

## <sup>115</sup>In NQR study with evidence for two magnetic quantum critical points in dual Ce site superconductor Ce<sub>3</sub>PtIn<sub>11</sub>

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<sup>115</sup>In nuclear quadrupole resonance (NQR) measurements have been carried out on Ce<sub>3</sub>PtIn<sub>11</sub>, a heavy fermion compound harboring two inequivalent Ce sites. This system exhibits magnetic transitions at  $T_{1n} = 2.2$  K and  $T_N = 2$  K, prior to entering a superconducting state below  $T_c = 0.32$  K. Previous measurements imply that magnetism and superconductivity are spatially separated and only the Ce(2) sublattice orders magnetically, with a quantum critical point at pressure  $p_c = 1.3$  GPa, while the Ce(1) sublattice is paramagnetic. However, the present nuclear relaxation rate behavior of  $1/T_1 \propto \sqrt{T}$  reveals the presence of critical spin fluctuations indicative of close proximity to another quantum critical point, presumably at a small negative pressure, which is associated solely with the Ce(1) sublattice. The ordered wave vector is found to be most likely  $(1/2, 1/2, h)$ .

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For materials in proximity of a “magnetic instability” or quantum critical point (QCP) where  $T_N \rightarrow 0$ , the abundance of low-lying and spatially extended antiferromagnetic (AFM) spin fluctuations of large amplitude are considered to be the cause for unconventional normal and superconducting (SC) states. Quite recently, a new heavy fermion (HF) antiferromagnet Ce<sub>3</sub>PtIn<sub>11</sub> was discovered. The material belongs to the Ce<sub>n</sub>T<sub>m</sub>In<sub>3n+2m</sub> class of layered HF materials with most prominent representatives at ambient pressure being CeIn<sub>3</sub> [local moment (LM)-AFM;  $T_N = 10.2$  K], CeCoIn<sub>5</sub> (HF-SC;  $T_c = 2$  K), CeRhIn<sub>5</sub> (HF-AFM;  $T_N = 3.8$  K), and Ce<sub>2</sub>RhIn<sub>8</sub> (HF-AFM;  $T_N = 2.8$  K). At ambient condition, Ce<sub>3</sub>PtIn<sub>11</sub> shows remarkable properties: Ce<sub>3</sub>PtIn<sub>11</sub> undergoes two successive magnetic transitions at  $T_{1n} = 2.2$  K and  $T_N = 2.0$  K, respectively, and becomes SC below  $T_c = 0.35$  K [1]. Upon applying hydrostatic pressure  $T_{1n}$  and  $T_N$  reduce and intersect with the SC state at  $p \approx 1.1$  GPa. Extrapolation of  $T_N \rightarrow 0$  reveals a critical pressure of  $p_c = 1.3$  GPa, which is considerable lower than in other compounds of this class, e. g.,  $p_c$  of CeRhIn<sub>5</sub> yields  $\approx 2.3$  GPa [2,3]. Noteworthy, for  $1.1 < p < 1.6$  GPa a non-Fermi-liquid state is observed which is characterized by an almost  $T$ -linear resistivity from  $T_c (\approx 0.7$  K) to temperatures even higher than  $T > 5$  K.

The discovery stirred a barely considered aspect; the majority of HF compounds investigated possess only one crystallographic independent LM site per unit cell. In HF compounds with multiple crystallographic inequivalent LM sites, such as Ce<sub>3</sub>PtIn<sub>11</sub>, the local environment of these two or more sites is different, leading to distinct different Kondo interaction strengths. It is easily conceivable that the ground state in such a compound is a microscopic coexistence of different electronic and magnetic sublattice states.

Figure 1 illustrates the unit cell of Ce<sub>3</sub>PtIn<sub>11</sub>. The Ce(1) surrounding is identical to Ce ions in Ce<sub>2</sub>PtIn<sub>8</sub>, which as a

matter of fact is paramagnetic (PM) down to lowest temperatures [4]. The Ce(2) ion has a CeIn<sub>3</sub>-like environment. On these bases it has been suggested that the Ce(1) sublattice is fully Kondo screened and makes the superconducting state while on the other hand the Ce(2) is responsible for the magnetic ordering [1]. As in Chevrel phases [5], borocarbides [6], and the high  $T_c$ 's [7], magnetism and superconductivity hence would coexist as two spatial separated ground states in Ce<sub>3</sub>PtIn<sub>11</sub>, a novelty in HF compounds. The purpose of this <sup>115</sup>In NQR study is to find microscopic evidence for such a scenario.

Single-crystal samples of Ce<sub>3</sub>PtIn<sub>11</sub> were grown by the self-flux method. Details about the preparation and characterization of the sample have been reported previously [1]. NQR spectra under zero field on the <sup>115</sup>In nuclear spins ( $I = 9/2$ ) were carried out using the standard  $\pi/2$ - $\pi$  spin-echo method described in Ref. [8].

The crystal structure of Ce<sub>3</sub>PtIn<sub>11</sub> harbors 11 In ions per unit cell, which are situated at four inequivalent positions (see Fig. 1). Adhering to standard conventions, the most symmetric In(1) site has local tetragonal symmetry ( $4/mmm$ ), followed by In(2) ( $4mm$ ), In(3) ( $2mm$ ), and In(4) ( $2mm$ ). The corresponding zero-field NQR frequencies of the respective In sites can be derived using the Hamiltonian [9],

$$\mathcal{H}_{\text{NQR}} = \frac{e^2qQ}{4I(2I-1)} \left[ 3I_z^2 - I(I+1) + \frac{1}{2}\eta(I_+^2 + I_-^2) \right], \quad (1)$$

where  $Q$  is the nuclear quadrupole moment ( $^{115}\text{In} Q = 0.810 \times 10^{-28} \text{ m}^2$  for <sup>115</sup>In),  $eq = V_{zz}$  is the principal component of the electric field gradient tensor  $V_{ij}$ , and  $\eta = (V_{xx} - V_{yy})/V_{zz}$  is the asymmetry parameter. The nuclear quadrupole resonance frequency is defined as  $\nu_Q \equiv \frac{3e^2qQ}{2I(2I-1)\hbar}$ . In the absence of a magnetic field, each In site exhibits four frequencies labeled

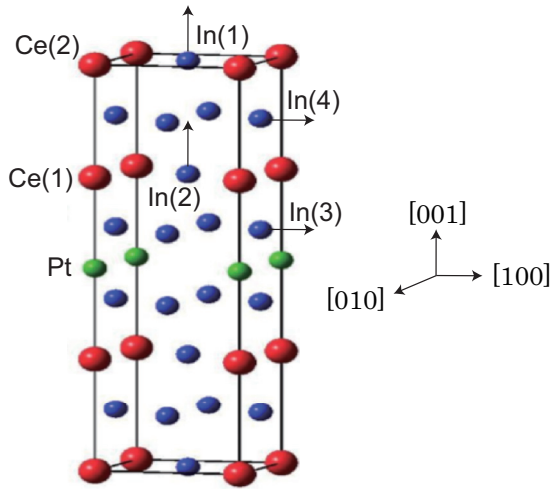


FIG. 1. Unit cell of  $\text{Ce}_3\text{PtIn}_{11}$  [space group  $P4/mmm$  and  $a = 4.6874(4)$  Å and  $c = 16.8422(12)$  Å [4]]. Ce(1) and Ce(2) are considered to be PM and AFM ordered, respectively, below  $T_N$  [1]. The arrows indicate the direction of the quantization axis at each In site, i.e.,  $V_{zz}$  determined by local symmetry and LDA calculations [10].

by  $f_n$  ( $n = 1-4$ ), being associated with the transitions between  $|I_z = \pm 1/2\rangle$  and  $|I_z = \pm 3/2\rangle$ ,  $|I_z = \pm 3/2\rangle$  and  $|I_z = \pm 5/2\rangle$ , and so on. For the In(1) and In(2) sites  $\eta = 0$ , and  $f_n$  obeys the rule  $f_n = n\nu_Q$ . In contrast, the In(3) and In(4) have  $\eta \neq 0$ , hence the resonance frequencies do not follow such a simple relation.

In Fig. 2(a) we show the NQR spectrum in the paramagnetic state measured at a temperature of 3.1 K. The peaks are narrow, corresponding to only a small distribution of electric field gradients, as expected for a high-quality single-crystal sample. The signal intensity of In(1) and In(4) is weak compared with that of In(2) and In(3), since the spin-spin relaxation time  $T_2$  is short at these sites (as well as the spin-lattice relaxation time  $T_1$ ) (see Fig. 3).

Table I lists calculated values of  $\nu_{Q,\text{calc}}$  and  $\eta_{\text{calc}}$  for  $\text{Ce}_3\text{PtIn}_{11}$  derived from local density approximation (LDA) band calculations [10]. By comparing these calculated values with experimental ones from the present measurements, we were able to decompose the spectra. First, the In(2) site has  $f_n$  ( $n = 1-4$ ) = 7.58, 15.16, 22.74, and 30.32 MHz, respectively, with  $\eta = 0$ . The experimentally determined  $\nu_Q$  is smaller than the theoretical prediction ( $\nu_{Q,\text{calc}} = 9.6$  MHz). However, the implied shift in LDA calculations toward higher frequencies seems to be systematic for heavy atoms [10,11]. An effect of  $f$ -electron localization due to correlations is not included in the LDA calculations, however, such an effect on  $\nu_{Q,\text{calc}}$  is not significant [12], thus it is reasonable to use the  $\nu_{Q,\text{calc}}$  values for site assignment.

The  $f_n$ 's for the In(3) site are easier to deduce. The transitions are located at 21.4, 28.7, 44.9, and 60.2 MHz in the spectra. As can be seen,  $f_3$  and  $f_4$  are accompanied by small satellite peaks at 44.3 and 59.4 MHz. They arise from the  $^{113}\text{In}$  isotope ( $I = 9/2$ ), which has a natural abundance of 4.3% ( $^{115}\text{In}$  is 95.7% abundant), and whose transitions obey the ratio  $^{113}f_n/^{115}f_n = ^{113}Q/^{115}Q$ . The other low-intensity transition visible and marked by a  $\Delta$  in Fig. 2(a) has a very

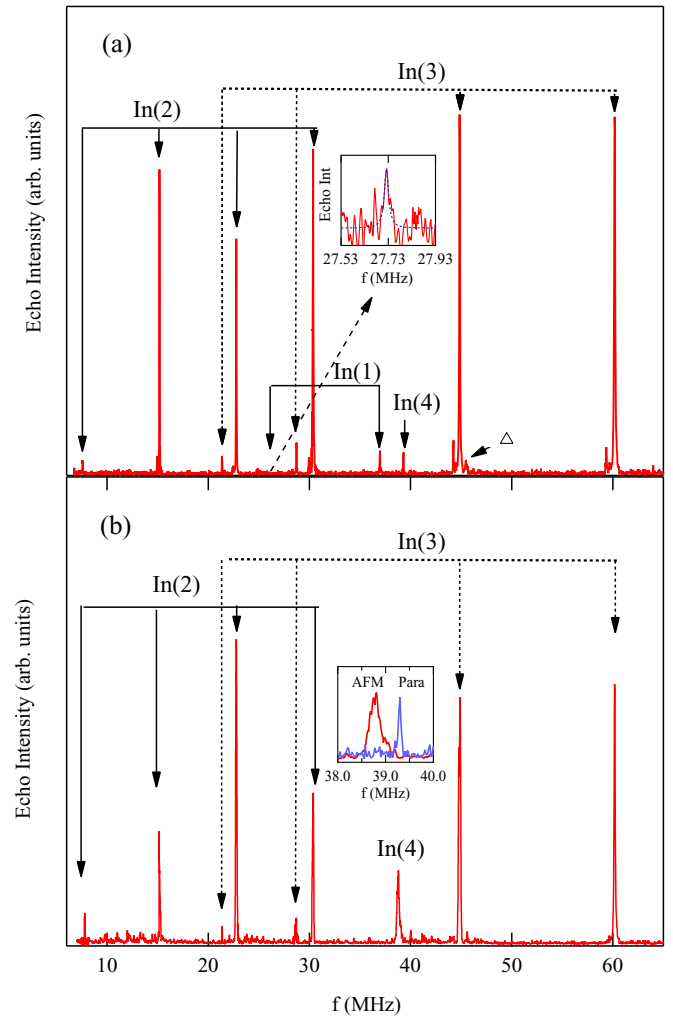


FIG. 2. (a)  $^{115}\text{In}$  NQR spectra in the paramagnetic state (3.1 K) under zero field. Since the  $f_3 = 3\nu_Q = 27.73$  MHz peak of the In(1) site is very weak (the intensity is ten times smaller than that of  $f_4 = 4\nu_Q = 36.97$  MHz), it is presented separately as an inset. The  $\Delta$  peak is due to an impurity. (b)  $^{115}\text{In}$  NQR spectra in the AFM ordered state (1.5 K) under zero field. The spectra of In(1) disappear and the spectrum of In(4) is broadened and shifted from 39.3 to 38.7 MHz. (Inset: The intensities are normalized, since they cannot be compared to each other precisely.) Although there seem to be some additional peaks (e.g., around 10 MHz), these were confirmed to be noise in longer acquisition time measurements.

long  $T_1$  ( $\sim 1$  s). It may be from an unknown, nonmetallic phase outside of the sample. We derived  $\nu_Q$  and  $\eta$  values for In(3) using the exact diagonalization of  $\mathcal{H}_{\text{NQR}}$  for the  $I = 9/2$  case.

We identify the peak at 36.97 MHz as  $f_4$  for the In(1) site for the following reasons. Accounting for  $\eta = 0$  at the In(1) site, the  $f_1$ ,  $f_2$ , and  $f_3$  transitions should thus appear at 9.24, 18.48, and 27.73 MHz. Unfortunately, the first two were not detected owing to their short  $T_2$  and small  $N$  (see Table I), while the  $f_3$  peak at 27.73 Hz stands only marginally out of the background [see the inset in Fig. 2(a)].

The remaining unassigned peak at 39.3 MHz should therefore correspond to the In(4) site. The absence of a signal at  $\frac{3}{4} \times 39.3 = 29.48$  MHz (if 39.3 MHz were  $f_4 = 4\nu_Q$

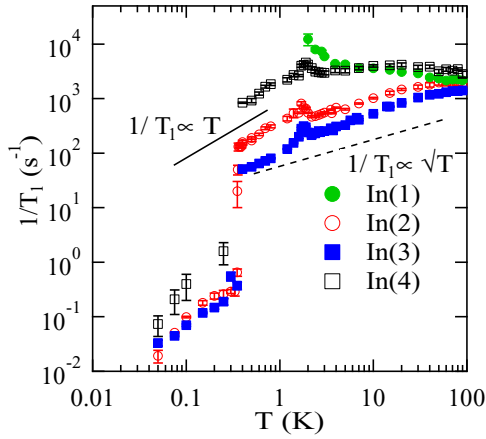


FIG. 3.  $T$  dependence of  $1/T_1$  at the In(1–4) sites. There are no data for the In(1) site below  $T_N$ , since the signal disappears. Solid and dashed lines correspond to the Korringa ( $1/T_1 \propto T$ ) and quantum critical AFM fluctuation ( $1/T_1 \propto \sqrt{T}$ ) cases, respectively.

with  $\eta = 0$ ) and  $\frac{4}{3} \times 39.3 = 52.4$  MHz (if 39.3 MHz were  $f_3 = 3\nu_Q$  with  $\eta = 0$ ) in measurements employing a large acquisition time compels us to conclude that  $\eta \neq 0$  for this site. However, we cannot state unambiguously whether the frequency corresponds to  $f_3$  or  $f_4$ . Factoring in an expected small value of  $\eta \sim 0.009$  causes the trend in frequency to shift between calculated and experimentally determined values (Table I); thus, the latter case most likely gives  $\nu_Q \approx 9.8$  MHz.

To further understand the spectra, we note that each In site has a unique spin-lattice relaxation rate  $1/T_1$  (Fig. 3). The foregoing assigned  $f_n$  peaks ( $n = 1-4$ ) yielding the same  $T_1$  are thus inherently linked to the same site.

Figure 2(b) displays the spectra in the AFM ordered state below  $T_N$ . The change of spectra at  $T_{1n}$  was too small to be detected in the present measurement. Remarkably, the spectra of In(2) and In(3) remain very nearly unchanged. In the case of CeIn<sub>3</sub>, upon entering the AFM state, a significant change is observed. Reflecting the appearance of internal fields, the  $f_1$  spectrum splits and the other transitions shift to lower frequencies. In addition, these spectra become broader [13]. Similar results are reported for CeRhIn<sub>5</sub> [14], where the spectrum of the In(1) site separates into two resonances, while the spectrum of the In(2) takes a more complicated form owing to incommensurate helical magnetic ordering [15]. The change is more dramatic for Ce<sub>2</sub>RhIn<sub>8</sub>. Not only do the spectra of the In sites broaden for  $T < T_N$ , but the spectra nearly disappear [16]. The absence of such changes for Ce<sub>3</sub>PtIn<sub>11</sub> suggests that no internal field appears in the AFM ordered state at

TABLE I.  $\nu_{Q,\text{calc}}$  and  $\eta_{\text{calc}}$  are calculated based on LDA band calculations [10].  $\nu_Q$  and  $\eta$  are obtained experimentally at 3.1 K.  $N$  is the number of atoms in the unit cell.

	$\nu_{Q,\text{calc}}$ (MHz)	$\eta_{\text{calc}}$	$\nu_Q$ (MHz)	$\eta$	$N$
In(1)	11	0	9.24	0	1
In(2)	9.6	0	7.58	0	2
In(3)	17.3	0.077	15.1	0.237	4
In(4)	11.5	0.0089	$\sim 9.8$	$\neq 0$	4

the In(2) and In(3) sites, which are located around the Ce(1) site in this system. We do observe a small shift and a clear broadening of the  $f_4$  spectrum of the In(4) site around 39 MHz [see also the inset in Fig. 2(b)], confirming that this site is exposed to an internal field. Furthermore, the spectrum of the In(1) site vanishes, indicating that a large and/or distributed internal field appears at this particular site. We note that internal fields at In sites are induced through the transferred hyperfine coupling between the Ce 4*f* electron and the In nuclear spin, which is roughly proportional to  $1/r^3$ , where  $r$  is the distance between the Ce and In sites. These observations therefore strongly point to an ordered moment only at the Ce(2) site, corroborating the perception of a magnetic Ce(2) sublattice on the one hand, and coexisting on the other hand with a superconducting Ce(1) sublattice to be realized in Ce<sub>3</sub>PtIn<sub>11</sub>. This was pointed out in the Introduction, although the presence of a tiny moment at the Ce(1) site cannot be explicitly excluded from the data.

In the following argument we make use of the fact that an internal field parallel to the quantization axis will have a much stronger effect on NQR frequencies than does a field perpendicular to the latter axis. Thus, the observed changes in NQR frequencies for In(1) and In(4) sites in the AFM state indicate that the internal field from AFM ordering has to lie parallel and perpendicular to the quantization axis for the In(1) and In(4) sites, respectively. Referring to Fig. 1, the internal field axis then lies along the [001] axis for In(1) and in the [100] plane at right angles to the quantization axis for In(4). We note two circumstances for the AFM propagation vector where these conditions would occur. First, if the magnetic wave vector is  $\mathbf{q} = (0, 0, \frac{1}{2})$  with the ordered moment at the Ce(2) site  $M_{\text{or}} \parallel [001]$  axis, or second, an incommensurate case where  $\mathbf{q} = (\frac{1}{2}, \frac{1}{2}, h)$ , and where  $M_{\text{or}}$  has a large component along the [001] axis that is tilted to cause modulation of the hyperfine field. Noting that  $\mathbf{q} = (\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$  in CeIn<sub>3</sub> [17],  $\mathbf{q} = (\frac{1}{2}, \frac{1}{2}, 0.297)$  under ambient pressure in CeRhIn<sub>5</sub> [18],  $\mathbf{q} = (\frac{1}{2}, \frac{1}{2}, 0)$  in Ce<sub>2</sub>RhIn<sub>8</sub> [19], and  $\mathbf{q} = (\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$  in CePt<sub>2</sub>In<sub>7</sub> [20,21], the second possibility most likely holds for Ce<sub>3</sub>PtIn<sub>11</sub>. Neutron diffraction measurements are strongly motivated here for a more precise determination of the ordered AFM structure.

The NQR spectra in the SC state are almost identical with Fig. 2(b) (thus not shown), confirming that the internal fields resulting from magnetic ordering are still present below  $T_c$ . The latter results prove the coexistence of magnetism and superconductivity in Ce<sub>3</sub>PtIn<sub>11</sub>.

Further insights into the magnetic and superconducting properties were obtained by measuring  $T_1$  as a function of temperature. A conventional inversion-recovery pulse technique was employed. Values of  $T_1$  were obtained at the  $f_4$  transition using fits to an appropriate relaxation function for spin  $I = 9/2$  [ $\eta = 0$  and 0.237 cases for In(1,2) and In(3) sites, respectively]. For the In(4) site we evaluated the data approximately using the relaxation function for  $\eta = 0$ .

Figure 3 displays the  $T$  dependence of  $1/T_1$  at the In(1–4) sites. The AFM and SC transitions are clearly observed at the In(2,3,4) sites, confirming that antiferromagnetism and superconductivity coexist microscopically in Ce<sub>3</sub>PtIn<sub>11</sub>. The anomaly in  $1/T_1$  at  $T_{1n}$  is quite small compared with that at

$T_N$ . Above  $T_N = 2$  K, the relaxation rate of In(2) and In(3) resembles the typical behavior of HF compounds [22,23]. At higher temperatures,  $1/T_1$  is nearly temperature independent, indicating that the  $4f$  electrons of Ce(1) ions are localized, in line with the observed Curie-Weiss behavior of the magnetization [1]. Upon lowering the temperature below  $T^* \sim 30$  K,  $1/T_1$  decreases, signaling the crossover into a coherent Kondo regime. In this intermediate temperature range ( $T_N < T < T^*$ ) the relaxation rate varies nearly as  $\sqrt{T}$ .

In contrast,  $T_1$  for the In(1) and In(4) sites shows a weak  $T$  dependence, reminiscent of the  $^{115}\text{In}$ - $T_1$  behavior observed in the case of  $4f$ -localized CeIn<sub>3</sub> [13]. Upon lowering temperature, the In(1) site displays a rapid increase in  $1/T_1$  at  $T \sim 3$  K. Since the spin-lattice relaxation is induced by magnetic fluctuations perpendicular to the quantization axis, this enhancement gives evidence for the emergence of strong magnetic fluctuations in the Ce(2) basal plane. The temperature of this effect matches well with the maximum in the susceptibility, which has been attributed to the presence of two-dimensional (2D) short-range AFM correlations [1].

Below  $T_N$ ,  $1/T_1$  becomes nearly proportional to  $T$ , i.e.,  $1/T_1 T$  is constant at the In(2,4) site, whereas the  $1/T_1 \sim \sqrt{T}$  behavior persists at the In(3) site. The Korringa-type  $T$  dependence indicates that nonquantum critical heavy quasiparticles remain in the AFM ordered state above  $T_c$ , which is consistent with large  $C/T$  values at low temperature [1,24].

The entrance into the superconducting condensate is marked by a sudden drop of the spin relaxation rate at the In(2,3,4) sites, much as in CePt<sub>2</sub>In<sub>7</sub> as well [25]. While the absence of a Hebel-Slichter coherence peak just below  $T_c$  already points to a non- $s$  wave, unconventional type of superconducting state, the sharp decrease is rather unusual. Below  $T_c$ ,  $1/T_1$  does not follow the particular power-law behavior expected for a nodal gap state; rather, the jump implies a first-order-like transition. The physical origin of the sudden decrease of spin relaxation rate below  $T_c$  remains elusive [25]. The Korringa-type behavior reappears below 0.3 K. We do believe that this finite density of states is not due to impurities, but rather is indicative of a gapless nature for the low-lying excitation spectrum in the coexistence of SC and AFM states in analogy to CeRhIn<sub>5</sub> [26].

In the following, we discuss the implications of  $T_1$  measurements above  $T_c$ . A  $\sqrt{T}$  behavior has been found in the normal state of CeRhIn<sub>5</sub> [27], Ce<sub>2</sub>RhIn<sub>8</sub> [15,16], Ce<sub>2</sub>PdIn<sub>8</sub> [22], and, for instance, in the noncentrosymmetric HF superconductor CeIrSi<sub>3</sub> [28] when being tuned towards a QCP. It is associated with critical spin fluctuations as corroborated by the isotropic spin fluctuation model, which in such a case predicts the relation  $1/T_1 \propto T \sqrt{\chi_q(T)} \propto \sqrt{T}$ , where  $\chi_q(T)$  represents the staggered susceptibility [29]. This observation thus strongly points to a close proximity to a QCP. The

accompanying spin fluctuations are largely confined to the Ce(1)<sub>2</sub>PtIn<sub>8</sub> layer (Fig. 1) as affirmed by the  $1/T_1 \propto \sqrt{T}$  behavior of In(3). This site is encapsulated in the Ce(1)<sub>2</sub>PtIn<sub>8</sub> layer and is farthest from the magnetic Ce(2)In<sub>3</sub> layer. The change of a  $\sqrt{T}$  dependence to a Korringa-type behavior below  $T_N$  of  $1/T_1$  for In(2) would therefore suggest that magnetic order suppresses these fluctuations.

The accumulated data are compatible with a scenario delineated in the Introduction: The Ce(2) ion located in the CeIn<sub>3</sub> layer maintains its  $4f$ -magnetic moment because of insufficient Kondo screening. The Ce(2) ions become magnetically coupled via a Ruderman-Kittel-Kasuya-Yosida (RKKY) interaction through the adjacent Ce(1)<sub>2</sub>PtIn<sub>8</sub> layer establishing long-range AFM ordering at 2 K. The ordering persists in the superconducting state as inferred from the In(4) spectra. The previously reported QCP at  $p_c = 1.3$  GPa thus is inherent to the Ce(2) sublattice [1]. In contrast, the Ce(1) ion is on the verge of magnetic ordering but the enhanced local on-site Kondo interaction just balances out the RKKY interaction. Thus the QCP of the Ce(1)<sub>2</sub>PtIn<sub>8</sub> layer [Ce(1) sublattice] is located exactly at  $p = 0$  or at slight negative pressure axis in the  $p$ - $T$  phase diagram. Moreover, the close vicinity to a QCP strongly supports the view that Ce(1)<sub>2</sub>PtIn<sub>8</sub> layer is primarily responsible for superconductivity.

Unlike recent experiments on hybrid heterostructures of CeIn<sub>3</sub>/CeCoIn<sub>5</sub> and CeRhIn<sub>5</sub>/CeCoIn<sub>5</sub> superlattices [30,31] where each block layer is several nm thick consisting of multiple unit cells of the respective material, Ce<sub>3</sub>PtIn<sub>11</sub> can be at best regarded as a stacking of perfectly matching monolayers or an infinite repetition of CeIn<sub>3</sub>/Ce<sub>2</sub>PtIn<sub>8</sub> interfaces. As such it is unlikely superconductivity would just be confined to the Ce(1)<sub>2</sub>PtIn<sub>8</sub> layer, which is further supported by the rather isotropic behavior of  $H_{c2}$  [32], in contrast to results on CeRhIn<sub>5</sub>/CeCoIn<sub>5</sub> superlattices [31]. However, the role of the Ce(2)In<sub>3</sub> layer in the SC properties is yet unclear. A spatial separation of superconductivity and magnetism could be linked to the two Ce sites, i.e., two different QCPs, which is an important issue to be addressed in future work on this system.

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