



Scalable Gate Architecture for a One-Dimensional Array of Semiconductor Spin Qubits

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(Received 13 July 2016; revised manuscript received 26 September 2016; published 28 November 2016)

We demonstrate a 12-quantum-dot device fabricated on an undoped Si/SiGe heterostructure as a proof of concept for a scalable, linear gate architecture for semiconductor quantum dots. The device consists of nine quantum dots in a linear array and three single-quantum-dot charge sensors. We show reproducible single-quantum-dot charging and orbital energies, with standard deviations less than 20% relative to the mean across the nine-dot array. The single-quantum-dot charge sensors have a charge sensitivity of $8.2 \times 10^{-4} e/\sqrt{\text{Hz}}$ and allow for the investigation of real-time charge dynamics. As a demonstration of the versatility of this device, we use single-shot readout to measure the spin-relaxation time $T_1 = 170$ ms at a magnetic field $B = 1$ T. By reconfiguring the device, we form two capacitively coupled double quantum dots and extract a mutual charging energy of $200 \mu\text{eV}$, which indicates that 50-GHz two-qubit gate-operation speeds are feasible.

DOI: [10.1103/PhysRevApplied.6.054013](https://doi.org/10.1103/PhysRevApplied.6.054013)

I. INTRODUCTION

The density of transistors in integrated circuits has been following Moore's law since its conception [1]. However, as the size of transistors approaches the size of a single atom, the laws of quantum physics will play an increasingly dominant role in computer architectures, making it difficult for this trend to continue for much longer. Despite this fact, the prospect of utilizing quantum-mechanical phenomena for information processing offers an opportunity to increase the power of computers for specific computational problems [2,3]. In order for functional quantum computers to become a reality, they will require an on-chip physical component with reproducible properties that can be incorporated into large-scale structures, much like the classical computer depends on the robustness of the transistor.

One of the leading candidates for the quantum analog of the transistor is the gate-defined, semiconductor quantum dot [4,5]. The spin state of an electron trapped in a quantum dot is an ideal physical system for storing quantum information [6–8]. Silicon, in particular, with its weak hyperfine fields, small spin-orbit coupling, and lack of piezoelectric electron-phonon coupling, has been shown to support single-spin coherence times as long as 28 ms [9]. However, the fabrication of reliable and scalable Si-based quantum dots has proved challenging. Independent of the need for a pure spin environment, quantum dots must have reproducible electrical properties for scaling. The relatively large effective mass of electrons in Si, along with the typically lower mobilities of Si two-dimensional electron gases, makes the fabrication of tightly confined, few-electron quantum dots with reproducible properties difficult [10].

In this paper, we present a quantum-dot gate architecture that may allow a path forward for scaling up semiconductor

quantum devices. Our device consists of 12 quantum dots, nine of which are arranged in a linear array and three that are used as sensitive charge detectors. The enhancement-mode device utilizes an overlapping aluminum gate architecture to achieve tight electronic confinement [11], while the undoped Si/SiGe heterostructure provides a clean, high-mobility interface [12] for the formation of well-behaved quantum dots with reproducible characteristics.

II. RESULTS AND DISCUSSION

The outline of the paper is as follows. We first evaluate the reproducibility of the nine dots in the array by extracting the critical parameters of single quantum dots formed under each plunger gate: the lever-arm, the charging energy, and orbital excited-state energy. We are able to reach zero electron occupancy in all nine quantum dots in the array, obtaining an average charging energy $E_c = 6.9 \pm 0.7$ meV and an average orbital energy $E_{\text{orb}} = 3.0 \pm 0.5$ meV. Using adjacent single quantum dots as charge sensors, we show that we are able to read out the charge state of the entire array with a signal-to-noise ratio (SNR) that allows for the observation of real-time tunneling events. Lastly, as a demonstration of the flexibility of the gate architecture, we perform single-shot spin readout and demonstrate strong capacitive coupling of two nearest-neighbor double quantum dots (DQDs).

A. Linear gate architecture

A false-color SEM image of the device is shown in Fig. 1(a) and a COMSOL simulation of the electron density n in the plane of the quantum well is shown in Fig. 1(b). In the upper half of the device, two sets of aluminum gate electrodes, with a pitch of 100 nm, are interleaved to form a

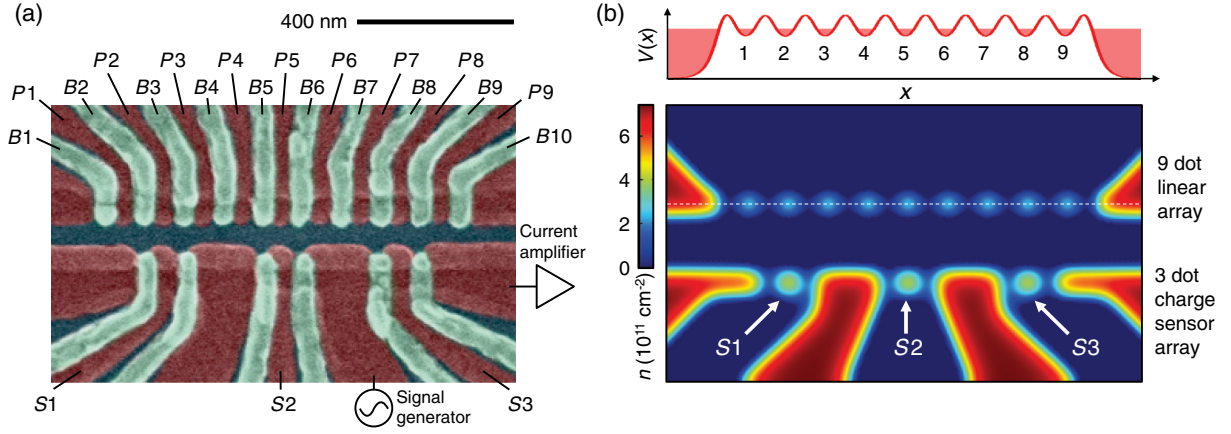


FIG. 1. (a) False-color scanning-electron-microscope image of the overlapping gate architecture. A linear array of nine quantum dots is formed under plunger gates $P1, P2, \dots, P9$. Tunnel couplings are controlled using barrier gates $B1, B2, \dots, B10$. Quantum-dot charge sensors are formed under gates $S1, S2$, and $S3$. (b) (Lower panel) COMSOL simulation of the electron density, n , in the quantum well. (Upper panel) The confinement potential, $V(x)$, along the dashed line in the lower panel.

linear array of nine quantum dots. A plunger gate controls the chemical potential of each quantum dot (shown in red), while barrier gates control the tunnel coupling of adjacent dots (shown in green). An aluminum screening layer restricts the action of the tuning gates to a one-dimensional channel [11]. High-sensitivity single-electron-charge detection is achieved using three single-dot charge sensors defined in a second one-dimensional channel that is formed in the lower half of the device. Aluminum gate material is used here due to the high quality of its native oxide layer. However, a fully complementary metal-oxide-semiconductor-compatible process may be desirable for industrial applications. We note that Si quantum dots have been fabricated elsewhere using polysilicon gates [13–15].

The gate architecture has a repeating unit-cell structure. Each unit cell consists of three quantum dots and a charge sensor. The device demonstrated here is constructed by concatenating three of these unit cells. Scaling to larger arrays could be achieved by adding additional unit cells. Given modern-day industrial standards for integrated-circuit fabrication, we believe that practical limitations to scaling such a gate architecture are likely to arise first from limitations in cryogenic control electronics, not from limitations due to gate-electrode fan-out. Engineering aspects associated with scaling qubit-supporting technologies are being pursued elsewhere [16]. The overlapping gate architecture demonstrated here has roughly 4.5 times the areal density of a widely used DQD depletion-mode gate pattern; we fit nine dots and three charge sensors in an area of approximately $1.5 \mu\text{m}^2$, the same area as a GaAs DQD and its two quantum-point-contact (QPC) charge detectors [17].

B. Characterization of the nine-dot array

Scaling to large arrays of quantum dots requires uniform and reliable single-quantum-dot characteristics. We adopt

three figures of merit to characterize the reproducibility of the linear array: the lever arm α , the charging energy E_c , and the orbital excited-state energy E_{orb} . We form a single quantum dot under each plunger gate, with the neighboring quantum dots tuned to the many-electron regime, and extract α , E_c , and E_{orb} for each dot using a combination of transport measurements, charge sensing, and pulsed-gate spectroscopy. Additional device-characterization data are shown in the Supplemental Material [18].

Lever arms are extracted from transport measurements of Coulomb diamonds at the $N = 0$ to 1 transition, where N refers to the number of electrons in the dot. The charge state of each dot is read out by measuring the conductance through the nearest single-dot charge sensor. As an example, Fig. 2(a) shows the charge-stability diagram of a quantum dot formed under plunger gate $P9$. Here, the derivative of the charge-sensor conductance, $d g_{S3} / d V_{P9}$, is plotted as a function of V_{P9} and V_{B10} . The lack of charge transitions for low values of V_{P9} indicates that dot 9 has been emptied of free electrons, reaching $N_9 = 0$ charge occupancy. Addition voltages for dot 9 are extracted along the vertical dashed line in Fig. 2(a) and converted into addition energies, E_{add} , using α . These addition energies are plotted in Fig. 2(b). For comparison, we also show the addition energies for dots 4, 6, and 8. The increase in E_{add} at the $N = 4$ to 5 charge transition is attributed to shell filling of the low-lying-spin and -valley degrees of freedom [19,20].

Pulsed-gate spectroscopy is performed in each dot at the $N = 0$ to 1 charge transition to extract the orbital excited-state energy E_{orb} [21,22]. A 500-Hz square wave with peak-to-peak amplitude V_{pulse} is added to the dc plunger-gate voltage to repeatedly load and unload an electron onto and off of the dot. For a small V_{pulse} , only the ground state is pulled below the Fermi level of the lead [the upper panel in Fig. 2(c)] and an electron tunnels onto the dot with a rate

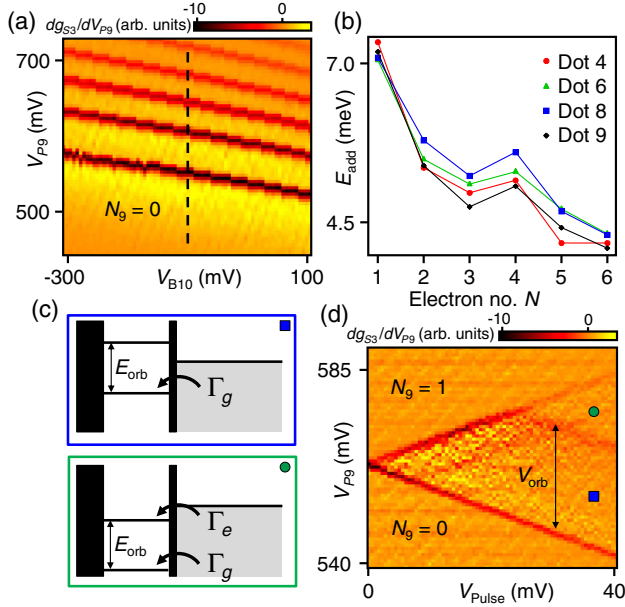


FIG. 2. (a) Charge-stability diagram of quantum dot 9. The derivative of charge-sensor-dot-3 conductance, dg_{S3}/dV_{P9} , plotted as a function of V_{P9} and V_{B10} . For low voltages, dot 9 is emptied of free electrons, reaching the $N_0 = 0$ charge state. (b) The addition energy, E_{add} , plotted as a function of electron number N for dots 4, 6, 8, and 9. (c) Pulsed-gate spectroscopy. The effective tunneling rate onto the dot is dependent on V_{pulse} . (d) An orbital excited state with energy $E_{\text{orb}} = \alpha V_{\text{orb}} = 3.4$ meV is visible in dot 9.

Γ_g . When the pulse amplitude exceeds V_{orb} , the electron can load into either the ground state or the first excited state [the lower panel in Fig. 2(c)]. The effective loading rate is increased due to the contribution from the excited state Γ_e and is visible in the charge-sensing data as a change in the average sensor conductance. From these data, we extract an orbital excited-state energy $E_{\text{orb}} = \alpha V_{\text{orb}} = 3.4$ meV for dot 9.

Similar characterization is performed on dots 1–8, and the results are summarized in Table I. The averaged figures of merit are $\alpha = 0.13 \pm 0.01$ meV/mV, $E_c = 6.9 \pm 0.7$ meV,

TABLE I. Lever-arm conversion between the gate voltage and energy α , charging energy E_c , and orbital excited-state energy E_{orb} for each of the nine dots in the linear array.

Dot	α (meV/mV)	E_c (meV)	E_{orb} (meV)
1	0.14	6.6	2.7
2	0.13	6.1	2.6
3	0.11	5.6	2.1
4	0.14	7.3	3.3
5	0.14	7.2	3.3
6	0.14	7.1	3.0
7	0.14	7.7	3.5
8	0.14	7.1	3.4
9	0.13	7.2	3.4

and $E_{\text{orb}} = 3.0 \pm 0.5$ meV. These charging energies are generally larger than those obtained with other device designs in Si/SiGe due to the tight confinement potential generated by the overlapping gate architecture, although still smaller than those achieved in Si metal-oxide-semiconductor devices [19]. Specifically, depletion-mode devices have achieved charging energies of less than 2 meV [23], while enhancement-mode architectures have yielded charging energies close to 5 meV [20]. Moreover, the large orbital-excited-state energies are comparable to those measured in GaAs devices, where the effective mass is nearly 3 times smaller than the effective mass of electrons in Si [5].

C. Sensitive charge detection

An important criterion for quantum-information processing is high-fidelity qubit readout. For both single-shot readout of an individual spin [24,25] and spin-to-charge conversion in double- [17] and triple-quantum-dot qubits [26], this criterion translates to a need for high-fidelity charge-state readout. We demonstrate high-sensitivity charge detection using the charge-sensor array. The three sensor dots give good coverage over the entire nine-dot array.

In order to characterize the charge-sensor performance, we first measure the shift in a charge-sensor Coulomb-blockade peak due to a change in the charge occupancy of a nearby dot in the linear array. As an example, in Fig. 3(a), we plot the conductance through charge sensor 3, g_{S3} , as a function of V_{P8} and V_{S3} . A Coulomb-blockade peak is visible in the sensor-dot conductance, and it abruptly shifts each time an electron is added to quantum dot 8. We measure a peak shift of $\Delta V_{S3} = 0.26$ mV at the $N_8 = 0$ to 1 charge transition. The shift in the charge-sensor-3 Coulomb-blockade peak position is also measured for dots 2–7 and is plotted in Fig. 3(c) as a function of the geometric distance, d , between each dot and the sensor dot. The shift falls off with a power law that is close to $1/d^3$.

Predictions for the shifts in the sensor-dot Coulomb-blockade peak position can be obtained by computing the capacitances of the device. We construct a three-dimensional model of the device based on the wafer growth profile and lithographic gate dimensions, representing the dots as metallic cylinders with a radius of 19 nm and height of 5 nm, each centered 7 nm below the Si/SiGe interface. The capacitances of the device are then computed using the fast-multipole-moment solver FastCap [27]. The expected shift is computed from the simulated capacitances using $\Delta V_{S3} = eC_m/C_pC_t$, where C_m is the mutual capacitance between the sensor dot and the single-electron dot, C_p is the capacitance between the sensor dot and its plunger gate, and C_t is the total single-electron-dot capacitance [28]. The computed shift scales as $\Delta V_{S3}(d) \propto 1/d^{3.02 \pm 0.05}$ and agrees nicely with the experimental data [see the solid black line in Fig. 3(c)]. We point out that the accuracy of this model is limited by uncertainty in the exact location of the quantum dots in the quantum well.

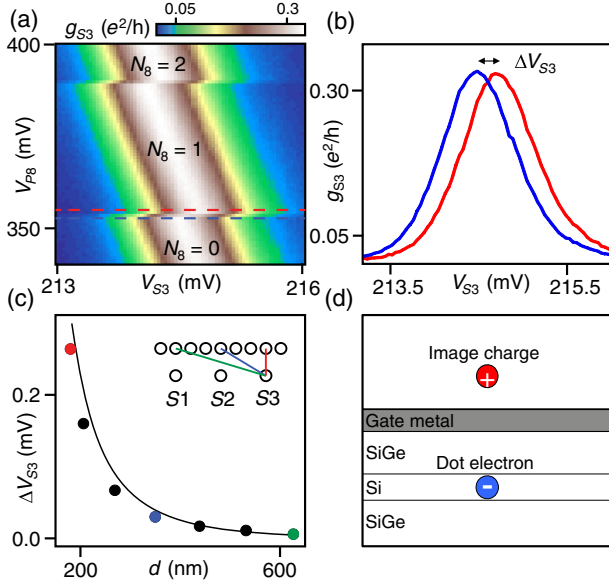


FIG. 3. (a) A Coulomb-blockade peak is visible in sensor-dot-3 conductance, g_{S3} , which is plotted as a function of the gate voltages V_{P8} and V_{S3} . (b) g_{S3} measured at the locations indicated by the dashed lines in (a). The Coulomb-blockade peak shifts by $\Delta V_{S3} = 0.26$ mV when N_8 changes by one electron. (c) ΔV_{S3} is measured for dots 2–8 and plotted as a function of the distance d from the sensor dot. The black line is the theoretical prediction. (d) The approximately $1/d^3$ power-law dependence is qualitatively understood as the field of a dipole formed by the electron in the quantum well (the blue circle) and its positive image charge (the red circle).

As in the case of a parallel-plate capacitor, one might expect the capacitance to scale as $1/d$. However, the overlapping gate architecture covers nearly the entire Si/SiGe heterostructure with metal, resulting in a significant amount of screening. The impact of this screening can be understood using the method of image charges [Fig. 3(d)]. An electron trapped in a quantum dot induces a positive image charge in the gate metal above. The resulting electric field due to the electron and its image charge is that of a dipole, which falls off with a $1/d^3$ dependence.

D. Real-time charge detection

The ability to resolve real-time charge dynamics allows the study of fundamental physical phenomena at the level of single electrons [29,30]. It also enables single-shot readout of single-electron spin states [24,25] and the discrimination of two-electron singlet and triplet spin states [17]. We now demonstrate high-sensitivity charge detection through the observation of real-time tunneling events [31,32]. Through a quantitative analysis of the charge-sensor response, we extract a charge sensitivity of $8.2 \times 10^{-4} e/\sqrt{\text{Hz}}$.

Figure 4(a) shows a color-scale plot of the current I through sensor dot 3 as a function of time, for a range of

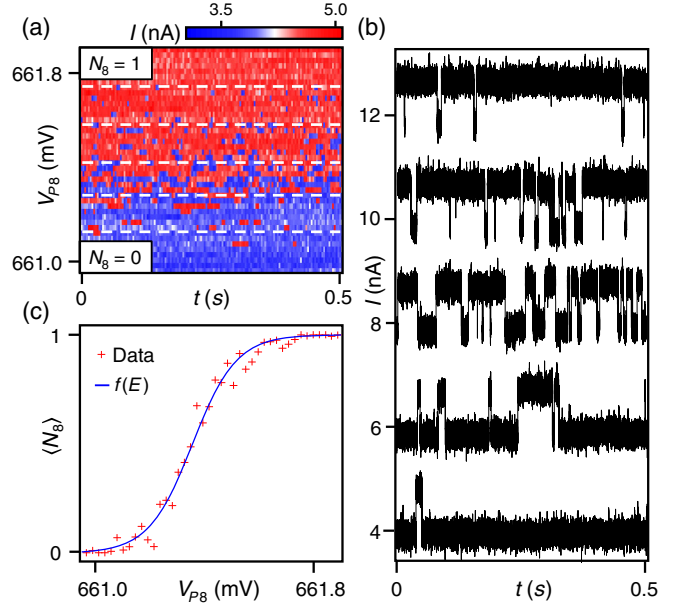


FIG. 4. (a) The current, I , through sensor dot 3, plotted as a function of V_{P8} and time, t , near the $N_8 = 0$ to 1 charge transition. (b) Time series extracted from the data in (a) at the positions shown by the dashed lines. The dwell time in the $N_8 = 1$ charge state increases as V_{P8} is made more positive. The traces are offset by 2 nA for clarity. (c) Time-averaged quantum-dot-8 occupation, $\langle N_8 \rangle$, extracted from the data in (a) and plotted as a function of V_{P8} . The data are fit to a Fermi function $f(E)$.

plunger-gate voltages V_{P8} , with dot 8 tuned up near the $N_8 = 0$ to 1 charge transition. Five time series extracted from this data set are plotted in Fig. 4(b). The lowest time series in Fig. 4(b) is acquired with $V_{P8} = 661.12$ mV. Here the dot is empty nearly all of the time. With V_{P8} slightly increased, the current shows signatures of real-time single-electron tunneling events and switches between two levels corresponding to the $N_8 = 0$ and 1 charge states. As expected, the dwell time in the $N_8 = 1$ charge state increases with an increasing V_{P8} . Using a threshold to discriminate between the charge states, we plot the time-averaged occupation of dot 8, $\langle N_8 \rangle$, as a function of V_{P8} in Fig. 4(c). We expect the population to follow a Fermi function as the chemical potential of the dot level is lowered past the Fermi level of the lead. The data in Fig. 4(c) are nicely fit to a Fermi function with an electron temperature $T_e = 120$ mK.

A detailed analysis of the real-time single-electron tunneling events can be used to determine the charge-sensor SNR and charge sensitivity. We first measure a 1-s time series of the current through the charge sensor with dot 8 tuned to the $N_8 = 0$ to 1 charge-degeneracy point. The data are acquired at a sampling rate of 500 kHz and a Kaiser-Bessel finite-impulse-response (FIR) filter is used to reduce the effective measurement bandwidth to 30 kHz, the 3-dB point of our room-temperature amplifier. A 30-ms-long segment of this time series is shown in Fig. 5(a).

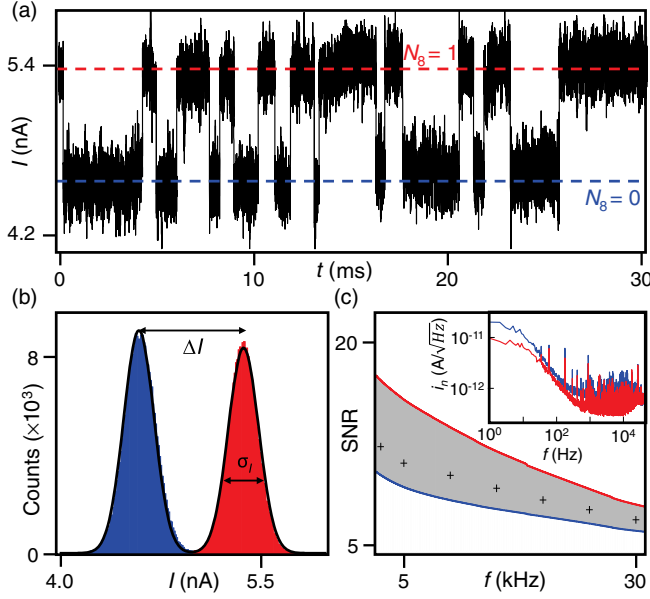


FIG. 5. (a) A time series of the current, I , through sensor dot 3, with dot 8 configured at the $N_8 = 0$ to 1 charge transition. (b) A histogram of a 1-s time series exhibits two Gaussian peaks with width $\sigma_I = 0.112$ nA separated by an amount $\Delta I = 0.772$ nA. (c) The $\text{SNR} = \Delta I / \sigma_I$ plotted as a function of the filter cutoff frequency, f (the black crosses). The data fall between the expected SNR for a current level of 4 nA (blue) and 6 nA (red) based on the measured noise spectra at each current level, shown in the inset.

Real-time tunneling events between $N_8 = 0$ and $N_8 = 1$ are seen as two-level switching in the measured current. A histogram of the full time trace is shown in Fig. 5(b). The two well-resolved peaks correspond to the two charge states. Each peak is nicely fit to a Gaussian curve with the width $\sigma_I = 0.112$ nA, corresponding to the current noise in our measurement setup. The centroids of the two Gaussian peaks are separated by $\Delta I = 0.772$ nA, which corresponds to the signal associated with a change in electron occupancy of one. For these data, we extract a $\text{SNR} = \Delta I / \sigma_I = 6.9$. By adjusting the FIR filter cutoff frequency, f , we plot the SNR as a function of the effective measurement bandwidth in Fig. 5(c), showing a decrease in the SNR with an increasing f .

A quantitative description of the SNR requires a more careful analysis of the experimental setup. We therefore measure the current noise of the device. The measured noise spectra, $i_n(f)$, at current levels of 4 nA (6 nA) are plotted as the blue (red) traces in the inset of Fig. 5(c). The noise is approximately white at high frequencies but exhibits a $1/f$ dependence at frequencies below 200 Hz. In addition, the overall noise level appears to be correlated to the derivative of the charge-sensor current with respect to gate voltage. We can use these spectra to calculate the expected noise for a 1-s-long time series by integrating over frequency from 1 Hz to the filter cutoff frequency, f :

$$\sigma_I^2(f) = \int_{1 \text{ Hz}}^f i_n^2(f') df'. \quad (1)$$

Using the measured signal $\Delta I = 0.772$ nA, we plot the expected SNR as a function of f in Fig. 5(c). The measured SNR falls within the shaded region between the two curves that delineate the expected SNR for current levels of 4 and 6 nA. For a 30 kHz bandwidth, the $\text{SNR} = 6.9$, implying an effective charge sensitivity of $8.2 \times 10^{-4} e/\sqrt{\text{Hz}}$. This sensitivity is higher than both the rf QPC (approximately $10^{-3} e/\sqrt{\text{Hz}}$) [33] and dispersive gate readout ($6.3 \times 10^{-3} e/\sqrt{\text{Hz}}$) [34]; however, our measurement bandwidth is limited to 30 kHz due to our current amplifier. Improvements to the SNR and the measurement bandwidth could be made by using a low-temperature preamplifier [35] in combination with a higher bandwidth room-temperature amplifier.

E. Versatility demonstrations

The nine-dot linear array is capable of hosting a diverse range of quantum-dot qubits. Using individual spins, nine nearest-neighbor exchange-coupled Loss-DiVincenzo qubits can be formed within the array [6]. The addition of a micromagnet above the gate pattern would allow single-spin rotations to be driven via electric-dipole spin resonance in a slanting Zeeman field [36]. With the gate voltages configured differently, four singlet-triplet qubits could be formed using pairs of electrons [17] and the qubits could be coupled via a dipole-dipole interaction [37]. The local magnetic fields in this case could be provided by the Overhauser field [38] or by using a micromagnet [39]. Alternatively, three exchange-only spin qubits could be defined, allowing full electrical control over the Bloch sphere of each qubit [26,40,41]. To demonstrate the versatility of this device architecture, we first perform single-shot readout of an electron spin to measure the spin lifetime, T_1 . We also form two capacitively coupled DQDs and measure an interaction strength of 200 μeV , which suggests a 50-GHz two-qubit gate-operation speed.

We now demonstrate single-shot spin-state readout on dot 8 in the linear array. For these measurements, the voltages on gates $P9$ and $B10$ are held at large positive values, so that the Fermi reservoir to the right of the array extends up to dot 8, with the tunneling rate to the lead controlled by the voltage V_{B9} . For clarity, the electron density in the plane of the quantum well for this device configuration is shown in Fig. 6(a). A three-step pulse sequence is employed to measure the spin-relaxation time T_1 at a magnetic field $B = 1$ T [24,25]. Starting with an empty dot, we plunge the chemical potential of the dot level far below the Fermi level of the lead, which allows an electron to load into either the spin-up or the spin-down state. After a time t_{wait} , we begin the readout phase by setting the chemical potential of the dot such that the spin-up and spin-down energy levels straddle the Fermi level of

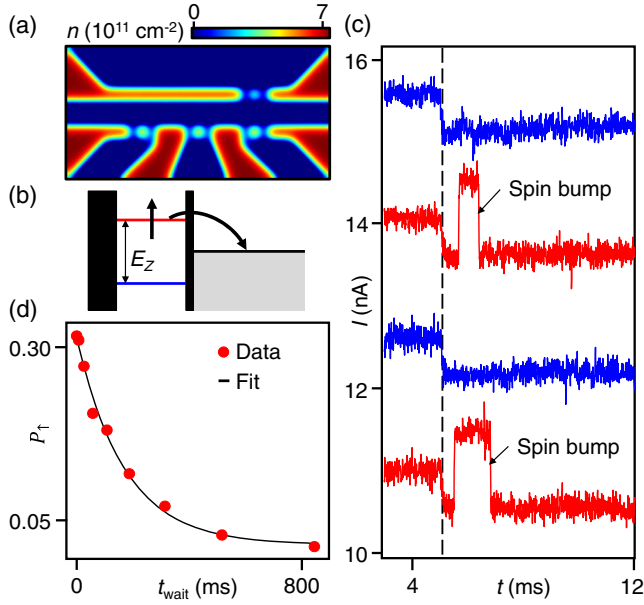


FIG. 6. Single-shot spin measurements. (a) Electron density n in the quantum well showing the configuration used to perform readout on dot 8. (b) A single-electron spin is measured by aligning the spin states such that a spin-up electron (the red level) can tunnel off of the dot and be replaced by a spin-down electron, while a spin-down electron (the blue level) does not have sufficient energy to tunnel off of the dot. (c) Example single-shot traces acquired at $B = 1$ T. The vertical dashed line at $t = 5$ ms marks the beginning of the readout phase. Red (blue) traces correspond to spin-up (spin-down) electrons. Spin-up events result in a “spin bump.” (d) P_{\uparrow} decays exponentially with t_{wait} , with a best fit $T_1 = 170 \pm 17$ ms.

the lead. If the electron on the dot is in the spin-up excited state, as shown in Fig. 6(b), the electron will tunnel off of the dot and then be replaced by a spin-down electron. The change in the charge occupancy of the quantum dot due to this process is visible in time-series measurements of the sensor-dot current, I , and is referred to here as a spin bump. In contrast, if the final spin state is spin-down, no spin bump will be observed. Lastly, we raise the chemical potential of both spin states above the Fermi level to empty the dot and complete the measurement cycle.

Examples of single-shot traces are shown in Fig. 6(c). Spin-up electrons are indicated by current pulses during the readout phase (the red traces) while spin-down electrons simply remain on the dot during the readout phase (the blue traces). We extract T_1 by varying t_{wait} and measuring the probability P_{\uparrow} of being in the spin-up state at the end of the measurement phase [see Fig. 6(d)]. Each data point represents an average of 10 000 single-shot traces. The resulting data are fit to an exponential decay with a best fit $T_1 = 170 \pm 17$ ms. The long spin-relaxation time is a defining feature of the Si “semiconductor vacuum.” Single-shot traces from dot 9 are shown in the Supplemental Material [18]. Single-spin readout for each

electron in the nine-dot array may be possible using a charge shuttling approach that was recently demonstrated in GaAs triple [42] and quadruple [43] quantum dots.

Capacitive coupling has been proposed to mediate two-qubit interactions [8]. Our compact gate design leads to large capacitive couplings. As a demonstration, we investigate the capacitive coupling of two adjacent DQDs. We use dots 6 and 7 to define one DQD and dots 8 and 9 to define a second DQD. The charge-stability diagrams for these DQDs are shown in Figs. 7(a) and 7(b). The barrier-gate voltage V_{B8} is set such that there is no tunneling between dots 7 and 8. As a result, the two DQDs are coupled only via a capacitive interaction C_m . Interdot detuning axes, ϵ_L and ϵ_R , are overlaid on the data in Figs. 7(a) and 7(b). By sweeping ϵ_L vs ϵ_R , we obtain the quadruple quantum-dot stability diagram shown in Fig. 7(c). The mutual capacitance C_m causes the $(N_6, N_7) = (1, 0)$ to $(0, 1)$ interdot charge transition to shift by $\Delta\epsilon_L = 0.77$ mV when the occupancy of the second DQD changes from $(N_8, N_9) = (1, 0)$ to $(0, 1)$. Using the lever-arm conversion between gate voltage and energy, this

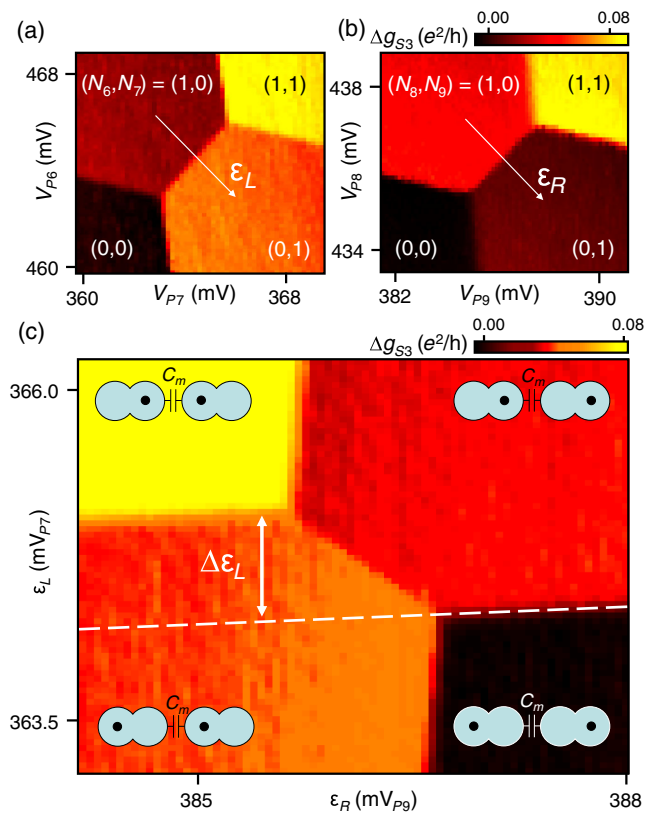


FIG. 7. Dots 6 and 7, and dots 8 and 9, are simultaneously tuned up to form two DQDs, as shown by the charge-stability diagrams in (a),(b). (c) The capacitive interaction between the two DQDs is extracted by measuring the quadruple-dot charge-stability diagram as a function of ϵ_L and ϵ_R . The $(N_6, N_7) = (1, 0)$ to $(0, 1)$ interdot charge transition shifts by $\Delta\epsilon_L = 0.77$ mV when ϵ_R is swept across the $(N_8, N_9) = (1, 0)$ to $(0, 1)$ interdot charge transition.

change corresponds to a 200- μeV energy shift (50-GHz two-qubit gate-operation time) [44]. By reducing the voltage V_{B8} on the barrier gate that separates the DQDs by 60 mV, we are able to reduce the coupling energy scale from 200 to 100 μeV . The coupling could be further reduced by increasing the lithographic distance between the two dots. As a further demonstration of device tunability, we show in the Supplemental Material that a few-electron triple quantum dot can be formed using dots 7–9 [18].

III. CONCLUSION

In summary, we develop a scalable one-dimensional quantum-dot gate architecture that yields quantum dots with uniform and reproducible characteristics. As a proof of concept, we have presented a 12-quantum-dot device consisting of a linear array of nine quantum dots and three single-quantum-dot charge sensors. From characterization measurements, we obtain standard deviations in the charging energies and orbital energies of less than 20% relative to their means: $E_c = 6.9 \pm 0.7$ meV, $E_{\text{orb}} = 3.0 \pm 0.5$ meV. We demonstrate the ability to detect real-time tunneling events in this large array, and we use this capability for single-shot measurements of the electron spin. As a final demonstration, we characterize the dipole-dipole coupling of two adjacent DQDs formed in the array and measure an interaction energy of 200 μeV , which bodes well for computing architectures that rely on capacitive coupling of the qubits.

ACKNOWLEDGMENTS

This work is funded by the ARO through Grant No. W911NF-15-1-0149, the Gordon and Betty Moore Foundation's EPIQS Initiative through Grant No. GBMF4535, and the NSF (Grants No. DMR-1409556 and No. DMR-1420541). Devices were fabricated in the Princeton University Quantum Device Nanofabrication Laboratory.

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