# Photoionization cross sections of the $5S_{1/2}$ and $5P_{3/2}$ states of Rb in simultaneous magneto-optical trapping of Rb and Hg

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We report the measurement of the photoionization cross sections of the  $5S_{1/2}$  and  $5P_{3/2}$  states of <sup>87</sup>Rb in a twospecies Hg and Rb magneto-optical trap (MOT) by the cooling laser for Hg. The photoionization cross sections of Rb in the  $5S_{1/2}$  and  $5P_{3/2}$  states at 253.7 nm are determined to be  $1^{+4.3}_{-1} \times 10^{-20}$  cm<sup>2</sup> and  $4.63(30) \times 10^{-18}$  cm<sup>2</sup>, respectively. To measure the  $5S_{1/2}$  and  $5P_{3/2}$  state fractions in the MOT we detected the photoionization rate of the  $5P_{3/2}$  state by an additional 401.5 nm laser. The photoionization cross section of Rb in the  $5P_{3/2}$  state at 401.5 nm is determined to be  $1.18(10) \times 10^{-17}$  cm<sup>2</sup>.

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## I. INTRODUCTION

Photoionization of atoms is a known source of losses in multispecies magneto-optical trapping when photons from the cooling beam for one species are energetic enough to ionize excited states of the other species [1,2]. In this article, we discuss the ionization process in the two-species Hg-Rb magneto-optical trap (MOT). Simultaneous trapping of cold Hg and Rb opens the way toward experiments in the field of fundamental physics. Particularly interesting features of Hg such as large mass, high nuclear charge, and variety of isotopes make this element relevant for experimental tests of the standard model [3–8]. Moreover, due to its low sensitivity for black-body radiation, Hg is regarded as the perfect candidate for the most accurate optical atomic clock [9,10]. On the other hand, the Hg-Rb molecule is appropriate for the search for the electric dipole moment of the electron [11,12].

For the future design of co-trapping experiments in a Hg and Rb mixture it is critical to address the problem of losses of the latter atom due to UV radiation, which originates from a cooling laser for Hg atoms. Earlier predictions of Aymar [13] suggest that it is likely that the Cooper minimum [14] for the photoionization of Rb should be observed close to the Hg cooling transition. The main goal of this paper is to elucidate previous theoretical predictions and estimate the influence of the 253.7 nm light on stability of the Rb MOT.

The wavelength of the cooling transition is 253.7 nm for Hg, which means the Hg cooling light can ionize Rb in both ground  $5S_{1/2}$  and excited  $5P_{3/2}$  states since photoionization from these states requires photon wavelengths shorter than 297 and 479 nm, respectively. The resulting losses restrict the number of Rb atoms in the Hg-Rb MOT. However, the

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respective cross sections for photoionization are small enough to allow simultaneous trapping of both species. Moreover, one can determine the values of the photoionization cross sections from observed atom losses in the Hg-Rb MOT setup.

The measurement is based on the method reported in [15] where atoms confined within a MOT were ionized from the excited state by an additional laser radiation and a subsequent decay of the trap fluorescence was measured. To date, several measurements of the cross sections of excited P and D states of various elements [16–22] have been reported for various wavelengths. It was also observed that the cooling photons in Cd MOT can ionize Cd from the excited  ${}^{1}P_{1}$  state of the cooling transition [23].

In the measurements reported here, since the 253.7 nm laser UV light ionizes Rb from both ground and excited states, relative populations in these states have to be determined to derive the photoionization cross sections. The excited  $5P_{3/2}$  state fraction was measured by photoionization by an additional 401.5 nm laser.

## II. PHOTOIONIZATION IN A DUAL MAGNETO-OPTICAL TRAP

In this paper, we study experimental sequences where only Rb atoms are trapped in the Hg-Rb MOT setup. The rate equation for the number of Rb atoms  $N_{\text{Rb}}(t)$  in the Hg-Rb MOT setup can be written as [16]

$$\frac{dN_{\rm Rb}}{dt} = L_{\rm Rb} (I_P^{253.7}) - (\gamma_{\rm Rb} + \gamma_P^{253.7}) N_{\rm Rb} - \beta_{\rm RbRb} \int dr^3 n_{\rm Rb}^2,$$
(1)

where  $L_{\rm Rb}(I_p^{253.7})$  is the Rb trap loading rate in the presence of ionizing radiation,  $\gamma_{\rm Rb}$  is the loss coefficient due to collisions with background gases,  $\gamma_p^{253.7}$  is the loss coefficient due to photoionization by 253.7 nm light,  $\beta_{\rm RbRb}$  is the loss coefficient due to the light-assisted collisions between the Rb atoms, and  $n_{\rm Rb}$  is the spatial density of Rb. In general, the photoionizing radiation of intensity  $I_p^{253.7}$  modifies the trap loading rate  $L_{\rm Rb}$ , as it removes a fraction of Rb atoms to be captured [18]. However, at fixed wavelength and intensity the trap loading rate  $L_{\rm Rb}$  can be treated as constant.

The collisions in Eq. (1) between cold Rb atoms can be ignored if the density in the Rb MOT is made low enough, e.g., by decreasing the intensity of the trapping beams. It yields the rate equation

$$\frac{dN_{\rm Rb}}{dt} = L_{\rm Rb} (I_P^{253.7}) - (\gamma_{\rm Rb} + \gamma_P^{253.7}) N_{\rm Rb}.$$
 (2)

This equation can be integrated with the initial condition  $N_{\text{Rb}}(t=0) = 0$  and the final formula for  $N_{\text{Rb}}(t)$  reads

$$N_{\rm Rb}(t) = \frac{L_{\rm Rb}(I_P^{253.7})}{\gamma_{\rm Rb} + \gamma_P^{253.7}} \{1 - \exp\left[-\left(\gamma_{\rm Rb} + \gamma_P^{253.7}\right)t\right]\}.$$
 (3)

$$i\frac{d}{dt} \begin{pmatrix} \rho_{5S_{1/2}} \\ \rho_{5P_{3/2}} \\ s \\ s^* \end{pmatrix} = \begin{pmatrix} -i\Gamma_{5S_{1/2}}^{253.7} & i\Gamma_{\rm sp} \\ 0 & -i\Gamma_{5P_{3/2}}^{253.7} - i\Gamma_{\rm sp} \\ U & -U & -\Delta \\ -U & U \end{pmatrix}$$

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If we assume that the photoionization processes from ground and excited states are independent, the loss coefficient  $\gamma_P^{253.7}$ due to photoionization by 253.7 nm photons can be expressed as [22]

$$\gamma_P^{253.7} = \left(\rho_{5S_{1/2}}\sigma_{5S_{1/2}}^{253.7} + \rho_{5P_{3/2}}\sigma_{5P_{3/2}}^{253.7}\right) \frac{I_P^{253.7}}{h\nu_P^{253.7}},\tag{4}$$

where  $\rho_{5S_{1/2}}$  and  $\rho_{5P_{3/2}}$  are the population fractions of the  $5S_{1/2}$  and  $5P_{3/2}$  states, respectively (it is assumed that  $\rho_{5S_{1/2}} + \rho_{5P_{3/2}} = 1$  in the Rb MOT),  $I_P^{253.7}$  is the photoionizing laser intensity,  $hv_P^{253.7}$  is its photon energy, and  $\sigma_{5S_{1/2}}^{253.7}$  and  $\sigma_{5P_{3/2}}^{253.7}$  are the photoionization cross sections from these states. Since the validity of the latter assumption is crucial for further investigation, even if this assumption is generally accepted, we have carefully examined the independence of both contributions.

To analyze the behavior of the rubidium atom exposed to ionization radiation we have represented it by a two-level model in the rotating wave approximation including the states  $5S_{1/2}$  and  $5P_{3/2}$  and we have solved the corresponding Bloch equations (5):

$$\begin{array}{cccc} & & U & & -U \\ & -i\Gamma_{\rm sp} & & -U & & U \\ U & & -\Delta - i\Gamma/2 & & 0 \\ & & & 0 & \Delta - i\Gamma/2 \end{array} \begin{pmatrix} \rho_{5S_{1/2}} \\ \rho_{5P_{3/2}} \\ s \\ s^* \end{pmatrix} .$$
 (5)

In the above equations  $\rho_{5S_{1/2}}$  and  $\rho_{5P_{3/2}}$  are the diagonal elements of the density matrix,  $s \equiv \langle 5P_{3/2} | \rho | 5S_{1/2} \rangle$  is its nondiagonal element (coherence),  $\Gamma_{\rm sp}$  is the relaxation rate due to spontaneous emission from the upper state to the lower one,  $\Gamma_{S_{1/2}}^{253.7}$  and  $\Gamma_{P_{3/2}}^{253.7}$  are ionization rates from the states  $5S_{1/2}$  and  $5P_{3/2}$ , respectively, due to the 253.7 nm ionizing laser field. The relaxation rate  $\Gamma/2$  for the coherence between the two states is  $(\Gamma_{\rm sp} + \Gamma_{S_{1/2}}^{253.7} + \Gamma_{P_{3/2}}^{253.7})/2$  [24]. The coupling between  $5S_{1/2}$  and  $5P_{3/2}$  states due to the trapping laser field detuned by  $\Delta = \omega - \omega_0$  from the atomic resonance  $\omega_0 = (E_{5P_{3/2}} - E_{5S_{1/2}})/\hbar$  is characterized by the Rabi frequency U.

In the absence of the ionizing laser, i.e., for the ionization rates  $\Gamma_{S_{1/2}}^{253.7} = \Gamma_{P_{3/2}}^{253.7} = 0$ , the evolution ends up in a steady state after a few lifetimes  $1/\Gamma_{sp}$ . The parameters of the steady state (populations of the two states and the corresponding coherence) depend on the model parameters  $(U, \Delta, \Gamma_{sp})$ . In the steady state the asymptotic values are

$$\rho_{5S_{1/2}}^{\text{steady}} = \frac{U^2 + \Delta^2 + \Gamma_{\text{sp}}^2/4}{2U^2 + \Delta^2 + \Gamma_{\text{sp}}^2/4},$$

$$\rho_{5P_{3/2}}^{\text{steady}} = \frac{U^2}{2U^2 + \Delta^2 + \Gamma_{\text{sp}}^2/4},$$

$$s^{\text{steady}} = \frac{U(\Delta - i\Gamma_{\text{sp}}/2)}{2U^2 + \Delta^2 + \Gamma_{\text{sp}}^2/4}.$$
(6)

Switching the ionizing laser on results in a slow depopulation of both  $5S_{1/2}$  and  $5P_{3/2}$  states.

We have solved the Bloch equations (5) using the Laplace transform. The result is that the populations and coherence

as functions of time are superpositions of terms of the form  $\exp(-iz_j t)$ , where  $z_j$  are the eigenvalues of the matrix of the Bloch equations. Note that in the absence of ionization one of the eigenvalues is zero and its corresponding term is the only one which survives after the steady state has been established. An example of the time dependence of the population of both states calculated for  $\rho_{5P_{3/2}}(t=0) = 0.32$ ,  $\Gamma_{\rm sp} = 2\pi \times 6.06$  MHz [25], and  $\Delta = 2\Gamma_{\rm sp}$  is shown in Fig. 1. Except for a relatively short time interval, where the Rabi oscillations appear (inset in Fig. 1), both states are depopulated exponentially.

The term of the matrix that includes the ionization rates can be treated as a perturbation and evaluated using the perturbation theory. The perturbation matrix is diagonal with the matrix elements:  $(-i\Gamma_S^{253.7}, -i\Gamma_P^{253.7}, -i(\Gamma_S^{253.7} + \Gamma_P^{253.7})/2)$ . Because the unperturbed matrix is non-Hermitian, applying the perturbation theory requires distinguishing between right and left eigenvectors. We are only interested in the correction to the zero eigenvalue. The corresponding right and left eigenvectors (unnormalized) are, respectively,  $\psi = (U^2 + \Delta^2 + \Gamma^2/4, U^2, U(\Delta - i\Gamma/2), U(\Delta + i\Gamma/2))$  and  $\tilde{\psi} = (1, 1, 0, 0)$ . The corrected eigenvalue is

$$\nu_{\rm ph} \equiv \frac{\langle \psi | W | \psi \rangle}{\langle \tilde{\psi} | \psi \rangle} = \rho_{5S_{1/2}}^{\rm steady} \Gamma_{5S_{1/2}}^{253.7} + \rho_{5P_{3/2}}^{\rm steady} \Gamma_{5P_{3/2}}^{253.7}.$$
 (7)

The effective ionization rate, common for both levels, is a mean value of the two ionization rates weighted with the steady-state populations. Since the cross sections are proportional to the probabilities, Eq. (7) justifies Eq. (4).

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FIG. 1. Results of numerical simulations of the dynamics of the rubidium atom in the presence of the 253.7 nm ionization radiation. The simulations were performed for the typical initial excited-state fraction equal to 0.32. Both ground-state (solid blue line) and excited-state (dashed red line) populations exhibit a perfectly exponential decay. Rabi oscillations before reaching the steady state are shown in the inset.

The excited  $5P_{3/2}$  state fraction  $\rho_{5P_{3/2}}$  can be detected with photoionization by a light at a wavelength between 297 and 479 nm. The solution of the loading rate equation of the weak Rb MOT in the presence of the 401.5 nm light is analogously given as

$$N(t) = \frac{L_{\rm Rb}(I_P^{401.5})}{\gamma_{\rm Rb} + \gamma_P^{401.5}} \{ 1 - \exp\left[-\left(\gamma_{\rm Rb} + \gamma_P^{401.5}\right)t\right] \}, \quad (8)$$

where

$$\gamma_P^{401.5} = \rho_{5P_{3/2}} \sigma_{5P_{3/2}}^{401.5} \frac{I_P^{401.5}}{h \nu_P^{401.5}} \tag{9}$$

is the loss coefficient due to photoionization by a 401.5 nm light,  $\sigma_{5P_{3/2}}^{401.5}$  is the photoionization cross section,  $I_P^{401.5}$  is the photoionizing laser intensity, and  $hv_P^{401.5}$  is its photon energy.

## III. MEASUREMENT OF THE PHOTOIONIZATION RATE AT 401.5 AND 253.7 nm

Our Hg-Rb MOT setup has been described in detail elsewhere [26], so only its most essential elements are presented below. For cooling and repumping the <sup>87</sup>Rb commercial external-cavity diode lasers (ECDLs) are used. The cooling laser beam is additionally amplified by a fiber-coupled tapered amplifier up to 700 mW. The frequency of these laser beams are stabilized by the Pound-Drever-Hall (PDH) [27] locking and the saturated absorption spectroscopy to an atomic resonance in a rubidium vapor cell.

Photoionization of ground-state Rb atoms is induced by the same laser system used to cool and trap Hg atoms. In this setup a 1014.8 nm laser light is used as a fundamental source and its light is frequency-quadrupled in a system of two doubling stages. The source laser is composed of a home-made ECDL and a tapered amplifier. Power buildup



FIG. 2. Loading curves of the  $^{87}$ Rb MOT in the presence (right, blue curve) and the absence (left, red curve) of the Hg cooling beams. Total intensity of the cooling light is 35 and 45.3 mW/cm<sup>2</sup> for 253.7 and 780 nm wavelengths, respectively. Both curves are the best fits given by Eq. (3).

bow-tie cavities are used to improve the efficiency of frequency doubling on lithium triborate (LBO) and beta barium borate (BBO) crystals. The Hg cooling laser frequency is stabilized to the narrow  $(7.5 \text{ kHz}) {}^{1}S_{0} - {}^{3}P_{1}$  transition in Sr by a stability transfer from an ultra-stable laser [28–30]. A small part of the fundamental 1014.8 nm light is uncoupled from the main beam before quadrupling and provided to a transfer cavity. The fundamental laser is locked to the ultra-stable laser by the PDH method. The same method is used to stabilize the length of the transfer cavity to the ultra-stable laser.

The vacuum system consists of two perpendicular arms connected to the science chamber. These two arms provide beams of mercury and rubidium atoms. The rubidium atomic beam is produced by a recirculating oven and slowed in the Zeeman slower. Mercury has a high vapor pressure at room temperature and it needs to be cooled to maintain highvacuum conditions. To lower the temperature of mercury a two-stage thermoelectric cooler is used. Between the cooler and the science chamber a two-dimensional magneto-optical trap (2D-MOT) is placed. This stage, although not required, since a 3D-MOT can be loaded directly from the mercury background vapor, improves the loading rate substantially.

The characterization of the MOT can be performed either by analysis of fluorescence images of the MOT taken by a charged coupled device (CCD) camera or by measuring the fluorescence light from the Rb and Hg atoms by a calibrated photodiode and a photomultiplier tube, respectively.

Figure 2 shows the loading curves of the <sup>87</sup>Rb MOT in the presence and absence of the Hg MOT cooling beams. To quantify how ionizing radiation depletes the Rb trap the source of Hg atoms is blocked. The losses introduced by the 253.7 laser UV light photoionization are clearly visible. The evolution of the number of Rb atoms is governed by Eq. (2). To characterize the UV light photoionization losses one has to know the photoionization cross sections of both ground and excited <sup>87</sup>Rb states as well as the population fractions of these states [Eq. (4)].



FIG. 3. Loading curves of the <sup>87</sup>Rb MOT in the presence (right, blue curve) and the absence (left, red curve) of 401.5 nm light with  $I_p^{401.5} = 30 \text{ mW/cm}^2$ . Both curves are the best fits given by Eq. (8).

### A. Calibration of ground $5S_{1/2}$ and excited $5P_{3/2}$ state fractions

To calibrate ground  $5S_{1/2}$  and excited  $5P_{3/2}$  state fractions the dependence of the photoionization rate by a light at 401.5 nm on the Rb trapping laser intensity was measured. The 401.5 nm light was generated by a free-running laser diode. The rough alignment of the 401.5 nm beam was based on the geometry of the vacuum chamber whereas the fine aligning was done by maximizing atomic losses from the trap induced by photoionization.

Typical loading curves of the <sup>87</sup>Rb MOT in the presence and absence of the 401.5 nm light are presented in Fig. 3. While the excited  $5P_{3/2}$  state fraction  $\rho_{5P_{3/2}}$ , under standard MOT operating conditions, could be estimated from the trapping laser parameters [31], it can also be directly calibrated by the measurement of the saturation of the photoionization rate with trapping laser intensity [15]. The model of the excitedstate fraction of two-state atoms in the MOT is

$$\rho_{5P_{3/2}} = \frac{I_{780}/I_{\text{sat}}}{2I_{780}/I_{\text{sat}} + 4(\Delta/\Gamma_{\text{sp}})^2 + 1},$$
(10)

where  $I_{780}$  is the total trapping intensity,  $I_{\text{sat}}$  is the saturation intensity,  $\Delta$  is the trapping laser detuning, and  $\Gamma_{\text{sp}}$  is the natural decay rate of the excited state ( $2\pi \times 6.06$  MHz for <sup>87</sup>Rb). Combining the model (10) with Eq. (9) yields the dependence of the loss coefficient  $\gamma_p^{401.5}$  on the total trapping intensity  $I_{780}$ :

$$\gamma_P^{401.5} = \sigma_{5P_{3/2}}^{401.5} \frac{I_P^{401.5}}{h\nu_P^{401.5}} \frac{I_{780}/I_{\text{sat}}}{2I_{780}/I_{\text{sat}} + 4(\Delta/\Gamma_{\text{sp}})^2 + 1}.$$
 (11)

The photoionization rate  $\gamma_p^{401.5}$  was determined by detecting fluorescence from the MOT during its loading alternately with and without the presence of the photoionization radiation. Figure 3 shows one pair of loading curves recorded in 401.5 nm photoionization experiment. To prevent detection of unwanted stray light the radiation from the MOT was filtered by a 780 nm interference filter and focused on a photodiode. To toggle the ionizing light on and off a mechanical shutter was used.



FIG. 4. Top: Dependence of the 401.5 nm ionization rate in the <sup>87</sup>Rb MOT (and the determined excited-state fraction) on the trapping laser intensity. The solid curve is a weighted fit of Eq. (11) with the effective saturation intensity  $I_{\text{sat}}$  and  $\sigma_{5P_{3/2}}^{401.5}$  being the free parameters. The dotted red line depicts its extension outside the fitting range. Experimental data are represented by scattered black and gray points, inside and outside valid fitting range, respectively. The vertical error bars represent one standard deviation of the mean calculated for a given intensity of the MOT beams. The horizontal error bars include uncertainty associated with the fluctuations of the intensity of the MOT beams (less than 1%) as well as the uncertainty in the MOT size measurement (less than 1.5%). The 401.5 nm ionizing laser intensity is kept at 17 mW/cm<sup>2</sup> within 3% of relative uncertainty. Bottom: Dependence of the reduced chi-squared of the fit (solid blue line) and the width of the histogram of the residuals (dashed red line) on the maximum value of the fitting range. The common minimum at 49 mW/cm<sup>2</sup> has been chosen as the best-fit value for the dependence shown in the upper part.

Two consecutive loading curves were measured and fit independently according to Eq. (6) giving loading rates  $\gamma_{\text{Rb}}$  and  $\gamma_{\text{Rb}} + \gamma_P^{401.5}$  for ionizing light off and on, respectively. The photoionization rate  $\gamma_P^{401.5}$  was determined by the difference of successive loading rates.

Figure 4 depicts the measured dependence of the 401.5 nm ionization rate in the <sup>87</sup>Rb MOT on the trapping laser intensity. The solid curve is a fit of Eq. (11) with the effective saturation intensity  $I_{\text{sat}}$  and  $\sigma^{401.5}$  being the free parameters. The determined value of  $I_{\text{sat}}$  calibrates the dependence (10) for a given geometry and detunings of all <sup>87</sup>Rb MOT beams.

As shown in Ref. [32], Eq. (11) fits experimental data well only for low enough intensities of the MOT beams. To determine the optimal upper limit of the useful fitting range we analyzed the quality of fits calculated for various ranges. We varied the upper limit while fixing the beginning of the

fitting range at zero intensity. The lower part of Fig. 4 shows the dependencies of the reduced chi-squared of the fit (solid blue line) and the width of the histogram of the residuals (dashed red line) on the maximum value of the fitting range. The general behavior of both curves is similar, except for low intensities, where the amount of points is too low to ensure reliable fit. The best-fit value corresponds to the common minimum of both curves which is equal to 49 mW/cm<sup>2</sup>.

The appropriate range of data corresponds to a solid part of the red line in Fig. 4. Outside that range (dotted red line) the data points start to be scattered and the dependence of the photoionization rate on the intensity of the MOT beams is negligible, making this area useless in further investigation. In comparing our experimental data with the results shown in Ref. [32], one should note that the distribution of measured values in both sets of the data is similar and it clearly shows a split between the scattered and the unscattered parts.

## B. Photoionization at 401.5 nm

The fit of Eq. (11) in Fig. 4 provides also the value of the photoionization cross section  $\sigma_{5P_{3/2}}^{401.5}$ . However, more precise value of  $\sigma_{5P_{3/2}}^{401.5}$  is determined by measurement of the dependence of the 401.5 nm ionization rate on the photoionizing laser intensity [Eq. (9)] while the intensity of the MOT beams (and consequently excited-state fraction) remains constant.

To measure the average intensity of the 401.5 nm ionizing radiation seen by the atoms in the MOT we used the formula [33]

$$\langle I \rangle = \iint \frac{I(x, y)N(x, y)}{N_0} dx \, dy, \tag{12}$$

where  $N_0$  is the total number of atoms in the MOT, and I(x, y) and N(x, y) are distributions of the intensity of the beam and the atoms, respectively. The intensity profile of the photoionizing beam was determined by a CCD beam profiler measurement to be a Gaussian function given by

$$I(x, y) = I_0 \exp\left(\frac{-2x^2}{\sigma_x^2}\right) \exp\left(\frac{-2y^2}{\sigma_y^2}\right), \qquad (13)$$

where  $\sigma_x = 2.096(28)$  mm and  $\sigma_y = 2.110(33)$  mm are  $e^{-2}$  half waists of the beam. Their values and uncertainties were derived from the two-dimensional Gaussian fit. The maximum intensity  $I_0$  can be expressed as

$$I_0 = \frac{2PT}{\pi \sigma_x \sigma_y},\tag{14}$$

where P is the power of the photoionizing beam and T is its transmission coefficient through the fused silica window which is equal to 0.95.

The distribution N(x, y) was determined by imaging fluorescence of the atoms trapped in the MOT on a CCD camera. The analysis of the image yields the Gaussian distribution

$$N(x, y) = \frac{2N_0}{\pi r_x r_y} \exp\left(\frac{-2x^2}{r_x^2}\right) \exp\left(\frac{-2y^2}{r_y^2}\right),$$
 (15)

where  $r_x = 1.47(1)$  mm and  $r_y = 1.54(2)$  mm are  $e^{-2}$  radii of the MOT. By putting together Eqs. (12)–(15) the formula (9)



FIG. 5. Dependence of the 401.5 nm photoionization rate  $\gamma_p^{401.5}$  in <sup>87</sup>Rb MOT on the photoionizing laser intensity  $\langle I \rangle$ . The red solid line is a linear fit to Eq. (17). The measurement was performed for the total intensity of the MOT beams equal to 35.2 mW/cm<sup>2</sup>, i.e., the excited-state fraction equal to 0.27.

can be rewritten as

$$\sigma_{5P_{3/2}}^{401.5} = \frac{hv_{5P_{3/2}}^{401.5}}{\rho_{5P_{3/2}}}A,$$
(16)

where A is obtained from a weighted linear fit of the formula

$$\gamma_P^{401.5}(\langle I \rangle) = A \langle I \rangle = A I_0 \frac{\sigma_x \sigma_y}{\sqrt{\left(r_x^2 + \sigma_x^2\right)\left(r_y^2 + \sigma_y^2\right)}}$$
(17)

to the data depicted in Fig. 5. We determined from Eqs. (16) and (17) that the value of the photoionization cross section at 401.5 nm is

$$\sigma_{5P_{3/2}}^{401.5} = 1.18(10) \times 10^{-17} \text{ cm}^2.$$
(18)

The uncertainty  $u(\sigma_{5P_{3/2}}^{401.5})$  has been estimated using standard uncertainty analysis

$$u(\sigma_{5P_{3/2}}^{401.5}) = h v_{5P_{3/2}}^{401.5} \sqrt{\left(\frac{u(A)}{\rho_{5P_{3/2}}}\right)^2 + \left(\frac{Au(\rho_{5P_{3/2}})}{\rho_{5P_{3/2}}^2}\right)^2}, \quad (19)$$

where u(A) is the uncertainty of A from the weighted linear fit of Eq. (17). The uncertainty u(A) involves the accuracy of the measurements of the Rb MOT radii, the waist, and the intensity of the ionization beam. The value of the  $u(\rho_{5P_{3/2}})$  has been extracted from the fit of Eq. (11) (solid red line in Fig. 4). Both terms in formula (19) contribute to the total uncertainty  $u(\sigma_{5P_{3/2}}^{401.5})$  with comparable level of significance.

#### C. Photoionization at 253.7 nm

# 1. $5S_{1/2}$ state

The photoionization cross section  $\sigma_{55_{1/2}}^{253.7}$  was determined by comparing the decay times of the MOT fluorescence with and without the presence of the photoionizing 253.7 nm light. To ensure all atoms were in the ground state during UV exposition, we used an appropriate timing sequence of the experiment [22,33]. After switching off all cooling and repumping beams by an acousto-optical modulator (AOM) we



FIG. 6. Timing sequence of the ground-state photoionization cross-section measurement. Solid red and dashed blue curves corresponds to the cooling and ionizing light, respectively. The inset shows the chopping phase in detail.

waited 45  $\mu$ s before exposure to the UV which is much longer than the lifetime of the 5 $P_{3/2}$  state (27 ns). Subsequently, the atoms were illuminated by a 275  $\mu$ s long pulse of the 253.7 nm light. The trapping beams were turned back on 45  $\mu$ s after switching off the UV light. The cycle was repeated until total depletion of atoms from the MOT. The total time of the sequence was 2.86 s. Figure 6 shows the timing scheme in detail.

To switch the light within the shortest possible time, fast rf switches with 2  $\mu$ s of switching time were used to drive the relevant AOMs. To ensure there were no stray resonant photons contributing to the excited-state fraction all possible sources of the resonant light were blocked during the UV operation. We checked also that no measurable leakage light was present on the AOM output.

To determine the photoionization cross section  $\sigma_{5S_{1/2}}$ , 212 decaying curves with chopped trapping and repumping beams were recorded with and without the alternating sequence of the UV pulses, giving decaying rates  $\gamma_P^{253.7} + \gamma_{Rb}$  and  $\gamma_{Rb}$ , respectively. Afterward, the averaged decaying rates  $\langle \gamma_P^{253.7} + \gamma_{Rb} \rangle$  and  $\langle \gamma_{Rb} \rangle$  were used to find  $\sigma_{5S_{1/2}}^{253.7}$  according to the formula

$$\sigma_{55_{1/2}}^{253.7} = \frac{h \nu_P^{253.7} \left( \left\langle \gamma_P^{253.7} + \gamma_{\rm Rb} \right\rangle - \left\langle \gamma_{\rm Rb} \right\rangle \right)}{\left\langle I_P^{253.7} \right\rangle}, \qquad (20)$$

where the average intensity of the photoionization light seen by the atoms  $\langle I_P^{253.7} \rangle$  was calculated according to Eqs. (12)–(15),

$$\langle I_P^{253.7} \rangle = \frac{2PT\eta}{\pi \sqrt{(r_x^2 + \sigma_x^2)(r_y^2 + \sigma_y^2)}},$$
 (21)

where  $\eta$  is a duty cycle equal to 0.545, according to the timing sequence. We determined the photoionization cross section to be

$$\sigma_{5S_{1/2}}^{253.7} = 1.0^{+4.3}_{-1} \times 10^{-20} \text{ cm}^2.$$
 (22)



FIG. 7. Dependence of the 253.7 nm photoionization rate  $\gamma_P^{253.7}$  in <sup>87</sup>Rb MOT on the photoionizing laser intensity  $\langle I \rangle$ . The measurement was performed for the excited-state fraction equal to 0.215(29). The linear fit (red solid line) to Eq. (23) gives the value of  $\sigma_{\text{eff}}^{253.7}$ .

The uncertainty of  $\sigma_{5S_{1/2}}^{253.7}$  is the standard uncertainty under assumption that  $\sigma_{5S_{1/2}}^{253.7}$  cannot be negative. It consists of two contributions, one related to the uncertainty of intensity of the photoionization light  $\langle I_p^{253.7} \rangle$  and the other due to the statistical spread of the differences between decaying rates. The statistical uncertainty is dominant because of low signalto-noise ratio in measurements of the photoionization from the  $\sigma_{5S_{1/2}}^{253.7}$  ground state. Surprisingly, even with the significant uncertainty, this result can be used for precise determination of the photoionization cross section of the excited state  $\sigma_{5P_{1/2}}^{253.7}$ 

## 2. $5P_{3/2}$ state

The determination of the photoionization cross section for the excited state  $\sigma_{5P_{3/2}}^{253.7}$  was based on Eq. (4) which can be rewritten as

$$\gamma_P^{253.7} = \frac{\sigma_{\text{eff}}^{253.7}(\rho_{5P_{3/2}})}{h\nu_P^{253.7}} I_P^{253.7}, \tag{23}$$

where

$$\sigma_{\rm eff}^{253.7}(\rho_{5P_{3/2}}) = \left(\sigma_{5P_{3/2}}^{253.7} - \sigma_{5S_{1/2}}^{253.7}\right)\rho_{5P_{3/2}} + \sigma_{5S_{1/2}}^{253.7} \tag{24}$$

is an effective photoionization cross section at 253.7 nm. The dependence of the  $\sigma_{\text{eff}}^{253.7}$  on the excited-state fraction  $\rho_{5P_{3/2}}$  has been measured for fractions from 0.215(29) to 0.357(18). Each  $\sigma_{\text{eff}}^{253.7}$  value was obtained from a linear fit according to the formula

$$\sigma_{\rm eff}^{253.7} = \frac{\gamma_P^{253.7}}{I_P^{253.7}} h v_P^{253.7}, \tag{25}$$

where the photoionization rates  $\gamma_P^{253.7}$  were determined by comparing exponential fits of the Rb MOT loading curves with 253.7 nm ionizing light on and off. The relative uncertainty  $u(\sigma_{\text{eff}}^{253.7})/\sigma_{\text{eff}}^{253.7}$  for each excited-state fraction was estimated by linear regression to be less than 4%. Figure 7 shows typical dependence of the photoionization rate  $\gamma_P^{253.7}$ on the photoionizing laser intensity measured for the excitedstate fraction of 0.215(29).



FIG. 8. Effective ionization cross section  $\sigma_{\text{eff}}^{253.7}$  vs excited-state fraction  $\rho_{5P_{3/2}}$ . The solid red curve is a weighted linear fit to the data. The transparent red area corresponds to the statistical uncertainty of the fit. To improve visibility of results the logarithmic scale was used. The inset shows the area near the fully populated excited state, i.e.,  $\rho_{5P_{3/2}} = 1$ .

Figure 8 shows the dependence of the effective cross section  $\sigma_{\text{eff}}^{253.7}$  on the excited-state fraction  $\rho_{5P_{3/2}}$ . The  $\sigma_{5S_{1/2}}^{253.7}$  determined above corresponds to  $\rho_{5P_{3/2}} = 0$ . The uncertainties of the excited-state fraction have been calculated as the standard deviation of the weighted mean of the data measured at a given intensity of the MOT beams. The photoionization cross section of the excited state  $\sigma_{5P_{3/2}}^{253.7}$  has been determined from a weighted linear fit (red line in Fig. 8) of Eq. (24) with  $\sigma_{5P_{3/2}}^{253.7}$  being the free parameter. The fit yields a value of

$$\sigma_{5P_{3/2}}^{253.7} = 4.63(30) \times 10^{-18} \text{ cm}^2.$$
 (26)



FIG. 9. Photoionization cross section of  $5P_{3/2}$  Rb state. Grey area corresponds to the theoretical results inferred from plot. The vertical dashed line denotes the photoionization threshold. Filled circles are our results. Other data points are experimental results extracted from the literature.



FIG. 10. Photoionization cross section of  $5S_{1/2}$  Rb state. The vertical dashed line denotes the photoionization threshold. Filled circle is our result. Other data points are experimental (Mohler, Marr, Lowell, Ciampini), theoretical (Chang, Aymar) and semiempirical (Weisheit) results extracted from the literature.

The uncertainty of  $\sigma_{5P_{3/2}}^{253.7}$  involves the accuracy of the weighted linear fit as well as the uncertainty of the measurement of  $\sigma_{5S_{1/2}}^{253.7}$ .

## **IV. DISCUSSION**

Our results are compared with data determined by other groups. Figures 9 and 10 show the dependence of the photoionization cross sections for  $5P_{3/2}$  and  $5S_{1/2}$  states on laser wavelength, respectively. All our results are consistent with previously reported experimental results [2,15,16,22,33–36] as well as theoretical predictions [13,37,38]. The value of  $\sigma_{5S_{1/2}}^{253.7}$  determined here confirms earlier results indicating that near this wavelength the Cooper minimum of the photoionization cross section for  $5S_{1/2}$  state is expected [13,35,36,38]. Our measured value  $\sigma_{5F_{3/2}}^{253.7}$  is a precise determination of the photoionization cross section for the  $5P_{3/2}$  state.

## V. CONCLUSION

In conclusion, we have determined the values of the Rb photoionization cross sections at 253.7 nm to be  $1.0^{+4.3}_{-1} \times 10^{-20}$  cm<sup>2</sup> and  $4.63(30) \times 10^{-18}$  cm<sup>2</sup> for  $5S_{1/2}$  and  $5P_{3/2}$  states, respectively. Additionally, the photoionization cross section for the  $5P_{3/2}$  state at 401.5 nm was found to be  $1.18(10) \times 10^{-17}$  cm<sup>2</sup>. Our results are consistent with the data reported by other groups. We have found that the cross section for the photoionization of Rb close to 254 nm is small enough to restrain the Rb losses when the trap is spatially overlapped with Hg MOT.

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