# Interlayer Exchange Coupling in Magnetic Hard-Soft Bilayered Structures

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Broadband ferromagnetic resonance (FMR) and high-temperature (*T*) FMR measurements are carried out to study interlayer exchange coupling (IEC) in a magnetic hard-soft bilayered system where the hard layer is a FePt thin film with strong perpendicular anisotropy and the soft layer is a thin film made of Fe, Co, or their alloys. The data indicate that the effective exchange field ( $H_{ex}$ ) produced by the IEC on the soft layer increases with a decrease in the thickness or saturation induction ( $4\pi M_s$ ) of the soft layer. With an increase in *T*,  $H_{ex}$  drops by an amount larger than  $4\pi M_s$ . The effective damping constant of the soft layer increases with  $H_{ex}$  and can vary by two orders of magnitude. In samples with  $H_{ex} > 4\pi M_s$ , the damping constant is insensitive to the choice of material of the soft layer. In samples with  $H_{ex} < 4\pi M_s$ , the damping constant strongly depends on the choice of material. When *T* is increased from room temperature to the Curie temperature of the hard layer, the FMR linewidth drops significantly in samples where  $H_{ex}$  is relatively large, but remains constant or even increases slightly at high *T* in samples where  $H_{ex}$  is very small. The effects of  $H_{ex}$  on the damping and linewidth can be understood by considering two distinct components in the overall damping, an intrinsic component mainly due to spin-flip magnon-electron scattering and an extrinsic component due to IEC-associated spin pumping at the interface.

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## I. INTRODUCTION

Bilayered systems that consist of a hard magnetic layer and a soft magnetic layer are of great interest. On one hand, it is fundamentally interesting to understand how the magnetic properties of one layer are influenced by the other layer via direct exchange coupling at the interface. On the other hand, the fact that the soft layer can significantly ease the magnetization reversal in the hard layer through a socalled exchange spring mechanism [1,2] makes the hardsoft bilayered structure a very attractive material system for energy-efficient, high-density data storage applications [3,4].

Despite the fundamental and technological importance of the hard-soft bilayered system, systematic experimental studies on how to control the interlayer exchange coupling (IEC) and how the IEC affects the dynamics in each layer are limited. This article reports on the IEC in a bilayered structure where the hard layer is a  $L1_0$ -ordered FePt thin film with strong perpendicular magnetic anisotropy (PMA) and the soft layer is a thin film made of ferromagnetic transition metals (FTM) Fe, Co, or their alloys. Comprehensive ferromagnetic resonance (FMR) studies are carried out on this bilayered system to explore (1) how the IEC-produced effective exchange field ( $H_{ex}$ ) on the soft layer varies with the soft layer thickness, the material choice of the soft layer, and the temperature and (2) how  $H_{ex}$  affects the FMR linewidth and damping of the soft layer.

The key results are as follows. First, the effective exchange field  $(H_{ex})$  on the soft layer increases with a decrease in the soft layer thickness (d). There exists a critical thickness below which one has  $H_{ex} > 4\pi M_s$  and above which one has  $H_{ex} < 4\pi M_s$ , where  $M_s$  denotes the saturation magnetization of the soft layer and  $4\pi M_s$  is the saturation induction. The critical thickness for this transition depends on the material of the soft layer and generally increases with a decrease in  $4\pi M_s$ . These results are consistent with the general expectation of  $H_{\text{ex}} \propto (M_s \cdot d)^{-1}$ . Second, when the temperature (T) is increased toward the Curie temperature  $(T_c)$  of the hard layer,  $H_{ex}$  drops by an amount larger than  $4\pi M_s$ , mainly because  $T_c$  of the hard layer is lower than that of the soft layer. Third, the damping of the soft layer increases with  $H_{ex}$ . By varying  $H_{ex}$ , the effective Gilbert damping constant ( $\alpha_{eff}$ ) can be tuned over two orders of magnitude, from 0.0055 to 0.552. Fourth, the damping of the soft layer is relatively insensitive to the choice of the material in the " $H_{ex} > 4\pi M_s$ " regime, but strongly depends on the material in the " $H_{ex} < 4\pi M_s$ " regime. Finally, with an increase in T, the FMR linewidth of the soft layer decreases substantially in structures with relatively large  $H_{ex}$ , but remains constant in structures with very small  $H_{ex}$ . The last three results can be understood in

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terms of the relative contributions of the intrinsic damping and the spin pumping to the overall damping. Here, spin pumping refers to the process in which the magnetization precession in the soft layer pumps a spin current to the hard layer, in a manner similar to the spin pumping effect in ferromagnet-normal metal heterostructures [5–8].

Four important points should be mentioned. (1) The hard-soft FePt/FTM system studied in this work is of great technological interest [9–12]. This is because this system has been widely accepted as the media material for next-generation heat-assisted magnetic recording (HAMR) drives [13]. (2) The conclusions from this work are of a general nature and can be applied to many other hard-soft bilayered systems, although they are drawn from a particular FePt/FTM system. (3) Although this study does not address how the IEC varies with the properties of and affects the damping in the hard layer, this question is equally important and is worthy of being explored in the future. (4) The discussions below focus on the effective exchange field  $H_{ex}$ , which is produced by IEC. Future studies that characterize and measure IEC in bilayered systems using other parameters, such as an exchange length and an effective exchange constant, are of great interest.

### **II. MEASUREMENT SAMPLES**

This study uses of twenty FePt/FTM samples, which are prepared by dc sputtering under the exact same conditions. The hard layers, grown on glass substrates, are the same in all twenty samples. They are 10-nm thick  $L_{10}$ -ordered FePt granular films with the segregants at the grain boundaries made of C and SiO<sub>2</sub>. However, the soft layers, which are grown directly on top of the hard layers, are all different. They are either made of different materials or are made of the same material but with different thicknesses. Table I lists the main properties of the soft FTM layers; the thicknesses are nominal values estimated on the basis of the sputtering growth rate, and the  $4\pi M_s$  values are all literature values [14]. To protect the soft FTM layers from oxidation, all samples are capped with a 3-nm thick carbon layer. The samples for the FMR measurements are all circular, with a diameter of about 2 mm.

The structural properties of the samples are characterized by XRD, TEM, and EELS techniques. The XRD and

TABLE I. Properties of the FTM layers in hard-soft FePt/FTM bilayered samples.

Material	Thickness (nm)	$4\pi M_s$ (kG)
Fe	2.7, 3.3, 4.0, 4.7	20.7
$Fe_{60}Co_{40}$	3.2, 4.3, 5.8	23.8
Fe <sub>40</sub> Co <sub>60</sub>	2.9, 4.3, 5.8, 7.2	23.0
$Fe_{10}Co_{90}$	3.2, 4.3, 5.8	19.2
Co	3.2, 4.3, 5.8	17.7
Co <sub>95</sub> Nd <sub>5</sub>	4.3, 5.8, 7.2	-



FIG. 1. Cross-section TEM images of FePt/Co bilayered samples. (a) Image of a FePt/Co(3.2 nm) sample. (b) Image of a FePt/Co(5.8 nm) sample.

TEM data confirm the  $L1_0$  phase of the FePt films, as discussed in Ref. [15]. Note that the FePt films in the samples studied here show structural properties very similar to those of sample S8 in Ref. [15]. Figure 1 shows representative cross-section TEM images obtained on the FePt/Co bilayered samples. The images clearly show the granular nature of the hard FePt layer and the continuous, nongranular nature of the soft Co layer. One can also see that the FePt/Co interfaces are not smooth, which makes the use of TEM analyses to accurately determine the thickness values of the soft Co layers impossible. This is why Table I lists the nominal thickness values. It is for the same reason that Table I gives the literature  $4\pi M_s$  values; the determination of the actual  $4\pi M_s$  values needs to take into account the film thickness and thus carries forward the errors in the film thickness estimation.

The static magnetic properties of the samples are measured by polar magneto-optical Kerr effect (MOKE) techniques; the detailed data are presented in the Appendix section. The magnetic hysteresis loops all look clean and smooth and show almost 100% remanence at zero fields. No two-stage switching is observed. These results show that the hard FePt layers have perpendicular anisotropy and the soft FTM layers are tightly coupled to the FePt layers. The MOKE data also show that for a given soft material, the coercivity of the bilayered sample decreases with an increase in the thickness of the soft layer and for a given soft layer thickness, the coercivity varies with the choice of the soft material. These results are consistent with the general expectation on the roles of the soft layer in the switching of the hard layer in a hard-soft bilayered system.

## **III. BROADBAND FMR APPROACH**

The FMR measurements include (1) frequency-dependent FMR measurements using a coplanar waveguide (CPW) and a vector network analyzer (VNA) at room temperature [16,17] and (2) temperature-dependent FMR measurements using a microwave cavity [18]. Figure 2 shows the experimental configuration and representative data for frequency-dependent FMR measurements. Figure 2(a) sketches the experimental setup, which mainly consists of a CPW device and a VNA. The CPW has a 50- $\mu$ m wide signal line, a signal line-to-ground spacing of 25  $\mu$ m, and a nominal impedance of 50  $\Omega$ . The sample is placed on the CPW with the soft layer side facing the CPW structure and the substrate side facing up. An external static magnetic field (*H*) is applied perpendicular to the sample plane to either magnetize the sample to saturation or enable FMR measurements. The measurement and data analysis procedures involve the following major steps:

(1) Magnetize the sample with a large magnetic field. For the data shown below, this field is 80 kOe.

(2) Measure the complex transmission coefficient  $S_{21}$  of the CPW/sample structure as a function of H at a fixed microwave frequency (f). Note that the field in this process is significantly smaller than that in (1). Figure 2(b)

presents representative  $S_{21}$  data, which are obtained at f=29 GHz with a sample where the soft layer is made of a 4.3-nm thick Co<sub>60</sub>Fe<sub>40</sub> film. The data show a clear resonance response, which corresponds to the FMR of the soft layer. The FMR of the hard layer is at a significantly higher frequency at room temperature due to the strong PMA field in the hard layer [19].

(3) Numerically fit the real and imaginary parts of  $S_{21}$  with theoretical  $S_{21}$  profiles [20,21] to determine the FMR field ( $H_{\text{FMR}}$ ) and the FMR linewidth ( $\Delta H$ ). The red curves in Fig. 2(b) show such numerical fits.

(4) Repeat steps (1)–(3) for different microwave frequencies.

(5) Plot  $H_{\text{FMR}}$  vs f and then fit the data, as shown in Fig. 2(c), using

$$f = |\gamma|(H_{\rm FMR} + H_{\rm eff}), \qquad (1)$$

where  $|\gamma|$  is the absolute gyromagnetic ratio and  $H_{\text{eff}}$  is the effective internal field and can be written as

$$H_{\rm eff} = H_{\rm ex} - 4\pi M_s, \tag{2}$$



FIG. 2. Broadband FMR measurements. (a) Experimental configuration. (b)-(d) Representative data measured on a FePt/Co<sub>60</sub>Fe<sub>40</sub>(4.3 nm) bilayered sample. (b) The real and imaginary parts of the complex transmission coefficient  $S_{21}$  of the CPW/sample structure measured as a function of the magnetic field at a microwave frequency (f) of 29 GHz. The dots show the data, while the red curves show numerical fits to theoretical  $S_{21}$  profiles. (c) FMR field vs f. The blue dots present the data, while the red line is a numerical fit to Eq. (1). The fitting yields the absolute gyromagnetic ratio  $|\gamma|$  and the effective internal field  $H_{\text{eff}}$  as indicated. (d) FMR linewidth vs f. The blue dots present the data, while the red line is a fit to Eq. (3). The fitting yields the effective Gilbert damping constant  $\alpha_{\text{eff}}$  and the inhomogeneity line broadening contribution  $\Delta H_0$  as indicated.

where  $4\pi M_s$  is the saturation induction of the soft layer. Note that both  $|\gamma|$  and  $H_{\text{eff}}$  are the fitting parameters and for the fit shown in Fig. 2(c), the corresponding values are indicated in the figure.

(6) Plot  $\Delta H$  vs f and then fit the data, as shown in Fig. 2(d), using

$$\Delta H = \frac{2\alpha_{\rm eff}}{|\gamma|} f + \Delta H_0, \tag{3}$$

where  $\Delta H_0$  is not associated with the damping but denotes the spatial sample inhomogeneity caused line broadening.  $\alpha_{\text{eff}}$  and  $\Delta H_0$  are the fitting parameters. The corresponding values for the fit in Fig. 2(d) are indicated in the figure. Note that  $\alpha_{\text{eff}}$  describes the effective damping of the soft layer rather than the overall damping of the entire bilayered system, because the measured resonance is from the FMR in the soft layer, as mentioned above.

### IV. RESULTS FROM BROADBAND FMR MEASUREMENTS

Figure 3 presents the data obtained through the abovedescribed procedure. Figure 3(a) gives the effective internal field ( $H_{\text{eff}}$ ) vs soft layer thickness (d) data. The data show a clear trend,  $H_{\text{eff}}$  increases with a decrease in d. If one considers Eq. (2) and the fact that  $4\pi M_s$  is usually independent of d, it can be concluded that  $H_{\text{ex}}$  is higher in samples with thinner soft layers. Note that although  $4\pi M_s$ is an intrinsic property of a magnetic material, it may be possible that in ultrathin films  $4\pi M_s$  decreases slightly with a decrease in d due to interfacial diffusion or surface oxidation. However, such a change in  $4\pi M_s$ , if any, should be relatively small, and it alone cannot account for the large  $H_{\text{eff}}$  variations shown in Fig. 3(a).

The data in Fig. 3(a) show four important results. (1)  $H_{\text{ex}}$  increases with a decrease in *d*, as mentioned above. (2) There exists a critical thickness  $(d_c)$ . If  $d > d_c$ ,  $H_{\text{eff}}$  is negative and one has  $H_{\text{ex}} < 4\pi M_s$ . If  $d < d_c$ ,  $H_{\text{eff}}$  is positive and one has  $H_{\text{ex}} > 4\pi M_s$ . (3)  $d_c$  strongly depends on the choice of material of the soft layer; except for the samples with the Fe soft layers, the  $d_c$  value generally increases with a decrease in  $4\pi M_s$ . (4) For a given soft layer thickness, the Fe samples show  $H_{ex}$  significantly larger than that of other samples. Note that the " $H_{ex} > 4\pi M_s$ " regime corresponds to the situation in which  $H_{ex}$  overcomes the demagnetization field in the soft FTM layer, leading to perpendicular orientation of the FTM magnetization in the absence of an external field. In contrast, in the " $H_{ex} < 4\pi M_s$ " regime, the dipolar interactions in the soft FTM layer dominate over  $H_{ex}$ , giving rise to in-plane orientation of the FTM magnetization in the absence of an external field.

The first three results discussed above are consistent with the general expectation of  $H_{ex} \propto (M_s \cdot d)^{-1}$  in hard-soft bilayered systems [22]. The reason for the last result is currently unknown. One possible reason is that the first atomic layer of the Fe film near the interface may also serve as the top atomic layer of the FePt film, resulting in a rather strong IEC and large  $H_{ex}$ . Those results together clearly suggest that one can tune  $H_{ex}$  in hard-soft bilayered systems by either varying the soft layer thickness or using different materials for the soft layer.

Figure 3(b) presents the  $\alpha_{\text{eff}}$  vs *d* data. Two results are evident from the data. First, via varying the material and thickness of the soft layer,  $\alpha_{\text{eff}}$  can be tuned over two orders of magnitude, with the lowest value being 0.0055 and the largest being 0.552. The physical mechanism that enables such a broad tuning range is discussed shortly.

Second, the data show a common trend -  $\alpha_{\text{eff}}$  increases with a decrease in *d*. This thickness dependence is relatively weak in the Fe sample, but is very strong in all other samples. For example, in the FePt/Fe<sub>40</sub>Co<sub>60</sub> sample,  $\alpha_{\text{eff}}$  increases by a factor of 43.8 when *d* is decreased from 5.8 to 2.9 nm. There are two possible reasons for the observed thickness dependence. First, the overall damping in a magnetic thin film may contain a contribution from two-magnon scattering [23–25] associated with surface roughness or defects on the surface or at the interface;



FIG. 3. Data from broadband FMR studies. (a) Effective internal field ( $H_{eff}$ ) vs soft layer thickness (d) for FePt/FTM bilayered samples where the soft FTM layers are made of different materials as indicated. (b) Effective Gilbert damping constant ( $\alpha_{eff}$ ) vs d for the same samples as for the data in (a). (c)  $\alpha_{eff}$  vs  $H_{eff}$ . The  $H_{eff}$  data are from (a), while the  $\alpha_{eff}$  data are from (b).

the weight of this contribution in the total damping is usually larger in thinner films. However, it seems that this mechanism alone cannot explain the rather big  $\alpha_{\text{eff}}$  changes shown in Fig. 2(b) if one takes into account that the two-magnon scattering is very weak in films magnetized perpendicularly [26,27]. Second, the observed thickness dependence may be associated mainly with the thickness dependence of  $H_{\text{ex}}$  since the data in Figs. 3(a) and 3(b) seem to show similar overall trends.

To clarify the above conjecture about the dominant physical mechanism for the strong thickness dependence shown in Fig. 3(b),  $\alpha_{\text{eff}}$  is plotted against  $H_{\text{eff}}$  in Fig. 3(c). One can clearly see that  $\alpha_{\text{eff}}$  increases with  $H_{\text{eff}}$ . This response suggests that  $\alpha_{\text{eff}}$  increases notably with  $H_{\text{ex}}$ and the d dependence shown in Fig. 3(b) is associated mainly with the change of  $H_{ex}$  with d, not the two-magnon scattering process. In addition, one can also see that the uppermost four data points over the 3-6 kOe field range show similar  $\alpha_{eff}$  values, while the left most five points in a relatively narrower field range show very different  $\alpha_{\rm eff}$  values, varying by a factor of 5. This result indicates that in the " $H_{ex} > 4\pi M_s$ " regime,  $\alpha_{eff}$  is insensitive to the choice of the material of the soft layer; in contrast, in the " $H_{\rm ex} < 4\pi M_s$ " regime,  $\alpha_{\rm eff}$  strongly depends on the choice of the material.

The above results about the damping can be understood by considering the presence of two distinct components in the overall damping constant, namely,

$$\alpha_{\rm eff} = \alpha_0 + \alpha_{\rm sp},\tag{4}$$

where  $\alpha_0$  denotes the intrinsic damping of the soft layer while  $\alpha_{sp}$  describes the extrinsic damping due to the pumping of spin by the precessional motion in the soft layer to the hard layer. As the spin pumping is associated with the exchange coupling of the moments in the soft layer to those in the hard layer,  $\alpha_{sp}$  increases with  $H_{ex}$ . This results in the increasing response shown in Fig. 3(c). As  $H_{ex}$  can be tuned over a wide range by varying the choice of the material and the thickness of the soft layer, as shown in Fig. 3(a),  $\alpha_{sp}$  can also be changed over a wide range, giving rise to the wide tuning range of the overall damping  $\alpha_{\rm eff}$  (two orders of magnitude) shown in Fig. 3(b). In the samples with large  $H_{ex}$ ,  $\alpha_{sp}$  can be significantly larger than  $\alpha_0$ , which explains the insensitivity of  $\alpha_{\rm eff}$  to the choice of the material shown by the uppermost four data points in Fig. 3(c). In contrast, in the samples with relatively low  $H_{\rm ex}$ ,  $\alpha_{\rm sp}$  is either comparable to or smaller than  $\alpha_0$ , giving rise to the strong dependence of  $\alpha_{\rm eff}$  on the choice of the material shown by the left most five data points in Fig. 3(c). Note that  $\alpha_0$  in ferromagnetic FTM thin films results mostly from spin-flip magnon-electron scattering (or interband scattering) and Fermi surface breathing-associated magnon-electron scattering (or intraband scattering), with the former being dominant at high temperatures while the latter is dominant at low temperatures [28–31]. Such scattering strongly depends on the properties of band structures in the material, so  $\alpha_0$  is usually material dependent. Note that magnon-photon scattering and eddy current can also contribute to the overall damping, but their contributions should be much smaller than the damping associated with the magnon-electron scattering in the samples studied in this work.

It should be highlighted that, as shown in Fig. 3(c), the  $\alpha_{\text{eff}}$  values of the three Fe samples seem to be off the trend. The actual reason for this is currently unknown, but it may share the same origin as the unusual  $H_{\text{ex}}$  response of the Fe samples discussed above. Two points should be made about the  $\alpha_{\text{eff}}$  values of the Fe samples. First, they are all substantially larger than the literature  $\alpha_0$  value in Fe, which is about 0.002 [32]. This is likely associated with the presence of the very strong IEC in the Fe samples. Second, they show a  $H_{\text{eff}}$  dependence much weaker than the  $\alpha_{\text{eff}}$  values in other samples. This is probably because all three Fe samples are in the " $H_{\text{ex}} > 4\pi M_s$ " regime, while the other samples exhibit different  $H_{\text{ex}}$  strengths.

Three notes should be made about the above discussions on the data in Fig. 3. First, the FMR analysis processes described above take a small-damping approximation, namely,  $(\alpha_{\rm eff})^2 \ll 1$ . In the case where the damping is strong, " $(\alpha_{\text{eff}})^2 \ll 1$ " is not true anymore and a full numerical analysis of the  $S_{21}$  data is needed. The uppermost four data points in Fig. 3(c) are obtained through the full analysis that does not use the small-damping approximation. Details about this analysis are provided in the Appendix section. Second, 20 samples are measured in the experiments, but Fig. 3(b) shows the data for 18 samples only. This is because only a few frequency points are obtained for the 4.7-nm-Fe sample and the 2.9-nm- $Fe_{40}Co_{60}$  sample due to experimental limitation. While the data are enough to reliably determine  $H_{\rm eff}$ , they do not provide enough information to calculate  $\alpha_{eff}$ . Third, it is known that  $\alpha_{sp}$  depends on the spin mixing conductance at the interface. Thus, it is expected that a change in the material of the soft layer should give rise to a change in the spin mixing conductance and a corresponding variation in  $\alpha_{\text{eff}}$ , but this effect seems to be weak because the data in Fig. 3(c) show that  $\alpha_{\text{eff}}$  does not notably vary with the choice of the material in the  $H_{\rm ex} > 4\pi M_s$  large- $\alpha_{\rm sp}$ regime.

### V. HIGH-T FMR APPROACH

The data presented above are all measured at room temperature. We now turn to the high-temperature (*T*) FMR measurements and analyses. Figure 4 shows the high-*T* FMR approach. Figure 4(a) shows a schematic diagram of the experimental system. The main components include a rectangular microwave cavity (purple), a diamond rod (yellow) with a diameter of 2 mm that loads the sample (red)



FIG. 4. High-temperature FMR measurements. (a) Schematic diagram of the experimental setup. (b) Representative FMR power absorption data (blue dots), a Lorentzian fit (red curve), and a Gaussian fit (green curve). The data are measured at T=373 °C on a FePt/Co(5.8 nm) bilayered sample. The Lorentzian fit yielded FMR field  $H_{\rm FMR}$  and peak-to-peak FMR linewidth  $\Delta H_{\rm pp}$  are indicated in (b).

into the cavity, and a ceramic heater (gray) that heats the sample through the diamond rod. These components are housed in a high-vacuum chamber and the measurements are performed at a pressure of about  $6.7 \times 10^{-3}$  Pa (or about  $5 \times 10^{-5}$  Torr) to prevent changes in sample properties due to oxygen during high-T measurements as well as to reduce temperature fluctuations during the FMR measurements. For the FMR data presented below, f is kept constant at 13.7 GHz, which is also the resonant frequency of the microwave cavity, while H is swept. Prior to placing the sample in the FMR system, the sample is magnetized by a perpendicular magnetic field of H = 80 kOe at room temperature. After placing the sample in the FMR system and heating it, prior to each FMR measurement, the sample is saturated by a field of H = 15 kOe. More details about this approach are provided in Ref. [18].

Figure 4(b) presents the FMR data (blue dots) measured at T = 373 °C on a sample where the soft layer is made of

a 5.8-nm thick Co film. The red curve shows a numerical fit to the derivative of a Lorentzian trial function. The Lorentzian fitting obtained FMR field ( $H_{\rm FMR}$ ) and peakto-peak FMR linewidth ( $\Delta H_{\rm pp}$ ) are indicated in the figure. Note that one has  $\Delta H_{\rm pp} = \Delta H/\sqrt{3}$ . A fit (green curve) to the derivative of a Gaussian trial function is also included in the figure. One can see that the Lorentzian fit is slightly better than the Gaussian fit, indicating that the inhomogeneity line broadening contribution to  $\Delta H_{\rm pp}$ , if any, is relatively small. In the case where a film sample has strong spatial inhomogeneity and the associated line broadening ( $\Delta H_0$ ) is large, the Gaussian function would fit the FMR data better than the Lorentzian function [33].

## VI. RESULTS FROM HIGH-T FMR MEASUREMENTS

The above-described high-*T* approach is used to study FMR in three samples whose soft layers are made of a 5.8-nm thick Co<sub>95</sub>Nd<sub>5</sub> film, a 7.2-nm thick Co<sub>95</sub>Nd<sub>5</sub> film, and a 5.8-nm thick Co film, respectively. These three samples are chosen because they show moderate  $\alpha_{\text{eff}}$  at room temperature, as shown in Fig. 3(b). The samples with larger  $\alpha_{\text{eff}}$  values show smaller signal-to-noise ratios in high-*T* FMR measurements. The measurements are carried out over a temperature range of T=25-600 °C. The measurement data are presented in Fig. 5.

Figure 5(a) gives  $H_{\text{eff}}$  as a function of *T*, where the  $H_{\text{eff}}$  data are calculated using Eq. (1) with the experimentally measured  $H_{\text{FMR}}$  data [see Fig. 4(b)] and a gyromagnetic ratio of  $|\gamma| = 2.8$  MHz/Oe. Two main results are evident from the data in Fig. 5(a). First, in all the samples,  $H_{\text{eff}}$  decreases with an increase in *T*. This result is most likely associated with the fact that the hard FePt layer has a Curie temperature of around  $T_c \approx 425 \text{ °C}$  [18] while the soft FTM layers usually have a much higher  $T_c$ . For example,  $T_c$  in bulk Co is about 1130 °C [34].  $T_c$  in Co thin films may be slightly lower than 1130 °C, but should be substantially



FIG. 5. Data from high-temperature FMR studies. (a) and (b) present the effective internal field  $(H_{\text{eff}})$  and the FMR linewidth  $(\Delta H_{\text{pp}})$ , respectively, as a function of temperature for three samples with different soft layers, as indicated. (c) Plots  $\Delta H_{\text{pp}}$  as a function of  $H_{\text{eff}}$ . The  $\Delta H_{\text{pp}}$  data are from (b), while the  $H_{\text{eff}}$  data are from (a).

higher than 425 °C [35]. Thanks to this difference in  $T_c$ ,  $4\pi M_s$  in the hard FePt layer drops faster than that in the soft FTM layer when T is increased toward 600 °C. The net effect is that with an increase in T,  $H_{ex}$  drops by a larger amount than the  $4\pi M_s$  of the FTM layer and  $H_{eff}$  decreases accordingly. Note that  $H_{ex}$  strongly depends on the magnetic moment in the hard FePt layer. Second, the 5.8-nm Co<sub>95</sub>Nd<sub>5</sub> sample shows larger  $H_{eff}$  values than the other two over the entire T range, indicating larger  $H_{ex}$  in this sample. This is because the soft FTM layer in this sample is thinner than in the 7.2-nm Co<sub>95</sub>Nd<sub>5</sub> sample and has a smaller  $4\pi M_s$  value than in the 5.8-nm Co sample. Thus, this result is generally consistent with the conclusion drawn from the data in Fig. 3(a).

Figure 5(b) presents the  $\Delta H_{pp}$  vs *T* data of the three samples. One can see that the *T* dependence of  $\Delta H_{pp}$ differs remarkably in the three samples.  $\Delta H_{pp}$  in the 5.8-nm Co<sub>95</sub>Nd<sub>5</sub> sample shows a rather strong *T* dependence.  $\Delta H_{pp}$  decreases by a factor of 5 when *T* is increased from 23 °C to 467 °C. In contrast,  $\Delta H_{pp}$  in the 7.2-nm Co<sub>95</sub>Nd<sub>5</sub> sample shows a much weaker *T* dependence and  $\Delta H_{pp}$  in the 5.8-nm Co sample is almost constant.

These results can be understood in terms of the *T* dependence of the two damping components in Eq. (4). Specifically, over the *T* range considered here,  $\alpha_0$  results mainly from spin-flip magnon-electron scattering. This scattering process requires both momentum and energy conservations, which can be satisfied more easily at high *T* [28–30]. As a result,  $\alpha_0$  is expected to increase with *T*. In contrast,  $\alpha_{sp}$  is expected to decrease with *T* because IEC is weaker and  $H_{ex}$  is smaller at higher *T* as suggested by the data presented in Fig. 5(a).

For the 5.8-nm Co<sub>95</sub>Nd<sub>5</sub> sample,  $H_{\text{eff}}$  is almost zero at room temperature, as shown in Fig. 5(a), indicating  $H_{\text{ex}} \approx 4\pi M_s$ . This means that IEC in this sample is relatively strong and  $\alpha_{\text{sp}}$  dominates over  $\alpha_0$  at room temperature. With an increase in *T*, IEC becomes weaker and  $\alpha_{\text{sp}}$ becomes smaller, giving rise to the large  $\Delta H_{\text{pp}}$  drop shown in Fig. 5(b).

The situation is completely different in the 5.8-nm Co sample. In this sample,  $H_{\text{eff}}$  is very small, as shown in Fig. 5(a). This indicates that IEC is relatively weak and  $\alpha_{\text{sp}}$  may be comparable with  $\alpha_0$ . With an increase in T,  $\alpha_{\text{sp}}$ decreases while  $\alpha_0$  increases, resulting in an overall flat response for  $\Delta H_{\text{pp}}$ , as shown in Fig. 5(b). When *T* is close to or higher than  $T_c$ ,  $\alpha_{\text{sp}}$  becomes so small that  $\alpha_0$  starts to become dominant. Since  $\alpha_0$  increases with *T* as discussed above,  $\Delta H_{\text{pp}}$  shows a slight increase over the *T* range of 500–600 °C.

In addition, the data in Fig. 5(b) also show that the three samples show comparable  $\Delta H_{pp}$  values near  $T_c$ , although they show very different  $\Delta H_{pp}$  values near room temperature. This observation supports the above interpretation. In brief, near room temperature,  $H_{ex}$  is very different in the three samples, resulting in very different  $\alpha_{sp}$  values and very different  $\Delta H_{\rm pp}$  values. Near  $T_c$ , IEC becomes absent in all the samples, resulting in negligible  $\alpha_{\rm sp}$  and comparable  $\Delta H_{\rm pp}$  values.

One can clearly see from the above discussions that IEC plays critical roles in the *T* dependence of the FMR linewidth. To further illustrate this,  $\Delta H_{pp}$  is plotted against  $H_{eff}$  in Fig. 5(c) in a way similar to the plot in Fig. 3(c). Note that both the changes of  $H_{ex}$  and  $4\pi M_s$  with *T* contribute to the variation of  $H_{eff}$ , but  $H_{ex}$  plays a bigger role due to the difference in  $T_c$  between the FePt and FTM layers, as discussed above. The plot surprisingly shows the same trend as the one in Fig. 3(c), even though the data here are measured at very different temperatures while all the data in Fig. 3(c) are measured at the same temperature, namely, room temperature. This consistency evidently confirms the above-discussed  $H_{ex}$ -damping correlation.

One can also see from the data in Fig. 5(c) that even though the overall trend is the increase of  $\Delta H_{\rm pp}$  with  $H_{\rm eff}$ , the slope varies notably with  $H_{\rm eff}$ . It is large in the relatively high  $H_{\rm eff}$  region and almost zero in the very low  $H_{\rm eff}$ region. This is consistent with the above interpretation of the  $\Delta H_{\rm pp}$  data presented in Fig. 5(b).

#### VII. CONCLUSIONS AND OUTLOOK

In summary, broadband FMR and high-temperature (T) FMR measurements are carried out to study IEC in a magnetic hard-soft bilayered system where the hard layer is a  $L1_0$ -ordered FePt thin film and the soft layer is a FTM thin film. The data indicate that the IEC-produced exchange field  $(H_{ex})$  on the soft layer strongly depends on the choice of material of the soft layer as well as the soft layer thickness. The thinner the soft layer is and the smaller  $4\pi M_s$  the soft layer has, the larger the field  $H_{ex}$  is. With an increase in T,  $H_{ex}$  drops by a larger amount than the  $4\pi M_s$  of the soft layer, resulting in an effective internal field that decreases with T. The IEC strongly affects the FMR linewidth and damping of the soft layer. The general trend is that both the FMR linewidth ( $\Delta H$ ) and the effective Gilbert damping constant ( $\alpha_{eff}$ ) increase with  $H_{ex}$ , but there are also several subtle effects associated with  $H_{ex}$ . In the  $H_{\rm ex} > 4\pi M_s$  regime,  $\alpha_{\rm eff}$  is insensitive to the choice of material of the soft layer. In the  $H_{ex} < 4\pi M_s$  regime, however,  $\alpha_{\rm eff}$  strongly depends on the choice of material. With an increase in T,  $\Delta H$  decreases substantially in samples where  $H_{ex}$  is relatively large, but remains constant or even increases slightly in samples where  $H_{ex}$  is very small.

Note that the wide tuning of IEC,  $H_{ex}$ , and  $\alpha_{eff}$  demonstrated in this work is realized through changes in the soft layer thickness and the material of the soft layer, but they can also be tuned through doping different impurities into the soft layer, controlling interface quality, or varying the properties of the hard layer. Future experimental studies on such tunability are of great interest.

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## APPENDIX

Figure 6 gives the magnetic hysteresis loops of hard-soft FePt/FTM bilayered samples measured by polar MOKE techniques. The thickness values of the soft FTM layers are indicated in the figure. The hysteresis loops all look clean and smooth and show almost 100% remanence at zero fields. No two-stage switching is observed. These results show that the hard FePt layers have perpendicular anisotropy and the soft FTM layers are tightly coupled to the FePt layers.

Figure 7 presents the coercivity values of the hardsoft FePt/FTM bilayered samples, which are determined according to the hysteresis loops given in Fig. 6. The data show that for a given soft material, the coercivity of the bilayered sample decreases with an increase in the thickness of the soft layer; for a given soft layer thickness, the coercivity varies with the choice of the soft material. These results are consistent with the general expectation on the roles of the soft layer in the switching of the hard layer in a hard-soft bilayered system.

The subsection below shows how to extract the FMR field and linewidth parameters in magnetic thin films with relatively large damping from broadband FMR measurement data. It is known that the power absorbed during an

FMR measurement is given by

$$P = -\frac{1}{2}\omega |h_0|^2 \operatorname{Im}(\chi), \qquad (A1)$$

where  $\omega$  is the angular frequency of the external microwave,  $h_0$  is the amplitude of the microwave field, and  $\chi$  is the magnetic susceptibility of the film.  $-\text{Im}(\chi)$  can be derived from the Gilbert equation in the usual manner

$$-\mathrm{Im}(\chi) = \frac{\frac{\omega_M}{4\pi} [\alpha \omega \omega_y^2 + \alpha \omega^3 (\alpha^2 + 1)]}{\left\{ \left[ (\omega_x \omega_y)^2 - \omega^2 (\alpha^2 + 1) \right]^2 + \alpha^2 \omega^2 (\omega_x + \omega_y)^2 \right\},}$$
(A2)

where  $\alpha$  is the Gilbert damping constant. There have been no assumptions based on the value of  $\alpha$ , whereas most previous works have utilized  $\alpha^2 \ll 1$ .  $\omega_M$  in Eq. (A2) is defined as

$$\omega_M = |\gamma| 4 \ \pi M_s, \tag{A3}$$

where  $|\gamma|$  is the absolute gyromagnetic ratio and is usually close to  $2\pi \times 2.8$  MHz/Oe. Because only the out-of-plane configuration is of interest here, one can write

$$\omega_x = \omega_y = |\gamma|(H_0 + H_{\text{eff}}), \tag{A4}$$

where  $H_{\text{eff}}$  is the effective internal field given by

$$H_{\rm eff} = H_{\rm ex} - 4\pi M_s. \tag{A5}$$

 $H_0$  in Eq. (A4) is the external static magnetic field applied perpendicular to the film plane. Following the previous methods for deriving an equation for the FMR linewidth,



FIG. 6. Magnetic hysteresis loops of hard-soft bilayered samples measured by polar MOKE techniques. The thicknesses of the soft layers are given in the figure.



FIG. 7. Coercivities of the hard-soft bilayered samples obtained from the hysteresis loops presented in Fig. 6.

the first step is to find the maximum power and then divide it by 2 to find the half maximum power. To do so, one evaluates

$$\left. \frac{\partial P}{\partial H_0} \right|_{\omega} = 0. \tag{A6}$$

Since the applied field is the quantity that is changing during the measurements, the frequency is considered to be fixed. The value of  $H_0$  that satisfies Eq. (A2) by making P a maximum is

$$H_{P\max} = \frac{\omega}{|\gamma|} \sqrt{2\sqrt{\alpha^2 + 1} - \alpha^2 - 1} - H_{\text{eff.}}$$
(A7)

In the limit of  $\alpha^2 \ll 1$ , the resonance condition for zero damping is recovered. The second step is to find  $H_0$  at both of the two half-maximum power values as well. To do this, one writes

$$\frac{1}{2}P(H_{P\max}) = P(H_0).$$
 (A8)

With Eq. (A1), Eq. (A8) can be rewritten as

$$\frac{1}{2} \operatorname{Im}[\chi(H_{P_{\max}})] = \operatorname{Im}[\chi(H_0)].$$
(A9)

Equation (A9) gives two solutions for  $H_0$ . One is for the half maximum on the left side of the peak, while the other is for the half maximum on the right side of the peak. The difference in these two will give the FMR linewidth  $\Delta H$ . Note that  $\Delta H$  is associated with the peak-to-peak linewidth by

$$\sqrt{3}\Delta H_{\rm pp} = \Delta H.$$
 (A10)

The above procedure gives rise to a linewidth as

$$\Delta H = G(\alpha) \frac{2(2\pi f)}{|\gamma|},\tag{A11}$$

where  $G(\alpha)$  is given by

$$G(\alpha) = x - y, \tag{A12}$$

$$y = \sqrt{\frac{\left(\alpha^{2} - \sqrt{\alpha^{2} + 1} + 1\right)^{2} - \frac{\alpha^{2}}{4}(\alpha^{2} + 1) + \sqrt{\alpha^{2} + 1}(\alpha^{2} - \sqrt{\alpha^{2} + 1} + 1) + \frac{\alpha}{4}\sqrt{\alpha^{2} + 1} - \frac{\alpha^{3}}{4}\sqrt{\alpha^{2} + 1}(\alpha^{2} - \sqrt{\alpha^{2} + 1} + 1) + \frac{\alpha}{4}\sqrt{\alpha^{2} + 1}}{\alpha\sqrt{\alpha^{2} + 1}},$$

ī.

The equation used to fit the real and imaginary parts of the experimentally measured complex transmission coefficient  $S_{21}$  can be written as

$$S_{21} = S_{21}^0 + DH_0 + \frac{\chi}{\chi_0}, \tag{A13}$$

where the first term on the right side describes the electronic background, the second denotes the linear electronic drift during the sweeping of the field, and  $\chi_0$  is the usual fitting parameter that has experimental parameters built in. Each term in Eq. (A13) has

a real part and an imaginary part associated with it, namely,

$$S_{21}^{0} = \operatorname{Re}(S_{21}^{0}) + i\operatorname{Im}(S_{21}^{0}), \qquad (A14)$$

$$DH_0 = \operatorname{Re}(DH_0) + i\operatorname{Im}(DH_0), \qquad (A15)$$

$$\frac{\chi}{\chi_0} = \operatorname{Re}\left(\frac{\chi}{\chi_0}\right) + i\operatorname{Im}\left(\frac{\chi}{\chi_0}\right), \qquad (A16)$$

where  $\chi = \chi_R + i\chi_I$  and  $\chi_0 = \chi_{0R} + i\chi_{0I}$  so that

$$\frac{\chi}{\chi_0} = \frac{1}{\chi_{0R}^2 + \chi_{0I}^2} [(\chi_{0R}\chi_R + \chi_{0I}\chi_I) - i(\chi_{0R}\chi_I + \chi_{0I}\chi_R)].$$
(A17)

The imaginary part  $\chi_I$  was given earlier for finding the linewidth. The real part is

$$\chi_R = \frac{\frac{\omega_M}{4\pi} [\omega_y^3 + \omega_y \omega^2 (\alpha^2 - 1)]}{\{[\omega_y^2 - \omega^2 (\alpha^2 + 1)]^2 + 4\alpha^2 \omega^2 \omega_y^2\}}.$$
 (A18)

The parameters  $S_{21}^0$ , *D*, and  $\chi_0$  have physical information about the VNA FMR setup and the sample built in and must be determined through the fitting of the  $S_{21}$  profiles.

The Gilbert damping constant  $\alpha$  can be obtained by fitting the  $S_{21}$  profiles with Eq. (A13). By repeating this process for the  $S_{21}$  data measured at different frequencies, one obtains the damping constants at different frequencies. The results usually show that the damping constant decreases with an increase in the frequency, but the Gilbert damping constant is known to be frequency independent. This apparent change is actually due to spatial film inhomogeneity caused FMR linewidth broadening. To reconcile this problem, Eq. (A11) is used to calculate a FMR linewidth from the damping constant at each frequency. The real damping constant can then be obtained by fitting the linewidth vs frequency data using

$$\Delta H = G(\alpha) \frac{2(2\pi f)}{|\gamma|} + \Delta H_{\rm ILB}, \qquad (A19)$$

where  $\Delta H_{\rm ILB}$  denotes the contribution from the film inhomogeneity line broadening and is frequency independent. This fitting yields the true Gilbert damping constant, which does not change with frequency. Thus, the procedure for the determination of the Gilbert damping constant  $\alpha$  in thin films with relatively large  $\alpha$  includes the following major steps:

(1) Measure  $S_{21}$  as a function of the field at a fixed frequency.

(2) Fit the  $S_{21}$  profiles with Eq. (A13) to determine the  $\alpha$  value.

(3) Use the  $\alpha$  value and Eq. (A11) to calculate the FMR linewidth  $\Delta H$ .

(4) Repeat steps (1)–(3) for different frequencies.

(5) Plot the FMR linewidth  $\Delta H$  as a function of the frequency and then fit the data with Eq. (A19) to obtain the true  $\alpha$ .

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