# Suppression of ferromagnetic spin fluctuations in the filled skutterudite superconductor SrOs$_4$As$_{12}$ revealed by $^{75}$As NMR-NQR measurements

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Motivated by the recent observation of ferromagnetic spin correlations in the filled skutterudite SrFe$_4$As$_{12}$ [Q.-P. Ding *et al.*, Phys. Rev. B **98**, 155149 (2018)], we have carried out $^{75}$As nuclear magnetic resonance (NMR) and nuclear quadrupole resonance (NQR) measurements to investigate the role of magnetic fluctuations in the newly discovered isostructural superconductor SrOs$_4$As$_{12}$ with a superconducting transition temperature of $T_c \sim 4.8$ K. Knight shift $K$ determined by the NQR spectrum under a small magnetic field ($\leqslant 0.5$ T) is nearly independent of temperature, consistent with the temperature dependence of the magnetic susceptibility. The nuclear spin-lattice relaxation rate divided by temperature, $1/T_1T$, is nearly independent of temperature above $\sim 50$ K and increases slightly with decreasing temperature below the temperature. The temperature dependence is reasonably explained by a simple model where a flat band structure with a small ledge near the Fermi energy is assumed. By comparing the present NMR data with those in SrFe$_4$As$_{12}$, we found that the values of $|K|$ and $1/T_1T$ in SrOs$_4$As$_{12}$ are smaller than those in SrFe$_4$As$_{12}$, indicating no obvious ferromagnetic spin correlations in SrOs$_4$As$_{12}$. From the temperature dependence of $1/T_1$ in the superconducting state, an *s*-wave superconductivity is realized.

## I. INTRODUCTION

Magnetic fluctuation is one of the key parameters to characterize the physical properties of strongly correlated electron systems. Antiferromagnetic spin fluctuations are considered to play an important role in many unconventional superconductors such as high-$T_c$ cuprates [1], iron-based superconductors [2–5], organic superconductors [6], and also heavy-fermion superconductors [7]. Alternatively, ferromagnetic spin fluctuations are also considered to be important in the mechanism of superconductivity in U-based superconductors [8,9] and in iron-based superconductors [2,10–14].

The importance of magnetic fluctuations has also been pointed out in the filled skutterudite compound $A$Fe$_4X_{12}$ ($A$ = alkali metal, alkaline earth metal, lanthanide, or actinide; $X$ = P or Sb), whose magnetic properties largely depend on the number of valence electrons of the $A$ ions [15–27]. In the case of $A$ = monovalent Na and K ions with $X$ = Sb, a weak ferromagnetism with a Curie temperature of $T_C$ = 85 K has been observed [15,16], while no magnetic order has been reported for the case of divalent alkaline-earth ions such as Ca, Sr, and Ba, where ferromagnetic spin fluctuations are considered to play an important role [17,18,24,25]. On the other hand, the importance of antiferromagnetic spin fluctuations has been pointed out in the trivalent ion systems of LaFe$_4$Sb$_{12}$ [17,26] and LaFe$_4$P$_{12}$ [21], although ferromagnetic fluctuations are also reported in LaFe$_4$Sb$_{12}$ [27].

The effects of magnetic fluctuations on the physical properties of filled skutterudite compounds with different $d$ electrons from 3$d$ to 4$d$ and 5$d$ have also been investigated by replacing Fe by Ru or Os [28–30]. From the magnetization, transport, and specific heat measurements, the 5$d$-electron compounds

of $A$Os$_4$Sb$_{12}$ ($A$ = Sr, Ba) are found to be placed between the Fe 3$d$ compounds with ferromagnetic spin fluctuations and the Ru 4$d$ compounds having no obvious strong electron correlation effects [28,29]. Although it is important to systematically study these physical properties of $d$-electron systems by changing $X$ ions such as P and As for deeper understanding of the role of $d$ electrons, not many studies have been carried out because of the difficulty in preparing those compounds.

Recently, new filled skutterudite arsenide compounds Sr$T_4$As$_{12}$ ($T$ = Fe, Ru, Os) were synthesized using a high-pressure synthesis technique [31], which provides a new opportunity for systematic studies of the role of $d$ electrons with 3$d$, 4$d$, and 5$d$. For the 5$d$-electron system, SrOs$_4$As$_{12}$ was found to be a new superconductor with a transition temperature of $T_c$ = 4.8 K [31]. For the 3$d$ and 4$d$ electron systems, on the other hand, SrFe$_4$As$_{12}$ and SrRu$_4$As$_{12}$ do not exhibit superconductivity down to 2 K, although the electrical resistivities show metallic behavior [31]. Magnetization and specific heat measurements [31] and theoretical studies [32] pointed out the ferromagnetic nature of SrFe$_4$As$_{12}$. Quite recently, ferromagnetic spin correlations were actually reported in the 3$d$ compound SrFe$_4$As$_{12}$ [33], similar to the case of $A$Fe$_4$Sb$_{12}$ ($A$ = Ba, Sr) [17–19]. Since the 5$d$ compound SrOs$_4$As$_{12}$ exhibits superconductivity, in contrast to the nonsuperconductors $A$Os$_4$Sb$_{12}$ ($A$ = Ba, Sr) [34], it is very interesting to investigate how the magnetic fluctuations changes in the newly discovered superconductor SrOs$_4$As$_{12}$.

Nuclear magnetic resonance (NMR) and nuclear quadrupole resonance (NQR) measurements are powerful techniques to investigate the magnetic and electronic properties of materials from a microscopic point of view.

It is known that the temperature $T$ dependence of the nuclear spin-lattice relaxation rate $1/T_1$ reflects the wave vector $q$-summed dynamical susceptibility. On the other hand, NMR spectrum measurements, in particular the Knight shift $K$, give us information on static magnetic susceptibility $\chi$. Thus, from the temperature dependence of $1/T_1T$ and $K$, one can obtain valuable insights into magnetic fluctuations in materials. Furthermore, $1/T_1$ measurements in the superconducting state provide important information for understanding the symmetry of Cooper pairs in superconductors.

In this paper, we report the results of $^{75}$As NMR, NQR, and magnetic susceptibility measurements performed to investigate the magnetic and electronic properties of $SrOs_4As_{12}$ from a microscopic point of view. Our experimental data indicate the strong suppression of ferromagnetic spin correlations in the superconductor $SrOs_4As_{12}$, in comparison with $SrFe_4As_{12}$, which exhibits electron correlations enhanced around ferromagnetic wave number $q = 0$ [33]. The temperature dependence of $1/T_1$ in the superconducting state evidences an $s$-wave superconductivity in $SrOs_4As_{12}$.

## II. EXPERIMENT

Polycrystalline $SrOs_4As_{12}$ samples were prepared at high temperatures and high pressures using a Kawai-type double-stage multianvil high-pressure apparatus [31]. The lattice constant of $SrOs_4As_{12}$ with a bcc structure (space group: $Im\bar{3}$) was determined by x-ray diffraction measurements to be 8.561 Å [31]. The magnetic susceptibility measurement was performed using a magnetic properties measurement system (Quantum Design) under a magnetic field of 5 T. NMR and NQR measurements of $^{75}$As ($I = \frac{3}{2}$, $\frac{\gamma_N}{2\pi} = 7.2919$ MHz/T, $Q = 0.29$ barn) nuclei were conducted using a laboratory-built phase-coherent spin-echo pulse spectrometer. The $^{75}$As NMR spectra were obtained by sweeping the magnetic field $H$ at a fixed frequency $f = 37$ MHz, while $^{75}$As NQR spectra were measured in steps of frequency by measuring the intensity of the Hahn spin echo. The $^{75}$As nuclear spin-lattice relaxation rate $1/T_1$ was measured with a saturation recovery method. The $1/T_1$ at each temperature was determined by fitting the nuclear magnetization $M$ versus time $t$ using the exponential function $1 - M(t)/M(\infty) = e^{-(3t/T_1)^\beta}$ for $^{75}$As NQR, where $M(t)$ and $M(\infty)$ are the nuclear magnetization at time $t$ after the saturation and the equilibrium nuclear magnetization at $t \to \infty$, respectively. $\beta \sim 0.8$ is nearly independent of temperature in the paramagnetic state; however, the values of $\beta$ show a complicated temperature dependence in the superconducting state below 4.8 K, as will be discussed later.

## III. $^{75}$As NMR AND NQR SPECTRA

Figure 1 shows the field-swept $^{75}$As NMR spectrum of $SrOs_4As_{12}$ at $T = 4.3$ K, where a complex NMR spectrum is observed. A similar complicated $^{75}$As NMR spectrum was observed in the isostructural compound $SrFe_4As_{12}$, which is due to a large nuclear quadrupolar interaction and a finite asymmetric parameter $\eta$ of the electric field gradient (EFG) tensor at the As site [33]. One can calculate the NMR spectrum from a nuclear spin Hamiltonian, which is the sum
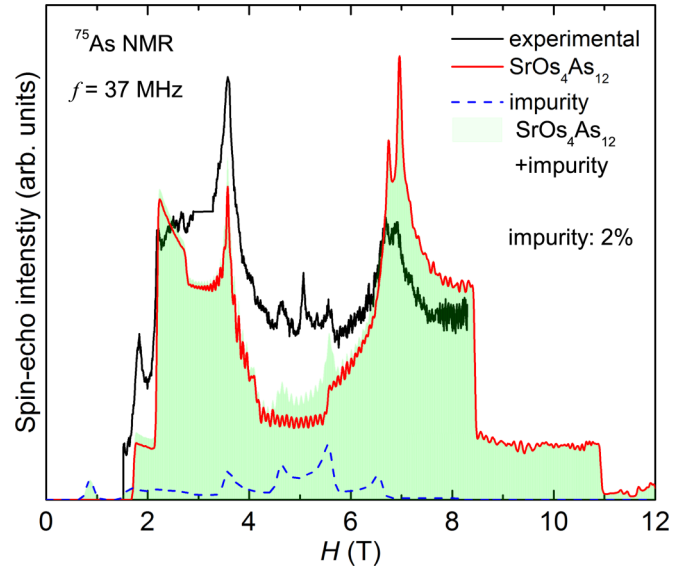


FIG. 1. Field-swept $^{75}$As NMR spectra of $SrOs_4As_{12}$ at $f = 37$ MHz and $T = 4.3$ K. The black curve is the observed spectrum, and the red curve is the calculated spectrum with $\nu_Q = 60.1$ MHz, $\eta = 0.45$. The blue dashed curve represents the calculated $^{75}$As NMR spectrum ($\nu_Q = 23.5$ MHz, $\eta = 0$) from the impurity phase [33]. The sum of the two calculated spectra is shown by the green area.

of the nuclear Zeeman ($\mathcal{H}_M$) and electric quadrupole ($\mathcal{H}_Q$) interactions:

$$\mathcal{H} = \mathcal{H}_M + \mathcal{H}_Q, \tag{1}$$

where

$$\mathcal{H}_M = -\gamma\hbar(1 + K)H\left[\frac{1}{2}(I_+e^{-i\phi} + I_-e^{i\phi})\sin\theta + I_Z\cos\theta\right] \tag{2}$$

and

$$\mathcal{H}_Q = \frac{h\nu_Q}{6}\left[3I_Z^2 - I^2 + \frac{1}{2}\eta(I_+^2 + I_-^2)\right] \tag{3}$$

in the coordinate of the principal $X$, $Y$, and $Z$ axes of the EFG. Here $H$ is the applied field; $h$ is Planck's constant; $K$ is the Knight shift; $\nu_Q$ is the nuclear quadrupole frequency, defined by $\nu_Q = eQV_{ZZ}/2h$, where $Q$ is the quadrupole moment of the As nucleus and $V_{ZZ}$ is the EFG at the As site; $\eta = \frac{V_{YY} - V_{XX}}{V_{ZZ}}$ is the asymmetry parameter of the EFG; and $\theta$ and $\phi$ are the polar and azimuthal angles between the direction of the applied field and the $Z$ axis of the EFG, respectively. As in our previous paper [33], we have calculated a powder-pattern NMR spectrum by diagonalizing exactly the nuclear spin Hamiltonian without using perturbation theory. The calculated spectrum with the NMR frequency $f = 37$ MHz, $K = 0$, NQR frequency $\nu_Q = 60.1$ MHz, and $\eta = 0.45$ reasonably reproduces the characteristic shape of the observed spectrum, as shown by the red curve in Fig. 1. However, we notice that, in addition to the calculated spectrum (red curve), there is another contribution ($\sim$2% spectral weight) of the $^{75}$As NMR spectrum with $\nu_Q = 23.6$ MHz and $\eta = 0$ to the total NMR spectrum. A similar contribution of the spectrum was
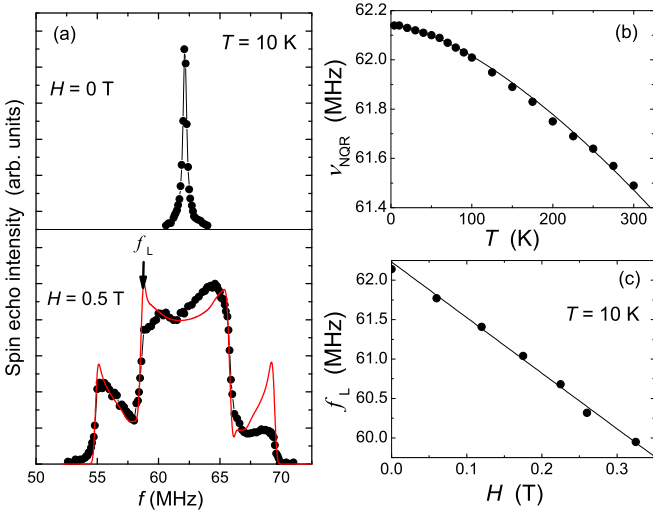
FIG. 2. (a) $^{75}$As NQR spectra measured at $T = 10$ K under zero magnetic field (top panel) and 0.5 T (bottom panel) in SrOs$_4$As$_{12}$. The red curve in the bottom panel is a simulated powder-pattern spectrum with $\nu_Q = 60.1$ MHz, $\eta = 0.45$, and $H = 0.5$ T. The arrow shows the position of the lower-frequency edge position $f_L$, whose position is attributed to $\theta = \pi$ (and also $\theta = 0$). (b) $T$ dependence of $^{75}$As NQR frequency $\nu_{NQR}$ in SrOs$_4$As$_{12}$. The black curve is $\nu_{NQR}(T) = \nu_{NQR}(0)(1 - \alpha_Q T^{3/2})$, with $\alpha_Q = 2.09 \times 10^{-6}$ K$^{-3/2}$ and $\nu_{NQR}(0) = 62.14$ MHz. (c) The external magnetic field dependence of $f_L$ at $T = 10$ K.

observed in SrFe$_4$As$_{12}$, for which the contribution was assigned to the impurity phase of the arsenic metal [33].

As for the principal axis of EFG at the As site, one cannot determine it from NMR spectrum measurements on the powder compound. As described in our previous paper [33], Tou *et al.* [35,36] determined the principal axis of the EFG at the Sb sites in the isostructural PrOs$_4$Sb$_{12}$ compound from NMR measurements using a single crystal, reporting that, although there is one crystallographically equivalent Sb site in the filled skutterudite structure, there are three different Sb sites with the principal axis parallel to [100], [010], and [001] of the crystal, respectively, due to the local symmetry of the 24$g$ site of the Sb ions. The same conclusion regarding the direction of the EFG at the Sb sites in CeOs$_4$Sb$_{12}$ was reported from $^{121}$Sb NMR using an oriented powder sample [37]. Since the crystal structure of the Sb compounds is the same as that of SrOs$_4$As$_{12}$, we consider the directions of the EFG at the As sites to be the same.

In the NQR spectrum under zero magnetic field for $I = 3/2$ where $\mathcal{H}$ has only $\mathcal{H}_Q$, one can observe a single transition line at a frequency of $\nu_{NQR} = \nu_Q\sqrt{1 + \eta^2/3}$. Using $\nu_Q = 60.1$ MHz and $\eta = 0.45$ at $T = 10$ K estimated from the analysis of the NMR spectrum, one expects the NQR line at $f \sim 62.1$ MHz, which is actually observed as shown in the top panel in Fig. 2(a). The peak position slightly shifts to lower frequency with increasing temperature, corresponding to the decrease in $\nu_{NQR}$ on increasing temperature, as shown in Fig. 2(b). Similar temperature dependence of $\nu_{NQR}$ was observed in SrFe$_4$As$_{12}$ [33] and also in other filled skutterudite compounds [23,38–42] in which the temperature dependence at higher temperatures is found to obey the empirical relation

$\nu_{NQR}(T) = \nu_{NQR}(0)(1 - \alpha_Q T^{3/2})$ with a fitting parameter $\alpha_Q$. This temperature dependence is considered to be due to thermal lattice expansion [43]. As shown by the solid curve in Fig. 2(b), the temperature dependence of $\nu_{NQR}$ in SrOs$_4$As$_{12}$ also follows the relation with $\alpha_Q = 2.09 \times 10^{-6}$ K$^{-3/2}$. The value of $\alpha_Q = 2.09 \times 10^{-6}$ K$^{-3/2}$ is slightly smaller than $3.21 \times 10^{-6}$ K$^{-3/2}$ for SrFe$_4$As$_{12}$ [33]. The linewidth of the NQR spectra (full width at half maximum $\sim 0.4$ MHz) is nearly independent of temperature from 4.3 to 300 K. This indicates that there is no structural or magnetic phase transition in the normal state of SrOs$_4$As$_{12}$.

## IV. $^{75}$As KNIGHT SHIFT

Determination of the Knight shift $K$ from the complex NMR spectrum shown in Fig. 1 is relatively difficult due to the strong quadrupole interaction and relatively large asymmetric parameter $\eta$ value. This is due to the fact that small changes in $\nu_Q$ and $\eta$ produce a change in $K$, leading to great ambiguity in determining $K$ from the simulation of the NMR spectrum. However, as has been reported [33], we have succeeded in determining the Knight shift data from the NQR spectrum under small magnetic fields lower than 0.5 T in SrFe$_4$As$_{12}$. Here we have applied the same method to SrOs$_4$As$_{12}$ to obtain the Knight shift data. As described in detail in Refs. [25,33], the NQR resonance frequency $\nu_{NQR}(H)$ under a small magnetic field can be written as [44]

$$\nu_{NQR}(H) = \nu_{NQR}(0) \pm \frac{\gamma_N}{2\pi} A(\eta)(1 + K)HF(\theta), \quad (4)$$

where $\nu_{NQR}(0)$ is $\nu_{NQR}$ at $H = 0$, $F(\theta) = \frac{\cos\theta}{2}[3 - (4\tan^2\theta + 1)^{1/2}]$, and $A(\eta)$ is a factor close to unity which depends on the value of $\eta$. Under magnetic fields, the random distribution of $\theta$ produces the rectangular shape of the powder-pattern spectrum where $\theta = 0$ (and also $\pi$) produces both higher- and lower-frequency edges. By measuring the external magnetic field dependence of the edge position of the NQR spectrum, one can determine the coefficient of the second term of Eq. (4), $A(\eta)\frac{\gamma_N}{2\pi}(1 + K)$, and thus the Knight shift if one knows the value of $A(\eta)$ since the value of $\frac{\gamma_N}{2\pi}$ is known. In the bottom panel of Fig. 2(a), a typical NQR spectrum observed at $H = 0.5$ T is shown, where the rectangular shape of the powder-pattern spectrum is clearly seen. The small peaks (at $\sim 55$ and 70 MHz) on both sides of the central rectangular spectrum are due to the mixing of states $|1/2\rangle$ and $|-1/2\rangle$ as a result of the zero-order mixing effect [45]. These features of the observed spectrum are relatively well reproduced by the calculated powder-pattern spectrum with $\nu_Q = 60.1$ MHz, $\eta = 0.45$, and $H = 0.5$ T using the Hamiltonian of Eq. (1), as shown by the red curve in Fig. 2(a).

Figure 2(c) shows the typical magnetic field dependence of $f_L$ at the lower edge position indicated by the black arrow in Fig. 2(a), exhibiting a clear linear behavior. From the slope, the Knight shift $K$ at 10 K was determined to be $-1.2\% \pm 2.5\%$. Here we used $A(\eta) = 0.9794$ as in the case of SrFe$_4$As$_{12}$ [33], where the value of $\eta = 0.4$ is close to $\sim 0.45$. Although the error is relatively large, this is much better than the case of the NMR spectrum from which we could not determine $K$. It is also noted that we did not include any anisotropy in the Knight shift in the calculated
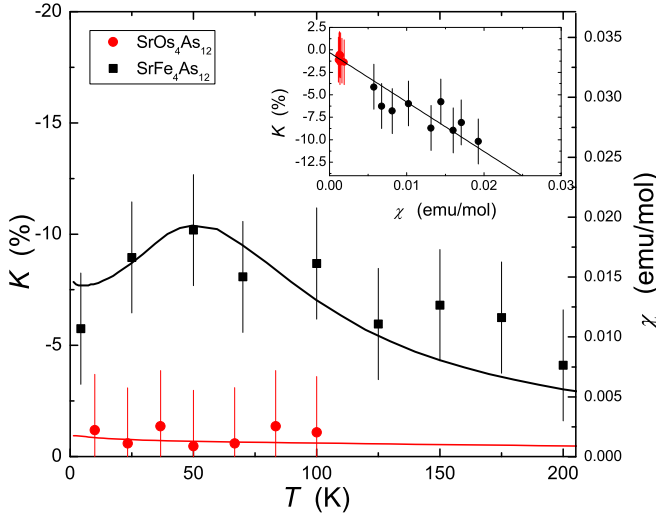
FIG. 3. Temperature dependence of the $^{75}$As Knight shift $K$ in SrOs$_4$As$_{12}$ (red circles) and SrFe$_4$As$_{12}$ (black squares) from Ref. [33]. Temperature dependences of the magnetic susceptibility $\chi$ are also plotted by the red and black curves for SrOs$_4$As$_{12}$ and SrFe$_4$As$_{12}$ [31], respectively. The inset shows $K$ versus the corresponding magnetic susceptibility $\chi$. The black line is a linear fit.

spectrum which reproduces the observed one shown above. This suggests that, although one expects an anisotropic part in the Knight shift due to the local symmetry of the Os ions (trigonal), the anisotropy is not significant and could not be detected within our experimental uncertainty. Therefore, the Knight shift discussed below is considered an isotropic part of the Knight shift.

Following the method described above, we determined $K$ at different temperature. Its temperature dependence is shown in Fig. 3, where the $K$ data in SrFe$_4$As$_{12}$ are also plotted [33]. In contrast to the case of SrFe$_4$As$_{12}$, where the broad minimum around ∼50 K was observed (note the sign of the vertical axis of Fig. 3 for the Knight shifts), $|K|$ values of SrOs$_4$As$_{12}$ are much smaller than those of SrFe$_4$As$_{12}$ and are nearly independent of temperature. These results are consistent with the magnetic susceptibility $\chi$ data whose temperature dependences are also shown by solid curves in Fig. 3 where the maximum in $\chi$ corresponds to the minimum in $K$ in SrFe$_4$As$_{12}$ due to the negative hyperfine coupling constant [33]. It is also noted that the values of $\chi$ in SrOs$_4$As$_{12}$ are more than one order of magnitude smaller than those in SrFe$_4$As$_{12}$. These results clearly evidence that the spin susceptibility of SrOs$_4$As$_{12}$ is much smaller than that of SrFe$_4$As$_{12}$.

In order to check whether or not the small values of $|K|$ actually correspond to the suppression of spin susceptibility, we have plotted Knight shifts for both compounds as a function of the corresponding $\chi$, as shown in the inset of Fig. 3. Since the NMR shift consists of a temperature-dependent spin shift $K_s(T)$ and $T$-independent orbital shift $K_0$, one needs to know $K_0$ to estimate $K_s(T)$. $K_0$ can be obtained from the intercept of the so-called $K$-$\chi$ plot shown in the inset. The solid line in the inset is the linear fit for data including both compounds, giving a nearly zero intercept, i.e., nearly zero $K_0$. Therefore, the observed $|K|$ can be considered as being mainly $K_s$, again indicating the strong suppression of the spin susceptibility
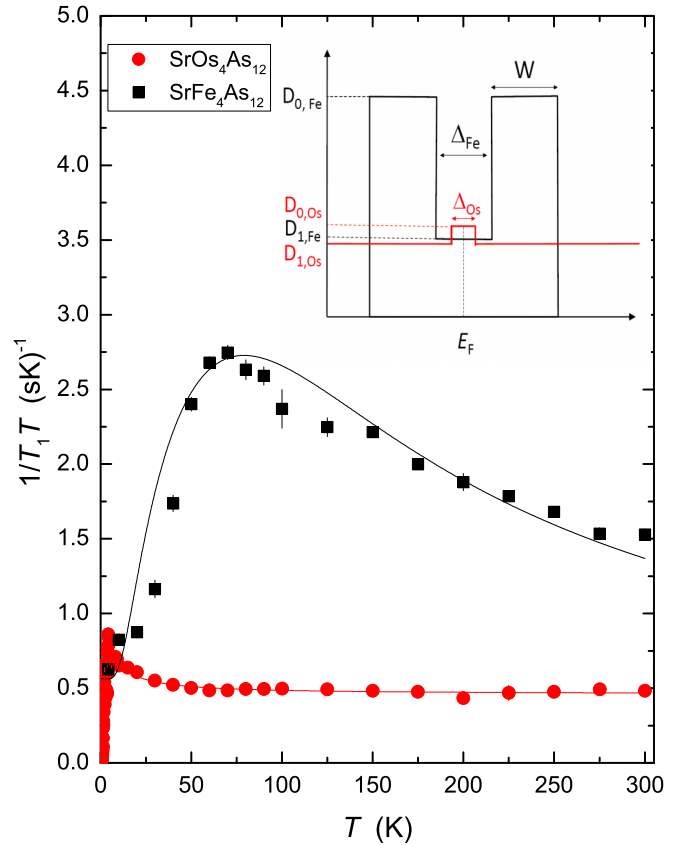


FIG. 4. Temperature dependences of $^{75}$As $1/T_1T$ in SrOs$_4$As$_{12}$ (red circles) and SrFe$_4$As$_{12}$ (black squares) from Ref. [33]. The solid lines are the calculated results based on the band structures near $E_F$ shown in the inset with the following set of parameters: $\Delta_{Os} = 40$ K and $\mathcal{D}_{0,Os}/\mathcal{D}_{1,Os} = 1.2$ for SrOs$_4$As$_{12}$ and $\Delta_{Fe} = 88$ K, $W = 220$ K, and $D_{0,Fe}/D_{1,Fe} = 2.6$ for SrFe$_4$As$_{12}$.

in SrOs$_4$As$_{12}$. The slope gives a hyperfine coupling constant $A_{hf} = -3.84 \pm 1.60$ kOe/$\mu_B$ [46].

## V. $^{75}$As SPIN-LATTICE RELAXATION RATE $1/T_1$

### A. Normal state

Figure 4 shows the temperature dependence of the $^{75}$As spin-lattice relaxation rate divided by temperature ($1/T_1T$) measured at the peak positions of the NQR spectra under zero magnetic field, together with the data for SrFe$_4$As$_{12}$ reported previously [33]. In contrast to the case in SrFe$_4$As$_{12}$ where the large enhancement of $1/T_1T$ at low temperatures was observed, $1/T_1T$ in SrOs$_4$As$_{12}$ seems to follow Korringa's law, $T_1T = $ const, at high temperature above ∼50 K, although the small increase can be observed at low temperatures in the normal state.

In our previous paper, to reproduce the temperature dependence of $1/T_1T$ for SrFe$_4$As$_{12}$, we employed a simple model in which a concave-shaped band structure shown in the inset of Fig. 4 was assumed [33]. In the model, the Fermi energy $E_F$ is assumed to be at the center of the dip, and $\Delta_{Fe}$, $W$, and the density of states $\mathcal{D}_{0,Fe}$ and $\mathcal{D}_{1,Fe}$ characterize the band

structure near $E_F$. Using the formula

$$\frac{1}{T_1} \sim \int_0^\infty \mathcal{D}^2(E) f(E)[1 - f(E)]dE, \qquad (5)$$

where $f(E)$ is the Fermi distribution function, we calculated $1/T_1T$ with the set of parameters $\Delta_{\text{Fe}} = 88\,\text{K}$, $W = 220\,\text{K}$, and $\mathcal{D}_{0,\text{Fe}}/\mathcal{D}_{1,\text{Fe}} = 2.63$, which reasonably reproduces the experimental data, as shown by the black curve in Fig. 4. The model is also used to reproduce the temperature dependence of the magnetic susceptibility in $\text{SrFe}_4\text{As}_{12}$ [33]. It is interesting to note that a similar model (but with no finite density of states at $E_F$) was applied to FeSi to explain the characteristic temperature dependence of magnetic susceptibility, specific heat, and thermal expansion [47].

In the case of $\text{SrOs}_4\text{As}_{12}$, the nearly temperature independent behavior of $1/T_1T$ indicates an almost flat band near $E_f$, in contrast to the case of $\text{SrFe}_4\text{As}_{12}$. In fact, as shown by the red solid curve in Fig. 4, the observed temperature dependence of $1/T_1T$ can be reproduced by the band model with a nearly flat structure near $E_F$ with a small ledge with width $\Delta_{\text{Os}} = 40\,\text{K}$ with $\mathcal{D}_{0,\text{Os}}/\mathcal{D}_{1,\text{Os}} = 1.2$. It turns out that the difference in the band structure produces significantly different behavior in $1/T_1T$ and could originate from the fact that Fe $3d$ electrons have a more localized nature than Os $5d$ electrons.

Now we discuss magnetic correlations in both systems based on the NMR data. As discussed in our previous paper, in order to discuss the magnetic correlations, it is useful to estimate the quantity $T_1TK_s^2$, where $K_s$ is the spin part of the Knight shift [48–50]. The so-called Korringa ratio $\mathcal{K}(\alpha) \equiv \frac{S}{T_1TK_s^2}$ is unity for uncorrelated metals. Here $S = \frac{\hbar}{4\pi k_B}(\frac{\gamma_e}{\gamma_N})^2$, where $\gamma_e$ and $\gamma_n$ are the electron and nuclear gyromagnetic ratios, respectively. Since $1/T_1T$ probes the dynamical spin susceptibility averaged over the Brillouin zone, it can be enhanced by either ferromagnetic or antiferromagnetic spin correlations. On the contrary, $K_s$ will be enhanced only for ferromagnetic spin correlations. Therefore, for antiferromagnetic correlated metals, $\mathcal{K}(\alpha)$ is expected to be greater than unity. On the other hand, one can expect $\mathcal{K}(\alpha)$ to be much smaller than unity for ferromagnetic spin correlations. $\mathcal{K}(\alpha) \sim 0.02$, much less than unity, was reported for $\text{SrFe}_4\text{As}_{12}$ [33], evidencing the ferromagnetic spin correlations. On the other hand, the small values of $|K|$ for $\text{SrOs}_4\text{As}_{12}$ increase the $\mathcal{K}(\alpha)$ values, suggesting much weaker ferromagnetic spin correlations in $\text{SrOs}_4\text{As}_{12}$. However, the estimate of $\mathcal{K}(\alpha)$ is rather difficult due to large errors in $K$. In addition, it should be noted that the observed $1/T_1T$ is the sum of two contributions: the spin and orbital relaxation rates. This also makes it difficult to estimate $\mathcal{K}(\alpha)$. Assuming $\mathcal{K}(\alpha) = 1$ for uncorrelated metals, $|K_s|$ is estimated to be 0.21% using the $1/T_1T$ values above 50 K in the normal state. $K_s$ would be consistent with the observed small values of $|K|$ for $\text{SrOs}_4\text{As}_{12}$ within our large experimental uncertainty. Thus, one can conclude that the ferromagnetic spin correlations observed in $\text{SrFe}_4\text{As}_{12}$ are strongly suppressed in $\text{SrOs}_4\text{As}_{12}$ [51].

It is interesting to point out that the $1/T_1T$ values for both systems are almost comparable at low temperatures below $\sim$20 K in the normal state. This indicates that the effective
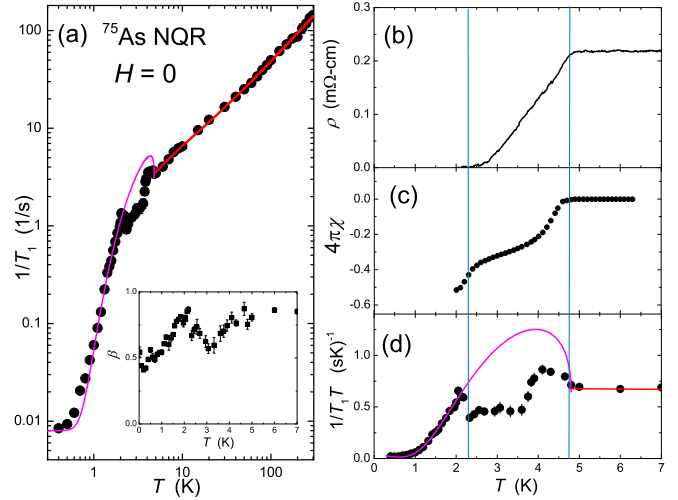


FIG. 5. (a) Temperature dependence of $1/T_1$ in $\text{SrOs}_4\text{As}_{12}$. The pink curve in the superconducting state is the calculated result based on the BCS theory The red curve in the normal state is the calculated results shown in Fig. 4. The inset shows the temperature dependence of $\beta$. (b) Temperature dependence of electrical resistivity from Ref. [31]. (c) Temperature dependence of volume magnetic susceptibility in the superconducting state estimated from the zero-field-cooled magnetic susceptibility data reported in Ref. [31]. (d) Temperature dependence of $1/T_1T$ in the low-temperature region together with the calculated result (pink curve) based on BCS theory. The vertical blue lines are just guides to the eye.

density of states at $E_F$, $\mathcal{D}(E_F)$, is nearly the same for the compounds at low temperatures, as actually illustrated in the inset of Fig. 4. Since $\mathcal{D}(E_F)$ generally correlates with $T_c$ in conventional BCS superconductors, one may expect the appearance of superconductivity in $\text{SrFe}_4\text{As}_{12}$. No superconductivity is, however, observed in $\text{SrFe}_4\text{As}_{12}$. Therefore, we speculate that the strong ferromagnetic fluctuations prevent superconductivity. As will be discussed below, the superconductivity in $\text{SrOs}_4\text{As}_{12}$ is revealed to be a spin-singlet $s$-wave state in which ferromagnetic fluctuations may compete since the ferromagnetic fluctuations would be favorable to inducing triplet Cooper pairs. In other word, the strong suppression of the ferromagnetic spin correlations could induce superconductivity in $\text{SrOs}_4\text{As}_{12}$. Therefore, one may expect superconductivity in $\text{SrFe}_4\text{As}_{12}$ if the ferromagnetic correlations could be suppressed. This would be possible by applying pressure since the nature of the localization of the $3d$ electrons responsible for the ferromagnetic spin correlations may be decreased. This interesting project is currently in progress.

### B. Superconducting state

Finally, we show the $T_1$ data in the superconducting state below $T_c \sim 4.8$ K. As shown in Fig. 5(a), $1/T_1$ shows a tiny, but visible, coherence peak (also known as the Hebel-Slichter peak) just below $T_c$ and decreases below 4 K, then exhibits a small peak around 2 K following the sudden decrease below $\sim$2 K, where $1/T_1$ seems to level off below $\sim$0.4 K. Although the temperature dependence of $1/T_1$ is complicated, it is important to point out that $1/T_1$ decreases largely by

more than two orders of magnitude below $T_c$ down to the lowest temperature of $\sim 0.4$ K. This clearly indicates that the superconductivity observed in $SrOs_4As_{12}$ is not filamentary or surface but bulk in nature, at least below $\sim 2$ K. In addition, the observation of the coherence peak just below $T_c$ [more clearly seen in Fig. 5(d)] is direct evidence of a conventional *s*-wave BCS superconductor. The observation of the peak also indicates that the relaxation process of the As nuclei in $SrOs_4As_{12}$ can be characterized to be magnetic, not electric [52,53]. The unusual and complicated behavior in $1/T_1$ in the temperature range of 2–4 K could be due to the distribution of $T_c$ in our sample, as can be seen in the resistivity and magnetization data [31]. As shown in Fig. 5(b), the electrical resistivity starts to decreases below 4.8 K and reaches nearly zero resistivity at $\sim 2.2$ K with a relatively broad superconducting-transition width $\Delta T_c = 2.6$ K. The distribution of $T_c$ can also be inferred from the two-step behavior in the volume magnetic susceptibility in the superconducting state estimated from the zero-field-cooled magnetic susceptibility measurements, as shown in Fig. 5(c). It is noted that the superconducting volume starts to increase below $\sim 4.8$ K on cooling and reaches $\sim 45\%$ around 2.2 K, where the zero resistivity is observed. The distribution of $T_c$ would create problems in estimating $T_1$ since the observed spectrum may be composed of at least two components of $^{75}$As NQR signals from the superconducting and normal states. In addition, the ratio of the signals from the superconducting and normal states could be changed with temperature due to the Meissner effect, which will produce complicated nuclear relaxation curves. In fact, as shown in the inset of Fig. 5(a), the temperature dependence of $\beta$ exhibits a complicated behavior with a local minimum around 3.5 K, showing the large distribution of $1/T_1$. Thus, since we consider that the temperature dependence of $1/T_1$ in $T = 2.2$–4 K is not intrinsic but extrinsic and more artificial, we will not discuss it in this paper. It is noted that, although a similar complicated behavior of $1/T_1$ was observed in SrtPtAs [54], later $T_1$ measurements with high-quality samples do not show the complicated behavior [55], suggesting that the quality of samples strongly affects the temperature dependence of $1/T_1$.

In order to test whether the observed temperature dependence of $1/T_1$ can be explained by an *s*-wave conventional superconductor model, we have calculated $1/T_1$ using BCS theory. Here the relaxation rate $1/T_{1s}$ in the superconducting state normalized by $1/T_{1n}$ in the normal state is expressed as [56]

$$\frac{T_{1n}}{T_{1s}} \propto \int_0^\infty [N_s(E)^2 + M_s(E)^2] f(E)[1 - f(E)] dE, \quad (6)$$

where $M_s(E) = N_0 \Delta / \sqrt{E^2 - \Delta^2}$ is the anomalous density of states (DOS) due to the coherence factor, $N_s(E) = N_0 E / \sqrt{E^2 - \Delta^2}$ is the DOS in the superconducting state, $\Delta$ is the energy gap, $N_0$ is the DOS in the normal state, and $f(E)$ is the Fermi distribution function. We convolute $M_s(E)$ and $N_s(E)$ with a broadening function assuming a triangle shape with a width of $2\delta$ and a height of $1/\delta$ [57]. The pink curve in Fig. 5(a) [also shown in Fig. 5(d)] is the calculated result with $\Delta(0) = 6$ K and $r = \Delta(0)/\delta = 5$. Here we add a constant term of $1/T_1 = 0.008$ (1/s) into the

calculated result to reproduce the temperature-independent behavior of $1/T_1$ observed below $\sim 0.4$ K. The origin of the temperature-independent behavior of $1/T_1$ is not clear at present, but it may originate from some sort of impurity effect. Although the calculated results do not reproduce the height of the observed coherence peak, they seem to capture the observed temperature dependence of $1/T_1$ (here again, except for the intermediate temperature range of 2.2–4 K). The value of $2\Delta(0)/k_B T_c$ is estimated to be 2.5 using the onset $T_c$ of 4.8 K. This value is slightly smaller than that of the BCS weak-coupling limit $2\Delta(0)/k_B T_c = 3.53$. It should be noted that the isostructural compound $CaOs_4P_{12}$ has been suggested to be a BCS-type superconductor with $T_c = 2.5$ K [58]. In order to discuss the superconducting properties of $SrOs_4As_{12}$ in detail, one needs good-quality samples with a much smaller distribution of $T_c$, and a detailed study of the superconducting properties of $SrOs_4As_{12}$ is a future project. However, it should be noted that our NMR measurements clearly indicate the *s*-wave BCS superconducting nature of $SrOs_4As_{12}$, even though the present samples show a relatively broad superconducting transition.

## VI. SUMMARY

In summary, we have carried out $^{75}$As NMR and NQR measurements on the superconductor $SrOs_4As_{12}$ and compared the results with those for the nonsuperconducting metallic compound $SrFe_4As_{12}$, in which ferromagnetic spin correlations play an important role. The Knight shift $K$ determined by the NQR spectrum under a small magnetic field ($\leqslant 0.5$ T) is nearly independent of temperature, which is consistent with the temperature dependence of the magnetic susceptibility. The values of $|K|$ in $SrOs_4As_{12}$ are much smaller than those in $SrFe_4As_{12}$, indicating the spin susceptibility of $SrFe_4As_{12}$ is strongly suppressed in $SrOs_4As_{12}$. A similar strong suppression in $SrOs_4As_{12}$ can also be observed in $1/T_1T$ data, whose temperature dependence is explained by a simple model in which we assume a flat band structure with a small ledge near the Fermi energy. The large suppression of $|K|$ and $1/T_1T$ in $SrOs_4As_{12}$ compared with those in $SrFe_4As_{12}$ indicates no obvious ferromagnetic spin correlations in $SrOs_4As_{12}$. Furthermore, the temperature dependence of $1/T_1$ in the superconducting state evidences a conventional *s*-wave superconductivity in $SrOs_4As_{12}$. These results suggest that the ferromagnetic spin correlations compete with the appearance of superconductivity in the Sr-based filled skutterudite arsenides, which may be consistent with the conventional spin-singlet *s*-wave superconducting state revealed by $1/T_1$ measurements.

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