Passive and active neutron signatures of ²³³U for nondestructive assay

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The thorium fuel cycle is emerging as an attractive alternative to conventional nuclear fuel cycles, as it does not require the enrichment of uranium for long-term sustainability. The operating principle of this fuel cycle is the irradiation of ²³²Th to produce ²³³U, which is fissile and sustains the fission chain reaction. ²³³U poses unique challenges for nuclear safeguards, as it is associated with a uniquely extreme γ -ray environment from ²³²U contamination, which limits the feasibility of the γ -ray-based assay, as well as more conservative accountability requirements than for ²³⁵U set by the International Atomic Energy Agency. Consequently, instrumentation used for safeguarding ²³⁵U in traditional fuel cycles may be inapplicable. It is essential that the nondestructive signatures of ²³³U be characterized so that nuclear safeguards can be applied to thorium fuel-cycle facilities as they come online. In this work, a set of 233 U₃O₈ plates, containing 984 g²³³U, was measured at the National Criticality Experiments Research Center. A high-pressure ⁴He gaseous scintillation detector, which is insensitive to γ rays, was used to perform a passive fast neutron spectral signature measurement of $^{233}U_3O_8$, and was used in conjunction with a pulsed deuterium-tritium neutron generator to demonstrate the differential die-away signature of this material. Furthermore, an array of ³He detectors was used in conjunction with the same neutron generator to measure the delayed neutron time profile of ²³³U, which is unique to this nuclide. These measurements provide a benchmark for future nondestructive assay instrumentation development, and demonstrate a set of key neutron signatures to be leveraged for nuclear safeguards in the thorium fuel cycle.

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I. INTRODUCTION AND BACKGROUND

Nuclear energy has long been considered a scalable, reliable candidate source of low-carbon electricity to replace fossil fuel-based power sources. In comparison to some other low-carbon sources like solar and wind, nuclear reactors can typically operate consistently independent of weather, time of day, or season. However, nuclear power is inextricably linked to the potential for nuclear proliferation, the risks of which must be mitigated. Proliferation risks are primarily mitigated by the International Atomic Energy Agency (IAEA) using nuclear safeguards as prescribed by the Treaty on the Non-Proliferation of Nuclear Weapons (NPT). Nondestructive assay (NDA) methods are well established and routinely practiced for plutonium, natural uranium (0.7%²³⁵U), and enriched uranium (>0.7%²³⁵U) in traditional light-water reactors (LWRs) and heavy-water (CANDU) fuel cycles [1,2]. However, some proposed advanced reactors and fuel cycles pose challenges to the current safeguards regime. In particular, there is a lack of NDA technology to adequately safeguard 233 U produced in thorium fuel cycles [3,4], compounded by the requirement that ²³³U be accounted separately from ²³⁵U when the two isotopes are colocated, since States with safeguards agreements in force with the IAEA must report quantities of ²³⁵U and ²³³U separately. [5].

A. Unique characteristics of ²³³U in the thorium fuel cycle

Uranium-233 produced in nuclear reactors by the absorption of a neutron in 232 Th and the subsequent β decays of ²³³Th and ²³³Pa is always accompanied by trace quantities of ²³²U, ranging from approximately 10 to 5000 ppm. This is due to several (n,2n) reactions and subsequent β decays in ²³²Th, ²³³Pa, and ²³³U, which occur in the presence of fast neutrons [6]. The presence of ^{232}U is key, as its decay chain is associated with high specific activity and a high branching ratio for high-energy γ -ray emission, principally at 2.6 MeV (²⁰⁸Tl, 35.9% branching ratio) [7]. Since 232 U is typically not separated from 233 U in thorium-based fuel cycles, this intense γ -ray environment is inextricably linked to any macroscopic quantity of ²³³U. The activity of the 2.6-MeV γ ray, which is emitted by ²⁰⁸Tl in 99.75% of its decays, with respect to ²³²U concentration and time since purification is approximated

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FIG. 1. Calculated activity of 2.6-MeV γ ray per one significant quantity of ²³³U (8 kg).

by

$$A_{208}(t, C_{232}) = B_{208}C_{232}\lambda_{232}N_{233}e^{-\lambda_{232}t}[1 - e^{\lambda_{228}t}], \quad (1)$$

where C_{232} is the initial ²³²U concentration, B_{208} is the branching ratio for production of ²⁰⁸Tl, λ_{232} is the ²³²U decay constant, N_{233} is the ²³³U population, and λ_{228} is the ²²⁸Th decay constant. This approximation is possible since the ²³²U half-life (69 y) is much longer than the ²²⁸Th halflife (1.9 y), and all other isotopes in the ²³²U decay series have much shorter half-lives, on the order of seconds to days [8]. The results of this calculation are shown for a significant quantity (SQ) of ²³³U (8 kg) [5] in Fig. 1.

B. Challenges in measurement of ²³³U-bearing items for safeguards

Many NDA measurements of fissionable materials conducted for the purpose of nuclear safeguards involve measurement of γ -ray spectra. These measurements may quantify the total mass of some isotope, or measure the relative concentration of isotopes in thick samples. γ spectroscopy, however, is not feasible for NDA of ²³³U items due to the intense contribution of γ rays from the ²³²U decay chain: the intensity of the 2.6-MeV γ -ray line does not

TABLE I. Potential (α, n) reactions in ²³³U-bearing compounds. Note that Ref. [9] gives (α, n) spectra for α radiation from ²³⁴U, which is similar to that of ²³³U.

Element	(α,n) reaction(s)	Q (MeV)	\overline{E}_n for ²³⁴ U α [9]
0	$^{17}\text{O} + \alpha \rightarrow n + ^{20}\text{Ne}$	0.587	2.24
	$^{18}\text{O} + \alpha \rightarrow n + ^{21}\text{Ne}$	-0.697	
Be	${}^{9}\text{Be} + \alpha \rightarrow n + {}^{12}\text{C}$	5.702	4.76
Li	$^{7}\text{Li} + \alpha \rightarrow n + {}^{10}\text{B}$	-2.790	0.33
F	$^{19}\text{F} + \alpha \rightarrow n + ^{22}\text{Na}$	-1.952	1.24



FIG. 2. (α, n) cross sections for various low-Z isotopes of interest in the thorium fuel cycle [10]. The shaded area represents possible α energies for ²³³U, as α particles lose energy via electronic interaction before interacting with any target nucleus. b, barn.

strictly correlate with the mass of ²³³U, and γ rays directly associated with the decay of ²³³U are low energy and low intensity and consequently not measurable above the Compton continua associated with the ²³²U lines [4]. As an alternative, neutron-based NDA methods may be useful for safeguarding ²³³U-bearing materials. Neutron signatures are relatively difficult to shield and generally provide more information about the bulk material as opposed to only the outer "skin" of the material, as may be the case due to self-shielding for γ -ray-based measurements. Some neutron emissions from ²³³U-bearing materials may arise from (α ,n) reactions in the material's chemical matrix, while others relate to the fissionable content of the material, either in aggregate or isotope specific.

C. Neutron signatures of ²³³U-bearing items *1. Spontaneous neutron emission*

Uranium-233-bearing objects of safeguards relevance may be in a material matrix with low-Z elements, such as oxygen (in U₃O₈ or UO₂), lithium, beryllium, or fluorine. α radiation emanating from ²³³U can be absorbed by low-Z elements, which may then emit a neutron. These (α ,n) neutrons typically have spectra that take the shape of continua up to the sum of incident α -particle energy and the Q value of the (α ,n) reaction, reduced by the excitation and recoil energy of the reaction product nucleus. The reaction pathways and average neutron energies of select (α ,n) sources are shown in Table I. Some (α ,n) spectra contain peaks and other structures, arising from their energy-dependent cross sections, shown in Fig. 2. A major caveat to the (α ,n)-based approach to ²³³U NDA is that the content of ²³²U also contributes to the (α ,n) signature of ²³³U compounds: the half-life of ²³³U (160 ky) is 2319 times longer than that of ²³²U (69 y), so the ²³²U α activity is significant even at ppm-scale concentrations. As a result, the α activity of ²³²U dominates in ²³³U samples where the ²³²U concentration is above approximately 433 ppm. Consequently, in poor-grade (high ²³²U content) samples, measurements based on (α ,n) reactions attribute most of the neutron signal to the nonfissile ²³²U.

The (α, n) neutrons may induce fission in ²³³U or other fissionable species present, and thereby produce additional neutrons, with a probability determined by the multiplication of the matrix, k_{eff} . Induced fission neutrons have a distinct multiplicity and spectrum from (α, n) neutrons, so the ratio of spontaneous (α, n) to induced fission neutrons can theoretically be measured. Since this ratio is related to multiplication, it may help indicate the fissionable matrix composition.

2. Differential die-away

Pulsed differential die-away (DDA) is a technique that measures the presence of fission neutrons emitted by a target after a pulsed active interrogation source is turned off [11]. Neutrons thermalizing in the environment typically have a long lifetime compared to the duration of an active interrogation pulse, and the resultant thermal neutron population that persists beyond the fast neutron pulse has a high probability of inducing fission in fissile materials [12]. Measurement of DDA is best done with a detector, which is sensitive to fast neutrons only, as the signal-to-noise ratio (SNR) when fissile material is present is orders of magnitude higher for fast neutrons than for thermal neutrons after the pulse [13]. This technique has been previously demonstrated using cadmium-shielded ³He detectors [11] and with organic scintillation detectors [12,14], the latter showing a more rapid die-away of the interrogation active background. In the case of 233 U and its associated γ -ray environment, however, organic scintillators may not be well suited, since the probability of pulse pile up, leading to particle misclassification, may lead to an unacceptable increase of the observed neutron background, or require extensive digital postprocessing [15].

TABLE II. Normalized delayed neutron group yields and halflives for fast neutron-induced fission in ²³³U and ²³⁵U [24].

Isotope	Group	1	2	3	4	5	6
²³³ U	Half-life (s)	55.6	19.3	5.04	2.18	0.57	0.221
	Yield	0.095	0.208	0.242	0.327	0.087	0.041
²³⁵ U	Half-life (s)	54.6	20.2	5.36	2.38	0.77	0.24
	Yield	0.057	0.192	0.190	0.357	0.120	0.084



FIG. 3. Delayed neutron time profiles for fast neutron-induced fission of 233 U and 235 U, from Eq. (2) and Table II, assuming 60 s of irradiation. The neutron reaction rates are normalized to their values at t = 0.

3. Delayed neutron emission

When nuclei undergo fission, the resultant neutron-rich fission fragments have some probability of emitting neutrons during their radioactive decay [16–18]. This process is referred to as β -delayed neutron emission, since these neutrons are emitted in coincidence with β radiation [19]. There are many delayed neutron precursors, which are typically condensed into six groups determined by their half-lives, ranging from 0.1 to 60 s [20]. Each fissionable isotope has a unique yield for each delayed neutron group, resulting in a unique delayed neutron time profile R(t) that can be modeled as

$$R(t) = B + C \sum_{i=1}^{6} Y_i [1 - e^{-t_b/\tau_i}] e^{-t/\tau_i},$$
 (2)

where *B* is a constant background, *C* is a scaling factor, *i* is the group, Y_i is the group yield, t_b is the buildup or irradiation time, and τ_i is the group mean lifetime, which is equivalent to $t_{1/2,i}/\ln(2)$ where $t_{1/2,i}$ is the group half-life. The delayed neutron group yields for ²³³U are shown in Table II and compared against those of ²³⁵U. When fission is induced during active neutron interrogation, this time profile can be measured to indicate the isotopic composition of fissionable material [21,22], and has been shown to be resilient to common neutron shielding [23]. The delayed neutron time profiles for fast neutron-induced fission of ²³³U are shown in Fig. 3

II. METHODS

In this work, measurement of the neutron signatures of ²³³U took place at the National Criticality Experiments



FIG. 4. Conceptual diagram illustrating the arrangement of detectors and electronics used to measure the ²³³U plates (above). Images of the measurement setup at NCERC (below).

Research Center (NCERC), an experimental venue at the Nevada National Security Site (NSSS), which holds a variety of test objects containing nuclear materials.

A. Target and interrogation source

The material used in the experiments described in this work was a set of fuel plates fabricated for the Zero Power Reactor (ZPR) at Argonne National Laboratory. These plates comprise 33 g²³³U₃O₈ powder in stainless-steel packets measuring $2 \times 3 \times 1/4$ " [25]. The plates are stored in groups of 12 in steel "soup cans," three of which are stored in a triangular lattice within an AT-400R radioisotope storage container. In these measurements, the ZPR plates could not be removed from their AT-400R container, which also contains a 1.5" lead pig around the cans. Each AT-400R container holds a total of 1.188 kg ²³³U₃O₈, approximately 984 g of which is ²³³U. The ²³³U used to fabricate these ZPR plates was produced with low ²³²U contamination, the average of which in all plates is 7 ppm. Even at this low concentration, the radiation exposure rate due to ²³²U daughters at equilibrium in a single plate is 1000 mR/h, measured 1.5" from the center of the plate surface. Among all 36 plates, the total 232 U activity is approximately 157 mCi, and the corresponding 208 Tl activity is 56.5 mCi. At this exposure level, most γ -sensitive detectors cannot be operated due to pulse pile-up issues. In this experiment, a single AT-400R containing 36 233 U₃O₈ ZPR plates was characterized. Due to the weight of the container and its lead pig, it was placed on the concrete floor of the laboratory.

The D-T generator used as an interrogation source was a Thermo Scientific model P211. This generator has a nominal total output of 10^8 n/s, in pulses of approximately 10-µs duration, operating up to 100 Hz. This low duty cycle and high pulse intensity is advantageous for DDA analysis, as the instantaneous neutron output during pulses is high, and there is sufficient time for the neutron population to decay between pulses.

B. Neutron detectors

To detect the fast neutron signatures corresponding to passive (α,n) emissions and active interrogation DDA, an Arktis Radiation Detectors S670 [26] high-pressure ⁴He scintillation detector was used. This detector is



FIG. 5. MCNP geometry for simulation of DDA and DN signatures.

intrinsically sensitive to only fast neutrons if an energy deposition threshold of approximately 300 keV is used [27], measures the energy of fast neutron-induced ⁴He recoils, and in doing so provides information on the incident neutron spectrum. This detector has a faster response time, smaller dead time, and better time resolution than most gas-based detectors based upon collection of ionization signal, since the ⁴He scintillation pulses have a duration of approximately 1 μ s. The detector and pulse analysis system applied is described in greater detail in Ref. [28].

Two MC-15 neutron multiplicity counters were also used to measure the delayed neutron time profile of the $^{233}U_3O_8$ plates. MC-15 detectors comprise an array of 15 ³He proportional counters embedded in a slab of highdensity polyethylene (HDPE) and are sensitive to a wide range of neutron energies [29]. They are self-contained, do not require any external electronics to function, and provide a logic (TTL) pulse output for each neutron detection event. These detectors are efficient in detecting neutrons in the energy range of delayed neutrons (approximately 0.001 to 2 MeV [19]), but because they must thermalize neutrons before detecting them, their time resolution is poor compared to the S670 detector. Consequently, MC-15 detectors were used to measure the time profile of delayed neutrons, but not DDA. The measurement configuration, showing the target material, interrogation source, and detectors are shown in Fig. 4.

C. Electronics and experimental operation

A CAEN V1725 14-bit, 250 MS/s digitizer and CAEN CoMPASS 2.0 software [30] were used to collect waveforms from the S670 and MC-15 detectors. The P211 D-T generator has analog control, and was configured to run at 100 Hz for 6000 pulses. A trigger out logic signal from the P211 pulse-forming network, approximately 10 μ s prior to neutron production, was also digitized. To measure the DDA time profile, the time period between events in the S670 detector and the most recent logic signal from the pulse-forming network were considered (i.e., between pulses), whereas for the delayed neutron time profile, the time period between events in the MC-15 detectors and the 6000th logic signal were considered (i.e., after the D-T generator was turned off). While the P211 settings ideally correspond to a total irradiation period of 60 s, it was observed that the actual pulse frequency of the generator was approximately 107 Hz, corresponding to an actual irradiation period of 56 s.

The passive fast neutron emission signature of the $^{233}U_3O_8$ plates was measured using the S670 detector for a total period of 1200 s, and also provided the passive background for measurement of the DDA signature. To measure DDA and delayed neutron emission, 40 irradiation cycles were carried out. The irradiation cycle period was 300 s, of which 56 s corresponds to pulsed irradiation to build up the delayed neutron precursor population and measure the DDA signature, and the remainder corresponds to D-T generator off time, which allows for measurement of the delayed neutron time profile. An additional 10 irradiation cycles were performed with the AT-400R container removed, to serve as an active background for the DDA measurement. The analysis shown in this work represents the data from all irradiation cycles in aggregate.

D. Monte Carlo simulation

The DDA and DN signatures of the $^{233}U_3O_8$ plates were simulated using MCNPX-PoliMi [31,32]. The geometry of the AT-400R container, shielding, and its contained ZPR plates is based on Refs. [33,34] and is shown in Fig. 5. The P211 D-T generator was approximated as a monoenergetic



FIG. 6. Passive fast neutron spectral signature of ${}^{233}U_3O_8$ measured with the S670 ⁴He detector, compared to the measured spectrum of ${}^{252}Cf$. The spectra are normalized to their integral above 300-keV energy deposition, above which there are no contributions from γ radiation.

14.1-MeV isotropic point source. In postprocessing, the temporal behavior of the neutron source was approximated by adding time randomly sampled from a 10- μ s-wide uniform distribution to each history in the PoliMi collisional output file. To simulate the delayed neutron time profile, neutron emissions from the ²³³U plates that occur more than 10 ms after the D-T generator pulse were recorded, since delayed neutron emissions occur on such a long time scale that their time signature is immune to radiation transport-induced time-distortion effects. To approximate the effect of the D-T generator irradiation period, time randomly sampled from a 56-s-wide uniform distribution was added to the delayed neutron histories.

III. RESULTS

A. Passive signatures

The passive spectrum of ${}^{233}U_3O_8$ is shown in Fig. 6 and compared against a ${}^{252}Cf$ spontaneous fission neutron



FIG. 7. DDA measurement of ZPR plates with the S670 ⁴He detector, compared against background and simulation.



FIG. 8. Delayed neutron decay measurement of ZPR plates as measured with MC-15 detectors (above) and simulated with MCNPX-PoliMi (below). Time profiles are normalized to the sum of the first 4 s. The measured time profile has 2-s-wide bins, while the simulated time profile has 0.5-s-wide bins. Fits to Eq. (2) and Table II are shown in red.

source, as measured with the S670 ⁴He detector. The neutron source emanating from the ²³³U₃O₈ plates exhibits a characteristically lower-energy endpoint when compared to the ²⁵²Cf fission source, as is expected from ^{17,18}O(α ,n) reactions. The intensity of this ²³³U O(α ,n) spectrum is proportional to ²³³U mass at low concentrations of ²³²U and at low multiplication, and is consequently a potential candidate for NDA of ²³³U under these circumstances.

B. Differential die-away

The DDA microscopic time profile of the ZPR plates measured with the S670 ⁴He detector is shown in Fig. 7 and compared against the sum of active and passive backgrounds. Only pulses corresponding to at least 300-keV recoil energy deposition were accepted in generating DDA time profiles, for both measurement and simulation. The fission neutron signal remained visible above background for about 1200 μ s after the generator pulse, in agreement with simulation. The measured DDA time profile shows a clear exponential decay significantly above the background, implying that DDA measured with this detector

TABLE III.	Results of fitting delayed no	eutron data in this work t	to various fissionable isotop	e delayed neutron parameter	s. Parameters
for ²³³ U and ²	²³⁵ U from Ref. [24], for ²³⁸ U	J from Ref. [35], for ²³⁹]	Pu from Ref. $[36]$, and for 2	³² Th from Ref. [37].	

Isotope	Dataset	С	В	χ^2/ndf
²³³ U	Measured	0.8450 ± 0.0140	0.0196 ± 0.0018	48.9 / 48
²³⁵ U		0.9146 ± 0.0172	0.0249 ± 0.0021	58.6/48
²³⁸ U		1.454 ± 0.080	0.0008 ± 0.2615	547 / 48
²³⁹ Pu		0.9288 ± 0.0046	0.025 ± 0.002	65.3 / 48
²³² Th		1.012 ± 0.005	0.0306 ± 0.0018	96.0 / 48
²³³ U	MCNPX-PoliMi	0.8591 ± 0.0005	0.00082 ± 0.00041	211 / 198
²³⁵ U		0.9202 ± 0.0007	0.0064 ± 0.0004	294 / 198
²³⁸ U		1.152 ± 0.007	0.0138 ± 0.0003	936 / 198
²³⁹ Pu		0.9369 ± 0.0064	0.0062 ± 0.0003	369 / 198
²³² Th		1.031 ± 0.009	0.0109 ± 0.0006	777 / 198

may be a strong candidate for confirmation of the presence of 233 U. At low multiplication, the fast neutron DDA signal intensity is proportional to fissile mass, so this technique may be used for quantification of total fissile content in the presence of 233 U, in the case that the measurement and neutron moderation geometries are tightly constrained.

C. Delayed neutrons

The delayed neutron time profile of 233 U measured with the MC-15 detectors is shown in Fig. 8, and compared to the simulated time profile. The time profiles are fit to Eq. (2), with tabular delayed neutron yields and half-lives for 233 U for 14.1-MeV neutrons given in Table II. The only fitting parameters used are the scaling factor *C* and the flat constant background *B*. To demonstrate the uniqueness of these fits to delayed neutrons from 233 U specifically, the fit results when the time profiles are forced to fit delayed neutron yield parameters for other fissionable isotopes are shown in Table III. Both the measured and simulated time profiles are best fit by the delayed neutron parameters for 233 U, however, the distinction is clearer in the simulated time profile, likely due to its superior statistics and lack of passive background.

IV. CONCLUSIONS AND FUTURE WORK

In this work, three signatures of 233 U were investigated for their feasibility in future NDA methods for international safeguards of thorium fuel cycles: passive fast neutron spectroscopy, differential die-away analysis, and delayed neutron time-profile analysis. An experiment was performed to measure these signatures at NCERC, using nearly a kilogram of 233 U in the form of 233 U₃O₈, representing the largest-scale NDA measurement of 233 U to date.

The fast neutron spectral signature of $^{233}U_3O_8$ is shown to be readily measurable with the γ -insensitive S670 ⁴He detector, and clearly differentiable from a generic spontaneous fission neutron source. Consequently, this technique could be well suited to discriminating between oxides of ²³³U and plutonium, for example.

Measurement of the fast neutron DDA time profile of ²³³U was also demonstrated with the S670 detector and a pulsed D-T neutron generator for the first time, indicating a potentially unique capability of the ⁴He scintillation detector.

The delayed neutron time profile of 233 U, induced using the same D-T neutron generator, was measured using an array of moderated ³He proportional counters. The measured time profile showed a good fit to the time profile generated from nuclear data, and matched the simulated time profile. Delayed neutron time profiles are isotope specific, so their measurement may allow for discrimination between and separate quantification of ²³³U and ²³⁵U, which is one of the primary challenges in NDA for safeguarding thorium fuel cycles. In future work, delayed neutron-based techniques should be further investigated with mixed-isotope (²³³U and ²³⁵U) items, so that separate isotope quantification can be demonstrated.

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