

Stability and Band-Gap Tuning of the Chalcogenide Perovskite BaZrS₃ in Raman and Optical Investigations at High Pressures

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We report experiments and calculations investigating the pressure and temperature dependences of the optical phonons in BaZrS₃, and the pressure dependence of its absorption edge. BaZrS₃ is a chalcogenide perovskite in a novel class of materials being considered for photovoltaics. It is studied by Raman spectroscopy as functions of temperature (at 1 atm) and pressure (at 120 and 295 K), and by pressure-transmission spectroscopy at 295 K. Density-functional-theory calculations predict the allowed Raman lines, their intensities, their pressure shifts, and the band-gap pressure shift. Cooling shifts all but one of the phonon peaks to higher frequencies; the temperature coefficients are typical of semiconductors. A strong low-temperature peak at 392.3 cm⁻¹ is attributed to resonant forbidden LO scattering; its shift with temperature has the opposite sign. The pressure coefficients of the phonon frequencies for all observed Raman peaks are positive, indicating no mode softening. The rates of pressure shift also are typical, and show the customary scaling with phonon frequency. Experiment and theory show good agreement on the pressure-induced frequency shifts. The BaZrS₃ absorption edge moves to lower energy with pressure, reflecting a reduction of the band gap. The measured shift is ~ -0.015 eV/GPa, slightly less than the density-functional-theory result of -0.025 eV/GPa. We find no evidence that the perovskite structure of BaZrS₃ undergoes any phase changes under hydrostatic pressure to at least 8.9 GPa. Our results indicate the robust structural stability of BaZrS₃, and suggest cation alloying as a viable approach for band-gap engineering for photovoltaic and other applications.

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I. INTRODUCTION

Chalcogenide perovskites containing group-VI anions including S and Se are emerging as a novel class of semiconductors with potential photovoltaic and optoelectronic applications [1–4]. Although first synthesized some six decades ago [5,6], these materials are scarcely investigated compared to their oxide counterparts, which have been studied intensively because of their geophysical significance [7], and because of their ferroelectric, piezoelectric, electrolytic, and optoelectronic properties enabling many advances in applications [8–13]. The recent advances in organic-inorganic halide perovskites as solar absorbers demonstrating power conversion efficiencies in the 20% range [14–16] has led to a revived interest in chalcogenide perovskites [1–4], in an effort to address the instability and toxicity issues faced by halide perovskites.

BaZrS₃ is a prototypical chalcogenide perovskite. It is theoretically predicted to be a direct-band-gap semiconductor with a band gap of ~ 1.7 – 1.85 eV. This is subsequently

confirmed by optical measurement [2–4]. The material shows strong absorption in the visible spectrum. The material is also shown to be stable against oxidation and moisture [3]. For a single-junction solar cell, the optimum band gap is 1.3–1.5 eV [17]. To tune the band gap of chalcogenide perovskites, cation or anion alloying can be employed. For example, full replacement of Ba in BaZrS₃ by Sr was shown to give a band gap ~ 2.1 eV in β -SrZrS₃ (distorted perovskite phase) and ~ 1.5 eV in α -SrZrS₃ (needlelike phase) [4]. Also, by substitutionally replacing a fraction of the Zr in BaZrS₃ with Ti, the conduction band is expected to be lowered, thereby tuning the band gap to smaller energies. Since Ti has a smaller atomic radius, the volume of the unit cell is expected to shrink with increasing Ti concentration. It is therefore desirable to explore whether BaZrS₃ is structurally stable against volume compression.

In the present study, we employ Raman spectroscopy and density-functional theory to investigate the pressure (P) and temperature (T) dependences of the optical phonons in this chalcogenide perovskite. Additionally, using optical transmission we show that the band gap of BaZrS₃ decreases with applied pressure, an important consideration for photovoltaics as noted above. Prior Raman studies on

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oxide perovskites [12,18–21] have established that a knowledge of the effects of pressure and temperature on the vibrational modes is fundamental to understanding the structural stability, bonding, and polarization states in perovskites, and the mechanisms that mediate changes in these properties. The effects of pressure on the phonons and the band gap in BaZrS_3 have not been measured previously. A brief initial report of the low-temperature Raman spectra of this material has appeared [3]. Prior reports of the Raman spectra at ambient conditions have been given for BaZrS_3 [4,22], BaMS_3 ($M = \text{Ti}$ and Nb) [23], and SrZrS_3 [4], and the ambient band gaps of these materials have also been reported from experiment and theory [1–4,22].

II. EXPERIMENT

Polycrystalline powders of BaZrS_3 suitable for Raman measurements are grown by high-temperature sulfurization of BaZrO_3 (>99% purity) in a CS_2 atmosphere. CS_2 gas (>99.8% purity) is introduced to the sample via conventional Ar transport methods. The CS_2 flow rate (10–20 standard cm^3/min), and the reaction time and temperature (~ 4 h at 1050°C) are optimized to obtain homogeneous BaZrS_3 without oxide phases or other impurity phases. The quality of the samples is confirmed by several characterization methods prior to our Raman experiments. Crystal structure and phase uniformity are assessed by x-ray ($\text{Cu K}\alpha$) diffraction using a dual-position graphite monochromator. The BaZrS_3 is found to be in the orthorhombic distorted perovskite $Pnma$ structure with the lattice constants $a = 7.04 \text{ \AA}$, $b = 9.98 \text{ \AA}$, and $c = 7.05 \text{ \AA}$ in agreement with prior results [6]. Within the instrument's detection limits of 1% concentration, no secondary phase is observed. The morphology and elemental composition are analyzed using a field-emission scanning electron microscope equipped with an energy dispersive x-ray spectrometer. A composition close to stoichiometry is found, with Ba:Zr:S proportions of 21.6:21.4:57.0. The small deviations from ABX_3 stoichiometry (a common situation in perovskites) probably arise from S vacancies due to the high-temperature synthesis. The band gap is estimated to be 1.74 eV by UV-visible diffuse reflection spectroscopy. A detailed account of the BaZrS_3 synthesis and sample characterization results is presented elsewhere [3].

Raman measurements are made using the 647, 676, and 752-nm lines of a CW Kr^+ laser. The spectra are collected using a 1-m double monochromator (Jobin-Yvon U1000) equipped with 1800-g/mm holographic gratings and a GaAs photomultiplier operating in photon counting mode. Because the samples are polycrystalline, polarized Raman spectra are not collected. Ambient pressure spectra are recorded at 295–14 K in a standard He closed-cycle cryostat. Spectra at high pressure are measured using ruby-calibrated diamond anvil cells (DAC) employing hardened stainless-steel gaskets with drilled sample chambers $\sim 200 \mu\text{m}\phi \times 70 \mu\text{m}$ deep. We record Raman spectra at 295 K [room

temperature (RT)] up to 8.9 GPa, and at 120 K up to 6.8 GPa. The pressure experiments at low temperature employ a separate liquid-He variable-temperature cryostat. The pressure medium in all of the DAC runs is 4:1 methanol:ethanol. This alcohol medium is hydrostatic to 9.5 GPa at RT and quasihydrostatic in a gasketed DAC at low T (i.e., strain gradients of $\lesssim 0.5$ GPa across the 200- μm -diameter gasket-sample chamber) [24,25].

III. DFT CALCULATIONS

First-principles calculations on the BaZrS_3 system are carried out based on density-functional theory (DFT) using the Perdew-Burke-Ernzerhof revised-for-solids functional [26], as implemented in the Vienna *ab initio* simulation package [27], and projector-augmented-wave potentials [28] are used together with a plane-wave basis set. Plane waves up to a kinetic energy cutoff of 30 Ry are employed. A Γ -centered $9 \times 7 \times 9$ k -point grid is used to sample the Brillouin zone. In structural optimization, the stopping criterion for atomic forces is set to be 0.2 mRy/bohr. The lattice constants are optimized by using the calculated stress [29]. At the equilibrium volume, the calculated stress is smaller than 0.1 GPa. The calculations first obtain the equilibrium lattice constants and the internal atomic coordinates at $P = 0$ GPa and $T = 0$ K. The distorted perovskite structure with the $Pnma$ space group [1] is used here. The optimized lattice constants found by the calculations are $a = 7.102 \text{ \AA}$, $b = 9.955 \text{ \AA}$, and $c = 6.957 \text{ \AA}$, in good agreement with the experimental values from previous ($a = 7.060 \text{ \AA}$, $b = 9.981 \text{ \AA}$, and $c = 7.025 \text{ \AA}$) [30] and the present works. The calculated result for the bulk modulus of BaZrS_3 at $P = 0$ is $B_0 = 75$ GPa. To calculate B_0 , we use the empirical equation of state proposed by Vinet *et al.* [31] and nine data points for volume varying between about $\pm 12.5\%$ of the equilibrium volume. To our knowledge, no measurements of B_0 for this material have been reported.

We next calculate the frequencies ν_i of the optical phonons using the linear response method [32] and the intensities of the Raman active modes following the method of Umari *et al.* [33]. The pressure shifts $(d\nu_i/dP)_{P=0}$ of the phonon frequencies are then computed by reducing the volume from the ambient value V_0 down to about $0.913 V_0$ in six steps. At each reduced volume the lattice shape and the internal coordinates are reoptimized while preserving the reduced volume. Then the external pressure P and the ν_i are calculated at each reduced volume.

From our DFT calculations we also obtain the change in energy of the direct band gap with pressure. This is found to be approximately linear with an average shift to lower energy of ~ -0.025 eV/GPa.

IV. RESULTS

Figure 1 shows the BaZrS_3 distorted perovskite structure. It has the orthorhombic space group $Pnma$ (D_{2h}^{16}) with

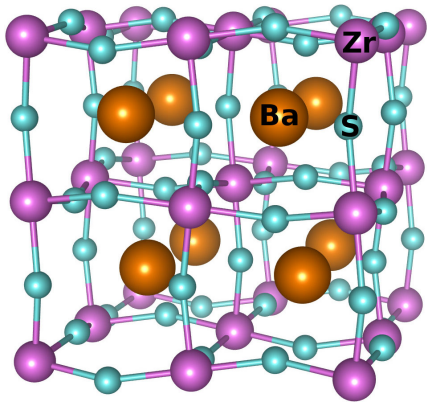


FIG. 1. BaZrS₃ distorted perovskite *Pnma* crystal structure.

four BaZrS₃ formula units per primitive unit cell. The lattice can be viewed as composed of distorted ZrS₆ corner-sharing octahedra, with each Ba atom centrally located in the spatial region defined by its neighboring S and Zr atoms. In this structural motif, twisting of the ZrS₆ octahedra about the *a* axis changes the symmetry from cubic to *Pnma* [34].

Group theoretical analysis for the *Pnma* (D_{2h}^{16}) structure reveals 57 zone-center optical phonons, classified according to $(7A_g + 5B_{1g} + 7B_{2g} + 5B_{3g}) + (9B_{1u} + 7B_{2u} + 9B_{3u}) + 8A_u$. Because of inversion symmetry, only the first 24 even (gerade) modes are Raman active. The next set of 25 odd-parity *B* modes are infrared active, and there are eight optically inactive *A_u* modes [35–37]. Genet *et al.* [38] have given diagrams of the mode geometries for this structure. Figure 2 presents the Raman spectrum of BaZrS₃ measured in this work at 14 K and $P = 0$ for the spectral range spanning the calculated intrinsic phonon frequencies of this material; the 676-nm laser line is used. Standard line-shape analysis (dashed and solid curves) is able to fit this spectrum with 16 peaks, and the labels designate the likely peak assignments. The vertical lines in the figure indicate

the calculated positions and relative intensities of modes with theoretical relative oscillator strengths greater than 2%. Table I lists the symmetries and theoretical frequencies ν_{theor} of the 24 Raman active modes, and also gives the measured positions ν_{expt} for the maxima of the fitted experimental peaks. In cases where the theoretical modes are too close to be experimentally resolved, identical experimental values of ν_{expt} are given (five pairs of lines). We see that the correspondence between experiment and theory for the frequencies and relative intensities of the spectral features observed below 325 cm⁻¹ is reasonably close. The predicted phonon frequencies are within 10 cm⁻¹ of the fitted peak maxima, and the relative intensities agree within 30%. The weak shoulders at 235 cm⁻¹ and at 378 cm⁻¹ [each marked by a (?)] may arise from two-phonon scattering, and these features are left unassigned at present.

The comparison is not as good between the B_{1g}^5 , B_{2g}^7 , and B_{3g}^5 modes and the measured peaks in the 390 – 440 cm⁻¹ region. Ishii *et al.* [22] show by a valence-force-field model that the phonons in this region correspond mainly to Zr-S stretching modes. We see in Fig. 2 that the 392.3-cm⁻¹ peak is the most intense feature in the 14-K Raman spectrum. This is at odds with the very weak oscillator strengths predicted by the DFT calculations for the B_{1g}^5 , B_{2g}^7 , and B_{3g}^5 modes, and so is puzzling. Also, the large width of the fitted peak at 400 cm⁻¹ makes this feature difficult to assign. Although its central frequency is close to that predicted for B_{2g}^7 , the peak's large width suggests that it may arise from a mixture of unresolved features. In the next section, we comment further on the scattering in the 390 – 440 cm⁻¹ region.

In summary of the above results, based on the comparison between experiment and theory, we find that the most plausible assignments of the observed Raman peaks are those presented in Table I. All but three of the intrinsic phonon modes can be assigned.

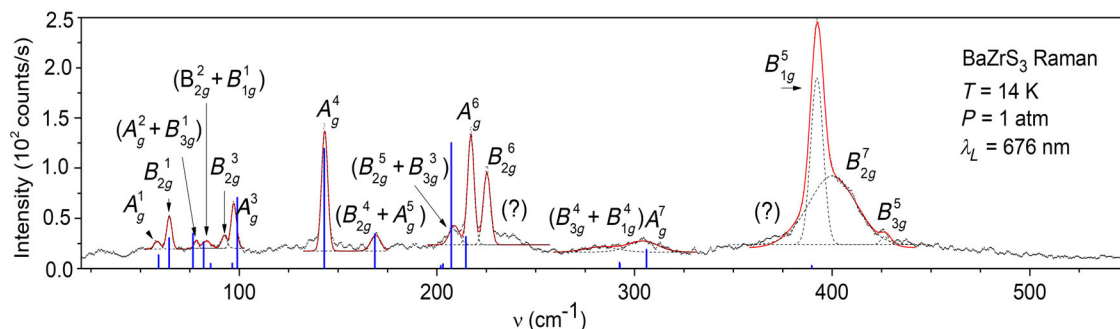


FIG. 2. Measured Raman spectrum (points) of BaZrS₃ at 14 K and $P = 0$ GPa. Dashed and solid red curves are best-fit results for the individual peaks and the cumulative spectrum, respectively. Labels give the peak phonon assignments based on comparison with the results of our DFT calculations. (See Table I, and text.) Question marks designate unassigned weak features that may arise from two-phonon scattering. Vertical lines indicate the theoretical strength of modes relative to the strongest DFT-calculated Raman peak (A_g^6 line at 206.8 cm⁻¹); calculated modes with theoretical strengths less than 2% of this maximum are not represented.

TABLE I. Raman assignments with theoretical (ν_{theor}) and fitted experimental (ν_{expt}) 14-K frequencies given in cm^{-1} . Adapted in part from Perera *et al.* [3].

| Mode | ν_{theor} | ν_{expt} | Mode | ν_{theor} | ν_{expt} | Mode | ν_{theor} | ν_{expt} | Mode | ν_{theor} | ν_{expt} |
|------------|----------------------|---------------------|------------|----------------------|---------------------|------------|----------------------|---------------------|------------|----------------------|---------------------|
| A_g^1 | 59.2 | 58.5 | B_{2g}^3 | 97.7 | 92.4 | A_g^5 | 168.6 | 169.0 | B_{3g}^4 | 289.7 | 283.3 |
| B_{2g}^1 | 64.0 | 64.6 | A_g^3 | 98.9 | 97.2 | B_{1g}^3 | 174.5 | | B_{1g}^4 | 290.2 | 283.3 |
| A_g^2 | 76.0 | 78.2 | B_{1g}^2 | 111.0 | | B_{2g}^5 | 201.7 | 208.9 | A_g^7 | 304.0 | 304.3 |
| B_{3g}^1 | 76.8 | 78.2 | A_g^4 | 142.8 | 143.2 | B_{3g}^3 | 202.9 | 208.9 | B_{1g}^5 | 387.5 | 392.3 |
| B_{2g}^2 | 81.6 | 83.4 | B_{3g}^2 | 160.1 | | A_g^6 | 206.8 | 217.2 | B_{2g}^7 | 398.6 | 400.1 |
| B_{1g}^1 | 85.8 | 83.4 | B_{2g}^4 | 167.7 | 169.0 | B_{2g}^6 | 214.6 | 225.3 | B_{3g}^5 | 417.6 | 426.5 |

V. TEMPERATURE DEPENDENCE

The effect of temperature on the ambient-pressure Raman spectrum of BaZrS_3 is studied between 14 K and RT. The recorded spectra are shown in Fig. 3. The Raman peaks shift in frequency and sharpen upon cooling, and the sharpening enables us to resolve four additional peaks (A_g^2 , B_{2g}^4 , B_{2g}^5 , A_g^7). The shift of all but one of the observed peaks is toward higher frequencies with decreasing temperature, the characteristic behavior for anharmonic phonon interactions in semiconductors [39,40]. The exception is the anomalously strong peak at 392.3 cm^{-1} (Fig. 3 and Table I). The observed maximum of this spectral feature moves in the opposite direction, to lower frequency with decreasing temperature.

The decrease of phonon frequency with increasing temperature has two sources—decay of the harmonic mode

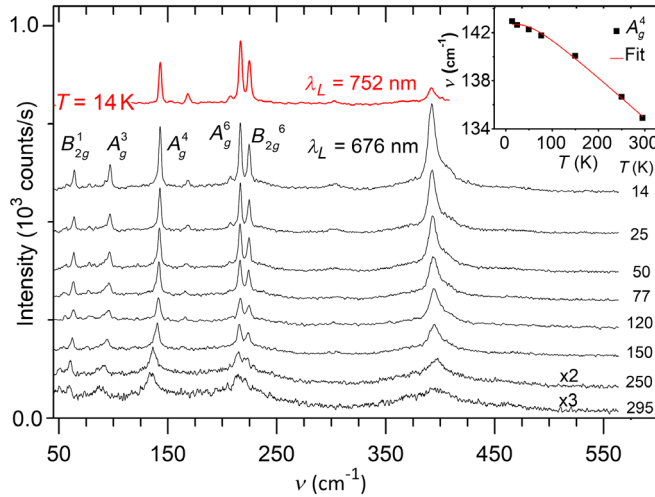


FIG. 3. BaZrS_3 Raman data taken at temperatures from 14 to 295 K using 676 nm (lower eight traces) and 752 nm (top trace) laser lines. Spectra are displaced for clarity. The 752-nm trace is scaled individually as described in the text. The latter result shows the strong resonant Raman effect on the 392.3-cm^{-1} peak. Gaussian line-shape fits are used to determine peak positions. The inset shows a sample fit of Eq. (1) to the temperature shift of the A_g^4 peak. Parameters for fit of Eq. (1) are given in Table II for all labeled peaks. Adapted in part from Perera *et al.* [3].

due to multiphonon interactions, and thermal-expansion-induced volume change. To characterize the thermal renormalization of the frequency, it is often useful to fit the measured results for the frequency $\nu(T)$ by the approximate expression [40,41]

$$\nu(T) = \nu_o - \Delta[1 + 2n(\nu_{\text{av}}, T)], \quad (1)$$

where ν_o is the harmonic frequency at $T = 0 \text{ K}$, Δ is the $T = 0 \text{ K}$ renormalization due to disorder effects (e.g., isotope disorder, impurities, defects), n is the Bose-Einstein population function, and ν_{av} is an average interaction frequency. This expression jointly includes the contribution of three-phonon decay (the dominant multiphonon process), and the effect of thermal expansion. Both mechanisms contribute sums of terms that exhibit a T dependence similar to that in Eq. (1); the fitted value of ν_{av} accounts for these sums in an average way.

In our experimental data six modes could be traced up to 295 K, including the anomalous 392.3-cm^{-1} feature that shifts to lower frequency with decreasing T . Table II gives the parameters found from the best fits of Eq. (1) for the five modes that exhibit the usual type of behavior. The dependence at high T is linear with negative slopes (last column of Table II), and the dependence for these modes tends to become sublinear in the range 40–60 K. The values of Δ and ν_{av} are typical of those in other semiconductor materials [41,42].

TABLE II. Fitted parameters in Eq. (1) that best describe $\nu(T)$ for five of the prominent BaZrS_3 Raman peaks in Fig. 3. Fourth and fifth columns give the quality of fit R^2 and the limiting high- T slopes, respectively.

| Mode | ν_o (cm^{-1}) | ν_{av} (cm^{-1}) | Δ (cm^{-1}) | R^2 | High- T slope (cm^{-1}/K) |
|------------|------------------------------|--|-------------------------------|-------|---|
| B_{2g}^1 | 64.6 | 57.9 | 0.72 | 0.996 | −0.0173 |
| A_g^3 | 98.2 | 63.2 | 1.25 | 0.999 | −0.0275 |
| A_g^4 | 145.6 | 116.2 | 2.92 | 0.994 | −0.0349 |
| A_g^6 | 217.1 | 93.1 | 0.68 | 0.966 | −0.0101 |
| B_{2g}^6 | 226.2 | 152.8 | 1.75 | 0.982 | −0.0159 |

Figure 3 allows us to follow the evolution of the intensity of the anomalous 392.3-cm^{-1} peak for Raman spectra recorded with the 676-nm laser line. With decreasing temperature this sharp peak rises rapidly out of the broad feature seen at 295 K in the $390\text{--}440\text{-cm}^{-1}$ region, and below 50 K, the 392.3-cm^{-1} peak is the most intense peak in the spectrum. Its frequency shift over the temperature range 14–150 K (where its position is not strongly up-shifted by the broad peak at higher frequency) is approximately linear with a slope of $\sim +0.018\text{ cm}^{-1}/\text{K}$. A satisfactory fit of Eq. (1) to the T dependence of the anomalous 392.3-cm^{-1} peak cannot be obtained. Equation (1) approaches $T = 0\text{ K}$ with vanishing slope, whereas the frequency of the 392.3-cm^{-1} peak asymptotes toward $T = 0\text{ K}$ with a positive slope.

To further explore the anomalously strong scattering in the $390\text{--}440\text{ cm}^{-1}$ region, Raman data are collected using 752-nm (1.65-eV) excitation. The top spectrum in Fig. 3 gives the 14-K result, with the intensity scaled so that the height of the A_g^6 peak matches that of the same peak in the second uppermost trace measured at 14 K using 676 nm (1.83 eV). Comparing these two spectra, we see that the relative intensity of the $390\text{--}440\text{-cm}^{-1}$ scattering, particularly the 392.3-cm^{-1} peak, is much reduced for 752-nm excitation. This strongly suggests that resonant forbidden LO-phonon scattering is the most likely cause of the $390\text{--}440\text{-cm}^{-1}$ anomaly [43]. Such scattering (due to the Frohlich mechanism) undergoes a much stronger resonant enhancement than the allowed scattering. Because 752 nm falls in the transparent region below the band gap of our BaZrS_3 powder sample ($E_g \sim 1.74\text{ eV}$), whereas 676 nm is resonant with the interband transitions, forbidden scattering is expected to contribute more strongly to spectra recorded with the latter line than with the former. The forbidden scattering is aided by the mixture of crystallite geometries available to support this process in our powder sample; the usual selection rules are relaxed due to the \mathbf{q} dependence of the Frohlich electron-phonon mechanism.

VI. PRESSURE DEPENDENCE

The effects of applied pressure on the Raman spectrum of BaZrS_3 are investigated at two different temperatures. Figure 4(a) shows several spectra recorded from 0.05 GPa to 8.9 GPa at 295 K; Fig. 4(b) presents spectra recorded at 120 K for various pressures up to 6.8 GPa. The pressure-Raman experiments conducted at 120 K are able to exploit the low-temperature sharpening of the spectra, thereby resolving more peaks and tracking their pressure dependences with greater precision. In both sets of data, we find that all of the observed peaks shift to higher frequency (i.e., phonon stiffening) with increasing pressure. In addition, the Raman intensity of the overall spectrum tends to decrease gradually as the pressure is raised. This change is smaller for the scattering in the $390\text{--}440\text{-cm}^{-1}$ region which

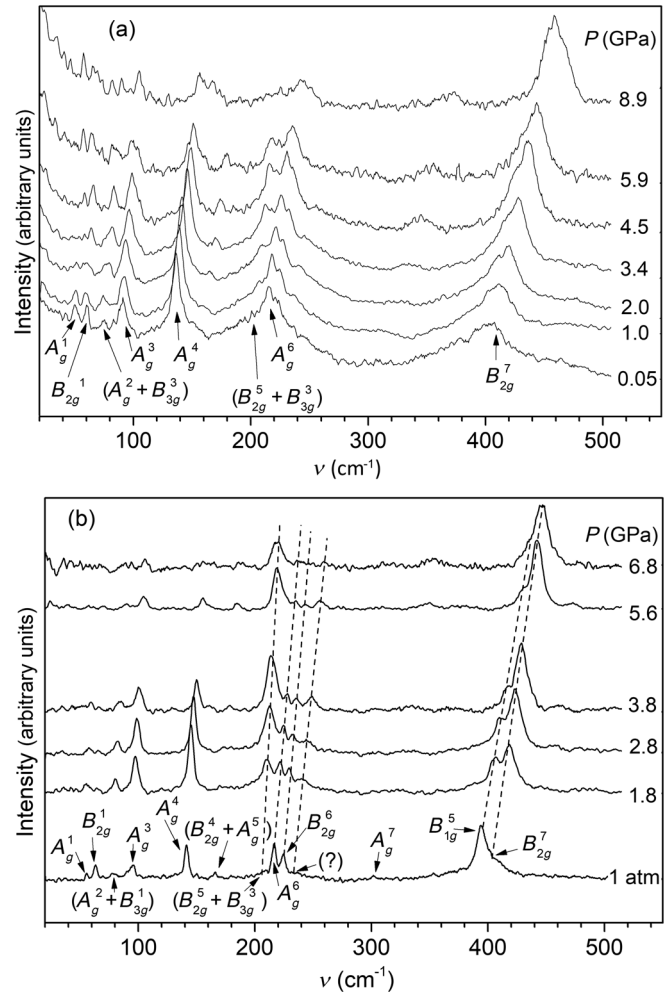


FIG. 4. Pressure-Raman spectra of BaZrS_3 recorded with the 647-nm laser line at (a) 295 K and (b) 120 K. Spectra are displaced for clarity. Phonon assignments are given for the peaks that can be followed with pressure. Feature marked by (?) is unassigned (see text). Dashed lines are guides to the eye showing shift of closely spaced peaks.

becomes more prominent at high pressure. However, no new peaks appear in the high-pressure spectra, and the changes in frequency and intensity occur continuously. Consequently, we conclude that there is no evidence for any first-order structural phase changes in BaZrS_3 under hydrostatic pressure up to the maximum of 8.9 GPa studied here. We can expect this lower pressure bound to apply also at reduced temperature even though our 120-K data extend only to 6.8 GPa. For these types of first-order transitions, the main result of decreasing temperature is to make the kinetics more sluggish without having a sensitive effect on the equilibrium phase boundary [21,44].

Figures 5(a) and 5(b) plot the shifts of the peak positions of the Raman lines that could be accurately followed as a function of pressure at 295 and 120 K, respectively. All of the peaks exhibit linear pressure shifts within experimental uncertainty. Furthermore, there appears to be no hysteresis

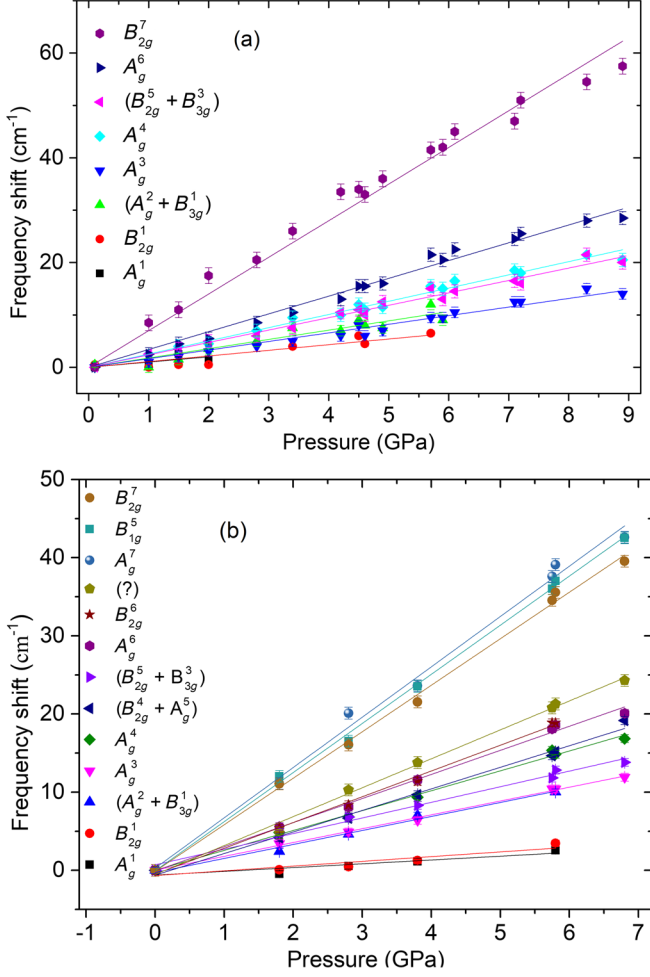


FIG. 5. Frequency shifts with pressure of the observed Raman peaks in Fig. 4 for (a) 295 K and (b) 120 K. Peak positions are determined by Gaussian line-shape fits. The mode correspondence of the plots follows the legends at left. The lines show the best linear fits to the data points.

in the pressure shifts, as data recorded for both increasing and decreasing pressure lie along the same best-fit lines. The lack of hysteresis also supports the absence of a first-order structure transition in the studied pressure range. The pressure coefficients $(d\nu/dp)_{\text{expt}}$ found from the slopes of the linear fits to the data at 120 K are tabulated in Table III. The pressure coefficients at 295 K exhibit a similar mode pressure dependence, but tend to be an average of $\sim 13\%$ larger. At present, the reason for this deviation is unclear; it may be that the compressibility is larger at room temperature than at 120 K, but this needs further investigation. However, we regard the 120-K data as the more accurate due to the sharpening of the spectra at low temperature. Moreover the 120-K data give a fairer comparison to the theory, since the DFT results are calculated for $T = 0$ K.

In Table III, we also list for comparison the linear pressure coefficients predicted for the BaZrS₃ modes by our DFT calculations, as well as the Gruneisen constants

TABLE III. Phonon pressure coefficients in $\text{cm}^{-1}/\text{GPa}$, and corresponding Gruneisen parameters γ , observed experimentally (expt) at 120 K and calculated by DFT theory (theor) in the present work. The DFT-calculated bulk modulus $B_0 = 75$ GPa is used for all γ values. Intrinsic BaZrS₃ modes are identified by their symmetry assignments. The mode labeled by (?), corresponding to the similarly marked feature in Fig. 4(b), may be due to two-phonon scattering.

| Mode | $[(d\nu)/dP]_{\text{expt}}$ | $[(d\nu)/dP]_{\text{theor}}$ | γ_{expt} | γ_{theor} | Mode | $[(d\nu)/dP]_{\text{expt}}$ | $[(d\nu)/dP]_{\text{theor}}$ | γ_{expt} | γ_{theor} |
|------------|-----------------------------|------------------------------|------------------------|-------------------------|------------|-----------------------------|------------------------------|------------------------|-------------------------|
| A_g^1 | 0.6 | 0.8 | 0.8 | 1.0 | A_g^4 | 2.5 | 2.4 | 1.3 | 1.3 |
| B_{2g}^1 | 0.8 | 1.0 | 1.0 | 1.2 | B_{3g}^4 | 3.7 | 7.6 | 1.2 | 1.9 |
| A_g^2 | 1.8 | 1.7 | 1.7 | 1.7 | B_{2g}^4 | 6.4 | 6.5 | 1.5 | 1.7 |
| B_{3g}^1 | 1.8 | 1.9 | 1.7 | 1.8 | A_g^7 | 6.3 | 7.5 | 1.2 | 1.8 |
| B_{2g}^2 | | 1.4 | | 1.3 | B_{1g}^5 | 5.9 | 5.3 | 1.1 | 1.0 |
| B_{1g}^1 | | 1.4 | | 1.2 | B_{2g}^7 | 5.7 | 5.7 | 1.1 | 1.1 |
| B_{2g}^3 | | 2.2 | | 1.7 | B_{3g}^5 | 5.6 | 5.6 | 1.1 | 1.0 |
| A_g^3 | 1.8 | 1.5 | 1.4 | 1.1 | | | | | |
| B_{1g}^2 | | 3.5 | | 2.4 | | | | | |
| | | | | | (?) | | | | |

$\gamma = -B_0[d \ln(\nu)/dp]_{P=0}$ computed from both the measured and calculated pressure coefficients using $B_0 = 75$ GPa, our DFT-calculated value for the bulk modulus. Generally, the agreement between experiment and theory for the pressure coefficients is quite good. The largest differences ($\sim 33\%$) are for the $(B_{2g}^4 + A_g^5)$ and $(B_{2g}^5 + B_{3g}^3)$ modes, and the latter is difficult to resolve in the measurements because of its close proximity to the intense A_g^6 peak. Otherwise, the theoretical pressure coefficients fall within $\pm 20\%$ of the corresponding measured rates of shift, which themselves have an uncertainty of $\pm 15\%$.

VII. DISCUSSION

We have found that the most likely source of the unexpectedly strong Raman features at $390\text{--}440\text{ cm}^{-1}$, dominated by the 392.3-cm^{-1} peak for $T < 50$ K, is resonant forbidden LO scattering aided by the mix of crystallite geometries in our powder sample that can support this process. Recently, forbidden LO scattering also was proposed to explain the presence of unexpected strong Raman peaks in the spectra of the halide perovskites CsSnX_3 ($X = \text{I, Br, Cl}$) [45,46].

Several other explanations are much less probable. Our samples are grown by sulfurization of BaZrO_3 in CS_2 , so at first sight one might expect O impurities to be a possible source of the anomalous scattering. However, a broad peak having similar strength and shape is seen at a comparable location in recent Raman results (room temperature) on BaZrS_3 grown directly from BaS, Zr, and S [4]. Hence, it is doubtful that the strong intensity of the $390\text{--}440\text{ cm}^{-1}$ scattering can be explained by O impurities. Also unlikely is an explanation based on the presence of other Ba-Zr-S phases, such as Ba_2ZrS_4 and $\text{Ba}_3\text{Zr}_2\text{S}_7$ which have a partially overlapping Raman band in the $400\text{--}500\text{ cm}^{-1}$ range [22]. The x-ray diffraction characterization of our material shows that these phases could at most make up 1% of the sample [3]. Accordingly, one does not expect that their Raman contributions would be sufficient to explain the $390\text{--}440\text{ cm}^{-1}$ scattering. We might also consider the involvement of two-phonon scattering [22]. However, in order for second-order processes to be responsible for the 392.3-cm^{-1} peak, they would need to give rise to the most intense feature in the spectrum at low temperatures, and this is again problematic. As remarked, the weak shoulders in Fig. 2 at 235 cm^{-1} and 378 cm^{-1} [marked by (?)] are possible two-phonon features. Under pressure [Fig. 4(b)], the former becomes a more defined peak as it separates from B_{2g}^6 , but the latter shoulder does not become separately resolved from the stronger peaks in the $390\text{--}440\text{-cm}^{-1}$ region. The interesting behavior of the $390\text{--}440\text{ cm}^{-1}$ Raman features warrants additional future study.

We also find that the overall intensity of the Raman spectrum weakens with increasing pressure. A pressure shift of the band gap to lower energy is the most likely

reason. This is predicted by our DFT calculations, which find that the band gap of BaZrS_3 is a direct gap with a negative pressure coefficient of ~ -0.025 eV/GPa. The observed Raman weakening reflects the enhanced attenuation of the incident and scattered photons due to the increase in absorption brought on by the down-shift of the band-gap energy with pressure.

To explore this further, a study is carried out on the pressure dependence of the absorption edge in a BaZrS_3 film sample at 295 K. Films suitable for transmission measurements in the DAC are grown by pulsed laser ablation of BaZrO_3 on sapphire followed by high-temperature sulfurization in CS_2 . The growth conditions and characterization are similar to our powder sample. Good quality films are obtained, again showing the $Pnma$ BaZrS_3 structure and composition near stoichiometry. The substrate is thinned to $\sim 45\text{ }\mu\text{m}$ to prevent pinching in the DAC. Data are recorded to 8.1 GPa on a $\sim 60\text{-nm}$ -thick film. The findings are summarized in Fig. 6 in which the spectra are represented in a plot of $(E\alpha)^2$ vs E , with α the absorbance. The pressure-induced energy shift ΔE_g of the band gap can be estimated by noting the change in the extrapolated zero crossings of the plotted absorption edges (dashed lines), according to the standard E dependence in a direct gap material [47]. We see that a slightly higher (~ 0.1 eV) estimate of the ambient gap is indicated in the film compared to the diffuse reflectance result for our powder material ($E_g = 1.74$ eV). This difference is attributed to the film's $\sim 60\text{-nm}$ thickness, which permits us to observe only the upper portion of the edge. Also in the DAC film experiments scattered light contributes some uncertainty to the data. Nevertheless, a reasonable

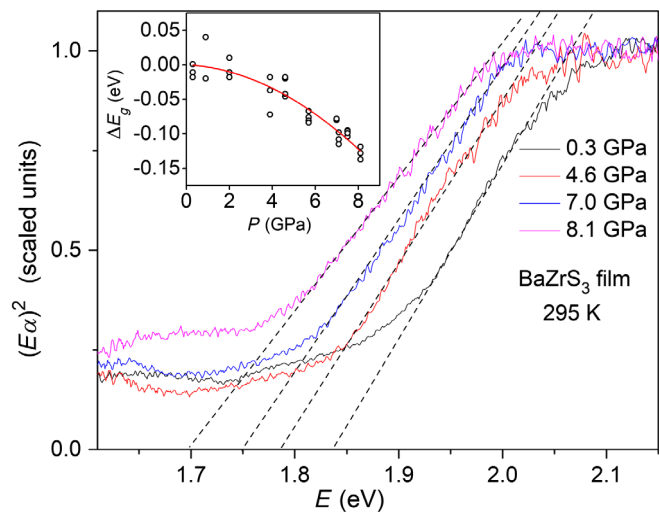


FIG. 6. Measured effect of pressure on the band edge of BaZrS_3 . Spectra are plotted as $(E\alpha)^2$ vs E ; α is the absorbance. Spectra are scaled vertically to match heights in the plateau region above 2.1 eV, and no reflectivity correction is made. Dashed lines extrapolate the edges to zero in order to estimate the pressure variation of the band gap in a consistent way. The inset shows the band-gap energy shift ΔE_g vs pressure with a quadratic fit to the data.

estimate of the band-gap *pressure shift* ΔE_g (Fig. 6, inset) can be obtained by means of this extrapolation procedure, applied *consistently* at each pressure. Our experimental results confirm the DFT-predicted trend that applied hydrostatic pressure reduces the band gap of BaZrS₃. The measured change for the total applied pressure of 8.1 GPa amounts to an average of roughly -0.015 eV/GPa, a bit less than the rate of shift found in our DFT calculations, and some nonlinearity in the measured pressure shift is observed. Reduction of the BaZrS₃ band gap under applied pressure is a favorable result for photovoltaic applications. This will be discussed further below.

The overall weakening of the Raman intensity might also be attributed to a progressive pressure-driven twisting of the S octahedra toward the ideal cubic perovskite phase; its cubic structure does not allow a first-order Raman effect. We can rule this out because it violates trends seen in oxide perovskites where the opposite behavior occurs. For example, in the BaCe_xZr_{1-x}O₃ system, pressure twists the O octahedra toward lower symmetry phases; the sequence with increasing pressure is cubic to rhombohedral to two different orthorhombic phases, the last being the *Pnma* structure [21]. Subsequent phase transitions to more complicated closer-packed structures occur at significantly higher pressures [20].

As remarked, there is no evidence from our experiments that the distorted perovskite *Pnma* structure of BaZrS₃ undergoes any first-order phase changes under hydrostatic pressure up to at least 8.9 GPa. None of the measured or calculated phonon frequencies in BaZrS₃ soften under applied pressure (no negative pressure coefficients), further supporting the structural stability against compression. This result is also found in a variety of oxide perovskites [7,12,21], and the robustness of the BaZrS₃ *Pnma* phase under pressure conforms to the structural trends for those perovskites alluded to above. Therefore, the results of our work indicate that over a considerable span of pressures, the crystal structure of BaZrS₃ is robust and stable against compression in its *Pnma* phase.

This robustness is an issue of some importance for photovoltaic and other applications. It suggests that band-gap tuning in the *Pnma* phase based on cation alloying of BaZrS₃ with other metals such as Ca, Sr, Ti, etc., should be possible for a wide range of compositions. In particular, if Zr⁴⁺ is partially substituted by Ti⁴⁺, the 3*d* orbitals of Ti⁴⁺ will lead to a downward shift of the conduction-band minimum, and lower the band gap [2]. This can in turn result in optimal matching of the band gap of this material with the solar spectrum for photovoltaic applications. Our BaZrS₃ powder material has a band gap of ~ 1.74 eV as determined by diffuse reflectance spectroscopy [3]. This is slightly higher than the optimum value of 1.3–1.5 eV required for a single-junction solar cell. Since the spatial size of Ti⁴⁺ is considerably smaller than that of Zr⁴⁺ (e.g., the ionic radius is $\sim 12\%$ smaller), Ti alloying will lead to

compression of the lattice. Studying the phase stability of BaZrS₃ under high pressure can provide crucial information for feasible doping concentrations.

Our DFT calculations for the compression of BaZrS₃ by hydrostatic pressure find that at 10.7 GPa the *Pnma* unit-cell volume of BaZrS₃ corresponds to the unit-cell volume that we calculate for BaTiS₃ in the analogous *Pnma* structure at $P = 0$ GPa. These results suggest that BaZr_{1-x}Ti_xS₃ should be able to accommodate high concentrations of Ti as judged from the apparent robustness found here for the *Pnma* phase under compression by hydrostatic pressure alone to 8.9 GPa.

Work based on first-principles calculation for the BaZr_{1-x}Ti_xS₃ alloy system predicted that phase separation into BaZrS₃ and BaTiS₃ is favored because of entropy effects when x is above 0.1 [2]. Early attempts to incorporate Ti were unsuccessful, possibly due to low synthesis temperature, not necessarily due to thermodynamics. At high alloy concentration BaZr_{1-x}Ti_xS₃ material does phase separate, however, an experimental study reported stable single-phase BaZr_{0.75}Ti_{0.25}S₃ synthesized under high-pressure (6 GPa), high-temperature (900 °C) conditions [48]. Future work is needed to explore the limits of metal alloying in perovskites based on BaZrS₃. Nevertheless, Ti alloying can be expected to be a viable means for reducing the band gap toward values closer to the optimal range for solar absorption with accompanying increases in power conversion efficiency [2]. Our own preliminary experiments are promising, indicating that a small alloy concentration of $\sim 5\%$ Ti is effective in reducing the gap by amounts on the order of the full 8.9-GPa shift in Fig. 6. Alloying with other cations could lead to wide tunability of the band gap, e.g., Ca²⁺ substituting Ba²⁺ can increase the band gap [3], which can enable other optoelectronic applications. The focus of the present investigation is on high-pressure optical studies of BaZrS₃, and a study of Ti alloying itself will be presented elsewhere.

The effects of pressure on the phonon frequencies in BaZrS₃ reflect a stable solid that obeys the quasiharmonic approximation. This behavior is typical in inorganic perovskites [7,12,21]. The phonon pressure shifts in BaZrS₃ (Fig. 5 and Table III) scale in proportion to the mode frequencies. Zallen and Slade [49] have shown that such scaling holds for solids with a single bonding type, and can be expected in ionic and covalent solids, but not in molecular crystals. The scaling of the pressure shifts means that the fractional rates of shift for the different phonon frequencies are approximately similar. The extent of this similarity is gauged by the range of the Gruneisen parameters. From Table III we see that the experimental and calculated Gruneisen parameters vary, respectively, between 0.7–1.7 and 0.9–1.9 (except $\gamma_{\text{calc}} = 2.4$ for the B_{1g}^2 mode), and within these ranges the mode dependence for both sets of values is similar. Overall, the agreement between experiment and theory for the phonon pressure coefficients (and γ values) is quite good.

VIII. SUMMARY

This work has reported experimental and theoretical studies of the Raman active phonons and the band-gap absorption edge in BaZrS₃, focusing on the effects of high pressure, and for the phonons also low temperature. DFT calculations predict the frequencies, relative intensities, and pressure shifts of the 24 allowed Raman lines at 0 K, as well as compute the pressure dependence of the band gap. We have been able to assign 21 of the 24 intrinsic Raman-active phonons to observed spectral peaks. The agreement with theory of the measured frequencies and intensities is excellent except for the stronger-than-expected features observed in the 390–440 cm⁻¹ region which include a puzzling sharp peak at 392.3 cm⁻¹. These anomalous features can be attributed to resonant forbidden Raman scattering driven by the Frohlich mechanism. Residual O impurities, other Ba-Zr-S phases, and two-phonon scattering are ruled out as likely causes. The measured temperature coefficients of the phonon frequencies have typical negative values, except for the 392.3-cm⁻¹ peak. The unusual temperature shift of this peak is not yet understood. With increasing pressure all measured Raman peaks shift linearly to higher frequency, revealing *no mode softening*. The rates of pressure shift are characteristic of inorganic perovskites, and scale with frequency as expected for a quasiharmonic solid. The calculated pressure coefficients of the intrinsic phonon modes agree closely with experiment. Measurements of the effects of pressure on the BaZrS₃ absorption edge find that the band gap shifts to lower energy at a rate of ~ -0.015 eV/GPa. This agrees in sign, but is smaller than, the theoretical shift of -0.025 eV/GPa predicted by our DFT calculations. There is no evidence that the distorted perovskite *Pnma* crystal structure of BaZrS₃ undergoes a structural phase transition under hydrostatic pressure to *at least* 8.9 GPa in our experiments. This apparent stability suggests that band-gap engineering by adding appropriate metals in alloys based on the BaZrS₃ *Pnma* phase should be explored for photovoltaic and other applications.

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