# Higher order mode damper for low energy RHIC electron cooler superconducting radio frequency booster cavity

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To improve RHIC luminosity for heavy ion beam energies below 10  $GeV/nucleon$ , the Low Energy RHIC electron Cooler (LEReC) is currently under commissioning at BNL. The linac of LEReC is designed to deliver a 1.6–2.6 MeV electron beam, with rms  $dp/p$  less than  $5 \times 10^{-4}$ . A 704 MHz superconducting radio frequency booster cavity in this linac provides up to 2.2 MeV accelerating voltage. With such a low energy and very demanding energy spread requirement, control of higher order modes (HOMs) in the cavities becomes critical and needs to be carefully evaluated to ensure minimum impact on the beam. In this paper, we report the multiphysics design of the HOM damper for this cavity to meet the energy spread requirement, as well as experimental results of the cavity with and without the HOM damper.

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### I. INTRODUCTION

To map the QCD phase diagram, especially to search for the QCD critical point using the Relativistic Heavy Ion Collider (RHIC), a significant luminosity improvement at energies below  $10 \text{ GeV/nucleon}$  is required. This can be achieved with the help of an electron cooling upgrade called the Low Energy RHIC electron Cooler (LEReC) [\[1\]](#page-8-0).

The electron accelerator for the LEReC consists of a dc photoemission gun and a 704 MHz superconducting radio frequency (SRF) booster cavity. The booster cavity for LEReC was converted from the SRF photocathode gun of the energy recovery linac (ERL) project [\[2\]](#page-8-1). A one-cell 704 MHz normal conducting cavity and a three-cell thirdharmonic (2.1 GHz) normal conducting cavity [\[3\]](#page-8-2) will be added to dechirp the energy spread and to compensate its nonlinearity, respectively. The linac of the LEReC is designed to deliver a 1.6–2.6 MeV electron beam, with rms  $dp/p$  less than  $5 \times 10^{-4}$ . The layout of the LEReC system is shown in Fig. [1.](#page-1-0)

The very low energy and small energy spread requirement make it important to control the higher order modes (HOMs) in these cavities, especially the 704 MHz SRF booster cavity. Starting from the analysis of the HOMs in the bare cavity, and the wake potential associated with these HOMs, we identified the dangerous modes. Based on rf, thermal, and mechanical analyses, we developed an HOM damper design to suppress these modes. A conditioning box was designed and tested to identify and overcome possible multipacting barriers of the damper at room temperature. The booster cavity was cryogenically tested without and with the HOM damper, and the results are also reported in this paper.

### II. BUNCH STRUCTURE, CAVITY HOMS, AND ENERGY SPREAD

### A. LEReC bunch structure

The LEReC design is a nonmagnetized cooling approach that uses electron bunches that match the ion beam velocity to cool each single-ion bunch. The ion beam in the RHIC to be cooled consists of 111 bunches, plus nine missing bunches for the abort gap, that are evenly distributed in the 3833.84 m circumference, with  $\gamma$  ranging from 4.1 to 6.1. It uses a 9 MHz rf system with a wide tuning range. In this paper, 9 MHz refers to the 120th harmonic of the RHIC revolution frequency, ranging from 9.104 to 9.256 MHz in the LEReC. The LEReC electron beam uses a macropulse structure, with electron macropulses aligned to the RHIC ion bunches. Each macropulse contains up to 30 flattop electron bunches spaced by 1.42 ns (704 MHz), with a 9 MHz macropulse repetition rate, or roughly 40% duty factor, and kinetic energies between 1.6 and 2.6 MeV. A mode of 1.6 MeV operation with full continuous wave (cw) operation at the 704 MHz frequency (no macrobunch structure) is also being considered. For all the modes mentioned above, there are electron bunches in the ion abort gap. In this case, the electron beam spectrum is not affected by the RHIC revolution frequency. Table [I](#page-1-1)

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FIG. 1. LEReC layout. The 704 MHz SRF booster cavity is in the top right corner, next to the dc electron gun.

summaries the proposed operating modes. The flattop electron bunch is introduced in detail in Sec. [III D.](#page-4-0)

### B. Cavity HOMs and energy spread

<span id="page-1-2"></span>The booster cavity was converted from the SRF photocathode gun (top right) of the ERL project [\[2\].](#page-8-1) In this figure, the left side is upstream and the right side downstream (i.e., the beam travels left to right). It is a 0.4 cell cavity operating at 2 K, with a maximum energy gain of 2.2 MeV. Key cavity parameters are listed in Table [II.](#page-2-0) In the ERL gun configuration, it had a room-temperature HOM damper located on the 10-cm-diameter downstream beam pipe, outside the cryomodule [\[4\].](#page-8-3) The HOM absorber consisted of 12 pieces copper-tungsten composition Elkonites 10W3 substrates that form a cylindrical, 16 cm inner diameter ferrite spool, with two  $50.8 \times 38.1 \times$ 3.18 mm nickel-zinc C-48 ferrite tiles soldered on each substrate. The geometric configuration of this absorber is identical to the new one shown in Fig. [3](#page-3-0). This spool is placed over a 3.9-cm-long, 10 cm I.D. 92% aluminum oxide ceramic window which is brazed on to the stainlesssteel beam pipe [\[4\]](#page-8-3).

The 10 cm inner diameter beam pipe has a  $TM_{01}$  cutoff frequency of 2.30 GHz. The cavity  $TM<sub>010</sub>$  fundamental mode frequency is 704 MHz. The first monopole HOM is the second-harmonic  $TM_{020}$  mode at 1.48 GHz, below the  $TM_{01}$  beam pipe cutoff frequency. This trapped  $TM_{020}$ mode could therefore not be damped by the original ferrite damper that is far from the cavity. The previously measured loaded Q of this mode was  $∼165,000$  at 2 K. However, note that, for this measurement, the fundamental power coupler (FPC) port was connected to a network analyzer, which did not represent the actual operating configuration. The FPC design in this cavity provides good coupling to both the fundamental mode and the  $TM_{020}$  mode. The cavity features two FPC ports, feeding from each side of the cavity with a broadband coaxial rf window separating the cavity vacuum from an air side narrow band doorknob transition to the WR1500 waveguide (not shown in Fig. [2](#page-2-1)); see Ref. [\[5\]](#page-8-4) for more details. These two WR1500 waveguides, after some transition pieces and phase shifters, then connect via a waveguide tee, which then connects to a narrow band circulator that protects the 1 MW klystron. Thus, the 1.48 GHz will be rejected by the narrow band components in the normal operating configuration. The simulation showed that, in the normal operating configuration, the Q of the TM<sub>020</sub> mode would actually be  $3.7 \times 10^{7}$ . With a 50.8  $\Omega$  R/Q and a 0.12 V/pC loss factor for the TM<sub>020</sub> mode, near resonant excitation of this HOM would induce well over 1 MV voltage fluctuation. There are still other dangerous modes below the beam pipe cutoff which can readily increase the beam energy spread well past the specified limit.

Note that, in simulations, the  $R/Q$  for each HOM, and thus its wake potential, are calculated with  $\beta = 1$ . This is not the case in actual operation, as the beam energy at the cavity entrance is only 400 keV. However, for the most critical mode TM<sub>020</sub>, with β at 1.0, the R/Q is 50.8 Ω; with

<span id="page-1-1"></span>TABLE I. Proposed operating modes, final operating modes with a dangerous HOM measured at 1.47834 GHz, and HOM-induced momentum spread in the worst-case scenario.

Proposed operating modes	1.6 MeV	1.6 MeV cw	$2.0 \text{ MeV}$	$2.6 \text{ MeV}$
Bunch charge [pC]	130	120.8	170	<b>200</b>
Value of 9 MHz [MHz]	9.104	9.104	9.187	9.256
Bunches per macrobunch (9 MHz)	30	<b>CW</b>	30	$24 - 30$
Beam current [mA]	35.9	85.0	47.0	$44.2 - 55.3$
Final operating modes	1.60 MeV	$1.60$ MeV cw	$1.92$ MeV	$2.60$ MeV
Dangerous HOM away from 9 MHz [MHz]	3.41	NA	1.34	>2.64
$dp/p$ from HOMs [ $\pm 10^{-4}$ ]	2.7	3.6	2.5	1.7

<span id="page-2-0"></span>



 $β$  at 0.9, it lowers to 37.7 Ω; and with  $β$  at 0.8, it is even lower, at 27.3 Ω. Using the  $R/Q$  value with  $β = 1.0$  is therefore conservative and safe.

#### III. HOM DAMPER DESIGN

#### A. HOM damper choice and rf design

<span id="page-2-2"></span>Because of time and resource constraints, the design and fabrication of a new cavity and cryomodule were not a practical option. Several ideas for reducing the impact of dangerous HOMs were investigated, including shifting the HOM frequencies via cavity tuning, shifting the rf spectrum of the beam, and damping the trapped modes via FPC coupling. Other methods include a new HOM damper design, which will be the topic of this section, as well as detuning the HOM frequency away from the nearest 9 MHz beam harmonic. This could be achieved by slightly changing the ion beam (and corresponding electron beam)

<span id="page-2-1"></span>

FIG. 2. Booster cavity with new HOM assembly: (a) Nb cavity; (b) helium vessel; (c) two FPCs, with the other one opposite to the one shown in the figure; (d) 5 K cold anchor; (e) 25 K cold anchor 1.3 cm width ring; (f) Cu tube for the HOM damper, with  $L$  its length from the tip to the electric short on the right side; (g) HOM absorber assembly, with details shown in Fig. [3;](#page-3-0) (h) HOM rf window assembly, with  $d$  the distance between its center and the electric short of the Cu tube, and details shown in Fig. [4](#page-3-1). Inset in the top right corner: ERL photocathode gun with old HOM assembly.

Lorentz factor  $γ$ , thus changing the exact frequency of the 9 MHz spectral components, or by changing the cavity HOM frequency.

We first evaluate the possibility to shift the cavity HOM frequency via the main tuner. For this to be a viable solution, the required minimum frequency shift in the most dangerous HOM is about 0.7 MHz (detailed later in this paper). The main tuner can adjust the fundamental frequency over approximately 1 MHz, from 703.77 to 704.74 MHz. Over this range, however, the  $TM_{020}$  HOM changes only 0.1 MHz. The cavity also has two FPC ports and is equipped with a dual-feed coupling system [\[6\]](#page-8-5). High-power waveguide phase shifters were placed at each FPC to permit the adjustment of external Q. Investigating the possible HOM frequency shift occurring over the available FPC  $Q_{ext}$  range [\[6\]](#page-8-5), both the fundamental frequency shift (4 kHz) and the  $TM<sub>020</sub>$  mode frequency shift (0.06 MHz) were far too small to be of practical use. In addition, one would obviously need to fix the fundamental frequency, as well as the FPC coupling strength to the designed value during operation.

Next, improved damping mechanisms were evaluated. Moving the ERL gun ferrite damper closer to the cavity was not an option. To couple sufficiently to the evanescent  $TM_{020}$  mode in the beam pipe, it would introduce a significant rf loss from the fundamental mode before any effective damping could be made to the  $TM_{020}$  mode. The FPC by itself is broadband and can couple to the  $TM_{020}$ mode. However, in the real system, it becomes impractical to use the FPCs for damping. A narrow band doorknob transition is used between the main WR1500 waveguide and the coaxial FPC structure. Damping HOM on the air side, upstream of the doorknob structure, is not viable, since the through attenuation of the doorknob at 1.48 GHz varies with the frequency, ranging from 13 to 40 dB within -5 MHz around 1.48 GHz, with the power dissipated on the doorknob wall to be negligible. Because of other physical modifications to the cavity on the upstream and downstream ends, as well as to the FPC, the exact frequency of  $TM_{020}$  would be impossible to predict, and thus the idea of damping on the air side after the doorknob structure was abandoned. Modifying the FPC structure between the doorknob and vacuum window to somehow introduce a high-power diplexer to couple out the  $TM_{020}$ mode was obviously impractical as well. Thus, any idea of HOM damping via the FPCs was abandoned.

Ultimately, the only viable solution for damping the HOMs that allowed for sufficient coupling to the trapped modes was a coaxial beam pipe coupler scheme, shown in Fig. [2](#page-2-1). A new cylindrical ceramic rf window and a ferrite absorber similar to the ERL SRF gun scheme are used in this design. We denote  $L$  the length of the Cu tube from its tip to the electric short on the right side and  $d$  the distance between the center of the rf window and the electric short; see Fig. [2](#page-2-1). To minimize the coupling to the fundamental  $TM_{010}$  mode, d

should be around  $(A/2 + 1/4)\lambda_{010}$ , and L should be around  $(B/2 + 1/2)\lambda_{010}$ . To maximize the damping to TM<sub>020</sub>, d should be around  $\left(\frac{C}{2} + \frac{1}{2}\right)\lambda_{020}$ , and L should be around  $(D/2 + 1/4)\lambda_{020}$ . In these constraints, A, B, C, and D are zero or a positive integer, and  $\lambda$  is the wavelength of the mode. This combination of  $d$  and  $L$  minimizes the HOM damper coupling to the fundamental mode and maximizes the coupling to the TM<sub>020</sub> mode. Note that, since  $\lambda_{010}$  is not exactly  $2\lambda_{020}$ , a CST Microwave Studio simulation is needed for optimization. The location of the coaxial opening should be optimized with the consideration of a number of important factors: rf heating from the fundamental mode, coupling strength to the  $TM_{020}$  mode, perturbation to the fundamental frequency, and FPC coupling, as well as possible multipacting between the coaxial opening and FPC couplers. In the final design, considering the actual dimensions of the cavity and beam pipe with the cryomodule, with the HOM damper placed right outside the cryomodule, and trying to make the assembly compact, we choose  $A = C = 0, B = 3$ ,  $D = 8$ , and  $d = 113.0$  mm,  $L = 848.4$  mm. With such a design, the dissipation of the fundamental mode on the ferrite is ∼10 W, and the quality factor of the 1.478 GHz mode is expected to be at 50 000.

### B. HOM absorber thermal and mechanical design

The HOM absorber, shown in Fig. [3](#page-3-0), is similar to the version for the ERL gun, consisting of 12 pieces 25% copper–75% tungsten composition Mi-Tech CW75 substrate, which has the same makeup as Elkonites 10W3 [\[7\]](#page-8-6). During inspection of the ERL gun absorber, cracks were found on the ferrite tiles. Instead of nickel-zinc C-48 ferrite, this damper uses TT2-111R ferrite tiles [\[7\]](#page-8-6) having a closely matched thermal expansion coefficient with the Mi-Tech CW75. The ferrite tiles are attached to the substrate using Duralco<sup>TM</sup> 125 silver filled epoxy. Although not strictly

<span id="page-3-2"></span>TABLE III. Thermal cycle test results.

Water cooling	No	Yes.
Heater power [W]	18	200
Temp increase on ferrite $[°C]$	70	10
Temp gradient across ferrite $[°C]$	14	120.

necessary, since the rf power dissipated on the absorber is small (with 10 W from the fundamental 704 MHz and HOM power as calculated in Sec. [III D\)](#page-4-0), we kept the water cooling channel design from the ERL gun HOM damper.

During thermal cycle testing, a heater was mechanically bonded to the two ferrite tiles on one substrate. Different amounts of power were applied to the heater without and with water cooling. We measured the temperature increase (from room temperature) on the ferrite (the side away from the heater), as well as the temperature gradient across the ferrite. The results for the substrate with the highest temperature increase are shown in Table [III](#page-3-2). All ferrite tiles showed no crack after these tests. With 12 pieces, the HOM damper should be able to handle 216 W power without water cooling and 2.4 kW with water cooling. Note that during these tests we did not try to push to its mechanical limit.

The dimensions of the rf window are close to the ERL gun HOM window. The ceramic braze assembly includes ceramic rings used to sandwich the stainless-steel braze flanges, to balance the stress produced during brazing. A short bellows is included to minimize stress applied to the window during assembly and operation (Fig. [4\)](#page-3-1).

The copper tube (center conductor) of the coaxial coupler assembly is cantilevered from the electrically shorted end and is susceptible to mechanical vibrations. Simulations were performed to check for mechanical resonances, and a resonance at 60 Hz was found. The

<span id="page-3-0"></span>

cooling channel on the back of each substrate.

 $(2)$ FIG. 3. HOM absorber assembly section view with 12 pieces of FIG. 4. HOM rf window assembly with (1) a sandwich ceramic substrates forming a cylinder, two ferrites on each substrate, and a window, (2) a stainless-steel bellows, and (3) a 304 stainless-steel

adaptor.

<span id="page-3-1"></span>

tube was redesigned with a "taper" in the wall thickness, varying from 4 mm on the electric short end to 1 mm at the open end. This shifted the lowest mechanical resonance from 60 to 90 Hz. Because of the difficulty in machining, the fabricated Cu tube is tapered with four steps instead of continuous tapering. Static deflection due to gravity, on the end close to the cavity, is 0.04 mm. The cavity with the HOM assembly is shown in Fig. [2.](#page-2-1)

A water channel is designed on the electric short end to help stabilize the Cu tube temperature. Because of the long, narrow thermal path, fundamental-mode-induced rf heating on the Cu tube can induce a 25 °C gradient from the shorted to the open end. In the thermal simulation of the booster cavity downstream end, we considered the rf-induced heat, as well as the thermal radiation between the Cu tube and beam pipe. The rf-induced heat at 2.2 MeV accelerating voltage is 4.6 W on the tapered Cu tube, 2.2 W on the stainless-steel beam pipe, and 0.2 W on the AlMg gasket for NbTi flanges between the Nb and stainless-steel beam pipe tubes, for a total of 7.1 W. With the water-cooled electrical shorted end at 20 °C, the open end Cu tip temperature increases to 45 °C. To be conservative in estimating the radiated heat, an emissivity of 0.1 is assumed for the tapered Cu tube (actual emissivity was measured to be  $\langle 0.025 \rangle$ , and 55 °C is assumed on the open end Cu tip. The open end of the tapered Cu tube faces the cavity downstream Nb beam pipe over a length of 4.7 cm, with the remainder facing the stainless-steel beam pipe. In this case, the thermal radiation from the tapered Cu tube is 7.5 W in total, with 2.0 W to the Nb cavity, 0.8 W to the Nb beam pipe, and 4.7 W to the stainless-steel beam pipe. The cavity is immersed in 2 K liquid helium, with the Nb beam pipe and the FPC ports conductively cooled. The AlMg gasket is cooled with supercritical 5 K helium, with a cooling capacity of ∼5 W. On the stainless-steel beam pipe, a 1.3 cm-wide cylindrical thermal anchor strapped to the 25 K heat shield is added, 5 cm downstream from the 5 K anchor, to reduce the load to the 5 K intercept, shown in Fig. [2\(d\)](#page-2-1). The heat load into the 2 K helium is 3.0 W, into the 5 K thermal intercept is 1.7 W (without the 25 K thermal anchor, it would be 5.7 W), into the 25 K thermal anchor is 4.3 W, and into the water cooling outside the cryomodule is 5.6 W. With 3 W from the radiation, and a possible beam halo heat load on the upstream side of the cavity, the 2 K cryostat loading, which was 18.3 W for the original ERL gun, is budgeted at 45 W. The maximum simulated temperature on the AlMg gasket with NbTi flanges is 6.56 K, on the Nb tube is 5.20 K, and on the stainless-steel beam pipe is 305.86 K.

#### C. HOM damper multipacting simulation

<span id="page-4-2"></span>Multipacting can cause the quality factor to drop and can limit the maximum cavity gradient. It is an electron avalanche effect due to the resonant multiplication of secondary electrons [\[8\]](#page-8-7). It depends on the secondary

<span id="page-4-1"></span>

FIG. 5. Multipacting simulation performed for the booster cavity HOM damper with TRACK3P. Electron impact energy (top), and number of impacts (bottom), along the HOM damper at accelerating voltage between 10 keV and 2 MeV. 0 m in the  $X$  axis represents the cavity surface on the equator, and 1 m the electric short of the Cu tube.

electron yield of the cavity surface material and the cavity shape. It is normally easy to find in a coaxial structure and, thus, needs to be carefully evaluated in our coaxial HOM damper. We use the TRACK3P solver from the SLAC ACE3P suite of codes [\[9\],](#page-8-8) scanning the accelerating voltage from 10 keV to 2 MeV with a 10 keV step size, and assumed seed electrons coming out of the whole section of the tapered Cu tube. As shown in Fig. [5,](#page-4-1) with seed electrons starting from the cavity surface on the equator, to the electric short of the Cu tube, possible multipacting appeared at the FPC ports, and it was confined in the coaxial section of the FPC. This multipacting had been previously simulated and experimentally conditioned away. On the ceramic rf window, all particles die after three impacts. The number of electrons with energies above 200 eV is small, and all are confined on the FPC section, which indicates that multipacting should not be a critical issue for this cavity.

### D. Energy spread with HOM damper

<span id="page-4-0"></span>In this section, we calculate the energy spread produced by the wakefield in the booster cavity. We take the intrabunch (head to tail) energy spread caused by the short-range wakefield, as well as the interbunch (bunch to bunch) energy spread caused by the long-range wakefield, into consideration.

The LEReC project uses a dc photoemission gun with a multialkali ( $CsK<sub>2</sub>Sb$  or Na $K<sub>2</sub>Sb$ ) cathode [\[10\].](#page-8-9) To get the desired 24 mm "flattop" line density distribution, 32 Gaussian laser pulses, with 0.6 mm rms length and 0.75 mm spacing, are stacked together [\[11\].](#page-8-10) In this case,

<span id="page-5-0"></span>

FIG. 6. Short-range wakefield of the flattop electron bunch, with a wake loss factor at 0.95  $V/pC$  and an energy spread factor at 0.53 V/pC rms with 1.6 MeV beam energy.

one cannot simply use a 1 cm rms length Gaussian bunch for the short-range wakefield simulation, since a 0.6 mm bunch exhibits a frequency content much higher than the 1 cm bunch. A short-range wakefield simulation was done using CST Particle Studio<sup>TM</sup> with a 0.6 mm rms Gaussian bunch at the speed of light. The result, as well as the charge distribution, was then calculated by "shift and stack" superposition, every 0.75 mm. The normalized results are shown in Fig. [6.](#page-5-0) The wake loss factor is the integration of the product of the wake potential and normalized bunch charge, and the energy spread factor is the rms deviation from the average energy loss. It is calculated by summing the weighted squares of the differences and taking the square root of the sum. These two factors were then divided by  $\beta^2$  for 1.6 MeV beam energy. The wake loss factor is 0.95 V/pC, and the energy spread factor is 0.53 V/pC rms. With a 100 pC electron bunch, the energy spread intrabunch is 53 V rms. Please note that the  $1/\beta^2$  factor is a simplified estimation based on Ref. [\[12\]](#page-8-11); following the method in Ref. [\[12\]](#page-8-11) leads to smaller wake loss and energy spread factors.

To calculate the interbunch energy spread from the longrange wakefield of the longitudinal modes, a straightforward way is to use the result shown in Fig. [6](#page-5-0) and shift and stack this result according to the beam pattern. This method is not used, because it is very time consuming, and because one cannot apply the "worst-case scenario" by artificially shifting each HOM frequency around, since the actual HOM frequency in the cavity might deviate from the rf simulation due to fabrication error, deformation during fabrication, operation, and tuning, etc. In this case, an eigenmode simulation is first done using CST Microwave Studio<sup>TM</sup>, with the simulation frequency ranging from the fundamental mode to the first longitudinal cutoff of the beam pipe. The single-bunch wake potential is then constructed using the eigenmode simulation results and is compared with the  $CST$  Particle Studio<sup>TM</sup> result. The multibunch wake potential is calculated by using the shift and stack method on the singlebunch wake potential, similar to the calculation of the flattop short-range wakefield.

For the 704 MHz SRF booster cavity, the downstream side beam pipe is 50 mm in radius, and a 40 mm radius tapered Cu tube for the HOM damper is inserted into this beam pipe. The beam pipe is further taped to 30.2 mm radius for a third-harmonic normal conducting rf cavity at 2.1 GHz next to it. The beam pipe cutoff frequency for 30.2 mm radius is 2.91 GHz for the  $TE_{11}$  mode and 3.81 GHz for the  $TM_{01}$  mode. We calculate the HOMs using CST Microwave Studio<sup>TM</sup> eigenmode simulation with a frequency up to 3.81 GHz. The result is then treated with the worst-case scenario by artificially changing the resonance frequency of each HOM to align with multiples of 9 MHz, and, for those modes that are close  $(\pm 20 \text{ MHz})$  to the multiples of 704 MHz, their resonance frequencies are changed to the multiples of 704 MHz.

With the single-bunch wake potential reconstructed from the eigenmode simulation results using the method in Ref. [\[13\]](#page-8-12) for a point charge, we then use the shift and stack method introduced above to get the multibunch multitrain wake potential, with 30 continuous bunches with 704 MHz frequency in a 9 MHz train with ∼40% duty factor. The results are consistent with the method proposed by Kim et al. [\[14\],](#page-8-13) since both methods are based on a delta function structure. For the 704 MHz booster cavity, the multibunch multitrain saturates at 4.92 kV voltage fluctuation. With the  $TM_{020}$  mode measured at 1.478 GHz 0.7 MHz away from the harmonic of the 9 MHz, the voltage fluctuation changes to 0.60 kV, corresponding to a maximum  $\pm 3.0 \times 10^{-4}$  dp/p peak to peak.

As mentioned in Sec. [III A](#page-2-2), it is practically difficult to tune the  $TM_{020}$  mode frequency. Pushing the  $TM_{020}$  mode away from the 9 MHz frequency (the repetition rate of the ion bunch, ranging from 9.104 to 9.256 MHz in LEReC) is accomplished by carefully selecting the ion bunch energy, with the electron bunch velocity matching the ion bunch velocity. Table [I](#page-1-1) shows the final operating modes; they are pulsed modes at 1.60, 1.92, and 2.60 MHz and a cw mode at 1.60 MHz. The highest  $dp/p$  caused by HOMs in this cavity in the worst case is  $\pm 3.6 \times 10^{-4}$  peak to peak with the cw mode at 1.60 MHz.

Please note here that we did not consider the beam loading effect of the fundamental mode at 704 MHz, even though it follows the same calculation showed above. This effect will bring extra energy spread and will be corrected by a combination of an additional 9 MHz cavity and rf power regulation for the booster cavity.

#### E. Emittance growth with HOM damper

The interbunch (bunch to bunch) emittance growth of the electron beam from the long-range wake potential of the transverse modes is calculated in a way similar to that of the interbunch energy spread. We use the same worst-case scenario as mentioned in Sec. [III D.](#page-4-0) Since the modes that are close to the multiples of the 704 MHz have low  $R_T/Q$ , none of these HOMs can accumulate voltage quickly within a train. In this case, it is easy to understand that the highest  $R<sub>T</sub>/Q$  will give the most perturbation, since we assumed that all modes will be multiples of 9 MHz. The most critical mode for a vertical kick (aligned with FPC) is at 1.0057 GHz, and the most critical mode for a horizontal kick (perpendicular to FPC) is at 1.0049 GHz. The vertical mode is measured at around 1.0065 GHz at 2 K liquid helium bath temperature; the horizontal mode is not coupled to the FPC and, thus, cannot be measured. They are both  $TM_{11}$  modes, and their polarizations are perpendicular to each other. The estimated maximum vertical kick is 5.2 kV, and for horizontal it is 1.43 kV for 0.5 mm displacement on each direction. Please note these two effects will not get stacked together, since these two resonances are 0.8 MHz away and they will not be multiples of 9 MHz simultaneously. In this case,  $\Delta x'$  is estimated to be 1.8 mrad for the vertical case and 0.51 mrad for the horizontal case and normalized  $\Delta \varepsilon$  to be 7.7 mm  $\times$ mrad for vertical and  $2.2$  mm  $\times$  mrad for horizontal with 1 mm rms beam size in the cavity. This is a rough upper limit estimation. With the specification  $\varepsilon$  at 2.5 mm  $\times$  mrad, the SRF booster cavity will contribute at most 3.1 times the emittance for the vertical case and 90% for the horizontal case. One can always limit the displacement at a smaller number, i.e., 0.02 mm, so that the contribution will decrease to 12% for the vertical case and 4% for the horizontal case. This can be achieved by steering the beam right after the dc gun using dipoles to the electric center of the booster cavity. With the resonance frequencies of these two modes away from the harmonic of 9 MHz, the transverse emittance will reduce. In this case, the displacement limitation can be relaxed accordingly. A 0.2 mm cavity alignment requirement was introduced. In case the transverse emittance is measured to be out of specification due to the above effect, dipole correctors between the dc gun and booster cavity will be used to minimize the average beam displacement.

#### F. HOM power estimation

In this section, a method to estimate the HOM power generated in the booster cavity with the HOM damper is introduced.

The bunch structure described in Sec. [II B](#page-1-2) is used for this analysis. The normalized beam spectrum  $F_{\text{norm}}(\omega)$  is shown in Fig. [7](#page-6-0). To scale it to  $I_{\text{ave}} = 0.085A$  current (1.6 MeV cw case), an  $I_{ave} * T = Q_T$  factor should be applied to the spectrum so that  $F(\omega) = F_{norm}(\omega) * Q_T$ , with T the total time in the electron beam structure that is used for FFT (for LEReC we use the RHIC revolution time) and  $Q_T$  the total charge of the electron within T.

For each HOM, the real part of the shunt impedance over the frequency is calculated using the following formula:

<span id="page-6-0"></span>

FIG. 7. Normalized beam spectrum (blue curve) with shunt impedance of the longitudinal HOMs (red dots) in the booster cavity.

$$
R(\omega) = \frac{R_0}{1 + Q_L^2(\frac{\omega_0}{\omega} - \frac{\omega}{\omega_0})^2}
$$

with longitudinal shunt impedance  $Q|V_z|^2/(\omega U)$ , shown as red dots in Fig. [7](#page-6-0), and transverse shunt impedance  $Q|V_z(r_0)-V_z(0)|^2/(\omega U)$  with displacement  $r_0$  at 0.5 mm. Please note that the definition of transverse shunt impedance is different from the typically used definition for a beam stability simulation by a factor of  $\left[\frac{c}{r_0\omega}\right]^2$ .

The power of each HOM is calculated using the following equation:

$$
P_{\text{HOM}} = \sum_{\omega} I_{\text{ave}}^2 F_{\text{norm}}(\omega)^2 R(\omega).
$$

With the worst-case assumption in Sec. II D, for the longitudinal modes, the  $TM_{020}$  mode that is 0.7 MHz away from the multiples of 9 MHz produces 0.13 W power. For comparison, when it is multiples of 9 MHz, it is going to be 164 W. The 3.536 GHz mode produces 29.5 W, with 49% damped on the section close to the water cooling channel close to the electric short and 29% on the ferrite. The 2.084 GHz mode produces 10.0 W, with 97% of power damped on the FPC. For the dipole modes, those at 1.0049 and 1.0057 GHz produce only 0.6 W in total in the worst case.

### IV. TEST ON HOM DAMPER

#### A. Conditioning box design and test

A multipurpose metal container, shown in Fig. [8](#page-7-0), is designed to bake, condition, and store the tapered Cu tube with the rf window, so that this damper can be as clean as possible, and can be conditioned as much as possible to be mulipacting-free, to avoid any contamination to the SRF booster cavity, as well as to preserve a reasonably good emissivity by blocking water vapor and oxygen from contacting the tapered Cu tube. This container includes a

<span id="page-7-0"></span>

FIG. 8. Multipurpose metal container designed to bake, condition, and store the tapered Cu tube with the rf window.

stainless-steel pipe, that is identical in structure to the downstream beam pipe of the cavity, and another Cu tube that is connected to two  $7/16$  feedthroughs to introduce rf power to this condition box, shown on the left in Fig. [8](#page-7-0). Because of the design of this HOM damper, it rejects the 704 MHz  $TM_{010}$  mode in the cavity. The distance d (defined in Sec. [III C\)](#page-4-2) cannot be altered. However, one can change the distance  $L$  to give a better coupling to the 704 MHz mode; this is done by the Cu tube inserted on the left side, which is slightly smaller than and is inserted into the tapered Cu tube to provide reasonable rf transmission without physical contact between them to avoid any contamination or damage. The surface of the inserted Cu tube that faces the tapered Cu tube is grooved to suppress the multipacting in this overlapped section.

This assembly was first cleaned in a class 100 clean room to a particulate-free condition. It was then baked at 200 °C with active pumping. A two-port network analyzer was connected to this box, with one port connected to one of the 7/16 feedthrough on the left and the other port connected to one of the pickup ports that is on the left of the ferrite damper, as shown in Fig. [8](#page-7-0). The other  $7/16$  feedthrough was connected to a short with a coaxial cable; changing the length of this cable changes the coupling to this condition box. The length of this cable is determined so that the field inside this conditioning box can be maximized with a certain rf power. After that, a 600 W amplifier was connected to the  $7/16$  feedthrough of this condition box, while the other  $7/16$  feedthrough remained the same (coaxial cable with a certain length and then a short). The goal of the high-power test is to achieve an rf field equivalent, or higher than that, in the SRF cavity with 2.2 MeV accelerating voltage. By applying as much as 420 W power at 704 MHz, the conditioning box reached an rf field equivalent to 3 MeV accelerating voltage in the SRF cavity. Some vacuum activities appeared with 300 W rf power, which is likely associated with the multipacting effect. Since with this rf power the corresponding accelerating voltage is ∼2.7 MeV, well above 2.2 MeV, it is not a concern. The HOM damper assembly was conditioned to multipacting-free and was stored under vacuum in this conditioning box till it was assembled to the SRF booster cavity.

### B. Cavity test without and with HOM damper

The cavity was first tested without a HOM damper. It reached 2.2 MeV accelerating voltage in the cw mode, with  $8-10$  mRem/hr radiation, 7.0 W static load, and 13.3 W dynamic load. It was then tested with a HOM damper. A network analyzer measurement showed that the quality factor of the  $TM_{020}$  mode is at 15 900, better than the simulated value at 50 000. During the high-power test, it reached  $2.26 \text{ MeV}$  in the cw mode, with  $8-18 \text{ mRem/hr}$ radiation, 7.0 W static load, and 18.3 W dynamic load. The temperature of NbTi flanges with an AlMg gasket, as well as that of the downstream Nb tube that is conductively cooled, increased with an increasing cavity gradient. The maximum temperature on the Nb tube was 6.6 K, 1.4 K higher than the thermal simulation. This is likely caused by the insufficient cooling time given to the 25 K thermal anchor added on the downstream [see Fig.  $2(e)$ ]. This thermal anchor was above 54 K during the high-power test. The test stopped at 2.26 MeV not because of any limitations by the cavity or HOM damper but because of the concern that a higher accelerating voltage might activate a field emitter and cause quality factor degradation, which was observed during the bare SRF booster cavity test at JLab.

### V. CONCLUSIONS

To meet the energy spread and emittance growth requirements of the LEReC project, an HOM damper was designed for the SRF booster cavity to damp the trapped  $TM<sub>020</sub>$  mode. Multiphysics simulations were performed to this design, which includes rf, thermal, mechanical, and multipacting simulations. Calculations on the energy spread caused by a short-range and long-range wakefield, on emittance growth and on HOM power estimation were done to ensure the effectiveness of this design. A multipurpose condition box was designed to bake, condition, and store the HOM damper. A SRF booster cavity without and with a HOM damper were tested cryogenically; results showed that this design meets the operational requirement at 2.2 MeV accelerating voltage and meets the damping requirement of the  $TM_{020}$  mode.

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