

# Phonon coherent transport leads to an anomalous boundary effect on the thermal conductivity of a rough graphene nanoribbon

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Coherent phonons can give rise to phenomena and physical mechanisms in different systems. Understanding phonon-boundary scattering is critical for the manipulation of thermal properties. In this paper, it is found that the thermal conductivity of rough graphene nanoribbon first monotonically changes, and then exhibits an oscillatory manner with the varying of surface boundary roughness. An obvious increase in thermal conductivity, up to 25.33%, can be observed as surface boundary roughness increases from 0.61 to 0.72. This is in contrast to the conventional understanding that thermal conductivity typically decreases when surface boundary roughness increases. Further, a frequency-resolved picture and lattice dynamics analysis identify that the anomalous boundary effect originates from the coherent nature of phonons, which results in the roughness-selected destructive interference of different modes. Besides, the oscillation will be reduced by introducing rough boundaries with different sinusoidal shapes, which increases the randomness. This abnormal boundary effect can also be extended to other materials, for example, hexagonal boron nitride monolayer, depending mainly on the anharmonicity. The study reveals physical insights into phonon-boundary scattering and may aid the design of heat management and thermoelectric devices based on the boundary effect.

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## I. INTRODUCTION

Boundary effects play significant roles in many fields, varying from chemical reaction dynamics [1], gene regulations [2], to especially condensed-matter physics [3–5]. Many physical properties of materials, for example, giant magnetoresistance of an Fe/Cr superlattice [6], spin-stripe correlation in superconductors [3], hydrodynamic flow of electron fluid [4], and photovoltaic properties of thin-film perovskites [5], can be modulated by changing boundary morphology or conditions. In the area of thermal science, phonon-boundary scattering is considered as one of the basic mechanisms to tailor thermal properties of materials, which has been widely adopted to facilitate heat dissipation by enhancing interfacial thermal conductance [7,8] and optimize energy conversion of thermoelectric by decreasing lattice thermal conductivity [9–12].

Considering the boundary effect on phonons, the wave (coherent) and particle (incoherent) nature will govern phonon transport in different behaviors and mechanisms [13,14]. As revealed by previous works, phonon coherent

transport impacts thermal conductivities via interference, which is quite different from incoherent phonons [15–18]. Several physical mechanisms induced by phonon coherent transport have been found in different systems, for example, phonon resonance hybridization in pillared structures, which blocks phonon transport and is not expected to scatter electrons [15,19], phonon localization in disordered superlattices, which results in the nonmonotonic dependence of thermal conductivity on system length [16,20,21], and mutual coherence among different phonon branches in highly anharmonic or complex materials [17,22,23]. The above findings all enrich our fundamental understanding of phonons and provide guidance for further phonon engineering and tailoring of thermal properties [10,24].

Theoretical and experimental studies reveal that phonon-surface boundary scattering blocks phonon transport, and by increasing surface-boundary roughness, thermal conductivity can be further decreased [9,25–29]. Considering the coherent nature of phonons, interference depends on both the wavelength of phonons and the characteristic structure size [30,31]. So, it is possible that a system with larger surface-boundary roughness can induce less destructive interference. When coherent transport dominates, a larger thermal conductivity may be realized

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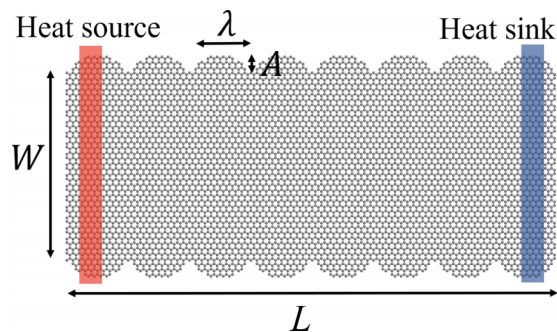


FIG. 1. Schematic picture of RGNR, which is made by tailoring two boundaries of GNR with the same sinusoidal curve. The  $\lambda$  and  $W$  is set as 2.49 and 5 nm, respectively.

on a system with larger roughness. A simulation study by a simple Lorentz gas model reported the nonmonotonic dependence of thermal conductivity on surface-boundary roughness [32]. However, the system is considered as an idea continuum harmonic media, adopting a gray heat carrier model, which does not consider phonon dispersion. Real materials all have nonlinearity, which plays a significant role in thermal transport [33], and consists of discrete atoms. Particularly, phonons have different wave vectors, frequencies, polarization, and wavelength, which have different contributions to thermal conductivity [23,33]. Can the nonmonotonic dependence of thermal conductivity on surface-boundary roughness be found in real materials? What are the underlying mechanism and spectral features?

In the paper, the thermal conductivity of rough graphene nanoribbons (RGNR, shown in Fig. 1,  $\kappa_{\text{RGNR}}$ ) is studied by nonequilibrium molecular dynamics (NEMD) simulation. Another two-stage dependence of  $\kappa_{\text{RGNR}}$  on surface-boundary roughness is found on RGNR. Including the parameter studies by changing the system length ( $L$ ), width ( $W$ ), temperature ( $T_0$ ), and randomness of sinusoidal shapes, the underlying mechanism of the anomalous dependence of  $\kappa_{\text{RGNR}}$  on surface-boundary roughness is clarified by means of lattice dynamics and a frequency-resolved picture, and this mechanism is mainly dependent on material anharmonicity.

## II. METHOD

The configuration of RGNR is achieved by tailoring two boundaries of GNR with the same sinusoidal curve, which is shown in Fig. 1. This structure can be synthesized with atomic precision through the bottom-up approach in experiment [34,35]. For this system, the boundary roughness is defined as  $u = A/\lambda$ , where  $A$  and  $\lambda$  are the amplitude and half-period of the sinusoidal curve, respectively (shown in Fig. 1). To keep  $\lambda$  the same in the following discussions for a system with specific length, the roughness is changed by adjusting  $A$ . Wave interference occurs when the characteristic length is comparable to the phonon wavelength.

As we focus on the temperature above 200 K where the phonon wavelength is small and about several nanometers. So, a value of 2.49 nm is set for  $\lambda$ . When temperature decreases, the characteristic length can be longer at about tens of nanometers. Then, the value of  $\lambda$  is comparable to experimental results. This is because low-frequency phonons dominate thermal transport at low temperature, which generally have long wavelengths. The lattice constant of RGNR is 0.1438 nm and the thickness ( $d$ ) is 0.335 nm.

It needs to be noticed that the displayed RGNR in Fig. 1 is its initial input morphology, which seems to have regular sinusoidal shapes and there is no randomness of surface boundaries. Here, to investigate the surface boundary's effect, the free-boundary condition is adopted. This is the commonly used strategy to investigate surface effect, as can be seen in various previous studies [36,37]. After structure relaxation, randomness will be naturally introduced by morphology reconstruction. That is, atoms at each sinusoidal shape will deviate from their initial positions randomly. Thus, each sinusoidal shape is different and can be treated as rough boundaries (a detailed discussion can be found in Part I within the Supplemental Material [38]).

NEMD simulations are performed using the LAMMPS package [39], and optimized Tersoff potential is adopted to describe interactions among atoms [40]. We should also notice that Simoncelli *et al.* and different researches proposed theoretical models to describe the phonon coherent effect by introducing an extra term of the off-diagonal part of the Wigner operator [17,22,23,41]. To calculate the contribution of the off-diagonal part (coherent effect) to thermal conductivity, different phonon information needs to get through first-principles calculation [17,41]. Due to the computational cost, the present studies adopting the theories are mainly focused on perfect crystal with simulated supercell containing tens, at most up to one or two hundred atoms. As MD simulation implicitly includes the phonon coherent and incoherent nature, it is a good choice to study the coherent phonon effect on nanostructures [15,16].

The free- and fixed-boundary conditions are applied in the transverse and longitudinal directions, respectively. To establish a temperature gradient ( $\nabla T$ ), the system is connected to the Langevin thermostats at the 5th to 12th and  $(N-12)$ th to  $(N-5)$ th layer (1.0 nm). Temperatures are  $T_R = T_0 (1 + \Delta)$  and  $T_L = T_0 (1 - \Delta)$ , respectively, where  $T_0$  is the average temperature and  $\Delta$  is the temperature difference. Further simulation details about the effect of the heat source can be found in Part II within the Supplemental Material [38]. The velocity Verlet method is used to integrate Newton's equation of motion with a timestep of 0.5 fs. Initially, the system is relaxed in the isothermal-isobaric ensemble (NPT) at  $T_0$  and 0 bar for  $2 \times 10^6$  steps. Then, the system is moved to the microcanonical ensemble (NVE), relaxed for  $5 \times 10^6$  steps. Finally, the temperature

and heat flux are averaged over  $1 \times 10^7$  steps under NVE. The results presented in this paper are averaged over six independent simulations with different initial conditions.

The thermal conductivity can be calculated by Fourier's law,

$$\kappa = -\frac{J}{W \cdot d \cdot \nabla T}, \quad (1)$$

where  $J$  is the heat flux from the heat source to the heat sink.  $W$  and  $d$  are the width and thickness of RGNR, respectively. The  $\nabla T$  is obtained through linear fitting of local temperature, not including the temperature jumps of both ends. It should be noticed that, the amplitude ( $A$ ) of the rough boundary is not included in  $W$ . So, when changing the  $u$ , the  $W$  stays the same.

### III. RESULTS AND DISCUSSION

#### A. Two-stage behavior of thermal conductivity

The dependence of  $\kappa_{\text{RGNR}}$  on surface-boundary roughness for systems with different  $L$  is shown in Figs. 2(a) and 2(b) (error bars for all data are shown in Part III within the Supplemental Material [38]). Here,  $T_0$  is 300 K, and  $W$  is fixed as 5 nm. It can be observed that, when  $u$  increases,  $\kappa_{\text{RGNR}}$  shows an anomalous two-stage behavior for all the four systems with different  $L$ . At the first stage,  $\kappa_{\text{RGNR}}$  monotonically decreases when  $u$  increases from 0.17 to 0.43. This is consistent with previous studies that larger surface-boundary roughness induces stronger phonon scattering and decreases thermal conductivity more heavily [9,26,27]. At the second stage, when  $u$  is larger than 0.43,  $\kappa_{\text{RGNR}}$  shows an oscillatory manner. Particularly, when  $u$  increases from 0.61 to 0.72,  $\kappa_{\text{RGNR}}$  exhibits a striking increase [as shown in Fig. 2(b)]. For example,  $\kappa_{\text{RGNR}}$  increases from 240.45 to 284.64  $\text{W m}^{-1} \text{K}^{-1}$  for the system with  $L$  equal to 100 nm. At the same time, it can be found that the oscillation of  $\kappa_{\text{RGNR}}$  at the second stage becomes stronger when  $L$  increases (details explained later). This can be obviously observed on the normalized  $\kappa_{\text{RGNR}}$ , which is shown in Fig. S4(a) within the Supplemental Material [38]. To quantitatively show this point, we focus on the increase ratio of  $\kappa_{\text{RGNR}}$  when  $u$  changes from 0.61 to 0.72. For systems with  $L$  equal to 40, 70, 100, and 130 nm, the increase ratios are 10.65%, 11.16%, 18.38%, and 13.44%, respectively. Noting that in the whole roughness range,  $\kappa_{\text{RGNR}}$  is larger for systems with longer  $L$ . This is due to the size-dependent thermal conductivity, which has been widely studied previously [42]. The dependence of  $\kappa_{\text{RGNR}}$  on surface-boundary roughness for systems with different  $W$  is provided in Part V within the Supplemental Material [38].

Changing  $T_0$  will also alter the roughness dependence of  $\kappa_{\text{RGNR}}$ , which is shown in Fig. 2(c). Here,  $L$  and  $W$  are fixed as 100 and 5 nm, respectively. It can be observed

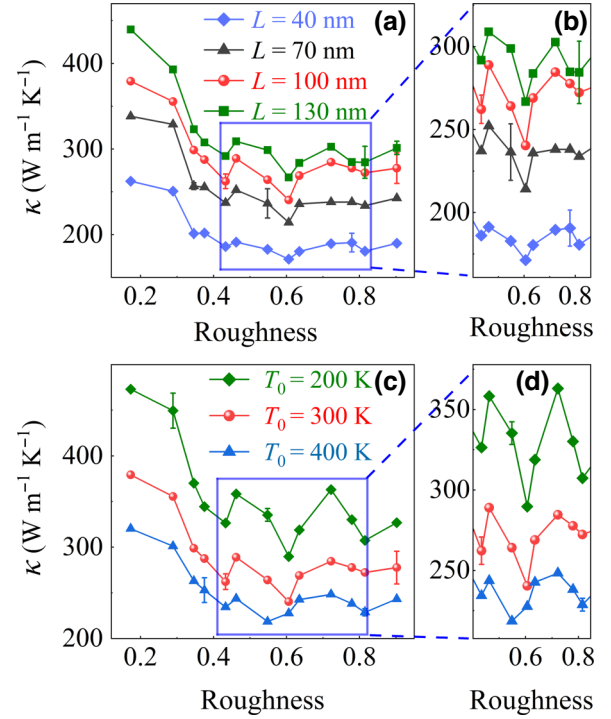


FIG. 2. Thermal conductivity of RGNR for systems with different (a) length and (c) temperature as a function of surface-boundary roughness. (b),(d) are picked from (a),(c), respectively, which focus on the oscillatory region.

that the increase of  $T_0$  weakens the oscillation of  $\kappa_{\text{RGNR}}$  at the second stage (see the normalized  $\kappa_{\text{RGNR}}$  in Fig. S4(b) within the Supplemental Material [38]). The increase ratios of  $\kappa_{\text{RGNR}}$ , by comparing systems with  $u$  changes from 0.61 to 0.72, are 25.33%, 18.38%, and 8.85% (13.47% for  $u$  changes from 0.55 to 0.72) when  $T_0$  is equal to 200, 300, and 400 K, respectively. This weakening of oscillation originates from the breaking of phonon coherence with the increase of  $T_0$ , which will be explained in detail later. Noting that in the whole roughness range,  $\kappa_{\text{RGNR}}$  decreases when  $T_0$  increases. This is due to the Umklapp multi-phonon scattering, which is strengthened as  $T_0$  increases [33,43].

#### B. Behind mechanism of roughness-selected destructive interference of different modes

To clarify the underlying mechanism, vibration eigenmode analysis of phonons in RGNR for systems with different  $u$  is carried out through the general utility lattice program (GULP) [44] using the same potential as NEMD simulation. The participation ratio (PR) for each mode (focused on  $u$  is equal to 0.61 and 0.72), which can quantitatively measure the spread out of mode [45, 46], is calculated and shown in Fig. 3(a) (calculation details are provided in Part VI within the Supplemental Material [38]). It can be found that for RGNR with smaller

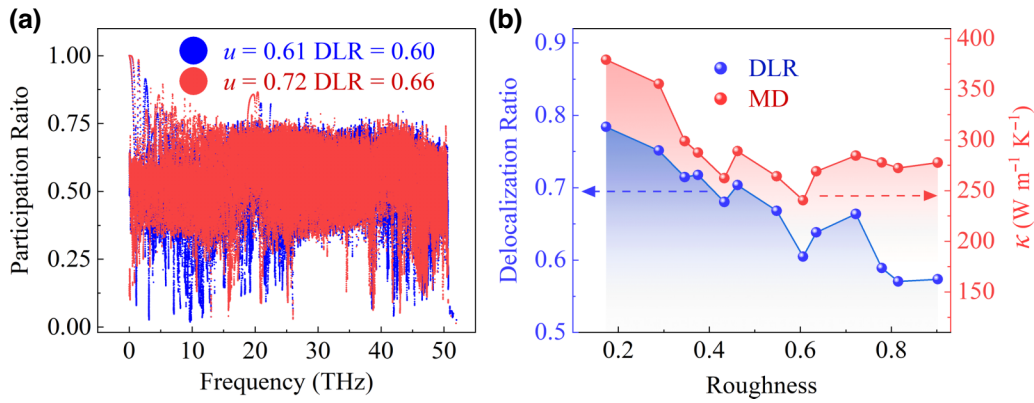


FIG. 3. (a) The PR for RGNR with  $u$  equal to 0.61 (blue dot) and 0.72 (red dot). The delocalization ratio (DLR) are calculated according to the definition in the text. (b) The comparison between DLR and thermal conductivity for RGNR with different boundary roughness.

$u$  (0.61, blue dot), phonons have smaller PRs in low and middle frequencies and several high frequencies. It means that many atoms cannot participate in the vibration of these modes (can also be treated as localized modes), which are experienced destructive interference. Thus, thermal conductivity decreases even  $u$  is smaller. If we focus on the normal case when  $u$  decreases from 0.61 to 0.46. As shown in Fig. S6(a) within the Supplemental Material [38], for RGNR with smaller  $u$  (0.46, green dot), phonons have larger PRs in low and middle frequencies. It means that more atoms can participate in the vibration. As a result, these phonons transport well at the system, leading to an enhancement in thermal conductivity when  $u$  decreases from 0.61 to 0.46.

It also needs to be noticed that, for RGNR when  $u$  is equal to 0.46 and 0.72, although their thermal conductivities are nearly the same (288.98 and 284.64 W m<sup>-1</sup> K<sup>-1</sup>), the modes that have smaller PR are different and distributed in different frequencies. As shown in Fig. S6(b) within the Supplemental Material [38], when  $u$  is equal to 0.72, modes near 10.5, 15.5, 21, 34.5, and 39 THz have smaller PR. However, when  $u$  is equal to 0.46, other modes appear near 19.5 THz, 45 THz and several low frequencies ranging from 4 to 9 THz that have smaller PR. This is because destructive interference is a combined effect, which depends on both roughness and wavelength. Since different modes have different wavelengths [23,30], for RGNR with a different  $u$ , modes that experience destructive experience are different. The above point can be figured out more obviously by the nonparticipation ratio, inverse of PR, as shown in Fig. S7 within the Supplemental Material [38].

Understanding the above mechanism of roughness-selected destructive interference, the increase of  $\kappa_{\text{RGNR}}$  when  $u$  increase is rational. A system with larger  $u$  induces destructive interference for fewer phonons. To better show that roughness-selected destructive interference is the underlying mechanism, the delocalization ratio (DLR)

is introduced, which is defined as the percentage of numbers of eigenmodes whose PR is larger than 0.5. According to this definition, a larger DLR means less destructive interference, and a larger thermal conductivity. As shown in the inset of Fig. 3(a), the DLR are 0.60 and 0.66 for RGNR when  $u$  is equal to 0.61 and 0.72, respectively. This means fewer phonons experience destructive interference when  $u$  increases and is equal to 0.72, which results in the larger  $\kappa_{\text{RGNR}}$ . More generally, the DLR for RGNR with different  $u$  ranging from 0.17 to 0.90 is calculated, and compared with the  $\kappa_{\text{RGNR}}$  shown in Fig. 2. As shown in Fig. 3(b), the DLR (blue dot) shares nearly the same trend as  $\kappa_{\text{RGNR}}$  calculated by NEMD (red dot). This further demonstrated that roughness-selected destructive interference induced by coherent phonons is the underlying mechanism, which is responsible for the anomalous roughness-dependent  $\kappa_{\text{RGNR}}$ , as well as the anomalous boundary effect in RGNR.

To further confirm that destructive interference is induced by rough boundaries, and visualize different modes. The distributions of amplitude for a specific localized mode ( $\omega = 1.12$  THz) and spread out mode ( $\omega = 20.80$  THz) are projected on the supercell of RGNR and shown in Fig. 4. As all eigenvectors are orthogonally normalized. For localized mode with  $\omega = 1.12$  THz, it distributes mainly on the rough boundaries. Atoms at the sinusoidal boundary area have much larger amplitude than those at the inner of the ribbon. That is, phonons transported along the longitudinal direction, which contribute to thermal conductivity, are localized at the boundaries. This will result in the decrease of participation ratio, and the projection of these localized modes is distributed at boundaries. However, for the spread out mode with  $\omega = 20.80$  THz, all atoms vibrate with nearly the same amplitude. Atoms at the ends of the sinusoidal boundary have even smaller amplitude than those at the inner of the ribbon. As the sinusoidal boundary areas are not directly contacted, different supercells are connected through the

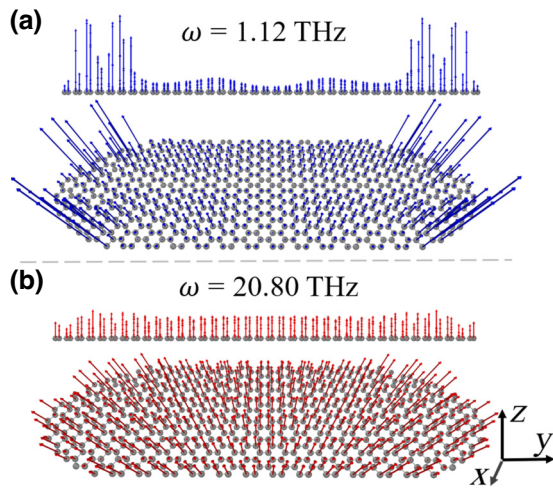


FIG. 4. Comparison and visualization of two eigenmodes with PR equal to 0.16 and 0.80 for RGNR when  $u = 0.61$ .

inner of the ribbon. The spread out modes can easily propagate along different supercells and contribute to thermal conductivity, while localized modes can hardly be transported. The above picture of phonon localization induced by the surface-boundary effect has been discussed in detail in various previous studies [37,47].

As lattice dynamics analysis presented above considers only the harmonic effect, to take the anharmonic effect into account, the decomposed spectral heat flux is extracted through NEMD by tracking force-velocity correlations among atoms [16,48]. Divided by cross-section area and temperature gradient, the frequency-dependent thermal conductivity can be obtained and is shown in Fig. 5. And the corresponding frequency-dependent thermal conductivity using a linear scale is shown in Fig. S8 of the Supplemental Material [38]. Here,  $T_0$  and  $L$  are equal to 200 K and 100 nm, respectively. The spectral

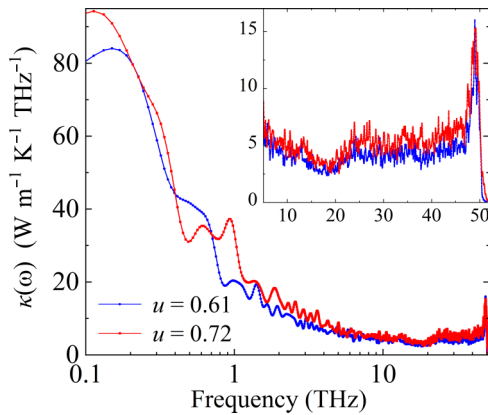


FIG. 5. The frequency-dependent thermal conductivity of RGNR with  $u$  equal to 0.61 (blue line) and 0.72 (red line) at 200 K. Inset: focus on a magnification of the frequency between 5 and 52 THz.

$\kappa_{\text{RGNR}}$  for the system with  $u$  equal to 0.72 is larger than that with  $u$  equal to 0.61 in many frequency ranges, especially for low-frequency modes. This is because low-frequency phonons have longer wavelength, and are more likely to show coherent nature. Thus, the boundary-roughness-selected destructive interference is more obvious at low frequency.

### C. Explanation for the length and temperature-dependent thermal conductivity

The temperature and system-length-dependent oscillation in  $\kappa_{\text{RGNR}}$  can be understood following the above rationale. When  $T_0$  increases from 200 K, 300 K to 400 K, the increase ratios of  $\kappa_{\text{RGNR}}$  when  $u$  changes from 0.61 to 0.72 decreases from 25.33% to 18.38% and 8.85%. This is because multiphonon scattering increases [33,43,49] as temperature increases. This destroys the phase information, as well as coherence of phonons. As interference is derived from the coherent nature of phonon. The breaking of coherence will weaken destructive interference, which leads to the anomalous boundary effect here. Thus, the oscillation in  $\kappa_{\text{RGNR}}$  weakens.

At the same time, as shown in Fig. 6, the increase ratio of  $\kappa$  obviously increases when  $L$  increases from 40 nm, reaching a maximum value of 25.33% and 18.38% at 200 and 300 K, respectively when  $L$  reaches 100 nm. However, as  $L$  further increases from 100 to 160 nm, a noteworthy decrease in oscillation of  $\kappa_{\text{RGNR}}$  is observed. When  $L$  increases to 160 nm, the increase ratios gradually decrease to 16.33% and 11.73% for temperatures of 200 and 300 K, respectively. This behavior differs from that observed in the range of 40 to 100 nm. This is because when  $L$  is small, more phonons whose velocities are parallel to or deviated from longitudinal direction in a certain degree can be ballistically transported from heat bath to heat sink. That is, they will not reach the surface boundaries,

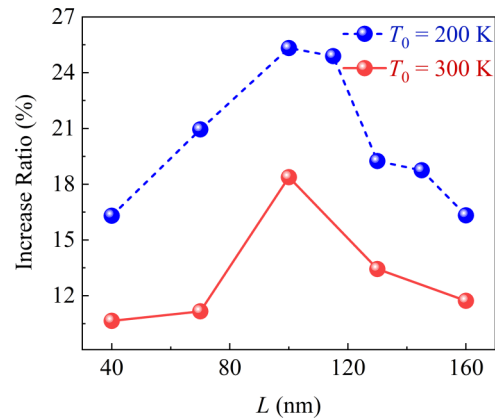


FIG. 6. The dependence of the increase ratio for RGNR on system length at 200 and 300 K, respectively.

and the boundary effect does not work. Under this condition, when  $L$  increases, more phonons will collide with rough boundaries, some will even experience multiple collision with boundaries. This will increase the possibility of destructive interference, and strengthen the oscillation in  $\kappa_{\text{RGNR}}$ . However, when  $L$  further increases and is larger than the mean-free-path of some modes. These modes will experience multiphonon scattering, which will also break coherence. As a result, the oscillation in  $\kappa_{\text{RGNR}}$  weakens. Thus, the increase of  $L$  brings two competitive mechanisms, which leads to the nonmonotonic change of increase ratio.

#### D. The effect of randomness induced by the difference of sinusoidal shapes on thermal conductivity

It also needs to be noticed that the randomness discussed above is introduced by morphology reconstruction under free-boundary conditions, which makes atomic locations at each sinusoidal area different. Except that, the randomness induced by the difference of sinusoidal shapes is also a key factor, which may affect the selection of localization modes. To check this point, we introduce randomness to the sinusoidal shape. That is, sinusoidal shape with different amplitude [as shown in Fig. 7(a)], termed as  $A'$ , is randomly introduced to RGNR to replace the original sinusoidal shape with amplitude equals to  $A$ . Here, we focus on the RGNR with  $L$  and  $W$  of 100 and 5 nm, respectively.  $T_0$  is fixed as 200 K.

Firstly, we focus on the effect of replacement percentage (RP), which is defined as the number of sinusoidal shapes with amplitude equal to  $A'$  divided by the total number of sinusoidal shapes. The  $A'$  is fixed as 0.72 nm. Taking the sketches of RGNR shown in Fig. 7(a) as an example, there are 14 sinusoidal shapes on each side of RGNR. By keeping the boundaries symmetrical, three sinusoidal shapes on each side are randomly selected and their amplitudes are replaced by  $A'$ . The RP is calculated as 21.4%. To investigate the effect of RP on oscillatory of  $\kappa_{\text{RGNR}}$ . The  $\kappa_{\text{RGNR}}$  is calculated for the structures with the same  $u$  of 0.61 and 0.72, where the  $\kappa_{\text{RGNR}}$  exhibits a striking increase as shown in Fig. 2. As depicted in Fig. 7(a), the increase ratio decreases as the RP increases. This means that the oscillation in  $\kappa_{\text{RGNR}}$  weakens as the sinusoidal shape randomness increases. However, even when RP reaches 37.5%, the  $\kappa_{\text{RGNR}}$  increase ratio remains at 11.77%.

Then, the RP is fixed, and we focus on the change of randomness by decreasing  $A'$  from 1.5 to 0.0 nm. Similarly, we also focus on the RGNR with the same  $u$  of 0.61 and 0.72 ( $A/\lambda$ ). As shown in Fig. 7(b), for both the two cases of RP equal to 2.5% and 25%, the increase ratio of  $\kappa_{\text{RGNR}}$  decreases as  $A'$  decreases. This is because the replaced  $A'$  is smaller than  $A$ , the randomness increases as  $A'$  decreases. When  $A'$  is reduced to 0 nm, the increase ratio of  $\kappa_{\text{RGNR}}$  is 2.6% for the system with larger RP equal

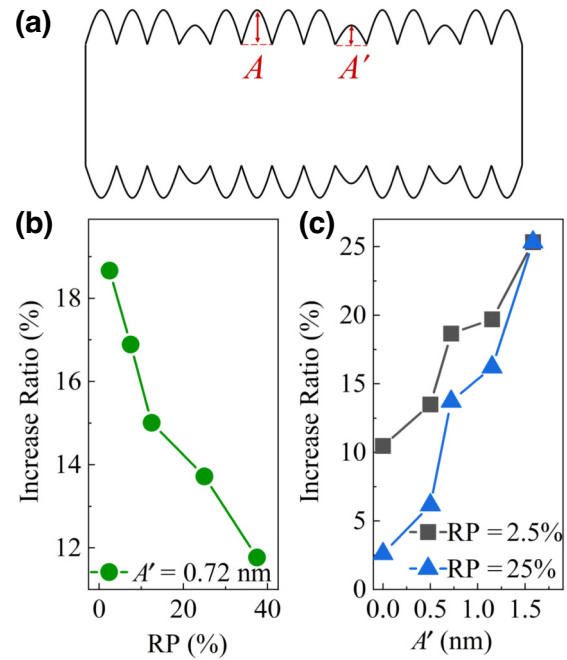


FIG. 7. (a) Sketches of RGNR with sinusoidal shape of different amplitude  $A'$ , which is randomly introduced. The increase ratio when  $u$  changes from 0.61 to 0.72 in the thermal conductivity of RGNR for systems with respect to the (a) replacement proportion and (b) amplitude after introducing randomness.

to 25%. This means the oscillation of  $\kappa_{\text{RGNR}}$  in the second stage almost disappears. Thus, we can conclude that the randomness induced by the difference of sinusoidal shapes will weaken the oscillation, which originates from the roughness-selected destructive interference of different modes. This is because it is the characteristic size of sinusoidal shape that selects the modes with certain wavelengths to be localized at the sinusoidal area where atoms are randomly localized. The introduced sinusoidal shape with different characteristic size will be broken in this selection, thus, weakening the oscillation.

#### E. Extended to other materials

As a final remark, we should emphasize that the anomalous phenomena of two-stage dependence of thermal conductivity on surface-boundary roughness is not only limited to the specific material of the graphene nanoribbon, which would be found on both nanoribbons and nanowires of other materials. Here, an alternative rough graphene nanoribbon is chosen because graphene has weak anharmonicity, and phonons in graphene have a long mean free path and wavelength [10,50]. As revealed here, the behind mechanism is roughness-selected destructive interference for different modes, which originates from the coherent nature of phonons. The anomalous boundary effect is expected to be found on other materials with weak anharmonicity at room temperature [15,50], and even

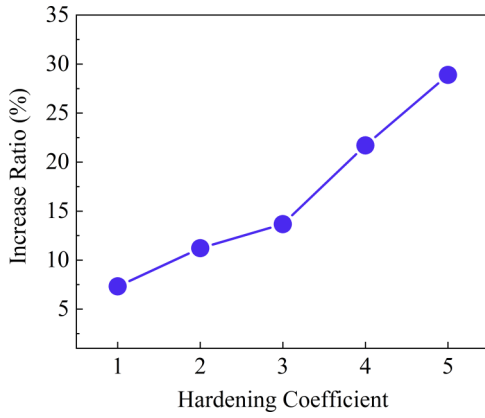


FIG. 8. The dependence of increase ratio for  $h$ -BN on the hardening coefficient of interatomic bonding force at 200 K.

materials with strong anharmonicity at low temperature where low-frequency phonons dominate thermal transport and generally have long wavelengths [51].

To support the above point, we also investigate the boundary effect on hexagonal boron nitride monolayer ( $h$ -BN). Adopting the same scenario as RGNR, we tailor two boundaries of  $h$ -BN with sinusoidal curve, and calculate the dependence of thermal conductivity for rough  $h$ -BN ( $\kappa_{Rh-BN}$ ) on surface roughness. The lattice constant of  $h$ -BN is 0.1449 nm, and its thickness is 0.33 nm. The Tersoff potential is used to describe the interaction between B-B, N-N, and B-N atomic pairs [52]. The NEMD simulation is performed under the same conditions as RGNR. Here  $T_0$  is 200 K, and  $W$  and  $L$  are fixed at 5 and 100 nm, respectively. The increase ratio is 7.32% for Rh-BN when the surface-roughness increases from 0.61 to 0.72, which is smaller than RGNR. This is because the  $h$ -BN has a stronger anharmonicity than graphene. To weaken its anharmonicity, we can harden its interatomic bonding force. The dependence of increase ratios of  $\kappa_{Rh-BN}$  on the hardening coefficient of bonding force is shown in Fig. 8. When the hardening coefficient is equal to 1, it corresponds to original  $h$ -BN. It can be observed that the increase ratio of  $\kappa_{RGNR}$  enhances as the hardening coefficient increases. When the hardening coefficient increases to 5, the increase ratio is up to 28.89%. Thus, we can conclude that the oscillating thermal conductivity can exist for other materials, which mainly depends on the anharmonicity.

#### IV. CONCLUSIONS

In summary,  $\kappa_{RGNR}$  is investigated by NEMD simulation. The results reveal that the  $\kappa_{RGNR}$  shows an two-stage dependence on surface-boundary roughness. At the first stage,  $\kappa_{RGNR}$  monotonically decreases when  $u$  increases. This is consistent with previous studies. At the second stage,  $\kappa_{RGNR}$  shows an oscillatory manner when  $u$  increases. Particularly, when  $u$  increases from 0.61 to

0.72,  $\kappa_{RGNR}$  exhibits a striking increase. System length and temperature can have large influence on this abnormal  $u$ -dependent  $\kappa_{RGNR}$ . After comparatively studying eigenmodes for RGNR with different  $u$  by lattice dynamics, it is demonstrated that roughness-selected destructive interference induced by coherent phonons is the underlying mechanism. Introducing rough boundaries with different sinusoidal shapes, which breaks the mode selection, will decrease the oscillation in  $\kappa_{RGNR}$ . Moreover, as this abnormal oscillation behavior of thermal conductivity mainly depends on anharmonicity, and can exist in other materials, for example, a hexagonal boron nitride monolayer. The findings here significantly enrich our fundamental understanding of phonon-boundary scattering and coherent phonon transport.

The rules of two-stage dependence of thermal conductivity on surface-boundary roughness will aid the design of materials for thermoelectrics and heat dissipation, which tie to phonon-boundary scattering. Specifically, to improve the efficiency of thermoelectric materials, increasing surface-boundary roughness to decrease lattice thermal conductivity (such as silicon nanowire) has become a widely adopted strategy [9]. The findings here indicate that continuously increasing surface-boundary roughness will not always work, a minimum thermal conductivity can be achieved by structures with certain roughness, which is related to their phonon properties. This scenario will be the same for heat-dissipation materials with high thermal conductivity, which are generally thought to be benefited from smaller surface-boundary roughness. The roughness of idea structures for heat dissipation is zero, while, this is impossible. Because rough boundaries are inevitable due to the decrease of coordination number for atoms at surfaces and chemical passivation [53]. As a result, choosing structures with certain roughness, which blocks phonon transport to the minimum degree is useful.

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