements of crystallographic strain tensor as described by Crooker *et al.* [4] and can give rise to SHE but that can also not explain the large magnitude of SMR observed in this study.

Recently, Lou *et al.* [52] demonstrated spin-phonon interactions leading to a change in thermal conductivity in both *p*-Si and *n*-Si [21,22]. While the charge carriers in *p*- and *n*-doped Si are different, the thermal transport is phonon mediated in both cases. We speculate that spin dependent electron-phonon scattering may also give rise to the observed SMR behavior reported earlier. In order to uncover the mechanistic origin of the behavior, we measured the transverse spin-Nernst effect (SNE) in *p*-Si (Supplemental Material J [14] and see, also, Refs. [53,54]). Whereas the magnetothermal transport measurement shows transverse SNE behavior in the measurements, experimental results are inconclusive as shown in Supplemental Material Fig. S14. However, these measurements do indicate the existence of interlayer spin-phonon coupling.

In heavy metals, a mechanistic reason for both SHE and SNE is large SOC [55]. However, that is not true for Si where thermal transport is mediated by phonons as opposed to charge carriers. Microscopically, spin dependent interactions with phonons cause transverse spin current or SHE during charge transport. Also, an inverse microscopic behavior occurs during thermal transport where phonons have spin dependent interactions with charge carrier and give rise to transverse spin current or SNE. Hence, a strain mediated spin dependent coupling between phonon and charge carrier is proposed to be the microscopic mechanism for SHE observed in this study.

V. CONCLUSION

This study presents experimental evidence of inhomogeneous strain mediated spin-phonon coupling in centrosymmetric nonmagnetic material [56]. The spin-phonon coupling and resulting efficient spin to charge conversion may be applicable to all diamond cubic semiconductors (GaAs, Ge,

InSb etc.) under inhomogeneous strain. Manufacturing processes for strain engineering already exists not only for Si but also for other semiconductors. Topological behavior can also arise from the inhomogeneous strain fields, which may also open simple materials systems for topological materials research irrespective of intrinsic spin-orbit coupling. In addition to proposed experimental studies, theoretical models that describe the spin-phonon coupling in centrosymmetric materials and resulting behavior also need to be developed. This work provides a starting point for such future studies.

The data that support the findings of this study are available from the corresponding author upon reasonable request [57].

ACKNOWLEDGMENTS

The fabrication of experimental devices was done at Center for Nanoscale Science and Engineering at UC Riverside. Electron microscopy sample preparation and imaging was done at the Central Facility for Advanced Microscopy and Microanalysis at UC Riverside. Theory and analysis was supported as part of Spins and Heat in Nanoscale Electronic Systems (SHINES) an Energy Frontier Research Center funded by the US Department of Energy, Office of Science, Basic Energy Sciences under Award No. DE-SC0012670. This work used the Extreme Science and Engineering Discovery Environment (XSEDE) [58], which is supported by National Science Foundation Grant No. ACI-1548562 and allocation ID TG-DMR130081.

P.C.L. carried out the SMR and SNE setup fabrication and did the SMR measurements. A.K. and R.G.B. fabricated the crystallography device fabrication and contributed to all the measurements. T.B. carried out the DFT calculations. S.K. conceived the idea, designed the experiments, coordinated the project, supervised the experimental work, performed data analysis, and led manuscript preparation. R.K.L. supervised the theory and computational work and analyzed the experimental data. S.K., W.P.B., and R.K.L. wrote the manuscript. All the authors discussed and commented on the manuscript.

The authors declare no competing interests.

P.C.L., A.K., and R.G.B. contributed equally to this work.

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