# Kinetics of Domain Switching by Mechanical and Electrical Stimulation in Relaxor-Based Ferroelectrics

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Ferroelectric materials have been extensively explored for applications in high-density nonvolatile memory devices because of their ferroelectric-ferroelastic domain-switching behavior under electric loading or mechanical stress. However, the existence of ferroelectric and ferroelastic backswitching would cause significant data loss, which affects the reliability of data storage. Here, we apply in situ transmission electron microscopy and phase-field modeling to explore the unique ferroelastic domain-switching kinetics and the origin of this in relaxor-based  $Pb(Mg_{1/3}Nb_{2/3})O_3-33\%PbTiO_3$  single-crystal pillars under electrical and mechanical stimulations. Results showed that the electric-mechanical hysteresis loop shifted for relaxor-based single-crystal pillars because of the low energy levels of domains in the material and the constraint on the pillars, resulting in various mechanically reversible and irreversible domain-switching states. The phenomenon can potentially be used for advanced bit writing and reading in nonvolatile memories, which effectively overcomes the backswitching problem and broadens the types of ferroelectric materials for nonvolatile memory applications.

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#### I. INTRODUCTION

Ferroelectric materials exhibit intrinsic coupling of spontaneous polarization and strain. Their ferroelectricferroelastic domains can be reversibly switched with voltage bias or mechanical stress. This characteristic has been used for high-density nonvolatile memories [1–[6\].](#page-8-0) In these devices, two opposite polarization directions act as the two logical signals, serving as memory bits which can be written and read through applying the electric field [\[3,7\]](#page-8-1). However, the instability of written ferroelectric domains, e.g., the time-dependent ferroelectric backswitching, has been a long-standing problem that causes significant data loss [8–[12\].](#page-8-2) Such backswitching results from the surface electrostatic or internal built-in elastic energy [\[8,13,14\]](#page-8-2) and has a higher impact on domains with small sizes. Small domain sizes are critical for high-density storage [\[15\]](#page-9-0). However, the relaxation of high-energy domain walls

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drives significantly ferroelectric backswitching when switched domain sizes are small [\[8\].](#page-8-2) Recently, ferroelastic domain switching by electrical stimulus has also been considered for memory applications [\[16,17\].](#page-9-1) However, the high elastic strain energy accompanying the ferroelastic domain switching tends to relax the switched domains, causing ferroelastic backswitching at zero bias [\[16,18\]](#page-9-1). Both ferroelectric and ferroelastic backswitching suggest the lack of reliability in domain switching under an electrical stimulus. Mechanical excitation is another possible way for controlling ferroelectric-ferroelastic domain switching [\[5,19,20\].](#page-8-3) Mechanical writing of ferroelectric polarization in a BaTiO<sub>3</sub> film has been realized [\[5\]](#page-8-3), in which polarization is 180 $^{\circ}$  reversed by mechanical loading as a result of a large strain gradient applied to the film surface by a probe via the mechanism of flexoelectricity [\[21,22\]](#page-9-2). Although stable domain patterns without relaxation for days are generated by mechanical writing, written domains are not reversible because of the unidirectional nature of the mechanical loading. Therefore, an alternative approach to overcome the above-mentioned limitations of

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using either electrical or mechanical excitation for memory applications of ferroelectric materials is necessary.

Relaxor-based ferroelectric single crystals with chemical compositions in the vicinity of the morphotropic phase boundary (MPB) have recently attracted significant attention due to their unique hysteresis behavior, ultrahigh piezoelectric properties, and electromechanical coupling factors [\[23\]](#page-9-3). Compared with normal ferroelectrics, relaxorbased ferroelectrics in MPB have abnormally small domain-wall energies, small coercive fields [\[24\],](#page-9-4) and miniature domain sizes which allow easy redistribution of invariant domain populations [\[25\].](#page-9-5) The domain-switching kinetics in a relaxor-based ferroelectric is different from that in normal ferroelectrics, which leads to the possibility of overcoming the abovementioned drawback. Previous research focused on the macroscopic materials responses of relaxor-based ferroelectric materials to electric or mechanical loading [\[23,26,27\]](#page-9-3), but little has been known about their microscopic responses.

Here, we apply *in situ* transmission electron microscopy (TEM) [\[25,28,29\]](#page-9-5) and phase-field modeling [\[30\]](#page-9-6) to explore the ferroelastic domain-switching kinetics under applied electrical and/or mechanical stimuli in  $Pb(Mg_{1/3}Nb_{2/3})O_3-33\%PbTiO_3$  (PMN-33%PT) relaxorbased single crystals. It is found that ferroelastic domain structures in PMN-33%PT single crystals are fully recoverable under a mechanical loading-unloading cycle (the mechanically reversible state) before electrical biasing. After applying a bias, domains become sensitive to mechanical load and exhibit only partial recovery (the mechanically irreversible state). However, the mechanically irreversible state returns to the mechanically reversible state after another mechanical loading-unloading cycle. Our results present the fundamental physics of domain-switching behavior in relaxor-based ferroelectrics and provide an approach to recover ferroelastic domain structures via a successive cycling of mechanical and electrical stimuli. Based on these discoveries, instead of trying to overcome the intrinsic instability of written ferroelectric domains, we propose a conceptual strategy to take advantage of the mechanically irreversible state and the mechanically reversible state for reliable bit writing and reading in nonvolatile memory devices. This expands the number of potential candidate materials for nonvolatile memory devices.

## II. IN SITU EXPERIMENT AND PHASE-FIELD SIMULATIONS

Figure  $1(a)$  presents a schematic of the *in situ* experimental setup. A bulk PMN-33%PT is fixed on a Cu plate using Pt deposition. Multiple PMN-33%PT pillars with dimensions of 2.0  $\mu$ m × 1.6  $\mu$ m × 0.06  $\mu$ m (length × width  $\times$  thickness) are produced using mechanical grinding and focused ion-beam processing. In situ mechanical and electrical stimulations in TEM are applied by a conductive tip. The Cu plate acts as an electrode and the conductive tip as the other electrode. A typical domain configuration observed from a pillar is presented in Fig. [1\(b\)](#page-1-0). Two types of domains appear with different contrast.

PMN-xPT with the composition  $x = 33\%$  is at MPB having a monoclinic structure [\[31,32\].](#page-9-7) The ferroelectric adaptive phase theory [33–[35\]](#page-9-8) suggests that monoclinic phases, consisting of miniaturization of stress-accommodating tetragonal domains, are microdomain averaged of tetragonal phases. A moderate constraint on the pillar exerted by the existence of oxygen vacancy, topological defects, and/or compositional variation in the

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FIG. 1. In situ TEM setup and ferroelastic domain configurations. (a) Schematic diagram of experimental setup. A bulk PMN-33%PT matrix with thin pillars is fixed on a grounded Cu platform using Pt deposition. A conductive tip connected to the electrical characterization module (ECM) acts as an indenter and electrode for mechanical and electrical loading. The actual allocation of the pillar and the tip is captured in the enlarged TEM image. (b) Dark-field TEM image (scale bar, 400 nm) and STEM-HAADF images (scale bar, 1 nm) showing a head-to-tail tetragonal  $a/c$ -domain configuration. Domain walls are indicated using blue dashed lines. Two parallel green lines indicate the area investigated in this study.

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FIG. 2. Ferroelastic domains switching by mechanical excitation. (a) A series of images (extracted from Video [1](#page-2-1) [\[41\]\)](#page-9-11) showing the evolution of ferroelastic domains under mechanical excitation. Domains are fully reversed after a mechanical loading-unloading cycle. Scale bar, 400 nm. (b) A load-bias–time curve showing the real-time application of the mechanical load with zero bias. Numbers 1 to 4 correspond to the image order in (a), indicating the position of the images in the curve. A load-displacement curve is shown in the inset graph.

relaxor-based single crystal is thus prone to a head-to-tail 90° ferroelastic domain configuration [36–[38\].](#page-9-9) This is confirmed by atomic-resolution scanning TEM (STEM) high-angle annular dark-field (HAADF) images shown in Fig. [1\(b\).](#page-1-0) Through the measurement of the displacement between Pb cations and their surrounding  $Mg/Nb/Ti$ cations in the HAADF images [\[39,40\],](#page-9-10) domains with light contrast (the c domain) are determined to have their polarization upward (see the bottom-left HAADF image), and domains with dark contrast (the  $a$  domain) have their polarization pointing to the right (see the top-right HAADF image), indicating that neighboring domains have a headto-tail 90° domain relationship. The 90° domain boundaries in Fig. [1\(b\)](#page-1-0) are indicated using blue dashed lines. Two parallel green lines are drawn in Fig. [1\(b\)](#page-1-0) to indicate the area of focus for the following investigation of domainswitching phenomena induced by external stimulation.

Stress is applied to pillars through moving the flat conductive tip toward the pillars in the displacement control mode with the displacement rate of  $3 \text{ nm/s}$  for approaching and -4 nm/s for retraction. The evolution of domain configuration during a mechanical loading-unloading cycle and the related load-bias–time curves (bias  $= 0$ ) are shown in Fig.  $2(a)$  (extracted from Video [1](#page-2-1) [41–[56\]\)](#page-9-11) and Fig.  $2(b)$ , respectively. Points 1 (before loading), 2, 3, and 4 in Fig. [2\(b\)](#page-2-0) correspond to the first, second, third, and fourth domain configuration in Fig. [2\(a\)](#page-2-0), respectively. With increasing load, the  $c$  domain shrinks and the  $a$  domain expands through the motion of the 90° domain boundaries toward the c domain. The initiation of the domain switching starts from domain boundaries. When the applied load reaches 22  $\mu$ N, the whole area is mostly occupied by a single  $a$  domain. Upon unloading, the domain configuration evolves in the opposite direction and the original domain configuration is fully recovered. The dark contrast lines in the c domain shown in Fig.  $2(a)$  (indicated by arrows) exist widely in relaxor-based ferroelectrics. It is caused by the existence of nanopolar regions [\[57\]](#page-10-0) or

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[VIDEO 1.](http://link.aps.org/multimedia/10.1103/PhysRevApplied.8.064005) A mechanical loading-unloading cycle.

regions of dipole glass in relaxor-based ferroelectrics [\[58](#page-10-1)–60]. These regions have local polarization variation compared with their surrounding areas. Because the loading and unloading processes are displacement control with constant displacement rates, the approximate linear loadtime curve for approaching and retraction and the inset fully reversible load-displacement curve in Fig. [2\(b\)](#page-2-0) indicate that the deformation process of the pillar is elastic without noticeable bending.

The maximum load is always kept to  $\sim$ 28  $\mu$ N to assure the comparability of different loading and unloading experiments. The maximum load corresponds to an applied stress of ∼300 MPa, which is very small compared to the fracture strength of the material, and therefore does not damage the material [\[61,62\].](#page-10-2) The applied stress needed to initiate domain-wall motion in this sample is around 40 MPa, which is well below the values reported for other materials [\[61\].](#page-10-2) This type of domain-wall motion is easily triggered due to the unpinning effect to the domain walls, which are commonly observed in relaxors around MPB [\[63,64\]](#page-10-3).

To explain the observed phenomenon in Fig. [2,](#page-2-0) phasefield calculations are conducted and the results are shown in Fig. [3.](#page-3-0) In our previous research [\[20\],](#page-9-12) we demonstrated that domain switching in PMN-38%PT occurs via the nucleation and growth of nanodomains because of the much smaller energy of nanodomains than bulk domains in PMN-38%PT. It is also reported that the strong pinning force acts on the domain walls, leading to nanodomain nucleation and motion rather than bulk domain-wall motion in this material [\[20\].](#page-9-12) In contrast, domain switching in PMN-33%PT reported here occurs via bulk domain motion, which is caused by the low energy of bulk domains in PMN-33%PT and the lack of a pinning force on the domain walls. For the PMN-33%PT with a unit-cell volume of 64.9  $\AA^3$  at room temperature, phase-field calculations show that the energy of a single-tetragonal  $a$  and  $c$  domain (see details in the phase-field calculations in the Supplemental Material S3 [\[41\]\)](#page-9-11) in a pillar is −0.443 and −1.05 meV, respectively, which is smaller than the energy of domains in PMN-38%PT and is 2 orders of magnitude smaller than the energy (∼100 meV) of tetragonal domains in normal ferroelectric materials. Notice that the energy of a domain or a domain structure represents the difference in energies between the cubic state and the tetragonal state (including the  $a$  domain and the  $c$  domain). The calculated energy of the bulk single-tetragonal domain includes ferroelastic energy and bulk free energy. The smaller energy of the 90° domain structure in PMN-33%PT without a strong pinning effect on domain walls indicates that the nucleation of nanodomain in PMN-33%PT is not energetically necessary and bulk domain-wall motion is preferred. The reversible domain switching in a mechanical loadingunloading cycle results from two reasons: (1) a small external field can activate domain-wall motion due to the small energy barrier among tetragonal domains [\[24\]](#page-9-4), agreeing with the easy polarization rotation around MPB; and (2) the elastic constraint to the PMN-33%PT pillar leads to remarkably different stress states for in-plane a domains and out-of-plane c domains, resulting in an asymmetric energy barrier between the two domains. In particular, the domain transition from the  $a$  domain to the c domain has a lower energy barrier (red solid line), as shown in Fig. [3\(a\).](#page-3-0) Figure [3\(b\)](#page-3-0) shows the hysteresis loops

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FIG. 3. Domain switching kinetics in a single-crystal PMN-33%PT pillar predicted by phase-field calculations. (a) The asymmetric energy barrier between a and c tetragonal ferroelastic domains (red solid line). Mechanical constraint exerted to the pillar breaks the original symmetric energy barrier, resulting in an easier domain transition from  $a$  domain to  $c$  domain (blue solid vector) compared to the reverse transition path (blue dash vector). Such different transition paths are not obvious in normal ferroelectrics due to their large energy barriers. (b) A displaced hysteresis loop (red solid line) for the PMN-33%PT pillar. Also displayed are hysteresis loops of a bulk relaxor single-crystal (black dash line) and normal ferroelectrics (green dashed line).

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FIG. 4 Ferroelastic domains switching by electrical excitation. (a) A series of images (extracted from Video [2](#page-4-1) [\[41\]\)](#page-9-11) showing the evolution of ferroelastic domains under electrical loading. Scale bar, 400 nm. (b) A load-bias–time curve. No mechanical load is applied during the whole process. The bias is applied from 0 V (5 s) to  $+10$  V (15 s) with the ramping rate of 1 V/s.

of normal ferroelectrics (the green dashed line), bulk PMN-33%PT (the black dash line), and PMN-33%PT pillars (the red solid line). Compared to the hysteresis loop of normal ferroelectrics, the hysteresis of a bulk PMN-33%PT single crystal is slim with a small coercive field [\[23\]](#page-9-3). An asymmetric and low-energy barrier of the PMN-33%PT pillar displaces the slim hysteresis to the left, making the initial ferroelastic domain structure closer to the domain state at a positive coercive field as shown in Fig. [3\(b\).](#page-3-0) As a result, a compressive loading-unloading cycle [blue dashed line in Fig. [3\(b\)\]](#page-3-0) can recover the initial ferroelastic domain structure. Figure [3\(b\)](#page-3-0) also indicates an irreversible state of polarization when a positive bias or a tension loading is applied (red solid line). This irreversible state can be compensated by applying a negative bias or a compression stress, leading to the recovery of the initial state.

Such reversible hysteresis loops are observed in a  $\langle 001 \rangle$ poled  $Pb(Zn_{1/3}Nb_{2/3})O_3-PbTiO_3$  relaxor-based single crystal with the easily activated 71° domain rotation [\[23\].](#page-9-3) In an aged  $BaTiO<sub>3</sub>$  single crystal, a defect-induced internal field pins and retracts ferroelastic domain-wall motion, leading to reversible domain switching [\[65\].](#page-10-4) However, these two reversible phase-transition processes are studied based on macroscale observations without knowing the effects of complex domain structures and heterogeneous nucleation of alternative domains. The present study, which utilizes the asymmetric domain-transition kinetics between tetragonal a and c domains in the ubiquitous microscopic 90° head-to-tail ferroelastic domain configuration, demonstrates an alternative approach for reversible domain switching.

The effect of a voltage bias on domain configuration is presented in Fig. [4\(a\)](#page-4-0) (extracted from Video [2](#page-4-1) [\[41\]](#page-9-11)). The corresponding load-bias-time curve (external load  $= 0$ ) is illustrated in Fig. [4\(b\).](#page-4-0) Again, points 1, 2, 3, and 4 in Fig. [4\(b\)](#page-4-0) correspond to the first, second, third, and fourth image in Fig. [4\(a\)](#page-4-0). Gentle contact between the conductive tip and the pillar is held for the close-loop electrical loading experiment. The bias is raised from 0 to  $+10$  V between 5 and 15 s with the ramping rate of  $1 \frac{\text{V}}{\text{s}}$  as shown in Fig. [4\(b\)](#page-4-0). Although no mechanical load is applied, there is still a small load detected, which is caused by the electrostrictive effect [\[66\]](#page-10-5) in ferroelectric materials. With the increase of the bias from 0 V to  $+2 \text{ V}$  $+2 \text{ V}$  $+2 \text{ V}$  (5 to 7 s in Video 2 [\[41\]\)](#page-9-11), the domain configuration did not change as the initiation energy for domain motion is not reached. Further increasing the bias results in the shrinkage of the  $a$  domain and the simultaneous expansion of the  $c$ domain. When the bias is increased to  $+10$  V, the whole area is occupied by nearly a single  $c$  domain as shown in the third image in Fig. [4\(a\).](#page-4-0) After retraction of the bias at 15 s, the a domain back switches and is gradually stabilized at 20 s, as shown in Fig. [4\(a\)](#page-4-0). Comparison of the initial and final domain configurations shows that the area of the  $c$  domain increases after an electrical loading cycle, i.e., the domain configuration is only partially recovered. This is consistent with our proposed mechanism indicated in Fig. [3\(b\).](#page-3-0) The resulting domain structure is stable and remains unchanged after four weeks.

Phase-field modeling shown in Fig. [5](#page-5-0) confirms the experimental results. It suggests a stable domain

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[VIDEO 2.](http://link.aps.org/multimedia/10.1103/PhysRevApplied.8.064005) An electrical loading-unloading cycle.

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FIG. 5. Phase-field modeling (a),(c),(e),(g) ferroelastic domain switching under a mechanical loading cycle, an electrical loading cycle, a mechanical loading cycle after electric loading, and a mechanical loading cycle after previous mechanical loading, respectively. White arrows represent the directions of polarization.  $(b)$ , $(d)$ , $(f)$ , $(h)$  Closed and open polarization-load curves corresponding to the phase-field modeling in (a),(c),(e), and (g), respectively. The blue lines indicate the loading process and the pink lines the unloading process.

configuration in a tetragonal ferroelectric holds 90° ferroelastic domain walls, which move along the direction normal to domain-wall planes under mechanical loading, as shown in Fig. [5\(a\)](#page-5-0). Polarization rotation occurs only around the domain walls [\[67\]](#page-10-6). One interesting feature of this initial ferroelastic domain configuration in the PMN-33%PT pillar is that this domain state locates around the positive coercive field. When a compressive loading-unloading cycle is applied, phase-field modeling suggests a recoverable domain switching as shown in Figs. [5\(a\)](#page-5-0) and [5\(b\).](#page-5-0) The change of polarization state  $\delta$  before and after this mechanical cycle is zero. Figure [5\(b\)](#page-5-0) shows a nucleation regime that activates the domain transition from the c domain to the a domain exists at the beginning of the compressive loading process (the increase of polarization region). After the domain-wall motion is activated, the polarization varies monotonically with the external stimulus, which results from the soft pinning force to domain-wall motion in the PMN-33%PT pillar. When positive voltage bias is applied to the initial ferroelastic domain structure, an incubation stage for domain-wall motion to promote the transition from the  $a$  domain to the  $c$  domain is not obvious [Figs. [5\(c\)](#page-5-0) and [5\(d\)\]](#page-5-0). In the bias unloading process, however, the energy released by the electric unloading process is not sufficient to activate reverse domain-wall motion, pinning the domain-wall motion. Thus, the domain structure does not reverse in this electrical loading-unloading cycle as shown in Figs.  $5(c)$  and  $5(d)$ .

Interestingly, mechanical loading after an electrical loading cycle erases the polarization introduced by the electrical loading-unloading cycle [Fig. [5\(e\)\]](#page-5-0). As is consistent with Fig. [3\(b\)](#page-3-0), the original ferroelastic domain configuration is recovered by applying a mechanical loading-unloading cycle. As a result, the stress-polarization loop is not a closed one [Fig. [5\(f\)\]](#page-5-0), i.e., the change of polarization  $\delta$  is not zero. After the first mechanical loading-unloading cycle following electrical cycles, the second mechanical loading-unloading cycle is applied, leading to reversible domain switching in Figs. [5\(g\)](#page-5-0) and [5\(h\).](#page-5-0) The phase-field simulation results are consistent with the proposed domain-switching kinetics shown in Fig. [3\(b\).](#page-3-0)

Experiments are conducted to confirm the phase-field simulation results on mechanical loading-unloading cycles after an electrical loading cycle. After an electrical loading cycle, mechanical loading-unloading cycles are applied to the same area as shown in Fig. [6](#page-6-0) and Videos [3](#page-6-1) and [4](#page-6-2) [\[41\]](#page-9-11). The load-bias–time curve for the first mechanical loading cycle is shown in Fig. [6\(b\).](#page-6-0) The domain configuration shown in the first image in Fig.  $6(a)$  is the back-switched configuration after an electrical loading cycle [the same as the last image in Fig. [4\(a\)\]](#page-4-0). Again, increasing mechanical loading leads to the expansion of the a domain that reaches its maximum size under the highest load. After unloading, the a domain shrinks but does not return to its original size and shape, i.e., the size of the  $c$  domain is smaller than that before mechanical loading, which confirms the simulation result in Fig. [5](#page-5-0) that domain switching is partially reversed.

The effect of mechanical loading for the second and subsequent mechanical loading cycles is shown in Fig. [6\(c\)](#page-6-0) and the corresponding load-time curve is presented in Fig. [6\(d\).](#page-6-0) The initial domain configuration [the first image in Fig.  $6(c)$  is the same as the final domain configuration presented in the last image of Fig. [6\(a\)](#page-6-0). After a complete mechanical loading-unloading cycle, the

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FIG. 6. Mechanically reversible and irreversible ferroelastic domains. A series of images (extracted from Videos [3](#page-6-1) and [4](#page-6-2) [\[41\]](#page-9-11)) of ferroelastic domains responding to the first mechanical loading-unloading cycle (a) and the second mechanical loading-unloading cycle (c) after an electrical loading cycle. Scale bars, 400 nm. (b) and (d) show the corresponding load-bias–time curves in which the highest load is restricted to  $\sim$ 28 μN.

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[VIDEO 3.](http://link.aps.org/multimedia/10.1103/PhysRevApplied.8.064005) The first mechanical loading-unloading cycle after an electrical loading-unloading cycle.

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[VIDEO 4.](http://link.aps.org/multimedia/10.1103/PhysRevApplied.8.064005) The second mechanical loading-unloading cycle after an electrical loading-unloading cycle.

domain configuration returns to its original structure shown in the first image of Fig. [6\(c\)](#page-6-0), suggesting that the previous mechanically irreversible state [Fig. [6\(a\)\]](#page-6-0) has been converted to a mechanically reversible state after the first mechanical loading-unloading cycle. The two continuous mechanical cycle processes indicate that the reversible nature of ferroelastic domains is repeatable.

## III. A PROPOSED APPROACH FOR BIT WRITING AND READING

It is now clear that an electrical loading-unloading cycle introduces the mechanically irreversible state and a subsequent mechanical loading-unloading cycle brings the domain configuration back to the mechanically reversible state. By taking advantage of the phenomenon, an advanced writing and reading approach for nonvolatile memories is proposed. In the following discussion, the mechanically reversible state, i.e.,  $\delta = 0$  in the polarization-stress curve after a mechanical loading-unloading cycle, is defined as the logical signal 0, while the mechanically irreversible state, i.e.,  $\delta > 0$  after a mechanical loading-unloading cycle, is defined as the logical signal 1.

When domains at the mechanically reversible state are subjected to a mechanical loading cycle, the mechanically reversible state remains. This provides the first logical expression:

reversible state þ mechanical loading cycle ¼ reversible state;

$$
0 + \sigma = 0.\t\t(1)
$$

If the mechanically reversible state is subjected to an electrical loading cycle, it transfers to the mechanically irreversible state and this can be expressed by

reversible state + electrical loading cycle = irreversible state,  
\n
$$
0 + E = 1.
$$
\n(2)

When mechanically irreversible domains experience a mechanical loading cycle, its state switches to the mechanically reversible one:

> irreversible state  $+$  mechanical loading cycle  $=$  reversible state,  $1 + \sigma = 0.$  (3)

Mechanically irreversible domains remain after another electrical loading cycle (see the Supplemental Material S1 [\[41\]](#page-9-11)), therefore,

irreversible state  $\phi$  electrical loading cycle = irreversible state;

$$
1 + E = 1.\tag{4}
$$

These four logical expressions provide the fundamental rules for logical identification in writing and reading bits. The ways of writing bits by mechanical and electrical excitations and reading bits by mechanical excitation are illustrated in Fig. [7\(a\)](#page-8-4), in which a four-cell matrix has the original logical states of  $Aa(1)$ ,  $Ab(1)$ ,  $Ba(0)$ , and  $Bb(0)$ [see the first matrix in Fig.  $7(a)$ ]. Based on the four logical expressions, applying mechanical stress to cells  $Aa$  and  $Ba$ , and electrical loading to cells Ab and Bb leads to the logical states of  $Aa(0), Ab(1), Ba(0), and Bb(1),$  as shown in the second matrix in Fig. [7\(a\).](#page-8-4) Reading the logical states in the four cells is achieved by applying mechanical stress to each of the cells and this process results in the logical state of 0 for all 4 cells, as shown in the third matrix in Fig. [7\(a\)](#page-8-4). Local polarization change  $(\delta)$  before and after mechanical excitation is used to determine the logical signal of each cell during reading. Aa and Ba follow rule (1) with  $\delta = 0$ while Ab and Bb follow rule (3) with  $\delta \neq 0$ . As has been defined above, it reads 0 if  $\delta = 0$  or 1 if  $\delta \neq 0$ , as shown in Fig. [7\(b\).](#page-8-4) Electrical reading can also be achieved when electrical-reversible states (the same state as the mechanical-irreversible state) and electrical-irreversible states (the same state as the mechanical-reversible state) are used as two memory states.

While the backswitching drawback can be overcome by using  $\delta = 0$  and  $\delta \neq 0$  as the two memory states, the

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FIG. 7. Writing and reading bits processes. (a) Mechanically reversible domains are denoted as the logical signal 0 while mechanically irreversible domains are the logical signal 1. In the writing process, by applying the bias to cells Ab and Bb, and mechanical loading to cells Aa and Ba, the logical states of the 4 cells become  $Aa(0)$ ,  $Ab(1)$ ,  $Ba(0)$ , and  $Bb(1)$ , which are independent of their initial states. In the reading process, mechanical loading is applied to the cells and transfers logical states in the cells to the mechanically reversible state (0). (b) By detecting the change of the polarization  $\delta$ , cells are read 0 when  $\delta = 0$  or 1 when  $\delta > 0$ . Cells are therefore read  $Aa(0), Ab(1),$  $Ba(0)$ , and  $Bb(1)$ .

designs of the corresponding reading circuit is not an easy task. A more efficient circuit design is therefore necessary for our proposed bit writing and reading strategy.

#### IV. CONCLUSIONS

In conclusion, in situ TEM experiments and phase-field modeling have been used to explore the combined effects of mechanical stress and electric loading on the ferroelastic domain structures in PMN-33%PT. Results show that domain structures can be in the mechanically irreversible state or the mechanically reversible state depending on if the structures have been subjected to electrical or mechanical excitation. These domain-switching behaviors are different from that of normal ferroelectric materials and relaxor-based ferroelectric materials with compositions that are outside MPB. This is due to the low and asymmetric energy barriers among different domains. The two domain reversibility states can be used to represent the logical signals 0 and 1 for nonvolatile memories. This logical calculation strategy is not affected by the ferroelasticferroelectric domain backswitching and therefore overcomes the long-standing problem of backswitchinginduced data loss in the memories, significantly enhancing the reliability of the nonvolatile memories. Further, this writing and reading method allows the use of ferroelastic domains (e.g., the 90° domains in this investigation) and therefore significantly broadens the number of candidate materials for nonvolatile memories.

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