

Superconducting order parameter and bosonic mode in hydrogen-substituted $\text{NdFeAsO}_{0.6}\text{H}_{0.36}$ revealed by multiple-Andreev-reflection spectroscopy

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Using intrinsic multiple-Andreev-reflection-effect spectroscopy, we studied ballistic superconductor-normal metal-superconductor (SnS) contacts in layered oxypnictide superconductors $\text{NdFeAsO}_{0.6}\text{H}_{0.36}$ with critical temperatures $T_c = 45 - 48$ K. We directly determined the magnitude of two bulk superconducting order parameters, the large gap $\Delta_L \approx 10.4$ meV, a possible small gap $\Delta_S \approx 1.8$ meV, and their temperature dependence. Additionally, a resonant coupling with a characteristic bosonic mode was observed—the boson energy at 4.2 K, $\varepsilon_0 = 10.5 - 11.0$ meV being less than the indirect gap ($\Delta_L < \varepsilon_0 < \Delta_L + \Delta_S$).

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I. INTRODUCTION

Despite extensive investigations of the oxypnictide superconductors $R\text{FeAsO}$ (R is rare-earth metal) of the 1111 family since the discovery of iron-based superconductivity in $\text{LaFeAsO}_{1-x}\text{F}_x$ [1], many of their properties seem still ambiguous [2–4]. Such a problem arises from a lack of large enough single crystals, which makes the 1111 family hardly suitable for many techniques, including angle-resolved photoemission spectroscopy (ARPES).

The layered crystal structure of the 1111 oxypnictides consists of quasi-two-dimensional superconducting Fe-As blocks separated by RO spacers alternating along the c direction. Being an antiferromagnetic metal at room temperature, the parent undoped compound $R\text{FeAsO}$ undergoes a structural and magnetic transition at T^* , thus turning to a spin-density wave (SDW) state below T^* . Being suppressed under electron or hole doping, the SDW state gives way to superconductivity. Unlike long-known fluorine-substituted 1111, hydrogen-substituted $R\text{FeAsO}_{1-x}\text{H}_x$ demonstrates a double-dome superconducting state in the phase diagram [5,6].

Below T_c , two superconducting condensates are developed with the large gap Δ_L and the small gap Δ_S order parameters. Preliminary band-structure calculations [7] showed several bands formed by Fe $3d$ orbitals crossing the Fermi level, with a formation of well-nested hole barrels near the Γ point and electron barrels near the M point of the two-Fe Brillouin zone. For the 1111 family, due to a scarcity of momentum-sensitive probes of the superconducting order parameter, the gap distribution across the Fermi surface is still ambiguous, which differs dramatically from the situation with the 122 family.

The initial suggestion that the large gap Δ_L developed in the hole bands and the small gap Δ_S in electron bands [8] was soon refuted for the majority of Fe-based superconductors. For now, Δ_S opening at the outer Γ barrel, whereas a “strong” condensate with Δ_L developing in all other bands crossing E_F , is considered to be uniform for pnictides. As for oxypnictides, although such convention seems partly consistent with a few available ARPES data [9,10], further studies are obviously required. Additionally, a strong renormalization of the calculated band structure in $\text{SmFe}_{0.92}\text{Co}_{0.08}\text{AsO}$ and $\text{NdFeAsO}_{0.6}\text{F}_{0.4}$ with critical temperatures $T_c = 18$ K and 38 K, respectively, was revealed [9,10], thus contradicting general expectations [8]. This led to the band-edge singularities turned to a close proximity of the E_F at Γ and M points of the momentum space. Such a nontrivial band picture, obviously unstable with respect to a fine tuning of the Fermi level, may cause featured density of states (DOS) and carrier concentrations, in the bands where $\Delta_{L,S}$ are developed in the superconducting state.

To describe multiple band superconductivity in iron-based superconductors, several models were suggested: s^{++} model of coupling through orbital fluctuations enhanced by phonons [11,12], s^\pm model of spin-fluctuation-mediated repulsion [3,8,13], a shape-resonance model [14], and orbital-selective pairing [15,16]. A spin resonance peak at the nesting vector was observed in neutron scattering probes [17]. According to theory, the energy $\hbar\omega$ of spin exciton should fulfill the resonance condition $\hbar\omega < (\Delta_L + \Delta_S)$ or $\hbar\omega < 2\Delta_L$ [18,19].

A characteristic feature of heavily hydrogen-substituted 1111 is a sizable increase in the c lattice parameter, which takes place in the $x \rightarrow 0.5$ region of the phase diagram [20]. Such an isostructural transition unaccompanied with AFM phase [21] relates to non-nematic orbital fluctuations, which are expected to gain T_c within the second superconducting dome [22]. From this point of view, the structure of the superconducting order parameter in H-substituted oxypnictides

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may contain extraordinary features, unlike other members of the 1111 family.

Here we present a direct probe of the superconducting order parameter in polycrystalline samples of hydrogen-substituted NdFeAsO_{0.6}H_{0.36} (hereafter Nd-1111H) by using intrinsic multiple-Andreev-reflection-effect (IMARE) spectroscopy. We determined the magnitudes of the two distinct superconducting order parameters and their temperature dependence, estimated intra- to interband coupling strength imbalance, and eigenparameters of both superconducting condensates (to be realized excluding interband coupling). A resonant coupling with a characteristic bosonic mode was observed, with the energy more than Δ_L and less than indirect gap ($\Delta_L + \Delta_S$) at $T \rightarrow 0$, which satisfies the theoretical condition [18,19].

II. EXPERIMENTAL DETAILS

The polycrystalline sample with the nominal composition NdFeAsO_{0.6}H_{0.36} was prepared in a cubic anvil high-pressure cell from the stoichiometric mixture of NdAs, FeAs, FeO, Fe, and Nd(OH)₃ powders. A pressure of 3 GPa was applied at room temperature. By keeping the pressure constant, the temperature was increased up to a maximum value of 1450 °C, maintained for 14 h, followed by cooling to room temperature in 3 h. Overall details of the experimental setup can be found in our previous publications [23,24]. X-ray measurements revealed the single-phase nature of the sample as well as the absence of a suitable amount of impurities. The occurrence of bulk superconductivity at critical temperature $T_c = 48$ K was confirmed by the magnetic measurements.

To make superconductor-normal metal-superconductor (SnS) junctions for Andreev spectroscopy experiments, we used a break-junction technique [25,26]. The sample was prepared as a thin rectangular plate with dimensions about $3 \times 1.5 \times 0.1$ mm³ and was attached to a springy sample holder by four contact pads made of In-Ga paste at room temperature. After cooling down to $T = 4.2$ K, the sample holder was gently curved, thus cracking the bulk sample, with a formation of two cryogenic clefts separated with a weak link, a kind of ScS contact (where c is a constriction). The resulting constriction turns far from current and potential contacts, which prevents junction overheating and provides true four-point probe. A layered sample splits along the ab planes where steps and terraces naturally appear; the height of the step is a multiple of the c unit cell parameter, whereas the terrace size appears about 10–100 nm. Typically, this is the case for polycrystalline samples of layered compounds as well. With regard to the 1111 family, highly expected is a number of cracked crystal grains with steps and terraces on its surface as shown by us earlier [26–28].

Under fine tuning the curvature of the sample holder, the two cryogenic clefts slide apart, touching various terraces; they remain tightly connected during sliding, which prevents impurity penetration into the crack and protects the purity of cryogenic clefts. Such tuning enables us to sweep the constriction area to realize a desired ballistic regime (the contact dimension d is less than the carrier mean free path l). In the majority of Fe-based superconductors we studied, the constriction is electrically equivalent to a thin layer of normal

metal of high transparency (about 95–98%), thus providing an observation of multiple-Andreev-reflection effect (MARE). As a result, the obtained current-voltage characteristics (CVC) and the $dI(V)/dV$ spectra are typical for the clean classical SnS-Andreev junction [29–33].

At temperatures below T_c , Andreev transport causes a pronounced excess current which drastically rises at low bias voltages (foot), and a series of dynamic conductance dips called subharmonic gap structure (SGS). At certain temperatures, the position of SGS dips directly relates to the gap magnitude [32,33],

$$eV_n(T) = \frac{2\Delta(T)}{n}, \quad (1)$$

where $n = 1, 2, \dots$ is natural subharmonic order. Unlike probing asymmetric NS and NIS junctions (I is insulator, N—normal metal, and S—superconductor), no fitting of $dI(V)/dV$ is needed in the case of SnS contact till T_c , which facilitates a precise measurement of temperature dependence of the gap. In principle, the first Andreev minimum could be slightly shifted toward lower bias, $V_{n=1} \lesssim (2\Delta/e)$ [29–33]. If such a thing happens, the gap value may be determined using the positions of the higher order SGS dips with $n \geq 2$. In the case of a two-gap superconductor, two SGS's are expected in the dynamic conductance spectrum.

For the junctions obtained in layered superconductors with a valuable anisotropy of electrical properties, the ballistics should be kept along both ab and c directions. Here, due to the current flowing along the c direction, the ballistic conditions are $l_c^{\text{inel}} > d_c$ and $l_{ab}^{\text{el}} > d_{ab}$, where l^{el} and l^{inel} are the elastic and inelastic mean free path and d_{ab}^2 is the constriction area to be estimated using Sharvin formula [34]. The number n^* of observed Andreev dips corresponds with the beginning of the foot at the bias voltage $eV = 2\Delta/n^*$, and indirectly determines the out-of-plane inelastic mean free path l_c^{inel} to d_c ratio: $n^* \approx 2l_c^{\text{inel}}/d$ [32,33] for the case of fully transparent contact.

Besides the single ScS contacts, Andreev arrays with ScSc...-S structure can also be formed in the break-junction experiment with layered samples [26–28]. Composed of m ScS junctions, such array peers a natural stack of equivalent resistors (with parallel normal and Andreev channels). Hence, in the $dI(V)/dV$ of the array, IMARE occurs, with the position of the Andreev features scaled by a factor of m as compared with that of a single SnS junction:

$$eV_n(T) = m \times \frac{2\Delta(T)}{n}. \quad (2)$$

IMARE is similar to intrinsic Josephson effect in SISI...-S array observed in high-temperature cuprates and other layered superconductors [26,35–37]. Gently readjusting the contact point, one can probe several tens of Andreev arrays with various diameters and numbers of junctions in one and the same sample and during the same cooldown. To the best of our knowledge, thus provided data statistics permits us to check the data correctness in terms of reproducibility. For the formed array, the number m is natural but accidental, so it can be determined by comparing $dI(V)/dV$ curves for various arrays: After scaling the bias voltage axis by m , the dynamic conductance spectrum turns to that of a single junction. In

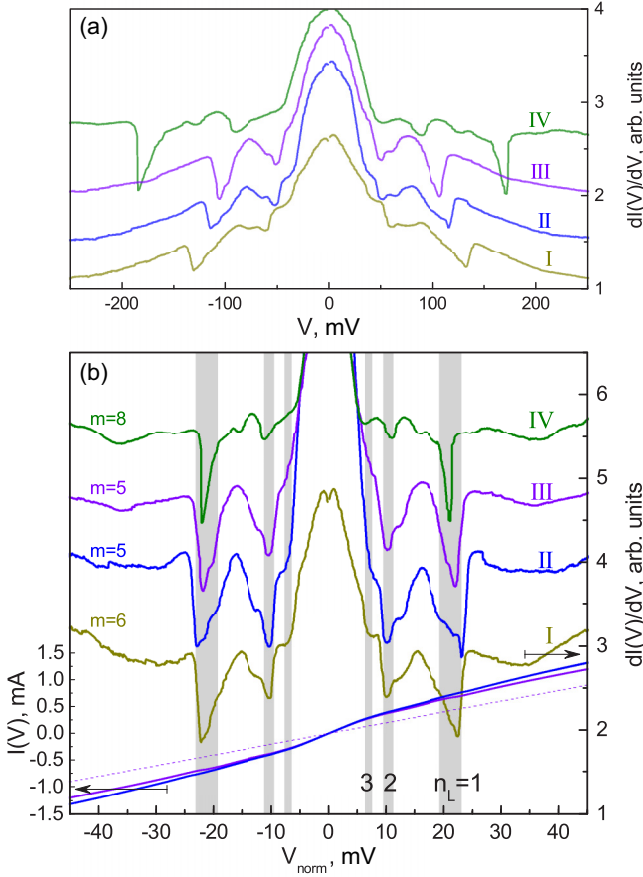


FIG. 1. (a) Raw dynamic conductance spectra measured at $T = 4.2$ K for SnS Andreev arrays with a various number of series junctions m . The curves were shifted vertically for clarity. (b) The same $dI(V)/dV$ spectra with suppressed monotonic background; the bias voltage axis was normalized with corresponding m ($V_{\text{norm}} \equiv V_{\text{array}}/m_i$). Also presented are current-voltage characteristics (left axis) for $m = 5$ junction arrays. Dashed line shows simulated ohmic $I(V)$ at T_c . Gray areas and $n_L = 1, 2, 3$ labels indicate the position of subharmonic gap structure dips for the large gap $\Delta_L \approx 10.4$ meV.

Figs. 1–3 and 5, each CVC and corresponding dynamic conductance spectrum is normalized using the determined m , thus corresponding to a single SnS contact. Hereafter, V_{norm} means V/m , whereas the current axis is kept unnormalized. The method of extracting m numbers is detailed in the Appendix.

As the method shows [26,27], Andreev dips in the dynamic conductance spectrum of array are more sharp and intensive than those for single SnS junctions; the larger the m , the sharper the $dI(V)/dV$ features. This firm experimental fact favors a natural origin of such arrays (as part of the layered structure) rather than a chain of independent nonequivalent grain-grain contacts [38].

During (I)MARE, electron could lose or gain its energy by coupling with some bosonic mode. At low temperatures, boson emitting seems more likely, whereas the energy of the bosonic mode ε_0 is up to 2Δ . A resonant interaction with a characteristic bosonic mode with peculiar energy ε_0 causes a fine structure in the $dI(V)/dV$ spectrum. Accompanying each Andreev dip, at higher bias, a less-intensive satellite dip

appears at position

$$eV_n = \frac{2\Delta + \varepsilon_0}{n}, \quad (3)$$

forming an additional subharmonic series. The resulting fine structure looks similar as compared with the case of microwave irradiated SnS junction first observed in YBaCuO [39].

Summarizing the advantages of IMARE spectroscopy of break junctions and natural arrays, this technique provides a precise and high-resolution probe of the bulk superconducting order parameter, its temperature dependence, and fine structure. In our studies, the dynamic conductance spectra were measured directly by a standard modulation technique [26,40]. We used a source of direct current mixed with a small-amplitude ac with frequency about 1 kHz from the external oscillator. The results obtained with this setup are insensitive to the presence of parallel ohmic conduction paths; if any path is present, the dynamic conductance curve shifts along the vertical axis only, while the bias stays unchanged.

III. RESULTS AND DISCUSSION

A. Subharmonic gap structures

Figure 1(a) shows typical raw dynamic conductance spectra of the break junctions formed in Nd-1111H samples at $T = 4.2$ K. The spectra demonstrate an excess conductance which rises toward low bias voltages, and a series of Andreev dips. The position of the dips is although irreproducible, since the spectra correspond to the arrays with various numbers of junctions, thus providing $\Delta \cdot m$ energy value. To reduce each spectrum to that of a single junction, the bias voltages were divided by $m = 6, 5, 5, 8$, correspondingly (from the bottom). For how these m were chosen, see the Appendix.

The normalized CVCs (for II and III spectra), as well as the spectra from Fig. 1(a) with suppressed monotonic background, are shown in Fig. 1(b) by similar colors. Normal-state CVC for the III spectrum at $T = T_c$, simulated with a dashed line, determines the normal resistance $R_N \approx 50 \Omega$ per junction. As compared with ohmic dependence, the CVC measured at 4.2 K demonstrates a pronounced excess current. To check the ballisticity of the constriction in the ab -plane, we take the following parameters. For a single crystal grain, the normal state in-plane resistivity $\rho^{ab}(T_c) = 0.13 - 0.15 \text{ m}\Omega \text{ cm}$ is similar to that of other oxypnictides synthesized in the same way [41–43], whereas the in-plane coherence length at $T \rightarrow 0$ is $\xi^{ab}(0) \approx 2.1 \text{ nm}$. Using the in-plane Ginzburg-Landau penetration depth for sister Sm-1111 single crystals with similar $\rho(T_c)$ from Ref. [44], $\lambda_{GL}^{ab}(0) \approx 200 \text{ nm}$, we determine the clean-limit value $\lambda_L^{ab} \approx 195 \text{ nm}$. Taking the average Fermi velocity [7] $v_F \approx 1.4 \times 10^8 \text{ cm/s}$, we get the ab -plane product of the bulk resistivity and the elastic carrier mean free path $\rho l^{\text{el}} = \mu_0 \lambda_L^2 v_F \approx (6.6 - 6.7) \times 10^{-7} \text{ m}\Omega \text{ cm}^2$, and therefore estimate $l^{\text{el}} \approx 44 - 52 \text{ nm}$ for single crystal of Nd-1111H. Finally, the diameter of the constriction [34] $2a = 2\sqrt{4\rho l^{\text{el}}/3\pi R_N} \approx 24 \text{ nm}$ is nearly two times less than the estimated elastic mean free path, thus proving the junction to be ballistic, with two to three Andreev subharmonics expected in the $dI(V)/dV$ spectrum. Generally speaking, a measure of ballisticity is not elastic but an inelastic

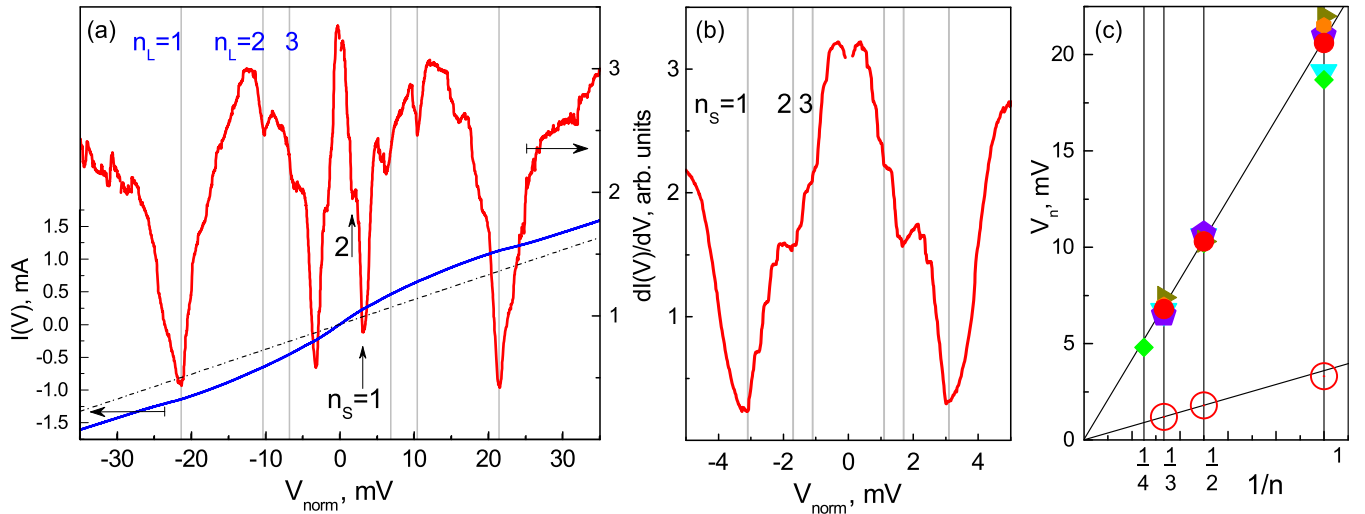


FIG. 2. (a) Dynamic conductance (right axis) at $T = 4.2$ K of Andreev array ($m = 12$ junctions) showing two subharmonic gap structures for the large gap $\Delta_L \approx 10.5$ meV (vertical gray lines and blue $n_L = 1, 2, 3$ labels) and for the small gap $\Delta_S \approx 1.8$ meV (arrows and n_S labels). $V_{\text{norm}} \equiv V_{\text{array}}/12$. Monotonic background is suppressed for clarity. Current-voltage characteristic (left axis) at $T = 4.2$ K and its simulation at T_c (dash-dot line) are shown for comparison. (b) The low-bias fragment of the $dI(V)/dV$ spectrum shown in (a), which details the Andreev structure of the small gap (vertical gray lines, $n_S = 1, 2, 3$ labels). Monotonic background is suppressed separately for positive and negative bias. (c) The SGS positions versus their inverse number $1/n$ for the large gap (solid symbols) and the small gap (open symbols) in $dI(V)/dV$ spectra of various Andreev arrays shown in Figs. 1–3 and 5. The data in (a), (b) panels are illustrated with red circles. Solid lines are guidelines.

mean free path to $2a$ ratio, to appear an order of magnitude higher than estimated $l^{\text{el}}/2a$.

The beginning of the drastic rise of dynamic conductance at low bias (foot) roughly matches the position of $n_L = 3$ subharmonic of the large gap, therefore, $n^* \approx 2l_c^{\text{inel}}/d_c \approx 3$ (both characteristic lengths are taken along the c direction) [33]. As a result, the ballistic along the c direction is also satisfied: $l_c^{\text{inel}}/d_c \approx 1.5$ for the case of fully transparent constriction. In case of high but finite transmission probability (0.1 – 0.2), this ratio tends to 2. The above estimates in the in-plane and out-of-plane directions signify two to three SGS dips are expected in the dynamic conductance spectra. Additionally, a pronounced excess current indicates a high-transparency Andreev mode.

The arrays I, II, and III were formed in one and the same sample sequentially. Under fine tuning of the holder curvature, the initial contact point onto a six-junction stack (curve I) jumped to a neighbor terrace onto a five-junction stack (curve II), then swept (curve III), thereby changing the area and resistance of the junction. However, despite such metamorphosis, the normalized dynamic conductance spectra look quite similar. Pronounced dips at $eV \approx \pm 21, \pm 10.4$ meV and shoulders at ± 6.9 meV being $n_L = 1, 2, 3$ subharmonics comprise SGS of the large gap $\Delta_L \approx 10.4$ meV. For comparison, the $dI(V)/dV$ spectrum for eight-junction array formed in the next sample from the same batch (curve IV) is shown in Fig. 1 as well. Remarkably, the position of the gap subharmonics is insensitive to the topology of the contact point onto the cryogenic surface, and to be reproducible from one sample to another. Therefore, the extracted Δ_L is a bulk order parameter independent of the contact dimension and almost unaffected with a surface proximity.

The CVC and the dynamic conductance spectrum which demonstrates two distinct SGS are shown in Fig. 2(a). n_L

labels point to Andreev dips of the large gap $\Delta_L \approx 10.5$ meV. At lower bias, another set of features presents (up arrows), beginning with a pronounced dip at $eV_{n_S=1} \approx \pm 3.3$ meV being much more intensive than the third-order $n_L = 3$ feature of the large gap. The position of this feature does not match that of the fourth-order subharmonic of the Δ_L expected at ± 5.5 meV. The fragment which details the low-bias region of the $dI(V)/dV$ curve is shown in the inset. After additional suppressing of monotonic background, minima at $|eV_{n_S=1}| \approx 3.3$ meV, $|eV_{n_S=2}| \approx 1.8$ meV, and shoulders at ± 1.2 meV become clear, all together could be interpreted as SGS of the small gap energy parameter $\Delta_S \approx 1.8$ meV.

The above interpretation seems for us the most reliable. Yet to be discussed are the other possible origins of such low-bias SGS [see open circles in Fig. 2(c)].

(1) Supposing the proximity effect origin, with a bulk order parameter inducing on the cryogenic cleft a formation of Cooper pairs with bond energy $\Delta_{\text{surf}} < \Delta_{\text{bulk}}$, one has to use the raw bias (unnormalized by m) to determine this surface order parameter. For the case at 4.2 K, the raw position of the feature pointed out by the up arrow in Fig. 3(a) is ≈ 39.6 meV, which corresponds to $\Delta_{\text{surf}} \approx 20$ meV. Obviously, being much larger than Δ_L , such an order parameter cannot be induced, thus making the considered case improbable.

(2) As could be numerically shown in the framework of Kümmel *et al.* theory [32], if Andreev bound states (ABS) appear in the constriction, with energies $\varepsilon_{\text{ABS}} < \Delta_{\text{bulk}}$, the dynamic conductance spectrum shows additional subharmonic structure at positions $(\Delta_{\text{bulk}} + \varepsilon_{\text{ABS}})/en$. Let us find a way to reproduce the observed low-bias structure. If $d_c \gg 10\xi_c(0)$, then relative to E_F , for the first Andreev level, $\varepsilon_{\text{ABS}} \rightarrow 0$. Thus, the additional structure caused by the in-gap ABS starts from $\approx \Delta_{\text{bulk}}/e$ bias which nearly coincides with the position of $n_L = 2$ dip being almost three times greater than observed.

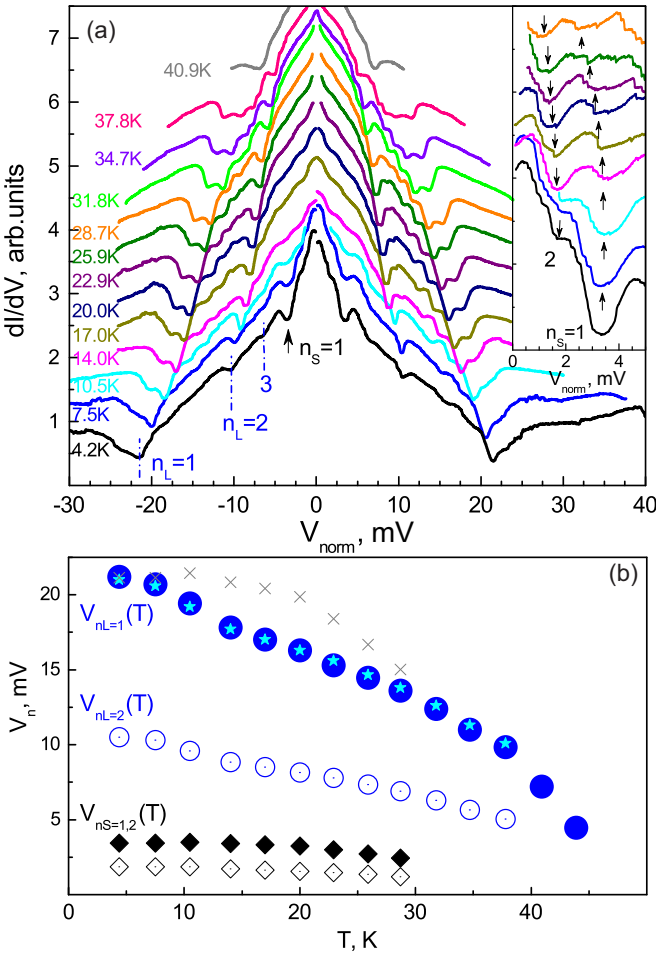


FIG. 3. (a) Evolution of the dynamic conductance spectrum with temperature for SnS Andreev array from Fig. 2(a). Dash-dot bars and $n_L = 1, 2, 3$ labels indicate the subharmonic gap structure dips for the large gap $\Delta_L \approx 10.5$ meV. The inset shows the low-bias fragments (with suppressed monotonic background) of the spectra shown in (a) which detail the first ($n_S = 1$, up arrows) and the second ($n_S = 2$, down arrows) features for the expected small gap $\Delta_S \approx 1.8$ meV. $dI(V)/dV$ curves are shifted vertically for clarity. (b) Temperature dependence of the first (solid symbols) and the second (open symbols) Andreev features $V_n(T)$ for the large gap (circles), and for the small gap (rhombs). Stars and crosses show how $2 \times V_{n_L=2}(T)$ and $V_{n_S=1}(T)$ dependencies, respectively, correspond with $V_{n_L=1}(T)$ for the large gap SGS.

The second minimum related to the ABS structure expected at $\Delta_{\text{bulk}}/2e$ is absent in the presented spectra. Therefore, this low-bias feature set cannot be caused by ABS.

(3) Consider superconducting gap anisotropy in the k -space or an appearance of parasitic junction in parallel. Both suggestions would cause an additional SGS which starts from unpredictable bias E^* but evolves with temperature similar to $\Delta_L(T)$. Nonetheless, the two observed structures behave differently [see $V_{n_S}(T)$ normalized by $V_{n_S}(0)/V_{n_L}(0)$ dependence shown by crosses in Fig. 3(b)], making these cases unrealistic.

(4) In the case of asymmetric junction SnS^* , where S^* is a single-gap superconductor with slightly reduced order parameter (for example, $\Delta^* \approx 5/6\Delta_L$), the dynamic conductance spectrum would show two subharmonic structures at

$(\Delta_L \pm \Delta^*)/en$. Therefore, the main $n = 1$ features are to appear at $11/6 \cdot \Delta_L \approx 2\Delta_L$ and $\Delta_L/6$. The position of the $(\Delta_L - \Delta^*)/en$ structure then suits the observed one. However, such tunneling transition is forbidden at $T \rightarrow 0$, whereas its probability increases with temperature. Would it be the case, the $dI(V)/dV$ features would intensify toward T_c . The experimental spectra in Fig. 3(a) (see the inset for details) demonstrate the opposite tendency. Yet, in the spectrum measured at 17 K, the minima almost vanish, thus to be distinguished after background suppressing only.

The position of the gap features in the dynamic conductance curves of various Andreev arrays versus their inverse number is summarized in Fig. 2(b). For the large gap (solid symbols), the resulting linear dependence tending to the origin agrees well with Eq. (1). Therefore, the large gap order parameter of the average magnitude $\Delta_L \approx 10.4$ meV is observed reproducibly in the Andreev spectra of Nd-1111H. The less-sloped line fits the positions of the second set of SGSs, which determines the characteristic energy ≈ 1.8 meV (open symbols). By analogy with other 1111 compounds [27,28,45], we suppose this energy corresponds to the small gap Δ_S .

B. Gap temperature dependence

Temperature evolution of the dynamic conductance of the Andreev array from Fig. 2(a) (original background is preserved) is shown in Fig. 3(a). In the spectrum measured at 4.2 K, the SGS dips of the large gap $\Delta_L \approx 10.5$ meV are marked with dashed bars. To detail the SGS of the small gap $\Delta_S \approx 1.8$ meV, in the inset we show the low-bias fragments of the spectra with suppressed monotonic background. Here, up arrows point to the first $n_S = 1$ dip position at various temperatures, down arrows- to the second one. As temperature increases, all gap features move toward zero bias. For the large gap, the position of the first (circles) and the second (open circles) dips versus temperature is presented in Fig. 3(b) and directly associated with the $\Delta_L(T)$ temperature dependence (Fig. 4). The large gap trend looks nontypical as compared with other 1111 oxypnictides we studied [28,45]. Nonetheless, when doubling the position of the second feature (originally located at $eV_2(T) = \Delta(T)$), it turns to that of the first one at all temperatures till T_c [stars in Fig. 3(b)]. On the one hand, such correspondence indicates that the observed features belong to one and the same SGS. On the other hand, it proves their noticeably curved temperature dependence originates from intrinsic superconducting phenomena natural to Nd-1111H rather than any undesired force (for example, local excess of the critical current density would lead to $V_{n_L=1}$ “overheating,” i.e., $V_{n_L=1} < 2V_{n_L=2}$).

Using the $V_n(T)$ dependencies [Fig. 3(b)], we obtain the temperature dependence of the large (solid circles) and the small gap (open circles) as an average between the SGS positions $\langle \Delta(T) \rangle = [V_{n=1}(T) + 2V_{n=2}(T)]/4$ shown in Fig. 4(a). The large gap dependence passes well below the single-band BCS-like curve: $\Delta_L(T)$ drops down at $T \approx 12$ K, then decreases gradually, turning to zero at local critical temperature (the temperature of the contact area transition to the normal state). Such unusual behavior reproduces the $\Delta_L(T)$ dependencies measured using data with other Nd-1111H samples from the same batch [triangles, rhombs, and squares in

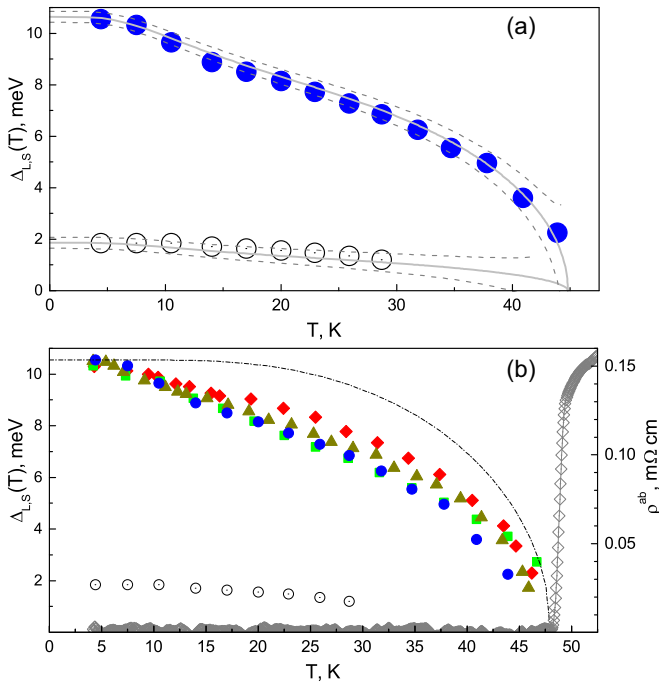


FIG. 4. Temperature dependence of the superconducting gaps obtained (a) using data in the previous figure and (b) compared with other $\Delta_L(T)$ measured with the samples from the same batch. $\Delta_L(T)$ dependencies are shown by solid symbols, $\Delta_S(T)$ by open circles. Theoretical fits using the two-band RBCS model are shown with solid lines (a), dash-dot line corresponds to a single-band BCS-like behavior (b). Gray dashed lines frame the confident intervals for the large and the small gap values. Resistive superconducting transition of the dense multicrystalline material is presented by gray open rhombs (right scale).

Fig. 4(b)], hence being independent of the resistance of the constriction or current density through the junction. Nonetheless, despite the large data statistics obtained for Nd-1111H (more than 100 SnS arrays), only once did we manage to get two SGSs for Δ_L and Δ_S up to T_c (shown in Fig. 3). In the majority of the obtained $dI(V)/dV$, the Andreev features of the small gap are undistinguishable (for example, see Fig. 1). However, one should not think of the obtained $\Delta_S(T)$ dependence as an artifact: Indirectly, our data favors the existence of the second order parameter, whereas an exact experimental reason seems to cause the strongly smeared SGS of the small gap in the obtained spectra, as discussed below.

The presumed small gap decreases more regularly with temperature increase. Obviously, the different temperature trend indicates that the resolved energy parameters relate to two distinct superconducting condensates coexisting in Nd-1111H. The characteristic ratio for the large gap $2\Delta_L/k_B T_c = 5.0 - 5.4$ exceeds the BCS limit 3.5, whereas for the small gap $2\Delta_S/k_B T_c \approx 0.9 \ll 3.5$, seemingly caused by interband interaction.

The obtained $\Delta_{L,S}(T)$ are fitted with a two-band BCS-like model based on Moskalenko and Suhl equations [46,47] using a renormalized BCS integral. To obtain the theoretical $\Delta_{L,S}(T)$ curves, besides the experimental values of T_c , $\Delta_{L,S}(T)$, we used $\alpha = \lambda_{LS}/\lambda_{SL}$, the ratio between effective

intraband and interband couplings $\beta \equiv \sqrt{\lambda_{LL}\lambda_{SS}/(\lambda_{LS}\lambda_{SL})}$ (λ_{ij} are reduced coupling constants extracted directly from the fit), and eigentemperature renormalization coefficient for each band as variables. Note the normal DOS at the Fermi level imbalance $N_S(0)/N_L(0) \neq \alpha$ (to get N_S/N_L , one should use full coupling constants, see, for example, page 2 in Ref. [48]). The resulting solid lines in Fig. 4(a) fit the case of a strong interband coupling comparable with the intraband one, with $\beta \approx 1.5$. Taking the cutoff energy $\hbar\omega_{\text{cut}} = 40$ meV and $\ln(E_F/\hbar\omega_{\text{cut}}) = 2$, we obtain the set of renormalized coupling constants $\lambda_{LL} = 0.33$, $\lambda_{SS} = 0.14$, $\lambda_{LS} = 0.49$, $\lambda_{SL} = 0.041$, which indicates λ_{LS} dominating over the other pairing channels. The notable curvature of $\Delta_L(T)$ seems caused by large α value. Additionally, the eigensuperconductivity of the Δ_L bands (to be realized in the case of $\lambda_{LS} = \lambda_{SL} = 0$) is close to the weak-coupling limit with $[2\Delta_L/k_B T_c]^{\text{eigen}} \approx 3.5$ and eigen critical temperature $T_L^{\text{eigen}} \approx 26.5$ K. In contrast, a moderate coupling develops in the Δ_S bands with $[2\Delta_S/k_B T_c]^{\text{eigen}} \approx 4$ and eigen critical temperature ≈ 0.33 K.

As a rule, the cutoff energy $\hbar\omega_{\text{cut}}$, generally ambiguous, is taken as such to fit the value of critical temperature. Here, T_c is determined experimentally, therefore the chosen $\hbar\omega_{\text{cut}}$ determines the values of the coupling constants, nevertheless without affecting the curvature of the theoretical $\Delta_{L,S}(T)$ fits. Under ω_{cut} variation, the unchanged also remain $[2\Delta_S/k_B T_c]^{\text{eigen}}$, α , and β : Being the manually adjustable parameters, they are determined in terms of the best fit to the experimental data. Significantly varying the cutoff energy, $\hbar\omega_{\text{cut}}$ even by $\pm 25\%$, we get the T_L^{eigen} deviation $\pm 6\%$, which remains almost stable. The only value notably modified under such $\hbar\omega_{\text{cut}}$ change is the eigen critical temperature of the small gap: Its variation is nonlinear and appears as high as -30% to $+40\%$, thus making the absolute value of T_S^{eigen} ambiguous.

C. Resonant coupling with a bosonic mode

Besides the parent SGS, in the most qualitative dynamic conductance spectra, we resolved a fine structure caused by a resonant boson emission along with MAR process. Figure 5 shows CVC and $dI(V)/dV$ curves for two sequentially formed Andreev arrays, with clear SGS for the large gap (gray vertical lines). The lower inset shows an excess Andreev current taken as $I(V) - I^{\text{Ohmic}}(V)$. The intensive dips at bias voltages 19.2, 10.3, 6.9, and 5.1 meV well satisfy Eq. (1) (accounting for the first dip slightly shifted toward less bias). The dip positions versus $1/n$ (circles in the inset) follow a line passing through the origin and determine $\Delta_L \approx 10.3$ meV.

Accounting for the dip at 5.1 mV is more pronounced than that at 6.9 mV, it could be attributed to the first dip $n_S = 1$ of the small gap $\Delta_S \approx 2.6$ meV. In that case, the absent higher-order Δ_S subharmonics ($n_S = 2$ dip is expected at 2.6 mV) could be considered as masked by a strong foot. Nonetheless, the supposed Δ_S value appears about 1.4 times larger than that extracted from Figs. 2 and 3, thus such attribution is ambiguous. Instead, we interpret the dip at 5.1 mV as relating to the large gap SGS ($n_L = 4$), whereas the beginning of the foot seems to intensify this dip as matching its position.

Accompanying the SGS for the Δ_L , less intensive dips at $V_{\text{res}} \approx 28.4, 15.8$ mV appear in Fig. 5, which resembles a typical fine structure observed in precedent IMARE probes with

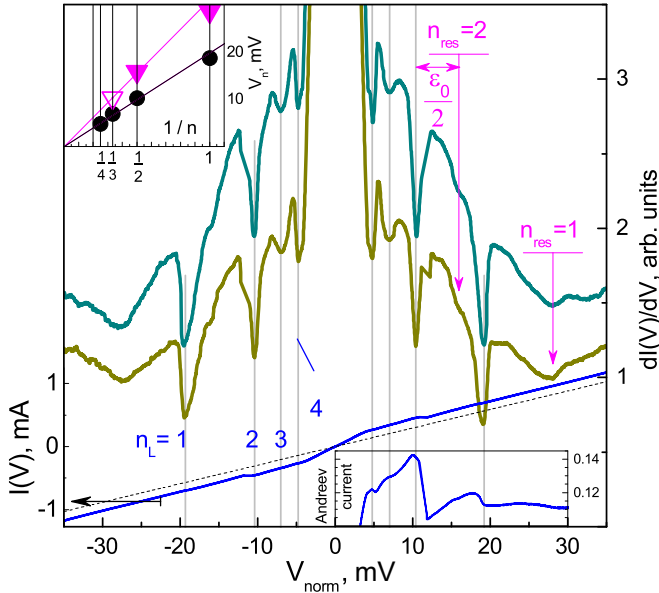


FIG. 5. Dynamic conductance spectra (right scale) measured at $T = 4.2$ K for Andreev arrays ($m = 14$ junctions). $V_{\text{norm}} \equiv V_{\text{array}}/14$. Gray lines and $n_L = 1 - 4$ labels indicate the subharmonic gap structure dips for the large gap $\Delta_L \approx 10.3$ meV. Vertical arrows point to the fine structure dips caused by resonant emission of bosons with energy $\varepsilon_0 = 10.5 - 11.0$ meV. CVC at $T = 4.2$ K (blue line, left scale) and its simulation at T_c (dashed line) are shown for comparison; the Andreev current component is presented in the lower inset. The upper inset shows the position of gap features (circles) and fine structure (triangles) versus their inverse number. Solid lines are guidelines.

Gd and Sm-based oxypnictides [49,50]. The satellite position is independent of the constriction dimension or resistance, and thus possibly originates from a resonant coupling with a characteristic bosonic mode. Earlier we showed [49,50] that the fine structure cannot be caused by an electron-phonon interaction or Leggett mode.

The satellite position (vertical arrows) in dependence of the inverse number is shown in the inset (triangles). The boson energy harmonics ε_0/n are therefore the “distances” between each satellite and the parent SGS dip [Eq. (3)]. Accounting for the first Δ_L dip shifts to bias lower than $2\Delta/e$, which possibly entails nonlinear shifting of the first bosonic resonance feature ($n_{\text{res}} = 1$ in the main panel of Fig. 5), it would be more correct to probe $V_{\text{res}2} - V_{n_L=2} \equiv \varepsilon_0/2$ (double arrow in Fig. 5) to estimate the boson energy $\varepsilon_0 = 10.5 - 11.0$ meV. Extrapolating the obtained $V_{\text{res}}(1/n)$ dependence, we get the expected position ≈ 10 mV of the third satellite (open triangle in the inset), which fits the position of the second gap subharmonic $n_L = 2$. Such overlapping seems the reason for $n_{\text{res}} = 3$ being unresolved as a distinct feature.

The estimated boson energy at $T \rightarrow 0$ is less than the indirect gap $\varepsilon_0 < \Delta_L(0) + \Delta_S(0)$, and, in accordance with theory [18,19], supports a spin-exciton nature of the observed boson. The energy which similarly fulfills the resonance condition was extracted by us earlier in other 1111 compounds within a wide range of critical temperatures [49,50]. The measurements of the temperature dependence $\varepsilon_0(T)$ are necessary to

clarify the nature of this phenomenon. Also, further studies are needed to check the result reproducibility.

D. Discussion

Summarizing the experimental data, our IMARE studies of Nd-1111H unambiguously show a presence of the bulk superconducting order parameter $\Delta_L = 10.45 \pm 0.15$ meV. Its characteristic ratio 5.0–5.4 joins the large statistics for oxypnictides with substitution sites in the spacer, collected by us earlier [28,45].

Some $dI(V)/dV$ measured with Nd-1111H demonstrate a second set of Andreev features at lower bias, which could be referred to as SGS for the small gap $\Delta_S \approx 1.8$ meV. Although the small gap features are poorly observed in the $dI(V)/dV$ spectra, several arguments could be shown pro and contra to the presence of the second superconducting condensate with Δ_S order parameter:

(1) If the observed Δ_L were a single order parameter, its temperature dependence would be trivial. On the contrary, reproducibly observed curvature starting at ≈ 12 K (Fig. 4) cannot be simulated in any conventional single-gap model. In principle, the only way to reproduce the curved $\Delta(T)$ within a single-gap approach is as follows. Relying on the ARPES data [9,10], an existence of the flat bands in the vicinity of E_F seems plausible, with extremely high carrier effective mass and DOS. Such nontrivial band structure could be sensitive not only to doping, but also to the temperature. In the superconducting state, such possible band shifting would cause a DOS at E_F temperature dependence $N_0(T)$. Even weak $N_0(T)$ alteration would result in relatively strong temperature dependence $\lambda(T)$, thus making it not a constant (always eliminated in conventional models) and providing unconventional behavior of the superconducting gap even within a single-gap approach.

(2) On the other hand, the obtained temperature dependencies (Fig. 4) are natural for the conventional two-gap model. In this framework, the reason for the curved $\Delta_L(T)$ is a cooperation of $N_S/N_L > 1$ and a moderate interband interaction in the momentum space with a “driven” superconducting condensate.

(3) In general, it is the Δ_S band contribution to Andreev conductivity which manages the observability of the small gap SGS in $dI(V)/dV$ spectrum. Evanescent band structure supposed near the Fermi level [9,10] is generally followed with low carrier concentration and possibly high DOS. In this sense, poorly observable SGS of the small gap may result from a lower concentration or mean free path for carriers from those bands, as compared with the bands where Δ_L develops.

From the experimentalist point of view, only the reproducible observation of the small gap features seems a key to the above-mentioned issue.

The outlined ambiguity in the small gap of Nd-1111H resembles the situation with other optimally doped oxypnictides having similar critical temperatures, studied previously [27,28,45]. We showed that faintly discernible in optimally doped (Sm,Th)OFeAs, the Δ_S Andreev features become more pronounced for underdoped samples as critical temperature decreases; with it, the small gap magnitude scales with T_c along with the large gap [28].

IV. CONCLUSIONS

By using IMARE spectroscopy, we probed the structure of the superconducting order parameter in polycrystalline samples of hydrogen-substituted $\text{NdFeAsO}_{0.6}\text{H}_{0.36}$ compounds with a critical temperature $T_c = 45 - 48$ K. At 4.2 K, we determined the two bulk superconducting gaps: The large gap $\Delta_L \approx 10.4$ meV, and a possible small gap $\Delta_S \approx 1.8$ meV. Supposing a two-gap scenario, the temperature dependence of the gaps could be fitted within a renormalized BCS two-band approach. We estimate that the large gap condensate is in a weak coupling limit, while a moderate pairing is developed in the bands with the small gap. The interband constant $\lambda_{LS} \approx 0.5$ dominates over the other pairing channels. Additionally, we revealed a resonant coupling of the Andreev current with a characteristic bosonic mode with energy $\varepsilon_0 = 10.5 - 11.0$ meV $< \Delta_L + \Delta_S$ at $T = 4.2$ K.

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APPENDIX: IMARE SPECTROSCOPY DETAILS

When cracking a sample with a layered crystal structure, array contacts are naturally developed on the steps and terraces of the cryogenic cleft. Although spectroscopy of such stacks seems rather advantageous, as compared with single junction study, one more intermediate purpose arises, namely, to determine the number of junctions in each formed array. Primarily, to solve this problem, large data statistics is essential. Above it was mentioned that the raw position of the Andreev feature becomes scaled by a factor of natural but accidental m , hence, the raw $dI(V)/dV$ spectrum provides

$\Delta \cdot m$ energy value. The details of the Δ value extraction from the raw experimental data are presented in Figs. 6(a)–6(f).

One possible way is to arrange in ascending order the positions of the second Andreev feature $V_{n_L=2} = m\Delta_L/e$ in the obtained raw $dI(V)/dV$ spectra, then to assign them natural numbers to get a straight line crossing the origin [Fig. 6(a)]. Of course, the obtained points should be held above the BCS-limit line $1.76k_B T_c$. For such $V_n(m)$ estimate, the position of the second ($n = 2$) Andreev subharmonic seems more suitable since exactly corresponding Δ (by contrast, the position of the first subharmonic could be a bit lower $2\Delta/e$ [32,33]). Figure 6(a) shows the dependence of raw $n_L = 2$ positions versus the selected m numbers well-fitted with a line.

In Fig. 6(c), the extracted values of Δ_L are shown [i.e., the raw position shown in Fig. 6(a) divided by the selected m]. Each bar represents a certain array, with the bar height corresponding to the number of junctions in the array. Remarkably, the selected set of m provides the gap value uncertainty less than 2%, thus proving the selected m set is correct. Noteworthy, there is no correlation between the gap value and the corresponding m , which indicates a bulk nature of the extracted order parameter.

For comparison, the gap values to be obtained when using another sets of m are shown in Figs. 6(d)–6(f). Figure 6(d) depicts the gap distribution Δ_L^* to be obtained when assuming the $m = 2$ junction array to be a single junction with $m_{\text{even}}^* = m/2$ (gray bars), $m_{\text{odd}}^* = m/2 \pm 0.5$ (horizontally and diagonally dashed bars, respectively). Under such normalizing, the contacts with even m provide reproducible and nonscattered but double Δ_L value (gray bars), whereas the odd m numbers are to be rounded, thus providing ambiguous gap value (dashed bars). Figures 6(e) and 6(f) expose the distributions following $m^+ = m + 1$ and $m^- = m - 1$, respectively. Clearly, Figs. 6(e) and 6(f) provide strongly scattered gap values, with obvious tendency $(\Delta_L^+, \Delta_L^-) \rightarrow \Delta_L$ with $m^{+,-}$ increase Figs. 6(d) and 6(e), thus badly supposing the wrong

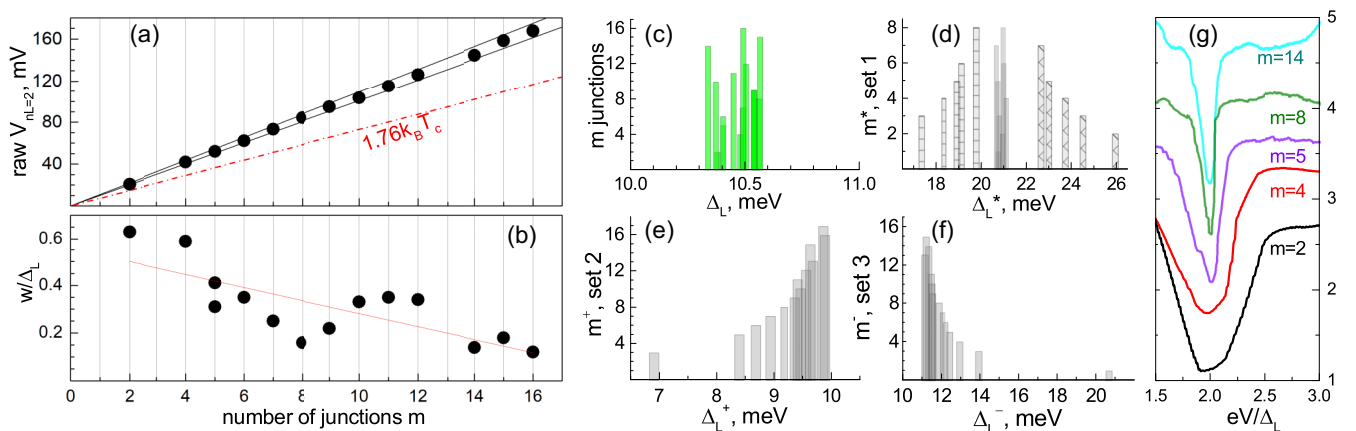


FIG. 6. (a) The raw positions of the second Andreev subharmonic $V_{n_L=2} = \Delta_L/e$ in the obtained $dI(V)/dV$ spectra versus the congruent m numbers of junctions in the stack. The dash-dot line designates the BCS limit $1.76k_B T_c$ below which the experimental points not to be. (b) The half width of the main $n_L = 1$ Andreev dips normalized to Δ_L in dependence on the number of junctions. Solid line is a guideline. The extracted $\Delta_L = 10.45 \pm 0.15$ meV values are shown in (c). For comparison, the large gap values to be obtained when the raw $V_{n_L=2}$ are normalized with other sets of $m_{\text{even}}^* = m/2$ (gray bars), $m_{\text{odd}}^* = m/2 \pm 0.5$ (horizontally and diagonally dashed bars, respectively), $m^+ = m + 1$, and $m^- = m - 1$, are shown in (e)–(f) panels. The bar height corresponds to the chosen m . (g) The main Andreev dips ($n_L = 1$) observed at $2\Delta_L/e$ bias in the representative spectra of Andreev arrays with various m . The $dI(V)/dV$ curves are shifted vertically for clarity; monotonic background was suppressed.

Δ_L^{\pm} correlation with the array properties. Thereby, the m set derived from Figs. 6(a) and 6(b) was used to normalize the $dI(V)/dV$ spectra shown in Figs. 1, 2, and 5.

It is noteworthy to compare the shape of the Andreev dip in the spectra of arrays with various m . Figure 6(b) shows the half width w of the main $n_L = 1$ dips in the obtained Andreev spectra versus the corresponding number of junctions. To compare the data, it is reasonable to normalize w by $\Delta_L(0)$ value or $k_B T_c$ to account for even its minor variation from one contact point to another. The data spread modulating the general decrease could be caused by a broadening parameter Γ which is, no doubt, different for each contact. Nonetheless, the covering tendency is that the larger the m , the narrower the Andreev dips in the $dI(V)/dV$ spectrum [the tendency is shown in Fig. 6(b) by a line].

A representative sample of the dip sharpening in the large- m arrays is shown in Fig. 6(g). The fragments of $dI(V)/dV$ curves with the first ($n_L = 1$) gap feature are put together and shifted vertically for clarity; the position of the dip was normalized by a factor of Δ_L/e . Such sharpening seems unsurprising since in the arrays with large m , the contribution of the bulk rather than surface to the conductance becomes more significant.

Accordingly, on the one hand, the study of arrays is preferable since it facilitates an observation of the bulk order parameter. On the other hand, measuring the dynamic conductance of the arrays with less m is favorable as well to determine the gap magnitude and correct set of m [see Figs. 6(c)–6(f)]. However wide the Andreev feature is, the dip position which directly scales with Δ is unaffected.

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