# **Spin fluctuation anisotropy as a probe of orbital-selective hole-electron quasiparticle excitations in detwinned Ba(** $Fe_{1-x}Co_x$ **)<sub>2</sub>As<sub>2</sub>**

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We use inelastic neutron scattering to study spin excitation anisotropy in mechanically detwinned Ba( $Fe_{1-x}Co_{x}$ )<sub>2</sub>As<sub>2</sub> with  $x = 0.048$  and 0.054. Both samples exhibit a tetragonal-to-orthorhombic structural transition at  $T_s$ , a collinear static antiferromagnetic order at wave vector  $\mathbf{Q}_1 = \mathbf{Q}_{AF} = (1, 0)$  below the Néel temperature  $T_N$ , and superconductivity below  $T_c$  ( $T_s > T_N > T_c$ ). In the high-temperature paramagnetic tetragonal phase  $(T \gg T_s)$ , spin excitations centered at  $\mathbf{Q}_1$  and  $\mathbf{Q}_2 = (0, 1)$  are gapless and have fourfold  $(C_4)$  rotational symmetry. On cooling to below  $T_N$  but above  $T_c$ , spin excitations become highly anisotropic, developing a gap at **Q**<sup>2</sup> but still are gapless at **Q**1. Upon entering into the superconducting state, a neutron spin resonance appears at **Q**<sup>1</sup> with no magnetic scattering at **Q**2. By comparing these results with those from angle-resolved photoemission spectroscopy experiments, we conclude that the anisotropic shift of the  $d_{yz}$  and  $d_{xz}$  bands in detwinned Ba(Fe1−*<sup>x</sup>*Co*<sup>x</sup>* )2As2 below *Ts* is associated with the spin excitation anisotropy, and the superconductivity-induced resonance arises from the electron-hole Fermi surface nesting of quasiparticles with the  $d_{yz}$  orbital characters.

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## **I. INTRODUCTION**

Unconventional superconductors such as copper oxides, iron pnictides, and heavy fermions are interesting because superconductivity in these materials is derived from their longrange antiferromagnetic (AF) ordered parent compounds [\[1\]](#page-7-0). Although there is no consensus on the microscopic origin of superconductivity, there is increasing evidence that electron pairing in these superconductors is mediated by spin fluctuations (excitations)  $[1-5]$ . In particular, superconductivity is intertwined with magnetic degrees of freedom, and forms a state coexisting with the static AF order in the underdoped regime [\[1–5\]](#page-7-0). Therefore, to understand the fundamental interactions that lead to unconventional superconductivity, it is important to investigate how magnetism interacts with superconductivity in the coexisting regime of unconventional superconductors.

In the case of Co-underdoped iron pinictide superconductors such as  $Ba(Fe_{1-x}Co_x)_2As_2$  with  $0.03 < x < 0.065$ , they exhibit a tetragonal-to-orthorhombic structural transition at  $T_s$ , a collinear static AF order below the Néel temperature  $T_N$ , and superconductivity below  $T_c$  ( $T_s > T_N > T_c$ ) as shown in Fig.  $1(a)$  [\[6](#page-7-0)[–11\]](#page-8-0). As a function of decreasing temperature, a collinear static AF order is established below  $T_N$ at wave vector  $\mathbf{Q}_1 = \mathbf{Q}_{AF} = (1, 0)$  [inset in Fig. [1\(a\)\]](#page-1-0). On further cooling across  $T_c$ , the static ordered moment decreases below  $T_c$  accompanied by the formation of a neutron spin

resonance coupled to superconductivity [\[9–12\]](#page-8-0). For optimally and overdoped  $Ba(Fe_{1-x}Co_x)_2As_2$ , where their  $T_s$  and  $T_N$  are suppressed and the system is in the paramagnetc tetragonal state, neutron spin resonance occurs at wave vectors  $Q_1$  =  $(1, 0)$  and  $\mathbf{Q}_2 = (0, 1)$ , and therefore obeys fourfold rotational  $(C_4)$  symmetry of the underlying tetragonal lattice  $[13-16]$ . While superconductivity clearly competes with static AF order in underdoped  $Ba(Fe_{1-x}Co_x)_2As_2$  [\[9–11\]](#page-8-0), much is unclear concerning how the superconductivity-induced neutron spin resonance interacts with spin waves from the AF-ordered phase. Although the collinear AF order and associated lowenergy spin waves should have twofold rotational  $(C_2)$  symmetry below  $T_N$ , the observed resonance and spin waves have the  $C_4$  symmetry from the presence of twin domains of the orthorhombic phase below  $T_s$  [\[9–11\]](#page-8-0). Therefore, to understand the interplay between spin waves associated with static AF order and the neutron spin resonance connected with superconductivity, one must carry out inelastic neutron scattering experiments on detwinned samples with static AF order and superconductivity.

In this paper, we report comprehensive inelastic neutron scattering experiments designed to study spin excitations in detwinned Ba(Fe<sub>1−*x*</sub>Co<sub>*x*</sub>)<sub>2</sub>As<sub>2</sub> with coexisting AF order and superconductivity. From the phase diagram of Ba(Fe<sub>1−*x*</sub>Co<sub>*x*</sub>)<sub>2</sub>As<sub>2</sub> in Fig. [1\(a\)](#page-1-0) established from our own and previous transport work  $[11]$ , we know that static AF order decreases with increasing Co doping, and competes with superconductivity, which increases with increasing Co doping  $[9-11]$ . To study the interplay of spin waves associated with the static AF order and resonance connected

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FIG. 1. (a) The phase diagram of  $Ba(Fe_{1-x}Co_x)_2As_2$  with the arrows indicating the Co-doping concentrations of our samples  $(x = 0.048$  and 0.054). The left-hand inset shows a schematic of the collinear AF ordering of the Fe spins in real space and the applied uniaxial pressure direction is marked by vertical arrows. The righthand inset is the corresponding reciprocal space map showing the AF ordering wave vector  $\mathbf{Q}_1$  (green) and wave vector  $\mathbf{Q}_2$  (red). The filled hexagonal and circular points represent  $T_s$  and  $T_N$ , respectively, obtained from resistance measurements. The filled and open square points mark  $T_c$  determined from the resistance and magnetic susceptibility measurements, and from Ref. [\[11\]](#page-8-0). Schematic Fermi surfaces of underdoped Ba(Fe1−*<sup>x</sup>*Co*<sup>x</sup>* )2As2 in (b) paramagnetic tetragonal state and (c) nematic state below  $T<sub>s</sub>$ . The red, green, and blue colors represent  $d_{xz}$ ,  $d_{yz}$ , and  $d_{xy}$  orbitals, respectively. The arrows mark nesting wave vectors  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$  between the *Z* and *X*/*Y* points. Our definition of the  $X/Y$  is switched from that of the ARPES work [\[29\]](#page-8-0). The normalized temperature-dependent resistance data indicate the superconducting transition temperatures of (d)  $x = 0.048$  and (e)  $x = 0.054$ .

with superconductivity, one must judiciously choose the Co-doping concentrations where the strength of the spin waves is comparable with the superconductivity-induced resonance [\[17,18\]](#page-8-0). For this purpose, we prepared single crystals of Ba(Fe<sub>1−*x*</sub>Co<sub>*x*</sub>)<sub>2</sub>As<sub>2</sub> with *x* = 0.048 and 0.054 [\[7](#page-7-0)[–9\]](#page-8-0). At zero external uniaxial pressure  $[19-22]$ , the  $x = 0.048$  samples have  $T_c = 18$  K,  $T_N = 52$  K, and  $T_s = 63$  K [Fig. 1(d)], and



FIG. 2. (a) Elastic rocking curve scans of the sample angle (A3) around  $Q_1 = (1, 0, 1)$  and  $Q_2 = (0, 1, 1)$  in uniaxial strained  $Ba(Fe_{0.952}Co_{0.048})_2As_2$ . The double peaks show the sample has two major domains separated by about 4.5◦. (b) Temperature differences of the transverse scans around  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$  in uniaxial strained  $Ba(Fe_{0.946}Co_{0.054})_2As_2.$ 

0.054 crystals have  $T_c = 21$  K,  $T_N = 38$  K, and  $T_s = 53$  K [Fig.  $1(e)$ ]. Upon detwinning these crystals using a device similar to previous work with about 40 MPa uniaxial pressure  $[23,24]$ , the system no longer has a clean  $T_s$  because the  $C_4$  rotational symmetry in the tetragonal phase is already broken by the applied pressure and  $T_N$  increases several K under pressure consistent with the earlier work [\[19–22\]](#page-8-0). We carried out inelastic neutron scattering measurements on nearly 100% detwinned Ba(Fe<sub>1−*x*</sub>Co<sub>*x*</sub>)<sub>2</sub>As<sub>2</sub>. In the normal state above  $T_c$  but below  $T_N$ , spin excitations are gapless and increase with increasing energy at the AF ordering wave vector  $Q_1$  = (1, 0), but have a ~12 meV gap at  $Q_2$  = (0, 1) [see inset in Fig. 1(a)], showing strong magnetic anisotropy. On cooling to below  $T_c$ , a neutron spin resonance at  $E_r$  and a spin gap at energies below  $E_r$  are formed at  $\mathbf{Q}_1 = (1, 0)$ , but there is no superconductivity-induced magnetic scattering at  $\mathbf{Q}_2 =$ (0, 1). On warming to temperatures slightly above the finite pressure  $T_N$ , the spin excitations are still anisotropic, showing much strong scattering at  $\mathbf{Q}_1 = (1, 0)$ . Finally, on warming to temperatures well above  $T_N$  and zero pressure  $T_s$ , spin excitations become the same at  $\mathbf{Q}_1 = (1, 0)$  and  $\mathbf{Q}_2 = (0, 1)$ , and obey the  $C_4$  rotational symmetry. By comparing these results with those from angle-resolved photoemission spectroscopy (ARPES) experiments [\[25–30\]](#page-8-0), we conclude that the anisotropic shift of the  $d_{yz}$  and  $d_{xz}$  bands of the electron Fermi

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FIG. 3. (a) Constant-**Q** scans at  $\mathbf{Q}_1$  below and above  $T_c$  in  $Ba(Fe_{0.952}Co_{0.048})_2As_2$ . The resonance is seen as intensity gain below  $T_c$  around  $E_r \approx 5.5$  meV. The gray data points represent the background scattering. (b) Identical scans at **Q**2. (c), (d) Background subtracted constant-**Q** scans below and above  $T_c$  at the  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$ points. The vertical arrow indicates the position of the neutron spin resonance.

pockets at the *X* and *Y* points in detwinned  $Ba(Fe_{1-x}Co_x)_2As_2$ below  $T_s$  is associated with the spin excitation anisotropy, and the superconductivity-induced resonance arises from the electron-hole Fermi surface nesting of quasiparticles with the  $d_{yz}$  orbital characters along the  $Q_1$  direction as shown schematically in Fig. [1\(c\).](#page-1-0)



FIG. 4. Constant-energy scans in  $Ba(Fe_{0.952}Co_{0.048})_2As_2$  below and above  $T_c$  with  $E_r = 5.5$  meV along the [H, 0, 1] and [0, K, 1] directions around (a)  $\mathbf{Q}_1$  and (b)  $\mathbf{Q}_2$ .



FIG. 5. Two-dimensional images of the spin excitations of  $Ba(Fe_{0.946}Co_{0.054})_2As_2$  within the [*H*, *K*] plane below and above  $T_c$  at energies of (a), (b)  $E = 5 \pm 1$  meV; (c), (d)  $E = 8 \pm 1$  meV; (e), (f)  $E = 12 \pm 1$  meV. The vertical color bars indicate scattering intensity in arbitrary units.

#### **II. EXPERIMENTAL RESULTS**

Our neutron scattering experiments were carried out on the FLEXX cold neutron three-axis spectrometer at Helmholtz Zentrum Berlin, Germany, and the MERLIN neutron timeof-flight (TOF) chopper spectrometer at ISIS, Rutherford-Appleton Laboratory, UK  $[31]$ . The detwinning ratio for  $Ba(Fe_{0.946}Co_{0.054})_2As_2$  samples used at ISIS was measured on the EIGER thermal neutron three-axis spectrometer at Paul Scherrer Institute, Switzerland. Sizable single crystals of Ba( $Fe_{1-x}Co_x$ )<sub>2</sub>As<sub>2</sub> were grown by self-flux method and cut along the *a*- and *b*-axis directions of the orthorhombic lattice below  $T_s$  [\[4\]](#page-7-0). Each cut sample was mounted on a specially designed aluminum-based sample holder with uniaxial pressure applied along the *b*-axis direction [\[23,24\]](#page-8-0). The total mass of our samples is  $\sim$ 2.5 g for the *x* = 0.048 used for FLEXX experiment,  $\sim$ 3.6 g for the *x* = 0.054 used for MERLIN and EIGER experiments. The momentum transfer **Q** in three-dimensional reciprocal space is defined as  $\mathbf{Q} =$  $Ha^* + Kb^* + Lc^*$ , where *H*, *K*, and *L* are Miller indices and **a**<sup>\*</sup> =  $\hat{\bf{a}} \cdot 2\pi/a$ , **b**<sup>\*</sup> =  $\hat{\bf{b}} \cdot 2\pi/b$ , **c**<sup>\*</sup> =  $\hat{\bf{c}} \cdot 2\pi/c$  with *a* = 5.615 Å,  $b = 5.573$  Å, and  $c = 12.95$  Å in the low-temperature orthorhombic state  $[9-11]$ . In this notation, the AF order occurs at the in-plane wave vector  $\mathbf{Q}_{AF} = (1, 0)$ , and there should be no elastic magnetic scattering at wave vector (0,1).

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FIG. 6. Two-dimensional images of magnetic scattering in  $Ba(Fe_{0.946}Co_{0.054})_2As_2$  along the [1, K] and [H, 1] directions at temperatures (a), (b) 4.6 K; (c), (d) 23 K; (e), (f) 60 K; (g), (h) 100 K. The incident beam energy is  $E_i = 25$  meV and the partial detwinning ratio of the sample has been corrected for.

For measurements on three-axis spectrometers, we aligned the samples in the  $[1, 0, 1] \times [0, 1, 1]$  scattering plane where we can measure the static magnetic order and excitations at both  $Q_{AF} = Q_1 = (1, 0, 1)$  and  $Q_2 = (0, 1, 1)$  simultaneously  $[23]$ . The fixed final neutron energies are  $E_f = 5$  and 14.7 meV for FLEXX and EIGER experiments, respectively. For experiments on TOF spectrometer MERLIN, the direction of the incident beam is parallel to the *c* axis. Using multi-*Ei* mode with a primary incident neutron beam energy of  $E_i$  = 80 meV and Fermi chopper frequency of  $\omega = 250$  Hz, we were able to measure with two additional incident energies of 25 and 12 meV, thus allowing spin excitations up to  $E < 70$  meV to be probed.

Figure  $1(a)$  shows the phase diagram of electron-doped  $Ba(Fe_{1-x}Co_x)_2As_2$  as determined from our transport measurements. Consistent with previous work [\[7\]](#page-7-0), we find that the ratio between the actual and nominal Co-doping level is about 0.74. For the experiments, we chose  $Ba(Fe_{1-x}Co_x)_2As_2$ with Co-doping levels  $x = 0.048$  and 0.054 as marked by vertical arrows in Fig.  $1(a)$ . Figures  $1(b)$  and  $1(c)$  show Fermi surfaces of underdoped  $Ba(Fe_{1-x}Co_x)_2As_2$  with coexisting AF order and superconductivity above and below the zero pressure  $T_s$ , respectively, as obtained from ARPES experiments on uniaxial pressure detwinned samples [\[25–30\]](#page-8-0). The temperature dependence of the normalized resistance for  $Ba(Fe_{0.952}Co_{0.048})_2As_2$  and  $Ba(Fe_{0.946}Co_{0.054})_2As_2$  reveals superconducting transition temperatures of  $T_c = 18$  and 21 K, respectively [Figs.  $1(d)$  and  $1(e)$ ].

In order to carry out inelastic neutron scattering experiments on detwinned  $Ba(Fe_{0.952}Co_{0.048})_2As_2$  and  $Ba(Fe_{0.946}Co_{0.054})_2As_2$ , one must mount crystals in a uniaxial detwinning device and apply uniaxial pressure along one axis of the orthorhombic lattice to detwin the

samples [see inset of Fig.  $1(a)$ ]. For fully detwinned samples, one would expect to observe magnetic Bragg intensity at  $\mathbf{Q}_1$  but no magnetic signal at  $\mathbf{Q}_2$ . Figures  $2(a)$ and  $2(b)$  show the background-subtracted rocking curve elastic scans around  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$  for Ba(Fe<sub>0.952</sub>Co<sub>0.048</sub>)<sub>2</sub>As<sub>2</sub> and  $Ba(Fe_{0.946}Co_{0.054})_2As_2$ , respectively. While the Ba(Fe<sub>0.952</sub>Co<sub>0.048</sub>)<sub>2</sub>As<sub>2</sub> sample is ~100% detwinned, there is a weak peak at  $\mathbf{Q}_2 = (0, 1, 1)$  for  $Ba(Fe_{0.946}Co_{0.054})_2As_2$ . Defining the detwinning ratio as  $\eta = (I_{10} - I_{01})/(I_{10} + I_{01})$ , where  $I_{10}$  and  $I_{01}$  are magnetic Bragg scattering at  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$ , respectively [\[32,33\]](#page-8-0), we find that Ba(Fe<sub>0.946</sub>Co<sub>0.054</sub>)<sub>2</sub>As<sub>2</sub> has a detwinning ratio of  $\eta \approx 85\%$ . Using the measured  $\eta$ , we can estimate the intrinsic magnetic scattering at  $\mathbf{Q}_1$ and **Q**<sup>2</sup> for different energy transfers, and thus determine the energy dependence of the magnetic scattering at these wave vectors and the related dynamic magnetic susceptibility  $\chi''({\bf Q}, E)$  [\[32,33\]](#page-8-0).

We first present our inelastic neutron scattering results for Ba(Fe<sub>0.952</sub>Co<sub>0.048</sub>)<sub>2</sub>As<sub>2</sub>. Figures  $3(a)$  and  $3(b)$  show the constant-**Q** scans at  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$  below and above  $T_c$ , as well as background scattering at wave vectors transversely rotated ∼15◦ from **Q**<sup>1</sup> and **Q**2. At **Q**1, the scattering increases with increasing energy, and superconductivity induces a resonance at  $E_r \approx 5.5$  meV below  $T_c$  [Fig. [3\(a\)\]](#page-2-0). Figure [3\(c\)](#page-2-0) shows background-subtracted scattering, suggesting that superconductivity opens a spin gap below about 2 meV. At **Q**2, we find no discernible signal above the background scattering both below and above  $T_c$ , suggesting the presence of a large spin gap in the normal state and that superconductivity does not induce any magnetic intensity [Fig.  $3(b)$ ]. The background-subtracted scattering in Fig. [3\(d\)](#page-2-0) suggests a spin gap of  $\sim$ 7 meV in both the normal and superconducting states, with detectable magnetic scattering above 8 meV. To further confirm these

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FIG. 7. The energy/*c*-axis wave-vector dependence of the spin excitations around the in-plane wave vector  $\mathbf{Q}_1$  (green) and  $\mathbf{Q}_2$  (red) positions at temperatures (a) 4.6 K, (b) 23 K, (c) 60 K, (d) 100 K. The incident beam energy is  $E_i = 25$  meV, and the vertical arrows indicate the energy values with integer *L*. The partial detwinning ratio has been corrected for.

results, we show in Figs.  $4(a)$  and  $4(b)$  constant-energy scans at  $E_r = 5.5$  meV at  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$ , respectively. While there is a clear magnetic peak centered at  $\mathbf{Q}_1$  that enhances the intensity below  $T_c$ , no discernible peak is seen at  $\mathbf{Q}_2$  below or above  $T_c$ .

The two-dimensional (2D) magnetic scattering images of  $Ba(Fe_{0.946}Co_{0.054})_2As_2$  in the  $(H, K)$  plane for different energy transfers below ( $T = 4.6$  K) and above ( $T = 23$  K)  $T_c$ are shown in Figures [5\(a\),](#page-2-0) [5\(c\),](#page-2-0) [5\(e\)](#page-2-0) and [5\(b\),](#page-2-0) [5\(d\),](#page-2-0) [5\(f\),](#page-2-0) respectively. At  $E = 5 \pm 1$  meV, the scattering is centered around  $\mathbf{Q}_1$  and clearly enhances below  $T_c$ , and there is no scattering at  $\mathbf{Q}_2$  [Figs.  $5(a)$  and  $5(b)$ ]. On increasing energy to  $E = 8 \pm 1$  meV, the situation is similar at  $\mathbf{Q}_1$  but there may be some scattering at  $\mathbf{Q}_2$  [Figs.  $5(c)$  and  $5(d)$ ]. On increasing energy to  $E = 12 \pm 1$  meV, superconductivity has little effect on spin excitations at  $\mathbf{Q}_1$  and there is weak magnetic signal at  $\mathbf{Q}_2$  [Figs. [5\(e\)](#page-2-0) and [5\(f\)\]](#page-2-0).

Figure [6](#page-3-0) summarizes the energy dependence of the spin excitations at  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$  as a function of increasing temperature. The energy dependence of the scattering is obtained by integrating wave vectors  $0.9 < H < 1.1$  around **Q**<sub>1</sub> in Figs. [6\(a\),](#page-3-0) [6\(c\),](#page-3-0) [6\(e\),](#page-3-0) [6\(g\)](#page-3-0) and  $0.9 < K < 1.1$  in Figs.  $6(b)$ ,  $6(d)$ ,  $6(f)$ , and  $6(h)$  around  $Q_2$ . The effect of the partial detwinning ratio was corrected using the method developed in Ref. [\[33\]](#page-8-0). Consistent with Figs. [4](#page-2-0) and [5,](#page-2-0) we find that superconductivity induces a broad resonance (or two resonances) around  $E_r \approx 5$  meV at  $Q_1$  [Figs. [6\(a\)](#page-3-0) and  $6(c)$ ] [\[17,34–37\]](#page-8-0), but has no effect at  $Q_2$  [Figs.  $6(b)$ ] and  $6(d)$ ] [\[38\]](#page-8-0). On warming to 60 K, which is above the zero pressure  $T_N$  and  $T_s$ , there is still clear magnetic excitation anisotropy [Figs.  $6(e)$  and  $6(f)$ ]. Finally, on warming to 100 K, the spin excitations at  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$  become essentially identical with no observable anisotropy.

To accurately determine the dynamic magnetic susceptibility anisotropy, which is associated with spin nematic order [\[39–45\]](#page-8-0) and may be important for superconductivity [\[46,47\]](#page-8-0), we cut the data in Fig. [6](#page-3-0) along the TOF direction, which couples the energy transfer of the spin excitations with *L* modulation. Figures  $7(a)$ – $7(d)$  show the temperature dependence of the magnetic scattering at  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$ . Consistent with earlier work [\[13,14\]](#page-8-0), we find that spin excitations at **Q**<sup>1</sup> have a strong *L* modulation with high magnetic intensity at  $L = 1, 3, \ldots$  [Figs. 7(a)–7(c)]. The spin excitations have a



FIG. 8. (a), (b) The energy dependence of the resonance along the  $\mathbf{Q} = [1, K]$  and [H, 1] directions in Ba(Fe<sub>0.946</sub>Co<sub>0.054</sub>)<sub>2</sub>As<sub>2</sub>. (c)–(h) The wave-vector dependence of the spin resonance at  $E = 5 \pm 1$ ,  $9 \pm 1$ ,  $13 \pm 1$  meV around  $Q_1$ . The vertical and horizontal dashed lines indicate the in-plane momentum integration range used in (a) and (b).

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FIG. 9. (a) Energy dependence of the resonance at **Q**<sup>1</sup> and **Q**<sup>2</sup> obtained by taking temperature differences of the constant-**Q** cuts below and above  $T_c$ . The vertical dashed lines indicate the energy integration range in Figs. [8\(c\)–8\(h\).](#page-4-0) (b) In-plane wave-vector dependence of the magnetic scattering near the resonance energy around **Q**<sup>1</sup> and **Q**2.

gap of about 8 meV at  $\mathbf{Q}_2$  below 23 K [Fig. [7\(b\)\]](#page-4-0), and become gapless and similar to those at  $\mathbf{Q}_1$  around 100 K [Fig. [7\(d\)\]](#page-4-0).

The impact of superconductivity on the spin excitations at **Q**<sup>1</sup> and **Q**<sup>2</sup> can be further evaluated by the temperature differences plot below and above  $T_c$ . Figures  $8(a)$  and  $8(b)$  confirm that superconductivity induces a broad resonance at  $\mathbf{Q}_1$  and has no effect at **Q**2. The in-plane wave-vector dependence of the resonance at  $\mathbf{Q}_1$  in Figs. [8\(c\),](#page-4-0) [8\(e\),](#page-4-0) and [8\(g\)](#page-4-0) reveals no strong evidence of an incommensurate dispersive resonance as seen in electron-doped  $Ba(Fe_{0.963}Ni_{0.037})_2As_2$  [\[48\]](#page-8-0) and holedoped Ba<sub>0.67</sub>K<sub>0.33</sub>(Fe<sub>1−*x*</sub>Co<sub>*x*</sub>)<sub>2</sub>As<sub>2</sub> with *x* = 0 and 0.08 [\[49\]](#page-8-0), possibly due to the fact that  $Ba(Fe_{0.946}Co_{0.054})_2As_2$  is still not close to optimal superconductivity, or our measurements have insufficient in-plane wave-vector resolution to resolve the expected transverse incommensurate scattering  $[48]$ . Figure  $9(a)$ shows the energy dependence of the resonance at  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$ , confirming the results of Figs.  $8(a)$  and  $8(b)$ . The wave-vector dependence of the resonance at different energies is plotted in Fig. 9(b), which again reveals no evidence of incommensurate scattering.

In previous work on nearly optimally doped  $BaFe<sub>1.9</sub>Ni<sub>0.1</sub>As<sub>2</sub> [32]$  $BaFe<sub>1.9</sub>Ni<sub>0.1</sub>As<sub>2</sub> [32]$  and  $BaFe<sub>2</sub>As<sub>2</sub> [24]$  $BaFe<sub>2</sub>As<sub>2</sub> [24]$ , spin excitation anisotropy associated with the spin-driven Ising-nematic phase was defined as  $\delta = (I_{10} - I_{01})/(I_{10} + I_{01})$ , where  $I_{10}$ and  $I_{01}$  are the inelastic magnetic scattering at  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$ , respectively. Here  $\delta$  is not related to the detwinning ratio  $\eta$ ,



FIG. 10. Temperature dependence of the  $E = 5$  meV spin excitations in Ba(Fe<sub>0.946</sub>Co<sub>0.054</sub>)<sub>2</sub>As<sub>2</sub> measured with  $E_i = 25$  meV at (a) 46 K, (b) 60 K, (c) 88 K, (d) 100 K. The scattering intensity has been corrected for the Bose population factor to obtain  $\chi''(\mathbf{Q}, E)$ .

which is determined from elastic magnetic Bragg peaks at **Q**<sup>1</sup> and **Q**<sup>2</sup> in a partially detwinned sample, but a measure of inelastic spin excitation intensity differences between **Q**<sup>1</sup> and  $\mathbf{Q}_2$  for a fully detwinned sample. For BaFe<sub>2</sub>As<sub>2</sub>, the spin excitation anisotropy  $\delta$  extends to about  $E = 180$  meV at 7 K (at zero uniaxial pressure,  $T_N \approx 138$  K), reduces to ~120 meV at 145 K (around pressure induced  $T_N$ ) [\[22\]](#page-8-0) and ~40 meV at 170 K (well above  $T_N$  under pressure), and finally becomes isotropic at 197 K  $[24]$ . In the case of BaFe<sub>1.9</sub>Ni<sub>0.1</sub>As<sub>2</sub>, the spin excitation anisotropy  $\delta$  is nonzero below about  $\sim$ 60 meV at 5 K (where  $T_N \approx T_s \approx 30 \pm 5$  K) and unchanged on warming to 35 K  $[32]$ . Figure 10 shows the temperature dependence of the magnetic scattering at the resonance energy of  $E_r \approx 5$  meV. On warming from 45 to 100 K, the scattering profile clearly changes from  $C_2$  to  $C_4$  symmetric and becomes isotropic.

To quantitatively determine the temperature/energy dependence of the spin excitation anisotropy  $\delta$  in  $Ba(Fe_{0.946}Co_{0.054})_2As_2$ , we estimate the energy dependence of the dynamic susceptibility  $\chi''(\mathbf{Q}, E)$ , which can be calculated by  $\chi''(\mathbf{Q}, E) \propto (1 - e^{-E/k_BT}) \chi'(\mathbf{Q}, E)$ , at  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$  as a function of increasing temperature. Figure  $11(a)$ shows the energy dependence of  $\chi''(\mathbf{Q}_1, E)$  and  $\chi''(\mathbf{Q}_2, E)$ at  $T = 4.5$  K, revealing magnetic anisotropy below about 30 meV. Each point of  $\chi''({\bf Q}, E)$  is obtained by integrating the magnetic scattering over wave vectors  $-0.05 < H < 0.05$ and  $-0.05 < K < 0.05$  around  $\mathbf{Q}_1$  or  $\mathbf{Q}_2$ . On warming to  $T = 23$  K [Fig. [11\(b\)\]](#page-6-0), 46 K [Fig. [11\(c\)\]](#page-6-0), 60 K [Fig. [11\(d\)\]](#page-6-0), 78 K [Fig.  $11(e)$ ], and 100 K [Fig.  $11(f)$ ], the spin excitation anisotropy gradually decreases and finally vanishes at 100 K. Figure  $11(g)$  shows the energy dependence of the spin excitation anisotropy  $\delta$  at different temperatures. Since Ba(Fe<sub>0.946</sub>Co<sub>0.054</sub>)<sub>2</sub>As<sub>2</sub> has  $T_N \approx 38$  K similar to nearly optimal electron-doped BaFe<sub>1.9</sub>Ni<sub>0.1</sub>As<sub>2</sub> with  $T_N \approx 30$  K [\[32\]](#page-8-0), one would expect similar spin excitation anisotropy in  $Ba(Fe<sub>0.946</sub>Co<sub>0.054</sub>)<sub>2</sub>As<sub>2</sub> and BaFe<sub>1.9</sub>Ni<sub>0.1</sub>As<sub>2</sub>, as confirmed by$ 

 $(a)$ 4.6K  $x = 0.054$ 

п

ſ.

(c) 46K  $x = 0.054$ 

(e)

Energy (meV) Energy (meV)

I

I

 $(1,0,L)$  $(0.1, L)$ 

 $(1,0,L)$  $(0,1,L)$ 

 $(1,0,L)$  $(0,1,L)$  78K  $x = 0.054$ 

0 10 20 30 40 50 60

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<span id="page-6-0"></span>,E)(a.u.)  $X''$  $(Q, E)$  x

χ''(Q,E)(a.u.) (χ''10-χ''01)/(χ''10+χ''01) χ''(Q,E)(a.u.) χ''(Q,E)(a.u.)

 $('(Q,E)(a.u.)$ 

-0.4 -0.2 0 0.2 0.4  $\frac{1}{2}$  0.6 0.8 1 1.2



comparing Fig. 11(g) and Fig. 4 of Ref. [\[32\]](#page-8-0). The magnetic anisotropy is clearly present above the pressure induced  $T_N$ .

### **III. DISCUSSION AND CONCLUSION**

To understand our neutron scattering results in terms of the electron-hole Fermi-surface nesting picture [\[50,](#page-8-0)[51\]](#page-9-0), we consider electron and hole Fermi surfaces of uniaxial pressure detwinned  $Ba(Fe_{1-x}Co_x)_2As_2$  above and below  $T_s$  as determined from ARPES measurements [\[25,26,29,30\]](#page-8-0). In the paramagnetic tetragonal state above  $T_s$ , the hole Fermi surfaces near  $\Gamma$  and *Z* points are composed of  $d_{xy}$  and degenerate  $d_{xz}/d_{yz}$ 

orbitals, respectively. If low-energy spin excitations arise from quasiparticle excitations between the hole-electron Fermi surfaces as suggested in an itinerant picture of magnetism and superconductivity [\[50](#page-8-0)[–52\]](#page-9-0), the electron-hole Fermi surface nesting of the  $d_{yz}$  and  $d_{xz}$  orbital quasiparticles are along the  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$  directions, respectively. Since a  $d_{xy}$  orbital has *C*<sup>4</sup> symmetry, it cannot by itself induce any anisotropic magnetic scattering through the hole-electron Fermi surface nesting along the  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$  directions.

When we cool  $Ba(Fe_{1-x}Co_x)_2As_2$  below  $T_s$  in the orthorhombic nematic phase, the *dyz* band of the electron Fermi surface at  $X/Y$  goes up in energy, while the  $d_{xz}$  band goes down in energy. Since these are electron pockets, the green part (the *dyz* band) of the Fermi surface near the Fermi level will shrink in size, while the red part (the  $d_{xz}$  band) of the Fermi surface will expand, resulting in different shaped Fermi surfaces as shown in Fig. [1\(c\).](#page-1-0) At the *Z* point, which has hole pockets, the changes for the  $d_{yz}$  and  $d_{xz}$  bands are opposite with much smaller amplitude [\[29,30\]](#page-8-0). So, we can basically assume that the holelike Fermi surfaces are not modified much below *Ts*. If spin fluctuations arise from intraorbital but interband quasiparticle excitations between hole and electron Fermi surfaces  $[53]$ , spin fluctuations along  $\mathbf{Q}_1$  should arise mostly from the *dyz* band scattering between the *Z* and *X* points. Similarly, one would expect spin fluctuations along the  $\mathbf{Q}_2$  direction to arise mostly from the  $d_{xz}$  band scattering between the *Z* and *Y* points [Figs.  $1(b)$  and  $1(c)$ ]. In the high-temperature paramagnetic tetragonal phase, the *dyz* and *dxz* orbital Fermi surfaces are degenerate, resulting in identical shapes for the electron Fermi pockets at the *X* and *Y* points, and an isotropic hole Fermi surface at the *Z* point [Fig. [1\(b\)\]](#page-1-0). The quasiparticle scattering across the hole-electron Fermi pockets along the **Q**<sup>1</sup> and **Q**<sup>2</sup> directions and associated spin fluctuations therefore have the same scattering intensity and behave identically.

On cooling to below  $T_s$ , the lifting of the  $d_{yz}$  band makes the electron Fermi pocket at the *X* point to be better matched with the  $d_{yz}$  orbital in the hole pocket, and the reduction in the  $d_{xz}$  band enhances the oval shape of the electron Fermi pocket at *Y* point as shown in Fig. [1\(c\).](#page-1-0) At the *Z* point, the hole Fermi surfaces also change line shape due to the rising *dxz* band and the reduction of the  $d_{vz}$  band, but to a much smaller extent compared with the shifts in Fermi surfaces at the *X*/*Y* points [Fig.  $1(c)$ ] [\[29,30\]](#page-8-0). Therefore, the major effect of the tetragonal-to-orthorhombic lattice distortion and associated nematic phase is to change the shapes of the electron Fermi pockets at the *X* and *Y* points as shown in Fig. [1\(c\).](#page-1-0) From a pure hole-electron Fermi surface nesting point of view [\[50\]](#page-8-0), the nesting condition along the **Q**<sup>1</sup> direction improves below *Ts* because of the better matched hole-electron Fermi surfaces of the *dyz* band [Fig. [1\(c\)\]](#page-1-0). On the other hand, the ∼30 meV downward shift of the  $d_{xz}$  band below  $T_s$  at the *Y* point enlarges the electron pocket along the  $Q_1$  direction [\[25\]](#page-8-0) and thus makes the  $d_{xz} - d_{xz}$  hole-electron Fermi surface nesting along the  $\mathbf{Q}_2$  direction less favorable.

If we assume that low-energy spin fluctuations in  $Ba(Fe_{1-x}Co_x)_2As_2$  arise from quasiparticle excitations between hole-electron Fermi pockets at the *Z* and *X*/*Y* points, spin fluctuations along the  $\mathbf{Q}_1$  and  $\mathbf{Q}_2$  directions should be sensitive to the nesting condition associated with the splitting

(g) T = 4.6K T = 23K

 $\bullet$  T = 46K  $\overline{\text{+ T}}$  = 60K T = 78K T = 100K

 $(1,0,L)$  $(0.1, L)$ 

 $(1,0,L)$  $(0,1,L)$ 

 $(1,0,L)$  $(0,1,L)$ 

10 20 30 40 50 60

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(b) 23K  $x = 0.054$ 

(d) 60K  $x = 0.054$ 

> (f) 100K  $= 0.054$

<span id="page-7-0"></span>energy between the  $d_{xz}$  and  $d_{yz}$  bands below  $T_s$ , and become  $C_4$  rotational symmetric above  $T_s$ . Since the splitting energy between the  $d_{xz}$  and  $d_{yz}$  bands is around 60 meV in undoped BaFe<sub>2</sub>As<sub>2</sub>, decreases to about 30 meV in Ba(Fe<sub>1-*x*</sub>Co<sub>*x*</sub>)<sub>2</sub>As<sub>2</sub> with  $x = 0.045$ , and vanishes around optimal superconductivity  $[25]$ , the energy scale of the spin fluctuation anisotropy  $\delta$ should decrease with increasing *x* and vanish near optimal superconductivity. This is qualitatively consistent with the spin anisotropy results on BaFe<sub>2</sub>As<sub>2</sub> [\[24\]](#page-8-0), BaFe<sub>1.9</sub>Ni<sub>0.1</sub>As<sub>2</sub> [\[32\]](#page-8-0), and Ba(Fe<sub>0.946</sub>Co<sub>0.054</sub>)<sub>2</sub>As<sub>2</sub> [Fig. [11\(g\)\]](#page-6-0), suggesting that low-energy spin fluctuations at the wave vector  $Q_1$  have a strong  $d_{yz}$  orbital character and arise from the  $d_{yz} - d_{yz}$ hole-electron Fermi surface quasiparticle excitations. Since superconductivity-induced neutron spin resonance in underdoped Ba(Fe<sub>1−*x*</sub>Co<sub>*x*</sub>)<sub>2</sub>As<sub>2</sub> only appears at  $Q_1$  (Figs. [3,](#page-2-0) [8,](#page-4-0) and [9\)](#page-5-0), it is tempting to argue that superconductivity in these materials arises mostly from electrons with *dyz* orbital characters [\[54\]](#page-9-0). However, such a picture is strictly only true within the itinerant model of magnetism and superconductivity in iron pnictides [\[54\]](#page-9-0).

The above discussion centers on the assumption that energy splitting of the *dxz* and *dyz* bands originates from orbital/nematic ordering below *Ts*. In a recent ARPES work on BaFe<sub>2</sub>As<sub>2</sub> [\[30\]](#page-8-0), it was argued that the splitting of the  $d_{xz}$  and  $d_{yz}$  bands is induced not by orbital/nematic order at  $T_s$ , but by static AF order occurring at a temperature  $T_N$  just below *Ts* [\[55\]](#page-9-0). In this scenario, spin fluctuations occurring at **Q**<sup>1</sup> in the AF-ordered state originate from spin waves of static ordered moments. The presence of a large spin gap at  $\mathbf{Q}_2$  [\[24\]](#page-8-0) and effective magnetic exchange coupling anisotropy [\[56\]](#page-9-0) can be well understood by including a biquadratic coupling term in the local moment Heisenberg Hamiltonian [\[57–59\]](#page-9-0). In the underdoped regime where superconductivity coexists with AF order, the broad (or double) resonance mode seen in neutron scattering experiments of twinned iron pnictides [\[17,34–37\]](#page-8-0) may arise from interacting spin waves with itinerant electrons [\[60\]](#page-9-0). In this picture, the resonance associated with the AF order should exclusively appear at **Q**1, while the resonance associated with itinerant electrons and simple nested Fermi surfaces should appear at both **Q**<sup>1</sup> and **Q**<sup>2</sup> [\[60\]](#page-9-0). Our results in Figs. [8](#page-4-0) and [9](#page-5-0) clearly disagree with this picture.

Alternatively, the neutron spin resonance [\[17,34–37\]](#page-8-0) can arise from orbital-selective pairing-induced superconducting gap anisotropy [\[61\]](#page-9-0). Here, the broadening of the resonance is a consequence of anisotropic superconducting gap in the electron pockets at the *X* and *Y* points. Below  $T_s$ , the unfavorable nesting condition of the  $d_{xz}$  band along the  $\mathbf{Q}_2$  means low-energy spin excitations are gapped at **Q**2. Therefore,

the appearance of the resonance exclusively at  $\mathbf{Q}_1$  suggests that superconducting electrons have mostly the  $d_{yz}$  orbital characters below the nematic ordering temperature *Ts*. In a recent work on detwinned FeSe [\[33\]](#page-8-0), which has no static AF order below  $T_s$  [\[62\]](#page-9-0), we again find that the superconductivityinduced resonance only appears at **Q**1, consistent with orbitalselective Cooper pairing in FeSe seen by scanning tunneling microscopy experiments [\[63\]](#page-9-0). This further supports the notion that orbital order and the nematic phase below  $T_s$  induce the energy splitting of the  $d_{xz}$  and  $d_{yz}$  bands in electron pockets, which in turn modifies the Fermi-surface nesting condition and associated spin fluctuations along the **Q**<sup>1</sup> and **Q**<sup>2</sup> directions.

In conclusion, our inelastic neutron scattering experiments on mechanically detwinned Ba(Fe<sub>1−*x*</sub>Co<sub>*x*</sub>)<sub>2</sub>As<sub>2</sub> with  $x = 0.048$  and 0.054, which has coexisting AF order and superconductivity, reveal highly anisotropic spin fluctuations with large magnetic scattering intensity at the AF ordering wave vector  $\mathbf{Q}_1$  and weak scattering at  $\mathbf{Q}_2$  at temperatures below the tetragonal-to-orthorhombic structural transition *Ts*. On cooling to a temperature above  $T_c$  but below  $T_N$ , a large spin gap appears at the  $\mathbf{Q}_2$  point and spin fluctuations are mostly centered at the **Q**<sup>1</sup> point. Upon entering the superconducting state, a neutron spin resonance appears at the **Q**<sup>1</sup> point with no magnetic scattering at the  $\mathbf{Q}_2 = (0, 1)$  point. By comparing these results with those from ARPES experiments, we conclude that the anisotropic shift of the  $d_{yz}$  and  $d_{xz}$  electronlike bands in detwinned  $Ba(Fe_{1-x}Co_x)_2As_2$  below  $T_s$  is associated with the spin excitation anisotropy, and the superconductivityinduced resonance arises from itinerant electrons with the *dyz* orbital characters. Therefore, low-energy spin fluctuations in underdoped  $Ba(Fe_{1-x}Co_x)_2As_2$  are highly orbital selective below *Ts*, suggesting that the orbital order and the nematic phase are correlated with spin fluctuations and superconductivity in underdoped iron pnictide superconductors.

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