Wavelength Dependence of the Laser-Excitation Process on a Silicon Surface

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We report a first-principles calculation for the wavelength dependence of a laser-excitation process on a silicon surface. Although a lower-frequency laser is reflected by a lower-density plasma, it can penetrate a thicker plasma sheet. Therefore, the depth of the laser processing depends on the width of the plasma at the surface and laser wavelength. The time-dependent density-functional theory and Maxwell's equations are simultaneously employed to elucidate the effect of laser propagation on laser-matter interaction under ultrafast pulse lasers (FWHM: 12 fs). A longer-wavelength laser field facilitates deeper melting and ablation in silicon, despite a lower critical plasma density. Such a deeper excitation by a longer wavelength is because of the penetration of the laser field through the plasma on the surface. The plasma-formation depth is saturated at approximately half the wavelength in silicon.

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I. INTRODUCTION

Processing of solid-state materials using femtosecond laser pulses has attracted considerable interest because of their potential applications in high-precision processing technology [1-12].

In particular, a pulse with a duration of a few tens of femtoseconds (fs) enables the processing of dielectric surfaces without thermal damage because this duration is considerably shorter than the thermalization duration (ps or more) [10,13]. Moreover, the excitation of dielectrics by intense laser fields is employed in plasma optics such as plasma mirrors [8,14].

Many experimental and theoretical works on laser processing using near-infrared (NIR) lasers have been reported [15–20]. However, recently, the progress of laser technology has made intense mid-IR (MIR) lasers available [21,22]. As the photon energy of the IR laser is considerably lower than the dielectric bandgap, nonlinear excitation (multiphoton absorption and tunnel ionization) is a critical process. In general, a theoretical treatment for laser-electron nonlinear interaction is described by the rate equation that includes the electron excitation by the Keldysh theory [23], the avalanche effect, Joule heating, and the Drude model [2].

The time evolution of the laser field can be described by Maxwell's equations, considering the material properties through the constitutive relations. For ordinary light pulses, the response of the medium is linear in the electromagnetic field, and is characterized by linear susceptibilities. However, for intense and ultrashort laser pulses, conditions that require theoretical treatment beyond the linear response are encountered. If perturbative expansion is no longer useful, the time-dependent Schrodinger equation must be applied for electrons and solved in the time domain.

For a many-electron system, the time-dependent density-functional theory (TDDFT) [24] has been applied for laser-molecule and solid-state interaction [25,26]. We consider the TDDFT as the only ab initio quantum method applicable to strong electromagnetic fields in condensed media. In our previous work, we developed a formalism and computational method to describe the propagation of an intense electromagnetic field in a condensed medium, incorporating the electron dynamics feedback to the electromagnetic field [27-29]. In particular, in the case of processing with an MIR laser, the plasma frequency of the excited electron-hole pairs affects the dynamics of the electromagnetic field at lower plasma density because the plasma density easily reaches the frequency of an MIR laser. Although a lower-frequency laser is reflected by the plasma at the surface with a lower laser intensity, a wider plasma sheet must be formed to reflect the MIR laser. Therefore, we must clarify the relationship between the excitation depth and laser frequency to understand laser processing under various laser frequencies.

In this study, we present the first-principles simulation of the laser frequency and intensity dependence of the laser-excitation process on a silicon surface employing the above multiscale approach. We assume an ultrafast pulse laser (12 fs FWHM) in the MIR-NIR frequencies. We present the position dependence of the excitation energy and electron-hole density with various laser parameters to

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elucidate the laser-excitation process and plasma-mirror formation at the surface.

The remainder of this paper is organized as follows: in Sec. II, we describe our first-principles multiscale formalism to calculate the laser-matter interaction on the surface. In Sec. III, we present the numerical results. In Sec. IV, we summarize the study.

II. COMPUTATIONAL METHOD

As the theory and its implementation employed in the calculation herein are described elsewhere [27,28,30], we explain it in brief. The laser pulse that enters from a vacuum and attenuates in the medium varies on a micrometer scale, whereas the electron dynamics occur on a subnanometer scale. To overcome these conflicting spatial scales, we develop a multiscale implementation, introducing two coordinate systems: a macroscopic coordinate X for laser-pulse propagation and a microscopic coordinate r for the local electron dynamics. The laser pulse is described by the vector potential $\vec{A}_X(t)$, which satisfies

$$\frac{1}{c^2}\frac{\partial^2 \vec{A}_X(t)}{\partial t^2} - \frac{\partial^2 \vec{A}_X(t)}{\partial X^2} = -\frac{4\pi e^2}{c}\vec{J}_X(t).$$
(1)

At each point X, we consider the lattice-periodic electron dynamics driven by electric field $E_X(t) = -(1/c)dA_X(t)/dt$. They are described by the electron orbitals $\psi_{i,X}(\vec{r}, t)$, which satisfy the time-dependent Kohn-Sham equation

$$i\hbar\frac{\partial}{\partial t}\psi_{i,X}\left(\vec{r},t\right) = \left\{\frac{1}{2m}\left[-i\hbar\nabla_{r} + \frac{e}{c}\vec{A}_{X}\left(t\right)\right]^{2} - \phi_{X}\left(\vec{r},t\right) + \mu_{xc,X}\left(\vec{r},t\right)\right\}\psi_{i,X}\left(\vec{r},t\right),$$
(2)

where the potential $\phi_X(\vec{r}, t)$, which includes the Hartree and ionic contributions, and the exchange-correlation potential $\mu_{xc,X}(\vec{r}, t)$, are periodic in the lattice. The electric current $J_X(t)$ is provided from the electron orbitals:

$$J_X(t) = -\frac{e}{mV} \int_V d\vec{r} \sum_i \operatorname{Re} \psi_{i,X}^* \left[\vec{p} + \frac{e}{c} \vec{A}_X(t) \right] \psi_{i,X}$$
$$+ J_{X,\mathrm{nl}}(t), \qquad (3)$$

where V is the volume of a unit cell; $J_{X,nl}(t)$ is the current caused by the nonlocality of the pseudopotential.

We solve Eqs. (1)–(3) simultaneously as an initial value problem, where the incident laser pulse is prepared in a vacuum region on the top of the surface, while all the Kohn-Sham orbitals are set to their ground states. In this study, we use the modified Becke-Johnson exchange potential (MBJ) [31] specified in Ref. [32] [Eqs. (2)–(4)] with an local density approximation (LDA) correlation



FIG. 1. Real and imaginary parts of the dielectric function calculated by TDDFT with the MBJ potential.

potential [33] in the adiabatic approximation. The MBJ potential improves the bandgap, which is underestimated in conventional LDA. Figure 1 depicts the real and imaginary parts of the dielectric function calculated by TDDFT with the MBJ as a function of the photon energy. The calculated optical bandgap is 3.0 eV, which is an improvement compared to that obtained using the LDA (2.4 eV) [27], and it is approximately equal to the experimental value (3.4 eV) [34].

Our multiscale calculation uses a one-dimensional grid with a spacing of 250 a.u. for the propagation of laser electromagnetic fields. At each grid point, the electron dynamics are calculated using an atomic scale cubic unit cell containing eight silicon atoms, which are discretized into 24³ Cartesian grids. We discretize the Bloch momentum space into $8^3 k$ points. The dynamics of the 32 valence electrons are treated explicitly; the effects of the core electrons are considered through the pseudopotentials [35,36]. The electromagnetic fields as well as electrons are evolved with a common time step of 0.04 a.u. Note that we discretize the Bloch momentum space into $16^3 k$ points for the calculation of $\varepsilon(\omega)$ (Fig. 1) to obtain a smooth spectrum. For multiscale calculation, we use a sparse k grid because of the limitation of the computational resource. Although this calculation may not provide fully convergent results, we do not expect the truncation to affect the physical results by more than 10% [27].

The incident laser field $E_{in}(X, t)$ in vacuum is

$$E_{\rm in}(X,t) = \begin{cases} E_0 \sin^2\left(\pi \frac{t_X}{T_p}\right) \cos(\omega_0 t_X) & 0 < t_X < T_p \\ 0 & T_p < t_X < T_e, \end{cases}$$
(4)

where E_0 is the peak electric field amplitude, ω_0 is the laser frequency, and $t_X = t - X/c$ describes the spacetime dependence of the field. The pulse length T_p is set to 31.2 fs, and the computation is terminated at $T_e = 48.3$ fs.



FIG. 2. Time evolution of the electromagnetic field for a laser frequency of 0.4 eV at intensities of (a) 1×10^{12} , (b) 5×10^{12} , and (c) 1×10^{14} W/cm².

III. RESULTS AND DISCUSSION

Figure 2 shows the time evolution of the electromagnetic field of the pulse laser whose frequency is 0.4 eV, around the silicon surface. The initial field (0 fs) is denoted by a red-dashed line. The laser collides with the silicon surface exhibiting reflection and transmission; these are denoted by a green-dotted line (19 fs). The blue-solid line denotes the field after laser-silicon interaction. The laser frequency is set to 0.4 eV, and the laser intensities are set to 1×10^{12} [Fig. 2(a)], 5×10^{12} [Fig. 2(b)], and 1×10^{14} W/cm² [Fig. 2(c)], respectively. For the least intensity [Fig. 2(a)], the reflection and transmission occur as linear processes. Therefore, the laser field in the silicon (X > 0) at 36 fs (blue-solid line) shows a profile similar to that of the incident field (red-dashed line for X < 0).

The reflectivity is defined by

$$R = \frac{\int_{-\infty}^{0} dX |E(X, t = T_e)|^2}{\int_{-\infty}^{0} dX |E_{\rm in}(X, t = 0)|^2},$$
(5)

where *E* is the electric field associated with the pulse. *R* is approximately 0.299, which is consistent with the reflectivity (0.30) calculated using the dielectric function [$\varepsilon(\omega = 0.4) = 11.5$]. Meanwhile, as the laser intensity increases, the profile of the laser field in silicon is deformed to be



FIG. 3. Incident laser reflectivity at frequencies of 0.4 eV (red circle), 0.775 eV (green triangle), and 1.55 eV (blue square), respectively, as a function of the incident laser intensity.

rectangular and the reflectivity increases because photoabsorption occurs dominantly around the pulse peak. Reflection by the electron-hole plasma at the surface occurs, and it is considerable at the highest intensity.

The laser intensity and frequency dependence of the reflectivity are depicted in Fig. 3. We assume three different frequencies: 0.4, 0.775, and 1.55 eV. In general, the dielectric function $\varepsilon(\omega)$ is modulated by the plasma response. The reflectivity is minimized when the screened plasma frequency at the surface coincides with the laser frequency. A dip in the reflectivity can be observed at intensities of 3×10^{12} , 5×10^{12} , and 7×10^{12} W/cm², for $\omega_0 = 0.4$, 0.775, and 1.55 eV, respectively. Above these critical intensities, the reflectivity increases up to 0.77 at the maximum intensity because of the metallic response of the plasma.

The laser-intensity dependencies of the reflectivity for each frequency exhibit qualitative differences. The increase in reflectivity becomes more moderate for lower frequencies, above the critical intensity. In all frequencies, the reflectivity shows the linearly dependence on log(In), where In is the laser intensity, around 2×10^{13} W/cm². Table I shows the reflectivities at 1×10^{13} and 5×10^{13} W/cm². The change of the reflectivity between 1×10^{13} and 5×10^{13} W/cm² is larger at higher laser frequency.

TABLE I. Reflectivity at laser intensities of 1×10^{13} and 5×10^{13} W/cm² with each frequency.

$\hbar\omega$ (eV)	$1 \times 10^{13} \text{ W/cm}^2$	$5 \times 10^{13} \text{ W/cm}^2$	Difference
0.4	0.35	0.575	0.225
0.775	0.33	0.625	0.295
1.55	0.33	0.655	0.325



FIG. 4. Laser-intensity dependence of the deposited energy $E_{ab}(X)$ at (a) 0.4, (b) 0.775, and (c) 1.55 eV.

The deposited energy per silicon atom is shown in Fig. 4 as a function of the depth from the surface. We compute the energy transfer to the medium from the electromagnetic side because calculation using the Kohn-Sham densities requires an explicit energy density functional for the MBJ potential. The energy transfer rate W is given by $W = -\vec{E} \cdot \vec{J}$, where E is the electric field associated with the pulse. The deposited energy density is given by $E_{ab}(X) = -\int dt W_X(t)$.

The two dashed-black lines denote the melting and cohesive energy of silicon. For laser processing, the melting energy is an important index, whereas, the cohesive energy indicates the ablation threshold [28]. In the case of melting, the time scale may be longer than that of the ablation. Then, the diffusion of the energy is also important. Our results clearly indicate that lower-frequency laser can excite silicon more deeply; this is not surprising, if we consider the propagation of the long wavelength, although a shallower excitation depth is expected for lower frequency because a higher multiphoton process is needed for the electron excitation process at lower frequency, because multiphoton process is a highly nonlinear process and sensitive to the laser intensity. The longer-wavelength light field can penetrate the thin plasma at the surface, when the thickness of the plasma sheet is considerably smaller than the wavelength in silicon.

From Fig. 3, the plasma functions as a mirror, above the critical intensities. However, the quality of the plasma mirror depends on the laser frequency. To elucidate the functioning of the plasma sheet as a mirror, and laser penetration into the plasma sheet, we depict the positiondependent electron-hole density (N_e) in Fig. 5. The laserintensity dependencies of N_e as a function of the position from the surface are shown in Figs. 5(a)-5(c). N_e is defined as the projection of $\psi_{i,X}$ to the ground states at the same vector potential ($\Phi_{i,X}$):

$$N_{e}(X) = \frac{1}{V} \sum_{ii'=\text{occ}} \left(\delta_{ii'} - |\langle \Phi_{i,X} | \psi_{i',X}(t=T_{e}) \rangle|^{2} \right), \quad (6)$$

at the end of the time evolution. We scale N_e using the critical density for the screened plasma:

$$N_{\rm cr} \equiv \frac{\omega_0^2 m^* \varepsilon(\omega_0)}{4\pi e^2},\tag{7}$$

where $m^* = 0.3m$ is the effective mass, $\varepsilon(\omega_0)$ is the dielectric function at frequency of ω_0 . $N_{\rm cr}$ is 0.008/atom for 0.4 eV, 0.033/atom for 0.775 eV, and 0.15/atom for 1.55 eV. Figure 5 shows the critical depth (X_{cr}) defined by the position $N_e(X_{cr}) = N_{cr}$ as a function of the laser intensity. Around the critical intensity, X_{cr} corresponds to the surface $(X \sim 0)$ at all the frequencies. It should be noted that N_e should be defined in the absence of an electric field because it modulates the ground state. In our calculation, the veryweak light field induced by the spontaneous oscillation of $J_X(t)$ renders N_e larger than the ideal value. In particular, in the case of 0.4 eV, whose $N_{\rm cr}$ is very small and the critical depth is large, X_{cr} is considered as the reference because the number of excited electron is affected by the tail of the laser pulse. However, our results provide sufficient accuracy for $X_{\rm cr}$ to discuss the plasma thickness [27].

With the increase in laser intensity, X_{cr} increases rapidly, immediately above the critical intensities (Fig. 5). However, X_{cr} is saturated at approximately 500 nm for 0.4 eV, 200 nm for 0.775 eV, and 100 nm for 1.55 eV. The wavelength in the material, λ_m , can be expressed as $\lambda_m = \lambda / \sqrt{\varepsilon(\omega)}$ below the optical band gap. Here λ is the wavelength in vacuum. In the case of silicon, $\sqrt{\varepsilon(\omega)} \sim 4$ [37]. Actually, in our calculation, ε is smaller than the experimental results, and is $\sqrt{\varepsilon(\omega)} \sim 3.6$. Therefore, the wavelength in the silicon is about quarter of λ . The saturated positions (X_{cr}^{sat}) correspond to half the wavelength in silicon (dashed lines) for all the frequencies. These results demonstrate that the functioning of the plasma mirror is inadequate until the plasma thickness increases sufficiently. The saturation of the reflectivity shown in Fig. 3 and $X_{\rm cr}$ (Fig. 5) indicate that the plasma reflection is saturated, when X_{cr} becomes quarter of the wavelength in silicon, in the case of 1.55 and 0.775 eV. After the plasma reflection is saturated, the thickness of the plasma accesses the X_{cr}^{sat} value.



FIG. 5. Laser-intensity dependence of the number of excited electrons $[N_e(X)]$ scaled by the critical electron number (N_{cr}) at laser frequencies of (a) 0.4 eV, (b) 0.775 eV, and (c) 1.55 eV. (d) Critical depth $N_e(X_{cr}) = N_{cr}$ for each frequency. The dashed lines indicate half of the wavelength for each frequency in silicon.

IV. CONCLUSION

In summary, a first-principles simulation of the laserintensity dependence on the processing of the silicon surface is presented in this study. The obtained results indicate that low-frequency (long-wavelength) laser can excite deeper layers. The frequency dependence of the laser-processing depth is attributed to the ratio between the thickness of the plasma sheet formed at the surface. The functioning of the formed plasma as a mirror is inadequate, until the thickness of the plasma becomes comparable to quarter of the wavelength in silicon. In particular, the thickness of the plasma accesses half the wavelength in silicon with an increase in laser intensity. It may be possible to optimize the characteristic depth of ablation and/or the melting of silicon using lasers of various frequencies. The wavelength dependence of the quality of the plasma mirror provides crucial insights for plasma optics.

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