


Enhancement of Josephson Critical Currents in Ferromagnetic $\text{Co}_{40}\text{Fe}_{40}\text{B}_{20}$ by Thermal Annealing

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The electrical and structural properties of $\text{Co}_{40}\text{Fe}_{40}\text{B}_{20}$ (Co-Fe-B) are tunable by thermal annealing. This is key to the optimization of Co-Fe-B-based spintronic devices, where the advantageously low magnetic coercivity, high spin polarization, and controllable magnetocrystalline anisotropy are utilized. Here, we report Nb/Co-Fe-B/Nb Josephson devices and demonstrate an enhancement of the critical current by up to 700% following thermal annealing due to increased structural ordering of the Co-Fe-B. The results demonstrate that Co-Fe-B is a promising material for superconducting quantum spintronic devices.

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Following the discovery of giant magnetoresistance [1,2] and the development of spin valves [3,4], $\text{Co}_{40}\text{Fe}_{40}\text{B}_{20}$ (Co-Fe-B) was identified as an alternative magnetic material to those that had previously been employed, particularly due to its low magnetic anisotropy and low switching energy [5,6]. In Co-Fe-B spintronic devices, the magnetoresistance can be optimized through a thermal annealing [7]. Specifically, for Co-Fe-B/MgO/Co-Fe-B magnetic tunnel junctions, thermal-annealing treatment leads to high tunneling magnetoresistance, exceeding 600% at room temperature [8]; neither Co-Fe-B nor Co-Fe as-grown devices display comparable efficiencies. Studies of diffusive (i.e., without a tunnel junction) Co-Fe-B spin valves have also demonstrated larger giant magnetoresistance effects following annealing treatment [9].

Although the advantageous properties of Co-Fe-B-based spintronic devices and their controllability through annealing have been well recognized in the field of spintronics, there has been only one other report on superconducting devices with Co-Fe-B [10]. This may be due to the strong magnetic exchange energy and the high electrical resistivity of Co-Fe-B [11], which should strongly quench the superconducting proximity effect, making it challenging to investigate the coupling of superconductivity and magnetism. However, the superconducting proximity effect in

Co-Fe-B could enable energy-efficient and fast superconducting (Josephson) devices because the low coercivity of Co-Fe-B reduces the energy required for writing operation and the large resistivity reduces the switching time $\tau = \Phi_0/2\pi I_c R_N$ [12–14], where Φ_0 is the magnetic flux quantum, I_c is the Josephson critical current, and R_N is the normal state resistance.

Here, we report Nb/Co-Fe-B/Nb Josephson devices with thin (<5 nm) Co-Fe-B barriers and investigate the effect of thermal annealing on the critical current. From measurement of the Josephson critical currents versus Co-Fe-B barrier thickness, we determine a superconducting coherence length in Co-Fe-B of approximately 1 nm. Annealing the devices at 400 °C for 30 min in vacuum results in the increase in the critical current by as much as 700% for a Co-Fe-B thickness of 4 nm. We associate this enhancement of the Josephson current with an increase in the electron mean-free-path length (i.e., reduced charge and spin-flip scattering) in Co-Fe-B along with improved transparency at the Nb/Co-Fe-B interfaces.

Nb(300 nm)/Co-Fe-B(d_F)/Nb(300 nm) trilayers are fabricated on $5 \times 5 \text{ mm}^2$ quartz substrates by dc magnetron sputtering in an ultrahigh-vacuum chamber with a base pressure better than 10^{-6} Pa. The sputtering targets ($\text{Co}_{40}\text{Fe}_{40}\text{B}_{20}$, Nb) are presputtered for 20 min to clean their surfaces. The films are grown in Ar at a pressure of 1.5 Pa at room temperature. Multiple quartz substrates are placed on a rotating circular table that pass below a series of stationary magnetrons. A series of stacks are prepared with different Co-Fe-B thicknesses

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($d_F = 1.5\text{--}4.5$ nm) between 300-nm-thick layers of Nb in a single deposition. Layer thicknesses are controlled by adjusting the angular speed of the rotating table.

Current-perpendicular-to-plane Nb(300 nm)/Co-Fe-B (d_F)/Nb(300 nm) nanopillar devices with square cross-section areas of about $A = 500 \times 500$ nm² are fabricated using a focused beam of Ga ions as described elsewhere [15]. A pulse-tube cryogen-free measurement system (Cryogenic Ltd) is used to cool the devices down to 1.6 K. Current-voltage $I(V)$ characteristics of the nanopillars are measured in a four-point configuration using the differential conductance mode of a Keithley 6221 ac-current source and a 2182 A nanovoltmeter. The Josephson critical current and normal state resistance of each device are determined by fitting the $I(V)$ characteristics to the resistively shunted junction model $V = R_N(I^2 - I_c^2)^{0.5}$. Since the coherence length in a ferromagnet is $\xi_F = (\hbar D_F / 2\pi E_{\text{ex}})^{0.5}$ in the diffusive limit [16] and I_c is proportional to $\exp(-d_F / \xi_F)$ [16], I_c enhancement can be realized by increasing the diffusion constant (D_F) or decreasing the magnetic exchange energy (E_{ex}) of the ferromagnet. Electrical measurements are performed on nanopillars both before and after thermal annealing. Thermal annealing is performed at 400 °C for 30 min in vacuum (10^{-5} Pa)—the typical postanneal condition [8,17] to promote crystallization. No magnetic field is applied during annealing. Annealed Co-Fe-B has lower resistivity than amorphous Co-Fe-B deposited at room temperature [18]. Although electrical properties of our Co-Fe-B films become increasingly metallic with annealing [see Fig. S2(b) within the Supplemental Material [19]], we can not detect x-ray diffraction peaks from the Co-Fe-B layer, which is likely due to small grain size of Co-Fe-B in the absence of a buffer layer (e.g., MgO [20]) that can promote crystallization with large grain size.

A typical Fraunhofer pattern, the critical current density J_c versus in-plane magnetic field H , for a Nb(300 nm)/Co-Fe-B(3.5 nm)/Nb(300 nm) nanopillar at 1.6 K before (solid curves) and after (dashed curves) thermal annealing is shown in Fig. 1(a) (see Fig. S1 within the Supplemental Material [19] for all the Fraunhofer patterns recorded in this study). $J_c(H)$ is hysteretic and the maximum values of I_c are obtained at nonzero applied fields ($\mu_0 H = \delta$) due to the intrinsic barrier magnetization [21,22]. In Fig. 1(b), we plot δ at 1.6 K versus d_F , which shows a linear increase in δ with d_F . By fitting δ versus d_F to $\delta = M_s(d_F - d_{\text{dead}}) / (2\lambda + d_F)$ [21], we obtain a volume saturation magnetization of $M_s = (643 \pm 21)$ emu cm⁻³, and a magnetically dead layer thickness at each Nb/Co-Fe-B interface of $d_{\text{dead}} = (0.33 \pm 0.09)$ nm, which is slightly thinner than those at Nb/Co ($d_{\text{dead}} = 0.4$ nm) and Nb/Fe ($d_{\text{dead}} = 0.55$ nm) interfaces [23] and consistent with the magnetization measurements of unpatterned Nb(30 nm)/Co-Fe-B(2–10 nm)/Nb(30 nm) samples [see

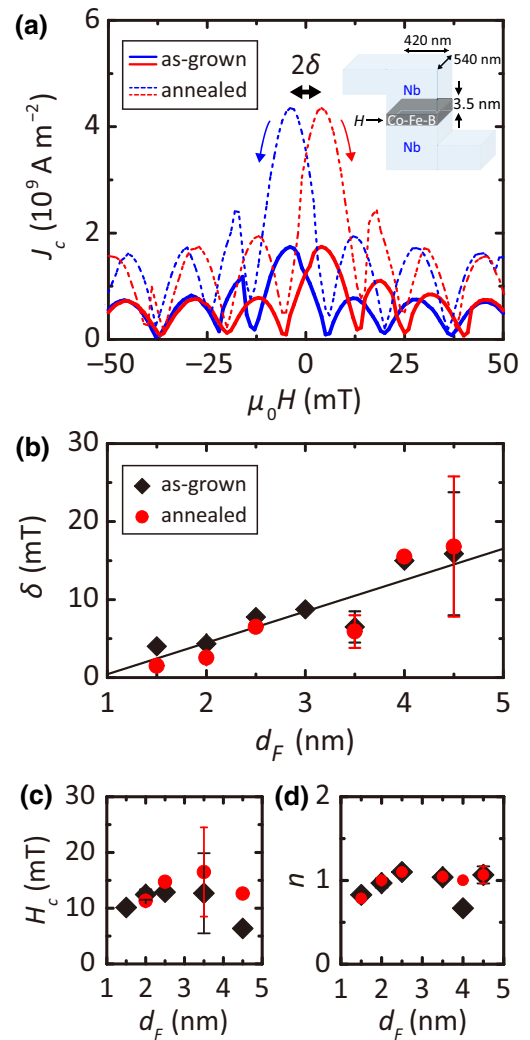


FIG. 1. (a) $J_c(H)$ pattern for a Nb(300 nm)/Co-Fe-B(3.5 nm)/Nb(300 nm) nanopillar before (solid lines) and after (dashed lines) thermal annealing at 400 °C for 30 min. The red (solid and dashed) line shows J_c with increasing H and the blue (solid and dashed) line shows J_c with decreasing H . The inset shows a schematic diagram of a nanopillar. (b) In-plane magnetic hysteresis (δ) for Nb(300 nm)/Co-Fe-B(d_F)/Nb(300 nm) nanopillars before (black diamonds) and after (red circles) thermal annealing. The vertical error bars represent the statistical scatter of δ for multiple nanopillars on the same circuit. The black line is a least-squares regression-line fit for the nanopillars before thermal annealing, giving a volume saturation magnetization of (643 ± 21) emu cm⁻³ and a magnetically dead layer thickness at each Nb/Co-Fe-B interface of (0.33 ± 0.09) nm. (c) An estimate of the coercive field (H_c) of the nanopillars versus d_F and (d) the magnetic field periodicity (n) of $I_c(H)$ versus d_F before (black diamonds) and after (red circles) thermal annealing. All data at 1.6 K.

Fig. S4(b) within the Supplemental Material [19]]. Here, $\lambda = 110$ nm [24,25] is an estimate of the London penetration depth of polycrystalline Nb. M_s obtained here is smaller than the maximum bulk

magnetization of 1300 emu cm^{-3} [11,26], implying a reduced magnetization in thin ($<5 \text{ nm}$) Co-Fe-B and, possibly, partial oxidation or Ga implantation in nanopillars. For $d_F = 4.5 \text{ nm}$, the magnetization of Co-Fe-B switches at $\mu_0 H_c < M_s(d_F - d_{\text{dead}})/(2\lambda + d_F)$ and hence the maximum in J_c occurs at $\delta \approx \mu_0 H_c$, resulting in a spread in δ due to variations in H_c . The relatively large deviations of δ for $d_F = 3.5$ and 4.5 nm from the linear fit are likely due to the variation in M and potential magnetic inhomogeneity [21] in the nanopillars at low fields. A clear change in δ is not observed following thermal annealing, suggesting that the magnetization of Co-Fe-B in nanopillars is unaffected by annealing, consistent with our magnetization measurements of unpatterned films [see Fig. S2(a) within the Supplemental Material [19]]. We estimate H_c of the nanopillars from H where the hysteresis of the $I_c(H)$ curves closes to δ (see Fig. S5 within the Supplemental Material [19]). For the d_F range investigated in this study, $\mu_0 H_c \approx 10 \text{ mT}$ [see Fig. 1(c)], consistent with the fact that $\delta \approx \mu_0 H_c$ at $d_F = 4.5 \text{ nm}$. In Fig. 1(d), we plot the normalized magnetic field periodicity (n) of $I_c(H)$ versus d_F , where n is determined from $\text{sinc}(n\Phi/\Phi_0)$ with $\Phi = \mu_0 H L(2\lambda + d_F)$ and L is the length of the junction perpendicular to the applied magnetic field. For the d_F range investigated, $n \approx 1$, indicating homogeneous supercurrents across the device areas and the absence of an anomalous higher (second) harmonic current-phase relationship, which has been reported for Josephson junctions with ferromagnetic barriers at a $0-\pi$ phase transition [23,27,28].

In Fig. 2(a), we plot the total specific resistance of the nanopillars (AR_N) versus d_F at 1.6 K before and after thermal annealing. From a least-squares regression-line fit ($AR_N = \rho_F \times d_F + 2AR_{\text{Nb/Co-Fe-B}}$), we estimate an as-grown Co-Fe-B resistivity of $\rho_F = (88 \pm 46) \mu\Omega \text{ cm}$, which is higher than the resistivity of a $\text{Co}_{60}\text{Fe}_{40}$ polycrystalline ferromagnetic alloy ($\rho \approx 15 \mu\Omega \text{ cm}$ at 10 K [29]). We also estimate the specific resistances of the two Nb/Co-Fe-B interfaces as $2AR_{\text{Nb/Co-Fe-B}} = (4.4 \pm 1.4) f\Omega \text{ m}^2$. The effective electron mean free path in as-grown Co-Fe-B is $l = 3\pi^2 \hbar / k_F^2 e^2 \rho_F = (1.8 \pm 0.9) \text{ nm}$, where \hbar is the Planck constant divided by 2π , $k_F = 0.104 \text{ nm}^{-1}$ [30] is the Fermi wave number in the majority band of Co-Fe-B, and e is the elementary charge. We observe a decrease in AR_N for all the devices following thermal annealing, suggesting a decrease in ρ_F (and increase in the electron mean-free-path length) as a result of increased structural order. The increased degree of scatter in AR_N versus d_F for the nanopillars after thermal annealing is likely due to the variation of the resistance of Co-Fe-B and Nb/Co-Fe-B interfaces induced by annealing. Such a variation is likely due to the stochastic nature of nucleation of structural changes affecting the electronic band structure and the resistivity at the Nb/Co-Fe-B interfaces. We estimate $2AR_{\text{Nb/Co-Fe-B}} = (2.1 \pm 1.7) f\Omega \text{ m}^2$ for the nanopillars

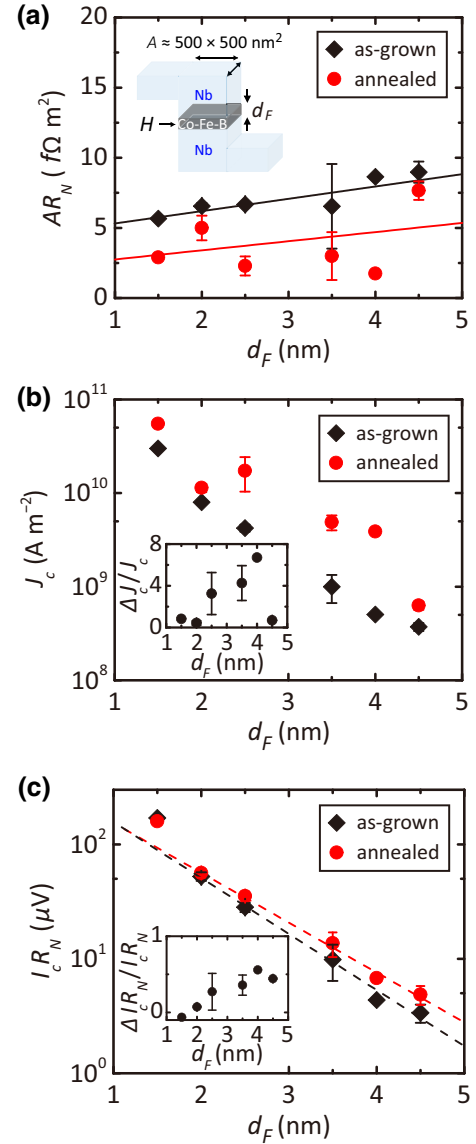


FIG. 2. (a) AR_N versus d_F before (black diamonds) and after (red circles) thermal annealing. The black line shows a least-squares regression-line fit for the nanopillars before annealing giving $\rho_F \approx (88 \pm 46) \mu\Omega \text{ cm}$ and $2AR_{\text{Nb/Co-Fe-B}} = (4.4 \pm 1.4) f\Omega \text{ m}^2$. For the annealed nanopillars, $\rho_F \approx (65 \pm 57) \mu\Omega \text{ cm}$ and $2AR_{\text{Nb/Co-Fe-B}} = (2.1 \pm 1.7) f\Omega \text{ m}^2$ from a least-squares regression-line fit (red line). (b) J_c versus d_F before (black diamonds) and after thermal annealing (red circles) at 400°C for 30 min . The inset shows the relative change in J_c following thermal annealing $[(J_{c,\text{annealed}} - J_{c,\text{as-grown}})/J_{c,\text{as-grown}}]$ versus d_F . (c) $I_c R_N$ versus d_F where the dashed lines are least-squares regression-line fits giving a coherence length in Co-Fe-B of $\xi_F = (0.93 \pm 0.02) \text{ nm}$ and $(1.00 \pm 0.04) \text{ nm}$, for the nanopillars before and after thermal annealing, respectively. The inset shows the relative change in $I_c R_N$ following thermal annealing $[(I_{cR_N,\text{annealed}} - I_{cR_N,\text{as-grown}})/I_{cR_N,\text{as-grown}}]$ versus d_F . The error bars in AR_N , J_c , and $I_c R_N$ represent the statistical scatter for multiple nanopillars. All data at 1.6 K .

after annealing from a least-squares regression-line fit, implying that the interface resistance is approximately halved after annealing.

The decrease in R_N through thermal annealing results in a notable enhancement of J_c [Fig. 2(b)]. An enhancement of J_c is observed for all nanopillars investigated. The relative J_c change following thermal annealing [defined as $(J_{c,\text{annealed}} - J_{c,\text{as-grown}})/J_{c,\text{as-grown}}$] is 80–700% depending on the Co-Fe-B thickness [see inset of Fig. 2(b)]. Since J_c is inversely proportional to $AR_N = \rho_F \times d_F + 2AR_{\text{Nb/Co-Fe-B}}$, the influence of the relative ρ_F change on the relative J_c change should become larger with increasing d_F . However, the relative J_c change does not show a clear d_F dependence, implying that the relative J_c change is predominated by the variation in $R_{\text{Nb/Co-Fe-B}}$ induced by thermal annealing.

To investigate the effect of thermal annealing on the coherence length of superconductivity in Co-Fe-B, in Fig. 2(c) we plot the characteristic voltage ($I_c R_N$) versus d_F at 1.6 K before and after thermal annealing. In superconductor-ferromagnet-superconductor Josephson devices, $I_c R_N$ typically oscillates with ferromagnetic barrier thickness due to $0-\pi$ phase transitions [23,31–35]. In our devices, $I_c R_N$ exponentially decays with d_F but we do not observe $0-\pi$ oscillations, implying that the periodicity of the oscillations is either much shorter or longer than the d_F range investigated. From the Fermi velocity ($v_F = 1.1 \times 10^6$ m s⁻¹ [30]) and the magnetic exchange energy of Co-Fe-B ($E_{\text{ex}} \approx k_B T_{\text{Curie}} = 113$ meV, where k_B is the Boltzmann constant and $T_{\text{Curie}} = 1313$ K [36]), an oscillation period is estimated to be $\pi v_F \hbar / 2E_{\text{ex}}$ [37] ≈ 11 nm, which is much longer than the d_F range and hence undetectable in this study. However, we note that there is a recent study demonstrating a $0-\pi$ oscillation of period 0.5 nm in Nb/Co₅₆Fe₂₄B₂₀/Nb [10] and such a short periodicity could be the reason for the apparent absence of the oscillation in our nanopillars.

The inset of Fig. 2(c) shows the relative change of $I_c R_N$ through thermal annealing [defined as $(I_c R_{N,\text{annealed}} - I_c R_{N,\text{as-grown}})/I_c R_{N,\text{as-grown}}$] increases with increasing d_F (i.e., the decay slope of $I_c R_N$ with d_F becomes shallower as a result of annealing). By fitting the decay slope to $I_c R_N \propto \exp(-\xi_F/d_F)$, the coherence length of superconductivity in Co-Fe-B (ξ_F) is estimated to be (0.93 ± 0.02) nm and (1.00 ± 0.04) nm for the devices before and after annealing, respectively. Considering that the magnetic moment of Co-Fe-B is unchanged following thermal annealing [see Fig. 1(b)], the enhancement of ξ_F is likely due to an increase in the electron mean free path of Co-Fe-B as a result of improved structural ordering, consistent with the decrease in R_N in Fig. 2(a).

In conclusion, we demonstrate Josephson coupling through Co-Fe-B alloy and its optimization with thermal annealing in Nb/Co-Fe-B/Nb nanopillars. We find

a notable enhancement of the Josephson critical current up to a maximum of 700% following thermal annealing at 400 °C, which is attributed to an increase in the proximity coherence length of superconductivity in Co-Fe-B and improved transparency at the Nb/Co-Fe-B interfaces. The thermal optimization of Josephson coupling following thermal annealing is attractive for the development of energy-efficient superconducting spintronic devices. Furthermore, electric current annealing treatments [38] on Josephson devices with Co-Fe-B could also tune device properties.

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