Optical injection of spin current into a zigzag nanoribbon of monolayer MoS₂ with **antiferromagnetic Kekule distortion**

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The Kekule pattern of the (anti)ferromagnetic exchange field on monolayer $MoS₂$ can be induced by proximity to the (111) surface of BiFeO₃ on both sides. The three-band tight binding model of the MoS₂ layer with Kekule patterned exchange field is applied to describe the heterostructures. The tight binding model is justified by the first principle calculations. The magnetization orientations of the substrates control the pattern of the exchange field, which then switches the band structures of the lowest zigzag edge states between being metallic and insulating. The lowest four zigzag edge bands provide conducting channels with a spin-polarized current. Optical excitation of carriers in these bands generates sizable spin and charge currents, which are theoretically modeled by the perturbation solution of the semiconductor Bloch equation. The injected spin currents have multiple resonant peaks at a few frequencies, which can be switched off by rotating the magnetization orientations of the substrates.

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I. INTRODUCTION

Transition metal dichalcogenides (TMDs) are exotic twodimensional materials with large spin-orbit coupling (SOC) that afterwards exhibit valleytronic and spintronic physics [\[1,2\]](#page-6-0). Optical excitation of valley-polarized excitons [\[3\]](#page-6-0) has been realized in experiments [\[4–9\]](#page-6-0) and proposed for use in valleytronic devices [\[10,11\]](#page-6-0). Optical injection of a spin current into monolayer TMDs has been studied and proposed for use in spintronic devices [\[12,13\]](#page-6-0). Because the band gaps of TMDs vary between 1 eV and 1.5 eV $[14,15]$, the optospintronics of TMDs in the bulk is restricted to the optical frequencies within the near-infrared and visible light range. Proximity to a ferromagnetic substrate induces a spatially uniform ferromagnetic exchange field on the TMD layer, which in turn induces valley splitting [\[16\]](#page-6-0). Because the inversion symmetry is broken, Rashba SOC is induced. As a result, spin mixing and canted spins are generated in the bulk and zigzag edge states. Recently, a theoretical study has suggested that the zigzag edges of TMDs carry a localized spin current with canting of the spin orientation [\[16\]](#page-6-0). Similar types of localized spin current at the edge of nanostructures with Rashba SOC have been predicted [\[17–20\]](#page-6-0). These systems host a spatially localized spin current as an information carrier, affording promising candidates for spintronic applications. The scheme for optical excitation of a localized spin current at the edge or topological interface of nanostructures makes integrated optospintronic devices feasible [\[21\]](#page-6-0). For the zigzag nanoribbons of TMDs, optical excitation of carriers requires a small optical frequency, which could be around 0.1 eV. As a

result, these nanostructures open the door for optospintronics with a far-infrared optical field as an excitation source.

The exchange field in TMD layers is critical for the property of a localized spin current. Replacing the ferromagnetic substrate by an antiferromagnetic substrate could also induce an exchange field in the TMD layer. Additionally, antiferromagnetic materials have multiple advantages over ferromagnetic materials for spintronic applications, such as the absence of parasitic stray fields and ultrafast magnetization dynamics [\[22–25\]](#page-6-0). Proximity of TMDs to the antiferromagnet MnO induces a uniform exchange field [\[26\]](#page-6-0) due to the lattice matching between the Mo or W atoms in the TMD layer and the Mn atoms on the (111) surface of MnO.

Kekule distortion has been studied in graphene heterostructures. Because of the outstanding physical characteristics of graphene [\[27\]](#page-6-0), multiple schemes of graphene-based spintronic physics have been studied, such as optical injection of spin and valley currents [\[28–32\]](#page-6-0) and robust spin currents into topological phases [\[33–35\]](#page-6-0). The Kekule distortion in graphene can be induced by proximity to a substrate with the same lattice structure but with a lattice constant $\sqrt{3}$ times that of graphene $[36-40]$. One example is graphene on In_2Te_2 [\[39\]](#page-6-0). A $\sqrt{3} \times \sqrt{3}$ supercell of graphene is conformal with the primitive unit cell of the substrate. The band folding in the supercell brings the K and K' valleys to the Γ point in the Brillouin zone. The Kekule distortion mixes the quantum states of the two valleys, which could open a bulk gap.

In this article, the proximity effect of TMDs on the (111) surface of BiFeO₃, which induces a nonuniform exchange field with the Kekule pattern, is studied. The effect changes the physical properties of the localized spin current at the zigzag edge. We consider the Kekule distortion of monolayer MoS₂, which is induced by intercalating MoS₂ between two substrates with a (111) surface of BiFeO₃,

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i.e., the $BiFeO₃/MoS₂/BiFeO₃$ heterostructure. Experimental fabrication of the monolayer $MoS₂/BiFeO₃$ heterostruc-ture is feasible [\[41\]](#page-6-0). At room temperature, BiFeO₃ is Gtype antiferromagnetic, so all Fe atoms at the same (111) plane have the same magnetization orientation [\[42–45\]](#page-6-0). The Fe atoms on the (111) surface arrange in a triangular lattice with a lattice constant of 5.50 Å $[42,43]$, which is only a 0.46% mismatch with $\sqrt{3}$ times the lattice constant of MoS₂, which is $a_0 = 3.19$ Å [\[46,47\]](#page-7-0). This article focuses on the Y-Kekule distortion. In one unit cell, the Fe atom on the surface of one substrate is on top of one of the three Mo atoms; the Fe atom on the surface of the other substrate is on top of a different Mo atom. The magnetic moments of the Fe atoms induce larger and smaller exchange fields at the nearest and next nearest Mo atoms, respectively. By rotating the magnetization orientation of the two substrates, the exchange fields of the three Mo atoms can be changed, in turn controlling the band structure of the zigzag edge states. With the appropriate Kekule pattern of the exchange field and energy level, the forward and backward moving zigzag edge modes have opposite spins. Optical excitation of carriers to these modes generates a sizable spin current, which is localized at the Mo-terminated zigzag edge.

This article is organized as follows. In Sec. II, the atomic structure of the $BiFeO₃/MoS₂/BiFeO₃$ heterostructure is described and the effective tight-binding Hamiltonian is de-scribed. In Sec. [III,](#page-3-0) the band structures and spin texture of zigzag nanoribbons are discussed. In Sec. [IV,](#page-4-0) optical injection of a spin current is calculated and discussed. In Sec. [V,](#page-5-0) the conclusion is given.

II. ATOMIC STRUCTURE AND TIGHT-BINDING MODEL

The lattice structure of the $BiFeO₃/MoS₂/BiFeO₃$ heterostructure with the Y-Kekule configuration is plotted in Fig. $1(a)$, which only indicates the lattice sites of Mo and S atoms. The primitive unit vectors of the bulk are $\mathbf{a}_{1(2)} =$ $rac{3\sqrt{3}}{2}a_0\hat{x} \pm \frac{3}{2}a_0\hat{y}$, which define the primitive unit cell of the bulk. The primitive unit cell includes three Mo atomic lattice sites with different magnetic exchange fields, which are indicated as different shapes of the lattice points in Fig. 1(a). We consider zigzag nanoribbons with translational invariance along the \hat{x} direction. The rectangular unit cell is defined by the vectors $\mathbf{a}_1 + \mathbf{a}_2$ and $-\mathbf{a}_1 + \mathbf{a}_2$ and contains two primitive unit cells. The unit cell of the zigzag nanoribbon consists of N_{zis} rectangular unit cells along the width direction, i.e., the *y*ˆ direction. The atomic structure within one rectangular unit cell of the $BiFeO₃/MoS₂/BiFeO₃$ heterostructure is plotted in Fig. 1(b). For better visualization, only two Fe layers in each $BiFeO₃$ substrate are plotted. Each Fe atom on the surface is on top of a Mo atom, which are connected by the dashed line in Fig. $1(b)$. The magnetic moment at the Fe atoms induces a magnetic exchange field at the Mo atoms. The strength of the exchange field depends on the distance between the Fe and Mo atoms. Thus the exchange field at the Mo atoms on top of an Fe atom is larger than the exchange field at the other Mo atoms that are not on top of an Fe atom. We assume that the Fe atoms of the bottom (top) $BiFeO₃$ substrate are on top of the Mo atomic lattice sites plotted as upward-pointing (downward-pointing) triangles in Fig. $1(a)$. Thus the bottom

FIG. 1. (a) Lattice configuration of a $MoS₂$ monolayer with antiferromagnetic Kekule distortion. The yellow dots represent the S_2 sites. The blue circular dots, upward-pointing triangles, and downward-pointing triangles represent the Mo sites with different magnetic exchange fields. The dashed line indicates the primitive unit cell. The dotted lines indicate the rectangular unit cells. (b) Three-dimensional atomic structure of the $BiFeO₃/MoS₂/BiFeO₃ heterostructure within one rectangular unit$ cell. The dashed and dotted lines connect the nearest and next nearest Fe and Mo atoms, respectively. The arrows at the Fe atoms represent the local magnetic moment.

(top) BiFeO₃ substrate induces exchange field $M_B (M_T)$ at the upward-pointing (downward-pointing) triangle lattice sites and $\lambda \mathbf{M}_{B}$ ($\lambda \mathbf{M}_{T}$) at the other lattice sites. The parameter λ characterizes the degree of nonuniformity of the exchange field induced by each substrate. If the substrate induces a nearly uniform exchange field, λ is nearly one; in contrast, if the substrate induces a highly nonuniform exchange field, λ is nearly zero. Combining the exchange fields from both substrates, the exchange field at the lattice sites plotted as upward-pointing triangles, downward-pointing triangles, and circular dots are $M_{\Delta} = M_B + \lambda M_T$, $M_{\nabla} = \lambda M_B + M_T$, and $M_{\odot} = \lambda M_B + \lambda M_T$, respectively. The strengths of the exchange fields from the top and bottom substrates are the same, which are designated as $B_0 = |\mathbf{M}_B| = |\mathbf{M}_T|$.

The heterostructure is modeled by the tight-binding Hamiltonian $H = H_{M_0S_2} + H_{ex} + H_R$. The Hamiltonian of monolayer $MoS₂$ is given by the three-band tight-
binding model with the three d orbital basis binding model with the three *d* orbital basis $\{|d_{z^2}, s\rangle, |d_{xy}, s\rangle, |d_{x^2-y^2}, s\rangle\}$ and spin index $s = \pm 1$. The Hamiltonian of the Rashba SOC H_R is given by the intrasite inter- $\{|d_{xy}, s\rangle, |d_{x^2-y^2}, s\rangle\}$ -orbital mixing matrix for each lattice site. The Rashba coupling strength is assumed to be $\lambda_R = 76$ meV. The detailed form of the Hamiltonians H_{MoS_2} and H_R can be found in Refs. [\[14\]](#page-6-0) and [\[16\]](#page-6-0), respectively. The Hamiltonian of the exchange field is given as $H_{\text{ex}} = \sum_{j} M_{cvv} \otimes (\mathbf{M}_j \cdot \sigma)$, with the summation covering all lattice sites, $M_{cvv} = \text{diag}\{1, 0.8252, 0.8252\}$, $\sigma = \hat{x}\sigma_x + \hat{y}\sigma_y + \hat{z}\sigma_z$, and $\sigma_{x,y,z}$ being the Pauli matrix of spin. The diagonal matrix elements of M_{cvv} are the magnetic coupling coefficient to the conduction and valence bands.

To justify the tight-binding model with the Kekule pattern of the exchange field, we performed density functional theory (DFT) calculations based on the projector augmented wave method as implemented in the Vienna ab initio simulation package (VASP) [\[48,49\]](#page-7-0). The generalized gradient approximation exchange-correlation functional [\[50\]](#page-7-0) was used. The SOC was neglected. The spin polarizations were collinear. The Hubbard U was chosen to be 4 eV for the *d* orbital of the Fe atoms. The lattice constant of the $BiFeO₃/MoS₂/BiFeO₃$ heterostructure was chosen to be 5.50 Å, which corresponds to the lattice constant of $a_0 = 3.175$ Å for the MoS₂ monolayer. The kinetic energy cutoff was set to 550 eV. Each BiFe O_3 substrate contains six layers of Fe atoms along the (111) direction. The Fe atoms in adjacent layers have opposite spin polarizations. The Fe atoms in proximity to the top and bottom surfaces of the $MoS₂$ monolayer have the same spin polarizations, corresponding to the tight-binding model with $M_T = M_B$. The Bi atoms at the open boundaries are passivated by hydrogen atoms. The heterostructures with both the Y-Kekule and O-Kekule configurations were calculated. The initial atomic structure of the O-Kekule configuration was obtained from that of the Y-Kekule configuration by shifting the atoms in the MoS₂ monolayer along the $+\hat{y}$ direction by 1.833 Å while fixing the atoms in the $BiFeO₃$ substrates. After structural relaxations in which the forces converged to less than 0.01 eV/Å, the interlayer distances between the $MoS₂$ monolayer and the Fe (111) surface were found to be 3.89 Å and 4.1 Å for the Y-Kekule and O-Kekule configurations, respectively.

The band structures of the heterostructures in the bulk with both types of Kekule configuration were calculated. The band structures of the Y-Kekule configuration are plotted in Figs. 2(a)–2(d) within the energy range of $[-2, 2]$ eV. At this energy scale, the band structures of the two Kekule configurations are nearly the same. Because the heterostructure contains a $\sqrt{3} \times \sqrt{3}$ supercell of the MoS₂ monolayer, the conduction band minima of pristine $MoS₂$ monolayer at the *K* and K' points are folded into the Γ point. Although the band gap of the heterostructure is 0.09 eV, the band gap of the localized band structure that is the projection to the $MoS₂$ monolayer is 1.67 eV, as shown in Figs. $2(a)$ and $2(b)$. Most of the quantum states in the $MoS₂$ monolayer are projected into the three *d* orbitals $(d_{z^2}, d_{xy}, d_{x^2-y^2})$, as shown in Fig. 2(a). The projections to the Fe (Bi, O, H) atoms are mainly distributed in the conduction band (valence band) above 1.8 eV (below 0 eV), as shown in Figs. $2(c)$ and $2(d)$, which have

FIG. 2. Orbital projected band structures for the $BiFeO₃/MoS₂/BiFeO₃$ heterostructure with the Y-Kekule configuration obtained from DFT calculations are plotted in (a)–(d). The Fermi energy is set to zero. The symbol size is proportional to its projection in the corresponding state. (a) Contribution from the three Mo *d* orbitals $(d_{z^2}, d_{xy}, d_{x^2-y^2})$. (b) Contribution from the other orbitals of $MoS₂$. (c) Contribution from Fe atoms. In (a)–(c), spin up and down states are plotted as solid (blue) and empty (red) dots, respectively. (d) Contribution from (Bi, O, H) atoms, with both spins being plotted as empty (magenta) squares. The band structures are zoomed in on around the Γ point for the Y-Kekule and O-Kekule configurations in (e) and (f), respectively. Only contributions from the three Mo *d* orbitals and (Bi, O, H) atoms are included in (e) and (f). The solid (blue) and dashed (red) lines in (e) and (f) are fittings of the spin up and down band structures by the tight-binding model, respectively.

small mixing with the conduction band minima of the $MoS₂$ monolayer. The projections to the (Bi, O) atoms have large weights in two bands above the Fermi energy, whose energy range overlaps with the conduction band minima of the $MoS₂$ monolayer, as shown in Fig. $2(d)$. By zooming in on the band structure near to the Γ point, as shown in Fig. 2(e), the projections to the $MoS₂$ monolayer and the (Bi, O) atoms are completely separated into two groups of bands. Because the groups of (Bi, O) atoms and the $MoS₂$ monolayer are spatially separated by the Fe atoms on the surface of the substrates, the quantum states in the $MoS₂$ monolayer and the (Bi, O) atoms are weakly mixed. As a result, the conduction band minima of the $MoS₂$ monolayer can be well described by the three-orbital tight-binding model, which neglects the mixing with the $BiFeO₃$ substrate. A recent experimental study of the $MoS₂$ bilayer showed that the quantum states in the conduction band minima are localized within each layer with the absence of interlayer tunneling [\[51\]](#page-7-0). Thus neglecting the orbital mixing between $MoS₂$ and $BiFeO₃$ in the $BiFeO₃/MoS₂/BiFeO₃$ heterostructure is reasonable.

The conduction band minima is fitted by the tight-binding model with a nonuniform exchange field, i.e., $B_0 = 4.3$ meV and $\lambda = 0.25$, and without SOC, as shown in Fig. [2\(e\).](#page-2-0) The fitting is qualitatively correct because the two conduction band minima for each spin are not degenerate. By contrast, for the heterostructure in the O-Kekule configuration, the conduction band minima are fitted by the tight-binding model with a uniform exchange field, i.e., $B_0 = 2$ meV and $\lambda = 1$, as shown in Fig. $2(f)$, as the two conduction band minima for each spin are degenerate. To demonstrate the qualitative features of the model, we assume stronger exchange coupling by using the parameters of $B_0 = 125$ meV and $\lambda = 0.25$ in the remainder of this article.

III. BAND STRUCTURE OF ZIGZAG NANORIBBONS

We consider zigzag nanoribbons with the width of five rectangular unit cells, i.e., $N_{\text{zig}} = 5$. The band structure of the zigzag nanoribbon can be obtained by diagonalization of the tight-binding Hamiltonian with a Bloch periodic boundary along the zigzag direction. In addition to the bulk states, edge states with energy within the bulk gap are found. For the pristine $MoS₂$ zigzag nanoribbon, the unit cell is three times smaller than that in Fig. $1(a)$ along the zigzag direction; the band structures of the edge states are connected to the conduction bands and have a finite gap with the valence bands $[14]$. By choosing the unit cell in Fig. $1(a)$, the two band valleys at the K and K' points are folded into the Γ point, i.e., $k_x = 0$. In the presence of the Kekule pattern of the magnetic exchange field, the two band valleys are coupled, which modifies the band structure of the bulk and edge states. The band structures of the edge states are shown in Fig. 3. Because the edge states are highly localized within two unit cells beyond each zigzag edge, the edge states of the two terminations hardly overlap. Thus the band structure of a zigzag edge with a larger width is nearly the same. If the magnetization orientation of the bottom substrate is fixed, then rotation of the magnetization orientation of the top substrate between parallel and antiparallel relative to that of the bottom substrate changes the band structures. For the edge states localized on the Mo-edge termination, the first edge band is gapped from the second edge band for parallel magnetization $[M_B = M_T$, as shown in Figs. 3(d) and 3(g)], and is connected to the second edge band for antiparallel magnetization $[M_B = -M_T$, as shown in Figs. 3(f) and 3(i)]. Similar features are found between the second and third edge bands. For the neutral system, the Fermi level fills up to the lowest six edge bands. With hole doping of $5/(36N_{\text{zig}})$ $[4/(36N_{\text{zig}})]$ in MoS₂, the Fermi level is between the first and second (second and third) edge bands. Thus the nanoribbon is switched between insulating and metallic by the rotation of the magnetization orientation, which can function as a spin valve [\[52,53\]](#page-7-0). For the edge states localized on the *S*-edge termination, the gap between the lower and higher two bands is also switched on and off by the rotation of the magnetization orientation. However, if the Fermi level is within this gap, then the Mo-edge termination edge state are always conducting, so the system cannot function as a spin valve. The spin valve function is due to the Kekule pattern of the exchange field. If

FIG. 3. Band structure of a zigzag nanoribbon with a width of FIG. 5. Band structure or a zigzag nanoriboon with a width of $5\sqrt{3}a_0$. The edge states localized on the Mo- and S-edge terminations are plotted as solid (blue) and dashed (red) lines, respectively. The orientations of the magnetizations in the substrates are (a),(d) $M_B =$ $M_T = B_0 \hat{z}$, (b),(e) $M_B = B_0 \hat{z}$ and $M_T = B_0 \hat{x}$, (c),(f) $M_B = -M_T =$ *B*₀ \hat{z} , (g) **M***B* = **M**_{*T*} = *B*₀ \hat{y} , (h) **M***B* = *B*₀ \hat{y} and **M***T* = *B*₀ \hat{x} , and (i) $M_B = -M_T = B_0 \hat{y}$. In (d)–(i), the possible band gaps above the first or second edge bands are indicated by the gray area.

the exchange field is uniform (i.e., $\lambda = 1$), the gaps in Fig. 3 do not appear for any combination of M_B and M_T .

Because of the Rashba SOC and the Kekule pattern of the exchange field, the edge state can support a one-way spin current. We focus on the system with a magnetization orientation of the substrates of $M_B = -M_T = B_0 \hat{z}$ [the system in Fig. $3(c)$]. The charge and spin currents are characterized by the velocity and spin-velocity operators, which are defined as $\hat{v}_x = (1/\hbar)\partial H/\partial k_x$ and $\hat{s}_{x,k} = \frac{1}{2}(\hat{v}_x \sigma_k + \sigma_k \hat{v}_x)$, respectively, where k_x is the wave vector along the zigzag nanoribbon and $\kappa = x, y, z$. The band structures exhibiting the expectation values of the velocity and spin-velocity operators in color scales are plotted in Fig. [4.](#page-4-0) The band structure is symmetric under $k_x \Leftrightarrow -k_x$. The velocity of the edge states is proportional to the slope of the band structures. Within the energy ranges marked by the gray area in Figs. $4(b) - 4(d)$, only two edge states with opposite velocities occur at each energy level. The features of four typical states within these energy ranges are plotted in Figs. $4(e)$ –4(h). The probability densities of the states are highly localized at the Mo-edge termination. For the two edge states in Figs. $4(e)$ and $4(f)$, the expectation values of spin-*x* (spin-*y*, spin-*z*) are the same as (opposite to) each other, so the expectation values of the spin-velocity operator are opposite to (the same as) each other. For the spin-*y* and spin-*z* components, this property can be designated as a oneway spin-velocity texture. For the other two edge states in Figs. $4(g)$ and $4(h)$, a similar property with larger expectation values of the velocity operator appears, which in turn generates a larger spin current. In the absence of the Rashba SOC or the Kekule pattern of the exchange field, these energy

FIG. 4. Band structure of the zigzag nanoribbon with a width of $5\sqrt{3}a_0$ and a magnetization orientation of the substrates of $M_B = -M_T$ $B_0\hat{z}$ [the same as that in Fig. [3\(c\)\]](#page-3-0). In (a), the bulk states are plotted as thin black lines; the edge states of the Mo- and S-edge terminations are plotted as thin and thick lines with color. The color scale corresponds to the expectation value of the velocity operator in the unit of nm/fs, i.e., $\langle \hat{v}_x \rangle$. In (b), (c), and (d), the energy range is zoomed in on; the color scale corresponds to the expectation value of the spin-velocity operator in the unit of nm/fs, i.e., $\langle \hat{s}_{x,x} \rangle$, $\langle \hat{s}_{x,y} \rangle$, and $\langle \hat{s}_{x,z} \rangle$, respectively. The physical features for the quantum states marked by a square, diamond, pentagram, or hexagram dot in (b) are plotted in (e), (f), (g), and (h), respectively. Only the three unit cells near the Mo-edge termination are plotted. The probability density at each Mo site is indicated by the size of the marker. The local spin moment at each Mo site, i.e., $\langle \sigma_x \rangle \hat{x} + \langle \sigma_y \rangle \hat{y} + \langle \sigma_z \rangle \hat{z}$, is indicated by the arrows. The velocity $\langle \hat{v}_x \rangle$ is indicated by the horizontal thick arrow in the top view.

ranges vanish. As the strength of the Rashba SOC decreases, the width of these energy ranges decreases. Optical excitation of carriers within these energy ranges could inject a large spin current with *y* and *z* components because the forward and backward traveling electrons carry spin currents with the same sign. In comparison, the spin current with the *x* component would be smaller because the forward and backward traveling electrons carry spin currents with opposite signs. Because the inversion symmetry is absent, the nondiagonal matrix elements of the velocity operator are not symmetric under $k_x \Leftrightarrow -k_x$. Thus optical excitation generates different carrier populations at the forward and backward traveling edge states, then injecting a charge current.

IV. OPTICAL SPIN INJECTION

The optical excitation is modeled by the semiconductor Bloch equation [\[21,](#page-6-0)[54\]](#page-7-0). In the presence of an optical field, the Hamiltonian has an additional interaction term, given as

$$
H_{I} = -\frac{e_0}{m_0 c} \mathbf{A}(t) \cdot \mathbf{P}, \qquad (1)
$$

where e_0 is the electron charge, m_0 is the electron mass, c is the speed of light, and **A** is the vector potential. Under the Coulomb gauge, the electric field is given by $\mathbf{E} = -\frac{1}{c} \frac{\partial \mathbf{A}(t)}{\partial t}$. We consider a continuous-wave harmonic optical field with linear polarization along the \hat{x} direction and a frequency of ω , so $\mathbf{E} = \text{Re}[E_0 e^{-i\omega t}] \hat{\mathbf{x}}$. In a realistic experimental condition, the plane wave of the optical field is approximated by the center part of the Gaussian beam with a beam width of one wavelength in vacuum, so the relation between the power of the Gaussian beam and the amplitude of the electric field is $P_0 = \frac{|E_0|^2 \pi}{4Z_0} (\frac{1240}{\hbar \omega})^2$, with $Z_0 = 376.73\Omega$ being the impedance of free space. We assume $P_0 = 10^{-5}$ W, so E_0 is a function of the optical frequency in our numerical simulation. The momentum operator along the \hat{x} direction is given by the velocity operator as $P_x = m_0 \partial H / \partial P_x = \frac{m_0}{\hbar} \partial H / \partial k_x$. Thus the interaction Hamiltonian is given as

$$
H_{I} = i\frac{e_{0}E_{0}}{\hbar\omega}\frac{\partial H}{\partial k_{x}}e^{-i\omega t} - i\frac{e_{0}E_{0}}{\hbar\omega}\frac{\partial H}{\partial k_{x}}e^{i\omega t}.
$$
 (2)

The time evolution of the density matrix obeys the semiconductor Bloch equation with the relaxation time approximation, given as

$$
i\hbar \frac{\partial \rho(t)}{\partial t} = [\rho(t), H + H_I] - \frac{\hbar}{\tau} [\rho(t) - \rho^{(0)}(t)], \quad (3)
$$

where τ is the relaxation time of the edge states. We assume $\tau = 1$ ps. The perturbation solution can be expanded as $\rho(t) = \rho^{(0)} + \rho^{(1)}(t) + \rho^{(2)}(t) + \cdots$, with $\rho^{(0)}$ being a diagonal matrix whose elements are given by the Fermi-Dirac distribution at temperature *T* . The second-order perturbation solution $\rho^{(2)}(t)$ includes second harmonic terms with timedependent factor $e^{\pm 2i\omega t}$ and zero harmonic terms $\rho_0^{(2)}$ that are independent of time. The injection of direct charge and spin currents is determined by the expectation of the velocity and spin-velocity operators multiplied by the zero harmonic terms

FIG. 5. Optical injection of charge and spin currents into the nanoribbon with a magnetization orientation of the substrates of **M**_{*B*} = −**M**_{*T*} = *B*₀ \hat{z} in (a)–(d) or **M**_{*B*} = **M**_{*T*} = *B*₀ \hat{z} in (e) and (f). The Fermi energy level is E_{F1} in (a),(c),(e) and E_{F2} in (b),(d),(f). The temperature in (a),(b) and (e),(f) is 300 K and that in (c),(d) is 70 K.

 $\rho^{(2)}(t)$, given as

$$
I_c = \frac{e_0}{3N_k a_0} \sum_{k,n,n'} \langle k,n|\hat{v}_x|k,n'\rangle \rho_{0,k,n',n}^{(2)} \tag{4}
$$

and

$$
I_s^{\kappa} = \frac{e_0}{3N_k a_0} \sum_{k,n,n'} \langle k,n|\hat{s}_{x,\kappa}|k,n'\rangle \rho_{0,k,n',n}^{(2)},\tag{5}
$$

where N_k is the number of sampling point of the Bloch wave number k . The definition of the spin currents in Eq. (5) is normalized by a factor (h/e_0) , so that they have the same unit as charge current.

The optical injection of charge and spin currents into the system with a magnetization orientation of the substrates of $M_B = -M_T = B_0 \hat{z}$ [the same as the system in Fig. [3\(c\)](#page-3-0) and Fig. [4\]](#page-4-0) versus the frequency of the optical field is plotted in Figs. $5(a)$ and $5(b)$, with a Fermi energy level of $E_{F1} =$ 0.2188 eV and $E_{F2} = 0.2731$ eV, respectively, and a temperature of 300 K. The charge current is small but nonzero because the excited populations of edge states at k_x and $-k_x$ at the same energy level are different. In most of the optical frequency range, $I_s^{y,z}$ is larger than I_s^x , which confirms the inference in the previous section. The spin currents peak at several resonant frequencies, which is due to the competition between the spin currents generated by the edge states within or outside of the energy ranges with a one-way spin-velocity texture [those in the gray area in Figs. $4(b) - 4(d)$. For example, for the first resonant peak at optical frequency $\hbar \omega = 0.028 \text{ eV}$, the optically excited electrons (holes) are populated around the band crossing above (below) E_{F2} . As the optical frequency decreases, no electron is populated within the energy ranges in the gray area, so the magnitude of the spin currents sharply decreases. As the optical frequency increases, more holes are populated outside the energy ranges in the gray area, which cancel the total spin currents; thus the magnitude of the spin current smoothly decreases. In Fig. $5(a)$, although the energy levels around the band crossing at E_{F2} are above the Fermi level E_{F1} , the equilibrium populations (i.e., diagonal terms of $\rho^{(0)}$) in these energy levels are sizable because of the thermal excitation at room temperature. Thus the optical field can excite electrons and holes at the upper and lower parts of the band crossing, respectively. Therefore, a resonant peak exists. If the Fermi level is raised to E_{F2} , as in Fig. $5(b)$, then the equilibrium population contrast between the upper and lower parts of the band crossing is larger, so the amplitude of the resonant peak becomes larger. For the same systems in Figs. $5(a)$ and $5(b)$, if the temperature is decreased to 70 K, then the injected currents change to those shown in Figs. $5(c)$ and $5(d)$, respectively. For the system in Fig. $5(c)$, the equilibrium population at the band crossing vanishes, as the energy levels around the band crossing are more than $k_B T$ above the Fermi level E_{F1} ; thus the first resonant peak disappears. For the system in Fig. 5(d), the equilibrium population contrast between the energy levels above and below the Fermi level E_{F2} is further increased, so the magnitude of the first resonant peak is larger than that in Fig. $5(b)$. In comparison, for a suspended MoS₂ nanoribbon without an exchange field, the spin currents have no resonant peak versus the optical frequency, and the maximum spin current is less than 0.1 pA.

If the magnetization orientation of the substrates is switched to be parallel, i.e., $\mathbf{M}_B = \mathbf{M}_T = B_0 \hat{z}$, then the optical injection of charge and spin currents is as plotted in Figs. $5(e)$ and $5(f)$. In these cases, the first few resonant peaks are switched off. The spin currents at the corresponding optical frequency are less than 0.1 pA. A few resonant peaks at a larger optical frequency with a smaller magnitude appear. This property can function as an optical spin valve because the spin currents are switched on and off by the rotation of the magnetization orientation. As the parameters of the heterostructure (B_0 , λ , and λ_R) change, the energy ranges with a one-way spin-velocity texture change, in turn changing the resonant frequencies and magnitudes of the peaks of the spin current. As the strength of the Rashba SOC decreases, the energy ranges become smaller, so the magnitude of the resonant peaks decreases.

V. CONCLUSION

In conclusion, intercalation of monolayer $MoS₂$ between two $BiFeO₃$ substrates can induce the Kekule pattern of the exchange field in the $MoS₂$ layer, which is controlled by the magnetization orientation of the substrates. By employing the tight-binding model, the numerical simulations reveal that the band structures and spin texture of the zigzag nanoribbon are dependent on the nonuniform pattern of the exchange field. The edge bands can be switched between metallic and insulating. With an antiparallel magnetization orientation of the substrates, large energy ranges with a oneway spin-velocity texture for spin-*y* and spin-*z* components are found. This property enhances the optical injection of a spin current. When the optical excitation generates the maximum population of edge states with a one-way spin velocity, the injected spin current peaks. If the magnetization orientation of the substrates is switched to be parallel, then the peaks are turned off because the band structures and spin texture are changed. As a result, the optical excitation of a

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localized spin current at the zigzag edge is controlled by the magnetization orientation of the substrates. Because the spin current is highly localized at the Mo-edge termination, experimental implementation of the scheme could be performed along a wide $MoS₂$ monolayer with a smooth zigzag Mo edge, rather than a narrow $MoS₂$ zigzag nanoribbon [\[55\]](#page-7-0).

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