


Multiparameter quantum sensing and magnetic communication with a hybrid dc and rf optically pumped magnetometer

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We introduce and demonstrate a hybrid optically pumped magnetometer (HOPM) that simultaneously measures one dc field component and one rf field component quadrature with a single atomic spin ensemble. The HOPM achieves sub-pT/ $\sqrt{\text{Hz}}$ sensitivity for both dc and rf fields, and is limited in sensitivity by spin projection noise at low frequencies and by photon shot noise at high frequencies. We demonstrate with the HOPM an alternative application of multiparameter quantum sensing: background-canceling spread spectrum magnetic communication. We encode a digital message as rf amplitude, spread among 16 channels from 29 to 33 kHz in a noisy magnetic environment, and observe quantum-noise-limited rf magnetic signal recovery enabled by quantum-noise-limited dc noise cancelation, reaching noise rejection of 15 dB at 100 Hz and more than 20 dB at 60 Hz and below. We measure signal fidelity versus signal strength and extrinsic noise in communication of a short text message. The combination of high sensitivity, quantum-noise-limited performance, and real-world application potential makes the HOPM ideally suited for the study of high-performance multiparameter quantum sensing.

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Quantum sensing employs quantum systems and quantum measurements to acquire precise information about the sensed environment, and is formalized via the theory of quantum parameter estimation [1]. Quantum sensing of single parameters, e.g., phase shifts or magnetic fields, has been extensively studied both theoretically and experimentally [2–4]. Standard quantum limits (SQLs) to sensitivity and other metrics [5,6] have been identified, and methods to surpass SQLs, known as quantum enhancement, have been devised [5,7]. Proof-of-principle quantum enhancement has been demonstrated in optical interferometry [8], atomic clocks [9–11], and optically pumped magnetometers (OPMs) [12–15]. Beyond-proof-of-principle quantum enhancement, in high-sensitivity practical instruments, has been demonstrated in a few cases [16–20]. These efforts revealed alternative aspects of quantum sensing, for example, the role of measurement backaction in sensors operating beyond the shot-noise limit [19,21,22].

Multiparameter quantum sensing (MPQS), the simultaneous estimation of two or more parameters with a quantum sensor [23,24], is a relatively recent frontier for quantum parameter estimation, with potential application in many sensing tasks, e.g., measurement of intrinsically vector quantities, such as fields, displacements, or rotations. Recent work in MPQS [25] has produced striking theoretical observations [25–30], including the possibility of better sensitivity when estimating multiple parameters than when estimating parameters separately [31] and proof-of-principle demonstrations [32–34].

Here we demonstrate another experimental system for MPQS, a hybrid dc and rf optically pumped magnetometer (HOPM) that simultaneously estimates two magnetic field parameters from measurements on a single atomic spin ensemble. The HOPM has the potential for simultaneous quantum enhancement using optical [19,35] and/or spin squeezing [15,32], or by more exotic methods such as N00N states [36,37]. With this system, we demonstrate simultaneous, quantum-noise-limited [38], sub-pT/Hz^{1/2} sensitivity in both parameters. Our HOPM implementation, based on alkali-vapor sensing methods, is suitable for miniaturization and manufacturing using proven techniques [39]. Together, these features will enable the use of MPQS methods in practical sensors.

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A natural application of the HOPM is reception of ultralow-frequency (ULF), very-low-frequency (VLF), and low-frequency (LF) magnetic signals, employed in radio communications through weakly conducting media, such as water [40] or rock [41]. In such media, the ULF-VLF-LF bands benefit from lower attenuation than higher frequencies, while also maintaining useful bandwidths. Potential applications include communications [42,43], geotechnical [44], scientific [45], and extraterrestrial exploration [46].

Due to the strong attenuation with distance in conducting media, both signal and environmental noise can be weak at the point of detection, leaving the receiver's intrinsic noise as the limiting factor. Using traditional antenna-based methods, a high sensitivity can be achieved at the cost of a large collection area, e.g., $2 \text{ ft}/\sqrt{\text{Hz}}$ at 30 kHz with a 1.69 m^2 antenna [45]. OPMs can be far more sensitive than ULF-VLF-LF antennas of similar size [47], allowing OPMs to function as ultracompact radio receivers [48]. OPM miniaturization can also greatly reduce sensor weight, useful for carried or aerial use [49,50]. Together with piezoelectric-based direct antenna modulation techniques, which make possible 10-cm-scale ULF-VLF-LF transmitters [51], miniaturization of ULF-VLF-LF receivers may enable small-footprint duplex communication links.

Radiofrequency OPMs employ magnetic resonances that are tuned by the application of a dc bias field. This tuning requires compensation of changes in the ambient dc field, which can experience large changes as a craft reorients in the Earth field or other strong local field. In the HOPM, such changes of the dc field can be monitored by the sensor itself, and feedback can be applied to maintain the desired tuning of the rf reception. When used in a field-locked-loop, this feedback allows both for cancelation of slow changes in the dc field and for selection of rf reception frequency. The simultaneous measurement of rf and dc fields is thus a MPQS problem that arises naturally in the application of OPMs to magnetic communications.

The paper is organized as follows: Sec. I describes a Bloch-equation model for the spin dynamics and optical signal generation, applicable to a variety of OPM protocols, and reviews quantum enhancement in paradigmatic dc and rf OPM strategies. Section II introduces the hybrid dc and rf OPM strategy. Section III describes the experimental implementation using an optically pumped ^{87}Rb vapor. Section IV describes experimental validation of the model. Section V describes a field-locked loop feedback system to stabilize the dc field seen by the atoms at a programmable value. Section VI describes sensitivity measurements, showing quantum-noise-limited performance. Finally, Sec. VII describes VLF-LF magnetic communications using the HOPM. Section VIII describes several natural extensions of the technique.

I. OPM DYNAMICS AND SINGLE-PARAMETER ESTIMATION STRATEGIES

In an optically pumped alkali vapor, a vector collective spin \mathbf{F} evolves by a stochastic differential equation containing the magnetic field as a parameter, for example, the Bloch equation

$$\frac{d}{dt}\mathbf{F}(t) = [-\gamma\mathbf{B}(t) + G_S S_3(t)\hat{z}] \times \mathbf{F}(t) - \Gamma\mathbf{F}(t) + R_{\text{OP}}(t)[\mathbf{F}_{\text{max}} - \mathbf{F}(t)] + \mathbf{N}_{\text{at}}(t), \quad (1)$$

where γ is the atomic gyromagnetic ratio, \mathbf{B} is the magnetic field vector, Γ is the spin-relaxation rate, R_{OP} is the optical pumping rate, \mathbf{F}_{max} , proportional to the number of atoms in the ensemble, is the value \mathbf{F} would take if fully polarized along the optical pumping direction, $G_S S_3(t)\hat{z}$ describes optical Zeeman shifts causing measurement backaction and \mathbf{N}_{at} is a Langevin noise term describing spin fluctuations [19]. The spin evolution is read out by off-resonance Faraday rotation, described by the input-output relation [52]

$$S_2^{(\text{out})}(t) = S_1^{(\text{in})}(t) \sin \phi(t) + S_2^{(\text{in})}(t) \cos \phi(t) \approx G_F F_z(t) S_1^{(\text{in})}(t) + N_{\text{opt}}(t), \quad (2)$$

where S_α , $\alpha \in \{1, 2, 3\}$ indicate Stokes parameters before $^{(\text{in})}$ or after $^{(\text{out})}$ the atoms, $\phi = G_F F_z$ is the Poincare-sphere rotation angle, G_F is a detuning-dependent coupling factor, \hat{z} is the propagation direction of the probe light, and N_{opt} is the quantum polarization noise of the detected Stokes component [5]. The approximation holds for small ϕ .

Two paradigmatic single-parameter quantum sensing approaches have been studied both theoretically and experimentally with OPMs: a canonical scalar magnetometer estimates $|\mathbf{B}|$ by orienting \mathbf{B} orthogonal to the readout direction (z), controlling R_{OP} to generate polarization orthogonal to \mathbf{B} , and observing the Larmor frequency $\omega_L \equiv \gamma|\mathbf{B}|$ with which \mathbf{F} precesses about \mathbf{B} . It has been shown that this technique is naturally backaction evading [32,53], and single-parameter sensitivity enhancement has been demonstrated [19]. A canonical rf magnetometer estimates a field $\mathbf{B}(t) = \mathbf{B}_{\text{dc}} + \mathbf{B}_{\text{rf}}(t)$, where $\mathbf{B}_{\text{rf}}(t)$ is relatively weak, sinusoidally varying, and orthogonal to the constant and known \mathbf{B}_{dc} , which is perpendicular to the readout direction (z). A phase-sensitive measurement of $\mathbf{B}_{\text{rf}}(t)$ is performed by controlling R_{OP} to generate polarization along \mathbf{B}_{dc} . In this strategy \mathbf{F} has small F_z component unless resonantly driven, i.e., if $\mathbf{F}_{\text{rf}}(t)$ has components oscillating at or near ω_L . In effect, the readout detects the earliest stages of the magnetic Rabi oscillation. With continuous probing, this allows estimation of both quadratures of $\mathbf{B}_{\text{rf}}(t)$ but does not evade measurement backaction, a condition that restricts the sensitivity to the SQL. With stroboscopic probing, i.e.,

a probe power $S_1(t)$ consisting of pulses spaced by an integer number of half-cycles, backaction is evaded, but only one quadrature can be estimated [54]. Spin squeezing [52,55,56], noise squeezing [57,58], and single-parameter sensitivity enhancement [20,59] have been demonstrated with such stroboscopic techniques.

The HOPM we present below combines a scalar and rf magnetometer in a single measurement protocol, with the possibility of backaction evasion and sensitivity enhancement when estimating both parameters simultaneously. As in the scalar OPM, the spin precession frequency is used to infer $|\mathbf{B}|$, and as in the rf OPM, the amplitude of the spin-precession signal is used to infer one quadrature of the rf field. A natural extension, which we also implement, is to operate with closed-loop control of \mathbf{B}_{dc} , to tune ω_L so as to maintain resonance in a fluctuating magnetic environment.

II. HYBRID-OPM MULTIPARAMETER ESTIMATION STRATEGY

The setup and operation of the hybrid dc and rf OPM are illustrated schematically in Fig. 1. Details of the apparatus are given in Sec. III and in Ref. [19]. A dc field \mathbf{B}_{dc} is applied, nominally along the $(\hat{x} + \hat{z})/\sqrt{2}$ direction and with magnitude B_{dc} . As in Bell-Bloom (BB) magnetometry [60], an optical pumping beam along \hat{z} drives the atomic spin \mathbf{F} with a pumping rate $R_{\text{OP}}(t)$, a periodic function of t with period $2\pi/\Omega_p$. When the optical pumping frequency approaches the Larmor frequency, i.e.,

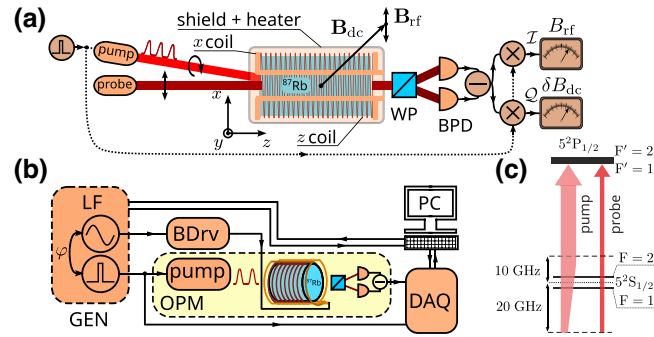


FIG. 1. Experimental setup of a hybrid dc and rf optically pumped magnetometer (HOPM). (a) HOPM consists of a shielded ^{87}Rb cell optically pumped (pump) in the Bell-Bloom configuration. Polarization rotation of the probe beam, proportional to the spin component F_z , is captured via a Wollaston prism (WP) and a balanced photodetector (BPD). dc magnetic field \mathbf{B}_{dc} in the x - z plane at 45° to the pump-probe direction allows hybrid dc and rf sensitivity. rf magnetic field \mathbf{B}_{rf} is aligned along the x axis. (b) Configuration of the HOPM for sensitivity measurements and characterization of the \mathcal{I}/\mathcal{Q} signals as functions of dc and rf magnetic fields. DAQ, data acquisition card; BDrv, low noise current driver. (c) Bell-Bloom pumping. Probe beam is 20 GHz blue-detuned from the D_1 $F = 1 \rightarrow F' = 2$ transition. The pump laser is 20 GHz blue detuned and rapidly swept to be 10 GHz red detuned once per modulation cycle.

when $\delta B_{\text{dc}} \equiv B_{\text{dc}} - \Omega_p/\gamma$ is small, it produces a resonant buildup of spin polarization, in which F_z and thus ϕ oscillate at frequency Ω_p . The rotation signal $S_2^{\text{(out)}}(t)$ is demodulated with a digital lock-in amplifier phase referenced to $R_{\text{OP}}(t)$, to obtain \mathcal{I} and \mathcal{Q} , the in phase and 90° quadrature components, respectively. The demodulation phase is chosen such that $\mathcal{Q} = 0$ at resonance, i.e., for $\delta B_{\text{dc}} = 0$.

An rf field $\mathbf{B}_{\text{rf}}(t) = [\mathcal{X}(t) \cos \Omega_{\text{rf}} t + \mathcal{Y}(t) \sin \Omega_{\text{rf}} t] \hat{x}$, with quadrature amplitudes $\mathcal{X}(t)$, $\mathcal{Y}(t)$ drives a magnetic resonance if the oscillation of $\mathbf{B}_{\text{rf}}(t)$ contains components near ω_L . Without loss of generality, we take the carrier frequency Ω_{rf} equal to Ω_p with phase lag φ , so that $\mathcal{X} = B_{\text{rf}} \cos \varphi$, $\mathcal{Y} = B_{\text{rf}} \sin \varphi$, where B_{rf} is the amplitude of the rf

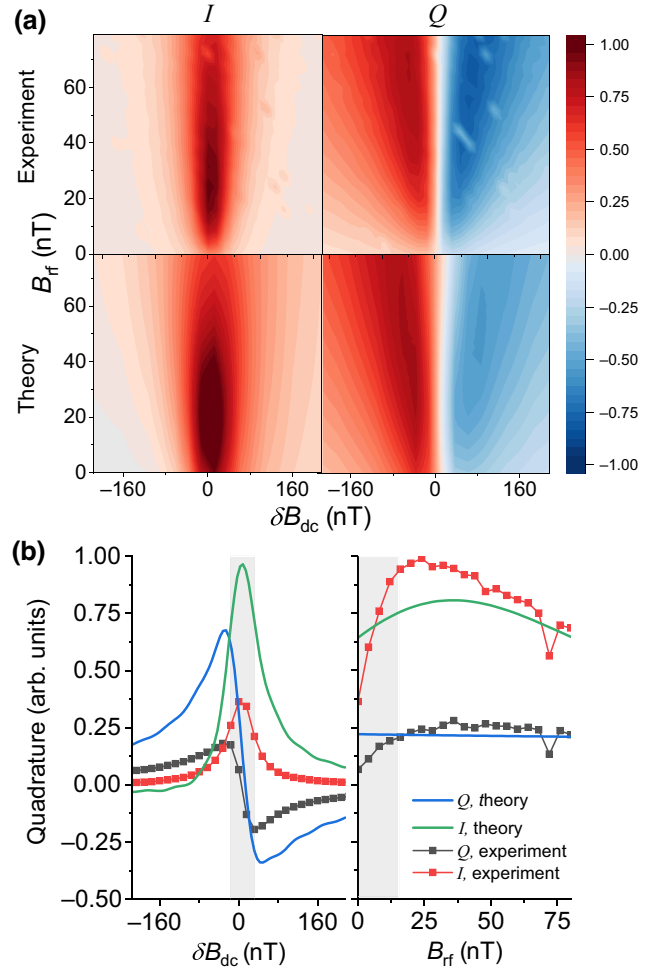


FIG. 2. Characterization of the HOPM. (a) Experimental and simulated dependence of the \mathcal{I} and \mathcal{Q} quadratures [rescaled by the same factor to achieve $\max_{B_{\text{dc}}, B_{\text{rf}}}(\mathcal{I}, \mathcal{Q}) = 1$], for small changes δB_{dc} in the offset magnetic field magnitude and for a range of small B_{rf} amplitudes with pump-resonant rf field ($\Omega_{\text{rf}} = \Omega_p$, phase locked). Simulations by numerical integration of Eq. (1), omitting the noise term. (b) Measured quadratures \mathcal{I} and \mathcal{Q} versus offset δB_{dc} from resonance and B_{rf} . Shaded bands indicate linear response region in which HOPM operates.

drive. Measured dependence of $(\mathcal{I}, \mathcal{Q})$ on φ is discussed in Appendix A. For $\varphi = n\pi, n \in \mathbb{Z}$, we have $\mathcal{Y} = 0$, hence \mathcal{X} encodes the amplitude of the rf field B_{rf} , which is our operating parameter of interest and will be used in the paper from now on. This drive modifies the \mathbf{F} oscillation and is reflected in the \mathcal{I} and \mathcal{Q} signals. This is shown in Fig. 2(a), which compares the response to B_{dc} and \mathcal{I} , as predicted by numerical integration of Eq. (1), omitting stochastic terms and by direct measurement. Relevant cross sections of Fig. 2(a) results are shown in Fig. 2(b). From these, we observe that \mathcal{Q} , which near resonance encodes the phase of the signal relative to the drive, principally responds to B_{dc} , while \mathcal{I} , which near resonance encodes the amplitude of the signal, principally responds to B_{rf} . That is,

$$\left| \frac{\partial \mathcal{I}}{\partial B_{\text{rf}}} \right|_{\mathcal{B}_0} \gg \left| \frac{\partial \mathcal{I}}{\partial B_{\text{dc}}} \right|_{\mathcal{B}_0} \quad \text{and} \quad \left| \frac{\partial \mathcal{Q}}{\partial B_{\text{dc}}} \right|_{\mathcal{B}_0} \gg \left| \frac{\partial \mathcal{Q}}{\partial B_{\text{rf}}} \right|_{\mathcal{B}_0}, \quad (3)$$

where \mathcal{B}_0 indicates the nominal operating point $\delta B_{\text{dc}} = B_{\text{rf}} = 0$. The above relations hold also in the neighborhood of \mathcal{B}_0 , in the ranges indicated by shaded bands in Fig. 2(b). Relative to experiment, theory overestimates the dc response $d\mathcal{Q}/dB_{\text{dc}}$ and underestimates the rf response $d\mathcal{I}/dB_{\text{rf}}$. This may be due to the simplicity of the spin dynamics model, Eq. (1), which describes only one of two hyperfine states, and greatly simplifies the optical pumping process [19,61]. Qualitative agreement seen in Fig. 2 nonetheless suggests the model correctly captures the essentials of HOPM operation.

III. HOPM CONSTRUCTION AND OPERATION

The experimental setup of the HOPM is shown in Figs. 1(a) and 1(b). Isotopically enriched ^{87}Rb and 100 Torr of N_2 buffer gas is contained in a cell with 3 cm internal path, placed inside a ceramic oven. A temperature of 105 °C is maintained by intermittent Joule heating, producing a ^{87}Rb vapor density of 8.2×10^{12} atoms/cm³. Surrounding induction coils in the x and z direction are driven by a low-noise current supply (TwinLeaf CSUA300 and either TwinLeaf CSUA300 or Koheron DRV300-A-40, respectively), generating the offset dc field of $B_{\text{dc}} \approx 4.3 \mu\text{T}$, corresponding to $\omega_L \approx 32$ kHz, and generating the rf field. Four layers of mu-metal shielding ensure environmental magnetic isolation. The OPM is pumped by a circularly polarized beam from a distributed Bragg reflector laser with power 200 μW unless otherwise specified, current modulated at frequency Ω_p (Sigilent SDG1025) in a Bell-Bloom scheme to generate a periodic pumping rate $R_{\text{OP}}(t)$. The collective atomic spin precession in the dc and rf magnetic field is observed with a shot-noise-limited polarimeter (Thorlabs PDB450A after polarization-splitting optics) sensing the polarization rotation of a linearly polarized 500 μW , 20 GHz blue-detuned

probe beam from a tunable frequency-doubled diode laser with a tapered amplifier (Toptica TA-SHG 110) or interchangeably from an external cavity diode laser (Toptica DL100). Parameters of pump (power, detuning, duty cycle) and probe (power, detuning) are optimized as in Ref. [62] for achieving the highest sensitivity for both quadratures, giving priority to dc of the field. An rf signal from a function generator drives induction coils through a low-noise controller to generate \mathbf{B}_{rf} . The signal driving the pump laser's current is phase (φ) and frequency synchronized with the rf oscillations. A DAQ records signals from the BPD and the pump current monitor.

IV. MODEL VALIDATION AND SIGNAL CHARACTERIZATION

Figure 2 shows the dynamical characterization of the HOPM, using the experimental setup presented in Fig. 1(b). For \mathcal{I}/\mathcal{Q} characterization a single-frequency rf carrier, phase locked ($\varphi = 0$) with the pumping signal, is employed with a range of amplitudes. \mathcal{I} and \mathcal{Q} are recorded as a function of applied B_{rf} and δB_{dc} . Results are shown in Fig. 2 and show a good agreement with model predictions.

V. FIELD-LOCKED-LOOP AND DC BACKGROUND REJECTION

We implement a field-locked loop, i.e., feedback from the measured \mathcal{Q} to the applied δB_{dc} , with set point $\mathcal{Q} = 0$. This maintains the \mathcal{I} responsivity $c_{\mathcal{X}}$ near its maximum value in the presence of external perturbations to \mathbf{B}_{dc} . The implemented servoloop is shown in Fig. 3(a). A digital-domain proportional-integral controller, implemented with an FPGA board (RedPitaya STEMLab 125-14 running PyRPL), drives an induction coil controller (TwinLeaf CSUA300) feeding the B_z coil. In this way, we obtain a fast closed-loop response and high noise rejection, as shown in Figs. 3(b) and 3(c), respectively.

To quantify the noise rejection, we operate the HOPM both in open-loop (OL), i.e., without feedback to \mathbf{B}_{dc} , and in closed-loop (CL), i.e., with feedback, both with added noise and without, and observe the resulting PSD \mathcal{P} of the demodulated signal \mathcal{I} . The added noise was approximately equal to 10 pT/ $\sqrt{\text{Hz}}$ white noise, filtered with successive 1-kHz low-pass and 1-Hz high-pass first-order digital filters and added in the digital domain, as depicted in Fig. 3(a). The resulting noise rejection factor

$$\xi(f) \equiv \frac{\mathcal{P}_n^{\text{OL}}(f) - \mathcal{P}_c^{\text{OL}}(f)}{\mathcal{P}_n^{\text{CL}}(f) - \mathcal{P}_c^{\text{CL}}(f)} \quad (4)$$

is shown in Fig. 3(c). We observe a response time of 3 ms and thus a few-hundred Hz bandwidth, and a measured background rejection of more than 20 dB below 60 Hz, dropping to 3 dB at about 260 Hz. We note that feedback to

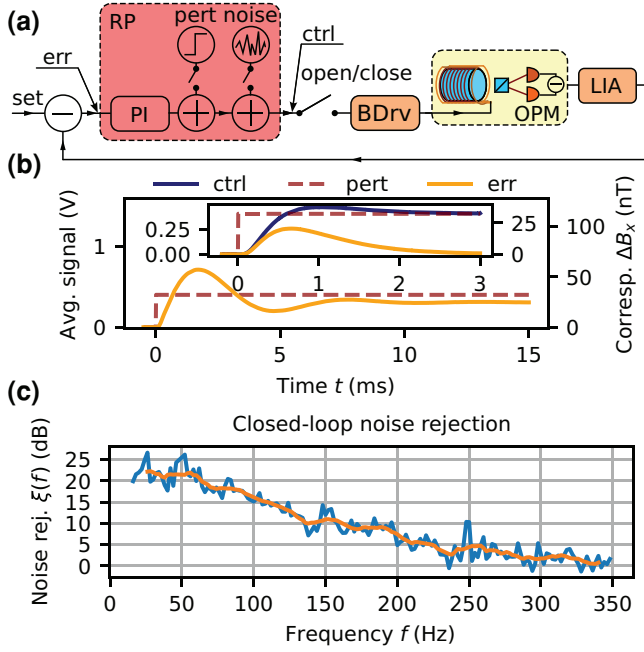


FIG. 3. Feedback loop characterization. (a) External magnetic field stabilization system. Lock-in amplifier’s (LIA) out-phase quadrature Q provides the feedback signal proportional to the deviation of the Larmor frequency from the optically pumped magnetometer’s (OPM) pumping frequency. Redpitaya (RP) board implements a proportional-integral controller (PI) and addition of a test perturbation signal (pert) in the digital domain. Control signal (ctrl) alters the B_z magnetic field component via a current controller (BDrv) driving induction coils. (b) Averaged (ten repetitions) open loop (main plot) and close loop (inset) responses to a ca. 32 nT step perturbation of the B_x magnetic field component. (c) Noise rejection $\xi(f)$ (blue) and $\xi(f)$ smoothed with a 20 Hz moving average (orange), see text.

a single component, here B_z , is sufficient to control B_{dc} , and thus the rf reception frequency, regardless of the direction of the dc magnetic perturbation.

VI. QUANTUM-NOISE-LIMITED SENSITIVITY

We write the power spectral density (PSD) for an observed quantity α as $S_\alpha(f)$, where f is the linear frequency. We also use this notation for the dc and rf magnetic sensitivities, i.e., we write the equivalent magnetic noise $S_\alpha(f)$, $\alpha \in \{B_{dc}, B_{rf}\}$. Sensitivity spectra of the HOPM were measured as in prior work with BB magnetometers [41,63,64]: coils and current drivers are calibrated by measurement of Larmor frequency in a low-density atomic vapor. The HOPM is then operated as described above, near its nominal operating point $\delta B_{dc} = 0$ and $B_{rf} = 0$. The response, defined as $R_I(f) \equiv dI(f)/dB_{rf}(f)$ ($R_Q(f) \equiv dQ(f)/dB_{dc}(f)$) is measured in two steps. First, we acquire quasistatically I versus B_{rf} with $\delta B_{dc} = 0$ (Q versus B_{dc} with $B_{rf} = 0$) and make a linear fit around the operating point to find $R_I(0)$ ($R_Q(0)$). Second, for a range

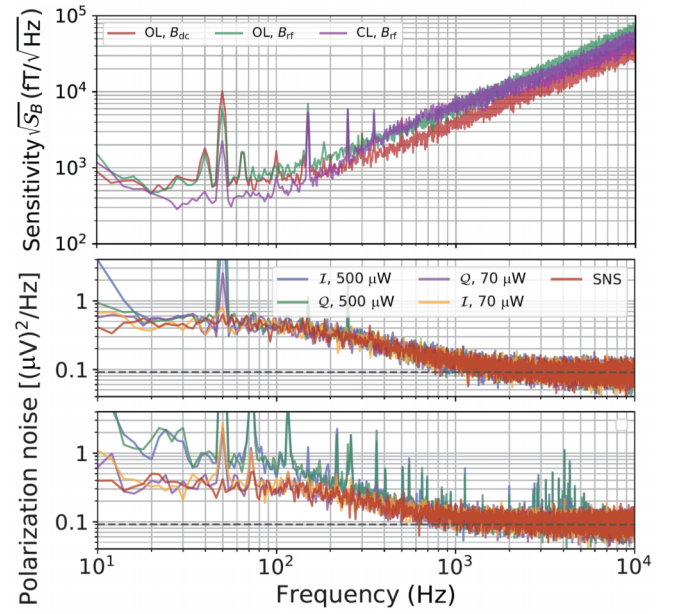


FIG. 4. Sensitivity and polarization noise after demodulation. Top: sensitivity of the magnetometer to a small harmonic perturbation at frequency f of: (OL, B_{dc}) the offset magnetic field magnitude B_{dc} with open feedback loop; (OL/CL, B_{rf}) amplitude of the resonant ($\Omega_{rf} = \Omega_p$) rf magnetic field with open (OL) or closed (CL) feedback loop. Bottom: photon-shot noise (PSN) and spin-projection noise (SPN), and measurement backaction (MBA) in the HOPM. Upper graph shows, for reference, the Faraday rotation spectrum in single-parameter dc field estimation, i.e., with the dc field along \hat{x} , as in Ref. [19]. Red curve shows power spectrum in the absence of optical pumping (spin noise spectroscopy, SNS), other solid curves show power spectra for the I and Q quadratures at different optical pumping levels, as indicated in the plot legend. Dashed line shows the inferred photon-shot-noise level. The observed quantitative agreement of spectra for the OPM and for SNS (which is intrinsically insensitive to technical noise affecting the spins), indicates the absence of other noise sources. Lower graph shows the corresponding spectra for the HOPM, i.e., with the dc field along $(\hat{x} + \hat{z})/\sqrt{2}$. Apart from noise spikes, the spectra show agreement of SNS and HOPM noise levels for weak, 70- μ W optical pumping, indicating that the spectra are dominated by a combination of PSN and SPN. In contrast, for strong, 500- μ W optical pumping, the system becomes sensitive enough in the 20- to 200-Hz band to reveal low-frequency magnetic noise and MBA, which from stochastic simulation of Eq. (1) has the same spectral shape as the SPN but grows with spin polarization and thus with optical pumping.

of frequencies f , the ratio $R_I^2(f)/R_I^2(0) = S_I(f)/S_I(0)$ ($R_Q^2(f)/R_Q^2(0) = S_Q(f)/S_Q(0)$) is measured by applying (with the function generator labeled LF in Fig. 1(b) a small harmonic perturbation to B_{rf} (B_{dc}), i.e., at frequency f and within the linear response regime, and recording $S_I(f)$ ($S_Q(f)$), obtained by Fourier transform with a Hann window. This ratio method automatically accounts for frequency dependence of the signal chain and data analysis.

The HOPM is then operated at the nominal operating point with no applied signal, and the residual noise PSD $S_{\mathcal{I}}(f)$ ($S_{\mathcal{Q}}(f)$) is recorded in the same way. The sensitivity is then calculated as $S_{B_{\text{rf}}}(f) = S_{\mathcal{I}}(f)R_{\mathcal{I}}^{-2}(f)$ ($S_{B_{\text{dc}}}(f) = S_{\mathcal{Q}}(f)R_{\mathcal{Q}}^{-2}(f)$).

Figure 4 shows measured sensitivities in closed-loop (CL) operation, stabilizing $\mathcal{Q} = 0$ and thus $\delta B_{\text{dc}} = 0$, and in open-loop (OL) operation, with δB_{dc} set to zero at the start of the acquisition and limited by passive stability. The experimental setup of the HOPM, configured for sensitivity measurements, is shown in Fig. 1(b). Apart from a few noise spikes, e.g., at multiples of the 50-Hz power-line frequency, and “ $1/f$ noise” below 20 Hz, the sensitivities, which are sub-pT/ $\sqrt{\text{Hz}}$ in the 10–200 Hz band of interest, are quantum noise limited, as we now show, using the methodology of Troullinou *et al.* [19].

Operating the system as in the sensitivity measurement just described, but at negligible atomic vapor density (achieved by allowing the cell to cool to room temperature), we observe linear scaling of $S_{\mathcal{I}}$ and $S_{\mathcal{Q}}$ with

probe power, confirming photon-shot-noise- (PSN) limited probing and establishing the PSN level. This same noise level is observed in HOPM operation in the frequency regime above 1500 Hz, see Fig. 4, confirming PSN-limited operation in this regime. Using spin-noise spectroscopy (signal acquisition in the presence of atoms and probe light but without optical pumping), we observe that the spectral region from 20 to 200 Hz is dominated by spin-projection noise (SPN), which exceeds PSN in this frequency regime. For the OPM in CL operation, we find the same noise level in this range, apart from a noise spike at the mains frequency. This confirms that this low-frequency regime is SPN dominated. For intermediate frequencies, the noise is dominated by a mixture of SPN and PSN.

VII. VLF-LF MAGNETIC COMMUNICATION WITH THE HOPM

To demonstrate background-canceling magnetic communication, we configure the hybrid magnetometer as

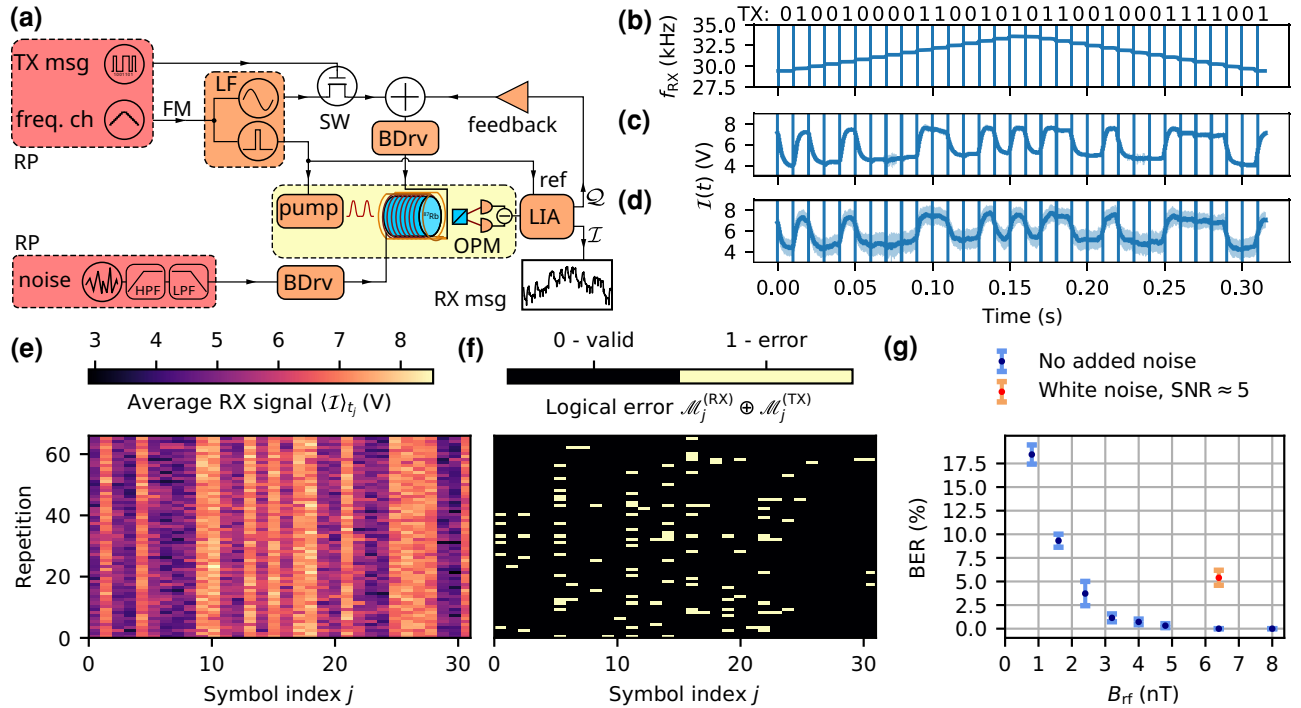


FIG. 5. Receiver operation. (a) OPM experimental setup configured as a magnetic rf receiver. Frequency modulation (FM) of rf carrier and OPM pumping signals selects the frequency channel $f_{\text{RX}}^{(j)}$ for each j -th symbol. Radio-frequency switch (SW) allows on-off-keying (OOK) of the rf carrier according to the binary message (TX msg, $\mathcal{M}^{(\text{TX})}$). A feedback loop on the \mathcal{Q} quadrature corrects the offset magnetic field B_x component for the Larmor frequency to match f_{RX} . Amplitude variation of the \mathcal{I} quadrature reveals the received symbols (RX msg, $\mathcal{M}^{(\text{RX})}$). Additional white Gaussian noise is introduced into the z -axis magnetic field B_z to simulate unshielded operation. (b) Carrier frequency f_{RX} switches symbol-to-symbol. (c),(d) Exemplary receiver signals with $B_{\text{rf}} = 6.39$ nT for a 32-bit transmitted message (TX) with the shade corresponding to one standard deviation over $N_{\text{TX}} = 67$ repetitions. (c) Without additional noise. (d) With white noise, here and henceforth at the SNR of ≈ 5 . (e) Average bit error rate (BER) of the received message. (f) Receiver signal \mathcal{I} averaged over j -th symbol window t_j and digitized signal (g) $\mathcal{M}^{(\text{RX})}$ compared (bitwise XOR) with the TX message $\mathcal{M}^{(\text{TX})}$, with white noise.

a frequency-hopping spread-spectrum (FHSS) magnetic field rf receiver (RX), see Fig. 5(a). To generate a VLF-LF signal, a 32-bit message is encoded with on-off keying (OOK) of \mathbf{B}_{rf} (generated with a coil inside the shielding) with amplitude $B_{\text{rf}} = 6.39$ nT, and symbol rate $f_{\text{OOK}} = 100$ Hz. Transmitted symbols are spread over 16 frequency channels $f_{\text{RX}}^{(1)}$ to $f_{\text{RX}}^{(16)}$ with a separation of 250 Hz and the channel hopping scheme $1 \rightarrow 2 \rightarrow \dots \rightarrow 16 \rightarrow 16 \rightarrow 15 \rightarrow \dots \rightarrow 1$, as shown in Fig. 5(b). The RX reception frequency is tuned in the same sequence, with $\Omega_p = 2\pi f_{\text{RX}}$, and with \mathbf{B}_{dc} set by feedback as in the closed-loop operation described above. Representative RX waveforms [$\mathcal{I}(t)$ quadrature] in the presence and absence of external noise (see Appendix for details) are shown in Figs. 5(c) and 5(d), together with the originally transmitted message (TX).

As shown in Fig. 5(f) [also visible in Fig. 5(d)] there are systematic deviations in the RX signal before digitization, with a simple thresholding strategy leading to symbol misclassification (details on threshold selection are given in the Appendix). Logical errors are depicted in Fig. 5(g). A visual inspection of the signal quality in Figs. 5(c) and 5(d) suggests that a tailored filtering and classification algorithm could greatly reduce the error rate. Figure 5(e) shows the measured bit error rate (BER) as a function of carrier amplitude, which shows the expected superexponential scaling with signal strength. Also shown is the BER for $B_{\text{rf}} = 6.39$ nT with added noise, corresponding to Figs. 5(d), 5(f) and 5(g).

VIII. DISCUSSION AND OUTLOOK

Due to the role of the dc magnetic field in tuning the HOPM-based receiver, its operation is inevitably prone to dc magnetic noise. In particular, low-frequency components within the HOPM rf bandwidth are most detrimental. We have demonstrated how a simple all-digital control system with a single proportional-integral (PI) controller reduces noise power spectral density in this frequency range up to about 20 dB. In the time domain, we observed a stabilization of a rapid 32 nT perturbation of B_{dc} in about 3 ms. We note that in the FHSS scheme the RX is synchronized with the TX. A straightforward improvement to our proof-of-principle demonstration would thus be to add a feed-forward magnetic field compensation, to make the Larmor frequency match the TX channel already from the moment it switches. Not only would this allow a faster settling time (hence higher TX-RX bandwidth) but also pseudorandom channel hopping and larger separations between frequency channels. A feedback loop would nonetheless remain an essential part of the system, to compensate the low-frequency environmental noise present in any unshielded system. With the sub-pT/Hz^{1/2} sensitivity of the HOPM, such a simple feedback loop can provide a highly precise control, compensating slow changes in

background field of any strength. The ability to follow sudden changes is in this implementation limited by the LIA bandwidth, which can be up to twice the carrier frequency.

For simplicity our TX-RX demonstration uses the on-off-keying (OOK) encoding, which maps the bit values to a two-state amplitude modulation (AM). The HOPM is also compatible with frequency- and phase-modulation encodings, e.g., minimal shift keying (MSK) encoding, currently a standard in high-power ULF-VLF-LF systems [45].

IX. CONCLUSIONS

We have described a hybrid optically pumped magnetometer (HOPM) that uses a single atomic ensemble to simultaneously measure dc and rf field components with quantum-noise-limited sub-pT/ $\sqrt{\text{Hz}}$ sensitivity. A need for simultaneous dc and rf sensing arises naturally in an important emerging application of atomic sensors—background-canceling VLF-LF magnetic communication with ultracompact receivers, which enables robust communication. The HOPM is thus a practical example of high-sensitivity multiparameter quantum sensing.

The high dc field sensitivity allows self-adaptation on few-ms timescales to perturbations of the magnetic environment, rejecting magnetic field noise by more than 20 dB at low frequencies and with a few 100-Hz bandwidth. Using this capability, we have shown quantum-noise-limited reception of an on-off keyed signal spread over 16 frequency-hopping channels separated by 250 Hz, in the presence of externally introduced magnetic field noise, simulating unshielded operation.

Simple modifications will allow more sophisticated protocols including quadrature coding, pseudorandom spread spectrum, and improved fidelity by model-aware signal processing. The technology shows the ability of multiparameter quantum sensing methods to meet application-specific sensor requirements, and opens directions for quantum enhanced atomic sensing and magnetic communications.

Data for Figs. 2–6 has been deposited at Ref. [65].

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APPENDIX A: $(\mathcal{I}, \mathcal{Q})$ -SPACE TRAJECTORY

Figure 6 shows an experimentally measured $(\mathcal{I}, \mathcal{Q})$ -space trajectory parameterized by φ , for $\delta B_{\text{dc}} = 0$ and small B_{rf} . For $\varphi = n\pi, n \in \mathbb{Z}$, we have $\mathcal{Y} = 0$, hence \mathcal{X} encodes the amplitude of the rf field, which is our operating parameter of interest. In the paper, we continue the description using amplitude of B_{rf} instead of \mathcal{X} .

APPENDIX B: THRESHOLD SELECTION FOR RECEIVER OPERATION

The threshold for the high or low logical level depends on the frequency channel. By observing a statistic of many transmissions, the channel-specific threshold is calibrated

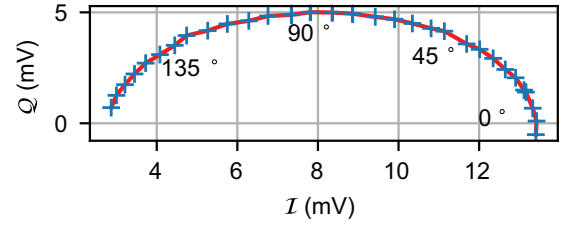


FIG. 6. $(\mathcal{I}, \mathcal{Q})$ -space trajectory. Blue crosses indicate \mathcal{I}/\mathcal{Q} values when a small B_{rf} of 4 nT is applied, for a range of phase offsets φ between the rf field carrier and the pump modulation $R_{\text{OP}}(t)$. Red curve is a linear interpolation between blue crosses.

by taking the running average $V_H^{(j)}$ ($V_L^{(j)}$) with a window of $N_w = 5$ logical symbols of the maxima (minima) within each symbol

$$V_H^{(j)} = \max_{k \in [j - \lfloor N_w/2 \rfloor, j + \lfloor N_w/2 \rfloor]} \langle \langle \mathcal{I}(t) \rangle_{t_k} \rangle_{N_{\text{TX}}}, \quad (\text{B1})$$

and by choosing the local threshold for the j th symbol as a midpoint $V_{\text{thr}}^{(j)} = (V_H^{(j)} + V_L^{(j)})/2$, where $\langle \cdot \rangle_{t_k}$ denotes the average over the k th symbol duration and $\langle \cdot \rangle_{N_{\text{TX}}}$ over the N_{TX} repetitions.

APPENDIX C: EXTERNAL NOISE FOR RECEIVER OPERATION

The feasibility of operation in a noisy environment (e.g., unshielded) is exemplified by adding Gaussian white noise to the z component of the magnetic field B_z , independent of the feedback loop, which alters the B_x component. A measurement with white noise is performed only for $B_{\text{rf}} = 6.39$ nT and a noise level corresponding to a $\text{SNR} = B_{\text{rf}}/B_{\text{noise}}$ of about 5, where $(B_{\text{noise}})^2$ is the noise power spectral density integrated over the 100-Hz transmission bandwidth. SNR was confirmed with OPM power spectral density measurements for a range of introduced noise powers.

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