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We investigate ferrimagnetic domain-wall dynamics induced by circularly polarized spin waves theoretically and numerically. We find that the direction of domain-wall motion depends on both the circular polarization of spin waves and the sign of net spin density of the ferrimagnet. Below the angular momentum compensation point, left- circularly (right-circularly) polarized spin waves push a domain wall towards (away from) the spin-wave source. Above the angular momentum compensation point, on the other hand, the direction of domain-wall motion is reversed. This bidirectional motion originates from the fact that the sign of spin-wave-induced magnonic torque depends on the circular polarization and the subsequent response of the domain wall to the magnonic torque is governed by the net spin density. Our finding provides a way to utilize a spin wave as a versatile driving force for bidirectional domain-wall motion.

DOI: [10.1103/PhysRevB.100.174403](https://doi.org/10.1103/PhysRevB.100.174403)**I. INTRODUCTION**

One class of ferrimagnets of emerging interest is a rare-earth (RE) transition-metal (TM) compound where the RE and TM moments are coupled antiferromagnetically. Owing to different Landé g factors between the RE and TM elements, RE-TM ferrimagnets exhibit two unique compensation temperatures: the magnetic moment compensation temperature T_M at which net magnetic moment vanishes and the angular momentum compensation temperature T_A at which net angular momentum vanishes [1–3].

Research on ferrimagnetic materials has focused on the understanding of their fundamental magnetism [4] and optical switching of magnetization [5–11]. Recently, RE-TM ferrimagnets have attracted renewed interest as they offer a material platform to investigate the antiferromagnetic spintronics [12–15]. Compared to ferromagnets that have served as core materials for spintronics research, antiferromagnets exhibit several distinct features such as the immunity to external field perturbations and fast dynamics due to antiferromagnetic exchange interaction. However, the external field immunity of true antiferromagnets results in experimental difficulty in both creating and controlling antiferromagnetic textures. On the other hand, RE-TM ferrimagnets have finite magnetic moment at the angular momentum compensation point at which the antiferromagnetic dynamics is realized. As a result, previously established creation and detection schemes for ferromagnets are directly applicable to RE-TM ferrimagnets. This simple but strong benefit of RE-TM ferrimagnets has recently

initiated extensive studies on ferrimagnets, which include magnetization switching [16–19], domain-wall (DW) motion [20–24], skyrmion (or bubble domain) motion [25–28], low damping [29], and efficient spin-transfer and spin-orbit torques due to antiferromagnetic alignment of atomic spins [30,31].

Among the previous studies listed above, the low damping of RE-TM ferrimagnets [29] is of particular interest from the viewpoint of magnonic applications based on ferrimagnets because it enables a long-distance propagation of spin waves (SWs). For ferromagnets [32–39] and antiferromagnets [40–43], it was reported that a SW can move a DW by transferring its angular momentum or linear momentum. Though the SW property in ferrimagnets was established [44–47], the effect of SWs on ferrimagnetic DW motion remains unexplored. In comparison to ferromagnets and antiferromagnets, antiferromagnetically coupled ferrimagnets exhibit a distinguishing feature of SW eigenmodes. In ferromagnets, a SW with only one type of polarization is permitted, which drives a DW towards the SW source through the angular momentum transfer [34–37]. In antiferromagnets, however, both the left- and right-circularly polarized SWs are allowed and energetically degenerate, which can transfer the linear momentum to a DW through the SW reflection [40,41,43], resulting in the DW motion away from the SW source. In antiferromagnetically coupled ferrimagnets, on the other hand, the degeneracy of the two circularly polarized SWs can be lifted depending on the net spin density of the ferrimagnet. Given that SW-induced DW motion in ferrimagnets has been unexplored, interesting and important questions remain unanswered: how a SW moves a ferrimagnetic DW and what the role of circular polarization of the SW is.

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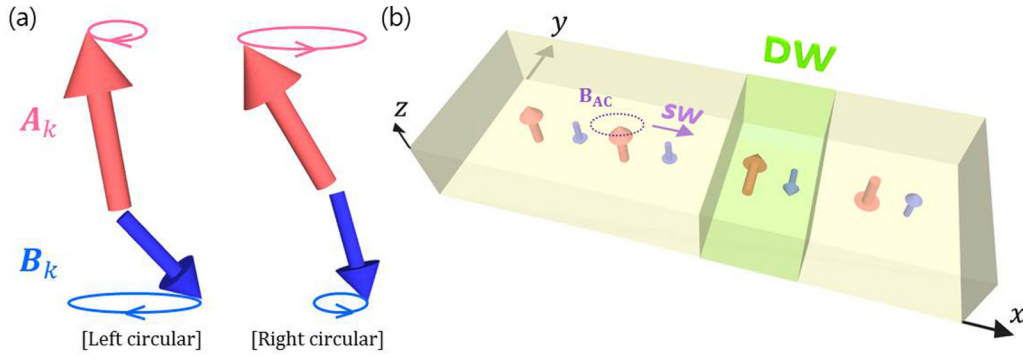


FIG. 1. (a) Illustration of the definition for left- and right-circular polarization in an antiferromagnetically coupled ferrimagnet. (b) Schematic graphic of a one-dimensional ferrimagnetic nanowire with a domain wall (DW). The domain wall is positioned at the center of the nanowire. The spin wave is excited by an external ac field (\mathbf{B}_{ac}) on the left side (252 nm apart from the DW).

In this paper, we study the dynamics of a ferrimagnetic DW induced by a SW in the vicinity of the angular momentum compensation temperature T_A . We investigate DW dynamics induced by left- and right-circularly polarized SWs [see Fig. 1(a) for an illustration of the two eigenmodes]. We begin with theoretical analysis based on the Lagrangian density and SW dispersion. We then conduct numerical simulation based on the atomistic Landau-Lifshitz-Gilbert (LLG) equation to confirm the analytical results. Our model system is shown in Fig. 1(b).

II. MODEL

Our model system is a simple bipartite ferrimagnet which consists of two sublattices labeled by A and B. We introduce the staggered vector $\mathbf{n} = (\mathbf{A}_k - \mathbf{B}_k)/2$, and $\mathbf{m} = \mathbf{A}_k + \mathbf{B}_k$, where \mathbf{A}_k and \mathbf{B}_k are the unit vectors of spin moment at a site k that belongs to the sublattices A and B, respectively. The Lagrangian density for the ferrimagnet is given by [26,47–49]

$$\mathcal{L} = [-s\dot{\mathbf{n}} \cdot (\mathbf{n} \times \mathbf{m}) - \delta_s \mathbf{a}(\mathbf{n}) \cdot \dot{\mathbf{n}}] - \mathcal{U}, \quad (1)$$

where $s = (s_A + s_B)/2$, $\delta_s = s_A - s_B$, $s_i = M_i/\gamma_i$ is the angular momentum density, M_i is the magnetic moment, γ_i is the gyromagnetic ratio for sublattice i , and $\mathbf{a}(\mathbf{n})$ is the vector potential for the magnetic monopole. The total energy \mathcal{U} includes the exchange energy and anisotropy energy as

$$\mathcal{U} = \frac{a}{2} |\mathbf{m}|^2 + \frac{A}{2} (\nabla \mathbf{n})^2 - \frac{K}{2} (\hat{z} \cdot \mathbf{n})^2 + \frac{\kappa}{2} (\hat{x} \cdot \mathbf{n})^2, \quad (2)$$

where a is the homogeneous exchange, A is the inhomogeneous exchange, K is the easy-axis anisotropy constant, and κ is the shape anisotropy constant. Shape anisotropy originates from nonvanishing net magnetic moment arousing dipole interaction, and we simplify the shape anisotropy energy as hard-axis anisotropy along the x axis. The Rayleigh function accounting for the dissipation is given by $\mathcal{R} = \alpha s \dot{\mathbf{n}}^2$ where α is the Gilbert damping constant. The dynamic variable \mathbf{m} can be expressed by

$$\mathbf{m} = -(s/a)\dot{\mathbf{n}} \times \mathbf{n}. \quad (3)$$

From the Lagrangian density and the Rayleigh dissipation, we obtain the equation of motion in terms of staggered vector \mathbf{n}

by integrating out the net magnetization variable \mathbf{m} [26,50]:

$$\rho \mathbf{n} \times \ddot{\mathbf{n}} + 2\alpha s \mathbf{n} \times \dot{\mathbf{n}} + \delta_s \dot{\mathbf{n}} = \mathbf{n} \times \mathbf{f}_n, \quad (4)$$

where $\rho = s^2/a$ parametrizes the inertia and $\mathbf{f}_n = -\delta\mathcal{U}/\delta\mathbf{n}$ is the effective field. After linearizing the equations for small-amplitude fluctuations from the uniform \mathbf{n} state, we consider the SW ansatz as $\mathbf{n}(x, t) = \text{Re}[(n_x \exp\{i(2\pi ft - kx)\}, n_y \exp\{i(2\pi ft - kx)\}, 1)]$, where n_x, n_y are the amplitudes of the SW ($|n_x|, |n_y| \ll 1$), f is the SW frequency, and k is the wave vector. By solving the linearized equations with this ansatz, we obtain the dispersion relation as

$$f_{\pm} = \frac{\pm\delta_s + \sqrt{\delta_s^2 + 4\rho(Ak^2 + K + \kappa/2)}}{4\pi\rho}. \quad (5)$$

Here the upper (lower) sign corresponds to the left-circularly (right-circularly) polarized SW. The resonance frequencies for left- and right-circularly polarized SWs are different except at the angular momentum compensation point T_A where the net spin density δ_s is zero. Figure 2 shows the agreement between the analytic dispersion relations of the SW [Eq. (5), lines in Fig. 2] and numerical results that will be discussed below (symbols in Fig. 2). To get the numerical results, we use the atomistic LLG equation which is described in detail below. Below or above T_A , the energy of the right-circularly polarized SW differs from that of the left-circularly polarized SW [see Figs. 2(a) and 2(c)]. At T_A [Fig. 2(b)], two circularly polarized SWs are degenerate, which is analogous with antiferromagnetic SWs. Although the shape anisotropy makes magnon polarizations elliptical rather than perfectly circular, in this paper, we focus on the regime where the shape anisotropy is much weaker than the easy-axis anisotropy and thus the polarizations of magnons are mostly circular.

We next look into the dynamics of ferrimagnetic DWs induced by SWs. We consider \mathbf{n} as $\mathbf{n} = \mathbf{n}_0 + \delta\mathbf{n}$ with DW texture \mathbf{n}_0 and small fluctuation $\delta\mathbf{n}$ ($|\delta\mathbf{n}| \ll |\mathbf{n}_0|$) with the constraint $\mathbf{n}_0 \cdot \delta\mathbf{n} = 0$ to keep the unit length of \mathbf{n} to linear order in $\delta\mathbf{n}$. We introduce two collective coordinates [51], the DW position $X(t)$ and center angle $\phi(t)$, and define a DW \mathbf{n}_0 by the Walker ansatz [52], $\mathbf{n}_0(x, t) = (\sin\theta \sin\phi, \sin\theta \cos\phi, \cos\theta)$ where $\theta = 2\tan^{-1}[\exp\{(x - X)/\lambda\}]$ and λ is the DW width. We consider the magnonic torque $\boldsymbol{\tau}_m$ that is given by

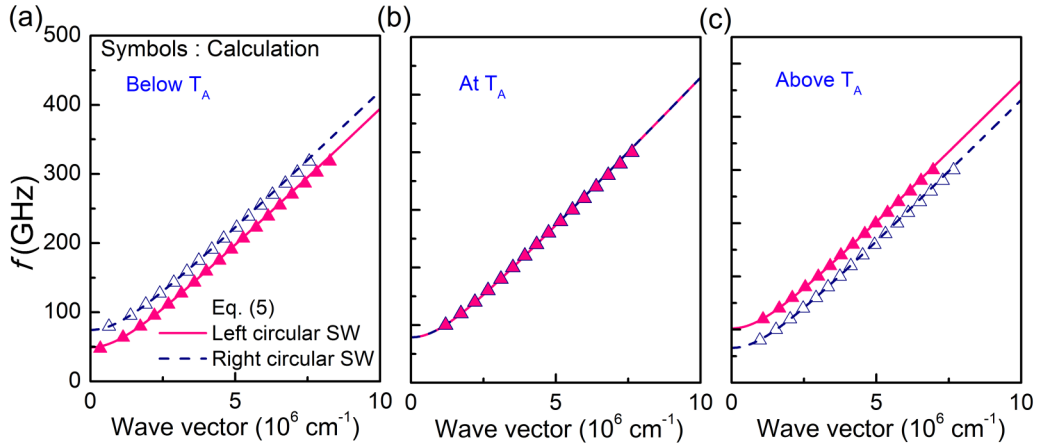


FIG. 2. Spin-wave dispersion relations (a) below T_A (corresponding to index 3 in Table I), (b) at T_A (index 6), and (c) above T_A (index 9). Symbols represent numerical simulation results and lines represent Eq. (5). Solid (open) triangular symbols correspond to the left-circularly (right-circularly) polarized spin wave.

[34,37,39,53]

$$\tau_m = -A[(\mathbf{J}_m \cdot \nabla)\mathbf{n}_0 - (\partial_x \rho_m)\mathbf{n}_0 \times \partial_x \mathbf{n}_0], \quad (6)$$

where magnon-flux density $J_m^x = \mathbf{n}_0 \cdot \langle \delta \mathbf{n} \times \partial_x \delta \mathbf{n} \rangle$ and magnon number density $\rho_m = \langle \delta \mathbf{n} \rangle^2 / 2$. The first term in Eq. (6) represents the adiabatic magnonic torque rooted in the magnon current, and the second term represents the nonadiabatic magnonic torque caused by the gradient of the magnon density. Inserting Eq. (6) into the staggered LLG equation Eq. (4), we derive two coupled equations of motion as

$$M\ddot{X} - G\dot{\phi} + M\dot{X}/\tau = F_m, \quad (7)$$

$$I\ddot{\phi} + G\dot{X} + I\dot{\phi}/\tau = -\kappa\lambda \sin 2\phi + T_m, \quad (8)$$

where $M = 2\rho A/\lambda$, $I = 2\rho\lambda A$, $G = 2\delta_s A$, and $\tau = \rho/\alpha s$ are the mass, the moment of inertia, the gyrotropic coefficient, and the relaxation time, respectively, and A is the cross-sectional area of the DW. Here, $F_m = (2A/\lambda) \int dV [(\partial_x \rho_m)\mathbf{n}_0 \times \partial_i \mathbf{n}_0]$ and $T_m = -2A \int dV [(\mathbf{J}_m \cdot \nabla)\mathbf{n}_0]$ correspond to the magnon-induced force and torque, respectively. We note that the sign of T_m is different for left- and right-circularly polarized SWs whereas the sign of F_m is independent of the circular polarization of SW. It is because the sign of J_m^x is different for left- and right-circularly polarized SWs whereas the sign of $\partial_x \rho_m$ is independent of the circular polarization of the SW. From Eqs. (7) and (8), we finally obtain the steady-state velocity of the DW below the Walker breakdown [54] as

$$v_{\text{DW}} = \frac{s}{2A(\alpha^2 s^2 + \delta_s^2)} \left(\alpha \lambda F_m + \frac{\delta_s}{s} T_m \right), \quad (9)$$

TABLE I. Used magnetic moments M_{TM} and M_{RE} and net spin density δ_s for transition-metal and rare-earth elements, respectively, in simulation. Index 6 coincides with the angular momentum compensation point T_A .

Index	1	2	3	4	5	6	7	8	9	10	11
M_{TM} (kA/m)	460	455	450	445	442	440	438	435	430	425	420
M_{RE} (kA/m)	440	430	420	410	404	400	396	390	380	370	360
δ_s (10^{-13} J s/cm ³)	-1.24	-0.93	-0.62	-0.31	-0.12	0	0.12	0.31	0.62	0.93	1.24

which is the central result of this paper. The first and second terms originate from nonadiabatic and adiabatic contributions, respectively. In Eq. (9), the ratio δ_s/s is an estimate of the degree to which the dynamics of the system is close to that of ferromagnets. The condition of $\delta_s/2s \rightarrow \pm 1$ represents the ferromagnetic limit, whereas that of $\delta_s/2s \rightarrow 0$ represents the antiferromagnetic limit. In the ferromagnetic limit ($\delta_s/2s \rightarrow \pm 1$), the second term in Eq. (9) becomes dominant for the DW motion. On the other hand, in the antiferromagnetic limit ($\delta_s/2s \rightarrow 0$), the second term vanishes and only the first term is responsible for DW motion.

To verify Eq. (9), we perform numerical simulations with the atomistic LLG equation. We start with the initial condition that the DW is located at the center of a one-dimensional nanowire as shown in Fig. 1(b). The SW is excited by an external ac field \mathbf{B}_{ac} on the left side of the DW. The atomistic LLG equation including the external ac field is given by

$$\frac{\partial \mathbf{S}_i}{\partial t} = -\gamma_i \mathbf{S}_i \times (\mathbf{B}_{\text{eff},i} + \mathbf{B}_{\text{ac}}) + \alpha_i \mathbf{S}_i \times \frac{\partial \mathbf{S}_i}{\partial t}, \quad (10)$$

where \mathbf{S}_i is the normalized spin moment vector, $\gamma_i = g_i \mu_B / \hbar$ is the gyromagnetic ratio, μ_B is the Bohr magneton, and α_i is the damping constant at a lattice site i . The odd (even) site i corresponds to the TM (RE) element. $\mathbf{B}_{\text{eff},i} = -\frac{1}{\mu_i} \frac{\partial \mathcal{H}}{\partial \mathbf{S}_i}$ is the effective field at each site, where μ_i is the magnetic moment per atom, one-dimensional discrete Hamiltonian $\mathcal{H} = A_{\text{sim}} \sum_i \mathbf{S}_i \cdot \mathbf{S}_{i+1} - K_{\text{sim}} \sum_i (\mathbf{S}_i \cdot \hat{z})^2 + \kappa_{\text{sim}} \sum_i (\mathbf{S}_i \cdot \hat{x})^2$, and A_{sim} and K_{sim} (κ_{sim}) are the exchange constant and easy-axis (shape) anisotropy for simulations, respectively. To excite the SW, an external ac field $\mathbf{B}_{\text{ac}} = B_0 [\cos 2\pi f t \hat{x} \pm \sin 2\pi f t \hat{y}]$ is applied on two cells at 252 nm away from the DW. We use the

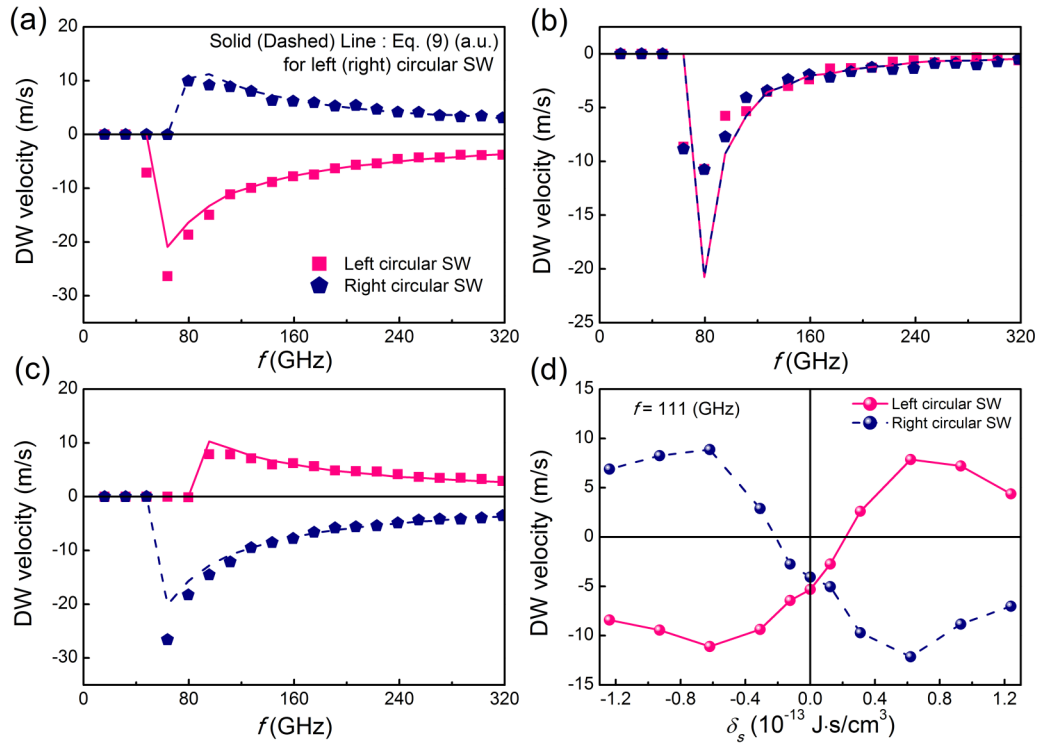


FIG. 3. Calculated domain-wall velocity results (a) below T_A , (b) at T_A , and (c) above T_A with various spin-wave frequencies. Symbols represent the simulation results and lines represent Eq. (9) (arbitrary unit). (d) Domain-wall velocity as a function of the net spin density δ_s at a fixed frequency $f = 111$ GHz. Negative δ_s corresponds to the case below T_A . Used parameters for each point coincide with the data as shown in Table I.

following simulation parameters: $A_{\text{sim}} = 1.64$ meV, $K_{\text{sim}} = 6.47$ μ eV, $\kappa_{\text{sim}} = 0.02 K_{\text{sim}}$, $B_0 = 100$ mT, the lattice constant is 0.42 nm, and the Landé g factor $g_{\text{RE}} = 2$ for rare earth and $g_{\text{TM}} = 2.2$ for transition metal [55]. We consider the damping constant is uniform for all sites, i.e., $\alpha_{\text{RE}} = \alpha_{\text{TM}} = 5 \times 10^{-4}$, for simplicity. We use magnetic moments M_{RE} and M_{TM} as listed in Table I.

III. RESULTS AND DISCUSSION

Figures 3(a)–3(c) show the simulation results of DW velocity as a function of the SW frequency. Figure 3(a) represents the results for the case below the angular momentum compensation point T_A . As the SW gap is different for left- and right-circularly polarized SWs [Fig. 2(a)], the threshold SW frequency for the DW motion is also different for left- and right-circularly polarized SWs. An interesting observation for the DW motion is that the moving direction of the DW depends on the circular polarization of the SW. The left-circularly (right-circularly) polarized SW moves the DW towards (away from) the SW source. This bidirectional DW motion is understood by the fact that left- and right-circularly polarized SWs carry the angular momentum with opposite signs. When the SW passes through the DW, the angular momentum of the SW is transferred to the DW so that the DW moving direction depends on the circular polarization of SW. This is directly related to the fact that the sign of T_m is different for left- and right-circularly polarized SWs, whereas the sign of F_m is independent of the circular polarization of the SW. Given that T_m and F_m in Eq. (9), respectively, cor-

respond to contributions from the adiabatic and nonadiabatic magnonic torques, the bidirectional DW motion depending on the circular polarization of SW evidences that the adiabatic magnonic torque is dominant over the nonadiabatic one.

Solid and dashed lines in Fig. 3(a) are calculated from Eq. (9), with F_m and T_m obtained from numerical calculations. Because the SW amplitude cannot be estimated exactly in the presence of the DW, we extract the SW amplitude when the SW propagates in the uniform ground state in the absence of the DW, and, thus, we use the arbitrary unit for Eq. (9). We find that the numerically obtained bidirectional behavior (symbols) is reasonably described by Eq. (9) in high-frequency ranges. In low-frequency ranges, a discrepancy between Eq. (9) and numerical results appears possibly because of nonlinear effects, which are not captured by our current analytical models. The results for the case above the angular momentum compensation point T_A [Fig. 3(c)] can be understood in a similar way. Contrary to the case below T_A , overall spin moments in the system are reversed so that the left-circularly (right-circularly) polarized SW makes the DW move away from (towards) the source.

To further elucidate SW-induced ferrimagnetic DW motion below and above T_A , we investigate the spin current J_s , which is defined as $J_s = -A\langle \mathbf{n} \times \partial_x \mathbf{n} \rangle$. Figure 4 shows the schematic of SW transmission through a DW (top panel) and the z component of the spin current J_s^z along the propagation direction (i.e., the x axis, bottom panel). For the left-circularly polarized SW (solid line), the spin current in the left domain part decreases gradually due to the damping. After the SW passes through the DW, the spin current abruptly flips its sign due

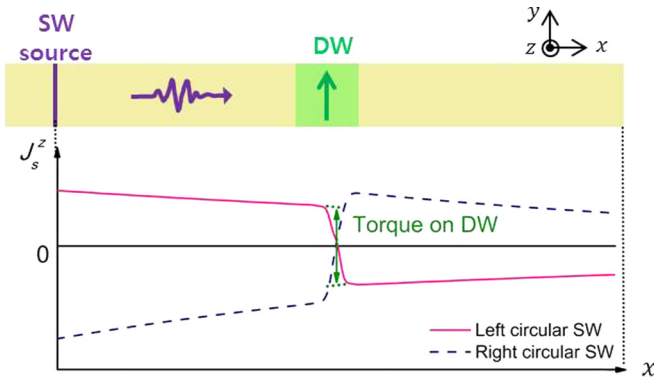


FIG. 4. Schematic of the transmitted SW (top) and the z component of the spin current J_s along the wire length. A DW is positioned at the atomic site $i = 2000$, and the SW source is at $i = 1700$. Assumed parameters are those with index 3 (i.e., below T_A) listed in Table I and the SW frequency is 95 GHz.

to overall reversal of spin moments. The spin-current change is transferred to the DW, resulting in the DW motion. For the right-circularly polarized SW (dashed line), the overall sign of the spin current is reversed. That is why the direction of DW propagation is opposite for left- and right-circularly polarized SWs. The sign of the spin-current change is the same below and above T_A , but δ_s changes its sign [see Eq. (9)] because the spin directions in the domain part change accordingly, which results in the sign difference of the DW velocity below and above T_A .

For the case at the angular momentum compensation point T_A (i.e., $\delta_s = 0$), both left- and right-circularly polarized SWs drive the DW to the same direction (i.e., towards the SW source) as shown in Fig. 3(b). We note that this DW moving direction at T_A is opposite to the direction of the DW motion induced by circularly polarized spin waves in true antiferromagnets [40,41]. In true antiferromagnets where the shape anisotropy is absent, circularly polarized SWs make the DW precess, which results in the SW reflection. The reflected SWs transfer linear momentum to the DW, and push the DW away from the SW source. For the case at T_A of ferrimagnets, however, the net magnetic moment is finite so that the shape anisotropy does not vanish. As a result, the DW experiences shape anisotropy, which prevents the DW precession. Therefore, the ferrimagnetic DW still serves as a reflectionless potential called the Pöschl-Teller potential [56] and its motion is governed by the force from the magnonic torque [the $\alpha\lambda F_m$ term in Eq. (9)]. As the sign of F_m is independent of the SW circular polarization, both left- and right-circularly polarized SWs pull the DW along the same direction, i.e., towards the SW source. This force-induced motion of the ferrimagnetic DW toward the spin-wave source at T_A is similar to the motion of the antiferromagnetic DW toward the spin-wave source for linearly polarized spin waves reported in Ref. [40].

Dependence of the DW velocity on the SW circular polarization is summarized in Fig. 3(d), which shows the DW velocity as a function of the net spin density δ_s at a fixed SW

frequency ($f = 111$ GHz). The sign of DW velocity depends not only on the circular polarization but also on the sign of the net spin density. We note that the DW velocity is not zero at T_A because the adiabatic and nonadiabatic contributions are not compensated at T_A .

IV. SUMMARY

We have investigated the SW circular-polarity dependence of ferrimagnetic DW dynamics theoretically and numerically. We find that the DW moves along the opposite direction depending on the circular polarization of SW. This bidirectional DW motion is caused by the fact that the signs of the spin current and the angular momentum transferred to the DW are opposite for left- and right-circularly polarized SWs. The overall tendency of the DW moving direction is reversed when the sign of the net spin density δ_s is reversed. At T_A where the angular momentum vanishes, the dissipative nonadiabatic magnonic torque is the main driving force so that the DW moves along the same direction (towards the SW source) regardless of the SW circular polarization. This was reported for biaxial antiferromagnetic DW dynamics with hard-axis anisotropy and/or Dzyaloshinskii-Moriya interaction (DMI) [57]. In this case, the hard-axis anisotropy suppresses the DW angle rotation identically acting as the shape anisotropy. It is analogous to ferrimagnetic DW dynamics at the angular momentum compensation point T_A . With the DMI, the speed of the antiferromagnetic DW is enhanced largely. It inspires us to carry out a further study on SW-induced dynamics of ferrimagnetic DWs combined with DMI.

Our finding of bidirectional ferrimagnetic DWs driven by SWs can be generalized to other ferrimagnetic topological excitations such as magnetic skyrmions and vortices. This bidirectionality of ferrimagnetic DW motion depending either on the SW circular polarization or on the sign of the net spin density will be useful for magnonic spintronics [58] because such bidirectional motion, which makes the device functionality versatile, can be realized without moving the location of a SW source. It has been shown that the spin-wave polarization can be controlled via electric gating [59], magnetic gating [60], or retarding effect by antiferromagnetic domain walls [42]. When combined with these rich spin-wave polarization control mechanisms, the bidirectionality of ferrimagnetic DW motion studied in this paper provides more possibilities in utilizing the interplay between spin-wave and magnetic texture for information processing.

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