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Two-photon excitation of rubidium atoms inside porous glass

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We study the two-photon laser excitation to the $5D_{5/2}$ energy level of ⁸⁵Rb atoms contained in the interstices of a porous material made from sintered ground glass with typical pore dimensions in the $10-100~\mu m$ range. The excitation spectra show unusual flat-top line shapes, which are shown to be the consequence of wave-vector randomization of the laser light in the porous material. For large atomic densities, the spectra are affected by radiation trapping around the D_2 transitions. The effect of the transient atomic response limited by the time of flight between pores walls appears to have a minor influence in the excitation spectra. It is however revealed by the shortening of the temporal evolution of the emitted blue light following a sudden switch-off of the laser excitation.

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I. INTRODUCTION

Light propagation in disordered systems is a subject of growing interest [1]. Motivated in particular by applications to medical imaging, much large attention has been paid to the study of light propagation in highly scattering and turbid media [2]. From a fundamental perspective, random media are studied in connection to Anderson's light localization [3] and as a possible support for random lasers [4]. Also, light propagation in random media has been suggested as a means to enhance spectroscopic sensitivity [5,6] and for energy storage [7].

The atoms from a dilute gas contained in the interstices of the random material can be seen as convenient local probes of the light inside the disordered medium. In addition, the atomic response to the light is affected, under suitable conditions, by the spatial confinement of the atomic motion imposed by the random material. Such confinement effects can have spectroscopic consequences, which in turn can be used to characterize the random medium [8].

The spectroscopic study of atoms under confinement began with one-dimensional confinement in vapor cells limited by flat transparent parallel windows with separations of the order of a few to hundred microns [9]. In these cells, due to the Doppler effect, laser excitation selects atoms with a well-defined velocity component in the direction of confinement. Since the atom-light interaction is limited by the time of flight between opposing windows, the response is enhanced for atoms with a small velocity component in the direction of confinement resulting in sub-Doppler structures in the transmission spectrum [9,10]. More recently, the study of atoms in thin cells was extended to submicron and even subwavelength cell length and novel effects were reported such as Dicke narrowing [11].

Two-dimensional atomic confinement was achieved and studied inside hollow optical fibers or photonic waveguides [12–14]. The limited time of flight of the atoms in the direction perpendicular to the fiber or waveguide axis can result in broadening of the excitation spectrum of the atoms by the fiber-guided light.

Few studies are concerned with atoms under three-dimensional confinement. Ballin *et al.* [15] recently reported the study of Cs atoms confined to the empty volume within a regular three-dimensional array of nanometric opals. Our work, concerned with vapor contained in the micrometric interstices of a porous medium, can be seen as an implementation of a three-dimensional confinement.

The study of atoms inside disordered porous media was initiated by Svensson *et al.* [5], who studied the absorption of O_2 molecules in a porous ceramic. In previous work we addressed the spectroscopic study of rubidium vapor inside the micrometric interstices of porous glass. We studied first one-photon atomic resonances in the transmission spectrum of the light exiting the porous sample after diffusion [8] or backscattering from the incident surface [16]. Later, the nonlinear pump-probe spectroscopy was studied using two lasers in resonance with the Rb D_1 lines [17]. In the present work we report the observation of two-photon excitation of 85 Rb atoms to the $5D_{5/2}$ energy level inside a porous material.

Our sample is made by compaction of ground glass grains. The shape of the interstices is random and highly irregular. Typical dimensions of the interstices are in the range 10–100 μm depending on the sample. Rubidium atoms are present as vapor inside the interstice volume and also in the condensed phase on the glass surface of the pores. The gas phase density can be controlled through temperature.

The porous sample is an efficient light scatterer. Light propagation inside the porous medium is diffusive with a mean free path estimated to be a few tenths of a millimeter. After penetrating a distance of several mean free paths, the light propagating inside the sample becomes a speckle field with random variations of amplitude, phase, and polarization over distances of the order of the optical wavelength [18]. Alternatively, the field inside the sample can be thought of as a superposition of plane waves with random wave vectors, amplitudes, and polarizations.

Due to their thermal motion, during typical light-atom interaction time, the atoms travel distances that are larger than the optical wavelength, thus exploring substantial changes in the optical field. Another consequence of the field randomization is that photons originated from the laser or emitted by the atoms cannot be distinguished by the direction of propagation

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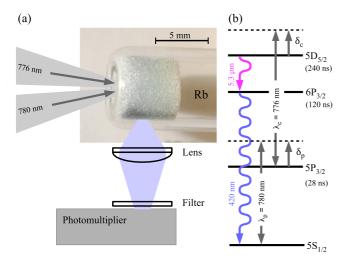


FIG. 1. (a) Experimental setup showing a porous cell. The lens images a portion of the porous medium surface on the photomultiplier window. The interferometric filter is centered around 420 nm with a 10-nm bandwidth. (b) Atomic levels and optical fields involved in the experiment.

since both experience similar diffusive propagation. Also, for sufficiently large vapor densities, the diffusive propagation of emitted photons through the sample favors reabsorption by resonant atoms leading to photon trapping [8].

A simplified energy-level scheme of ^{85}Rb is presented in Fig. 1. The hyperfine level structure is not shown. For the excited states $5P_{3/2}$ and $5D_{5/2}$ the maximum hyperfine level separations are 93 and 34 MHz, respectively, which are substantially smaller than the Doppler width. Two-photon excitation was achieved along the process $5S_{1/2} \rightarrow 5P_{3/2} \rightarrow 5D_{5/2}$. The excited level $5D_{5/2}$ has a 239-ns lifetime [19]. Its main radiative decay path involves an infrared transition to levels $6P_{3/2}$ followed by the emission of blue light with 420-nm wavelength [20].

II. EXPERIMENTAL SETUP

A picture of a porous sample is shown in Fig. 1(a). The samples were obtained from ground glass compacted and sintered at the flat end of a cylindrical 6-mm-diam glass tube. The size of glass particles was selected using sieves and decantation columns. The cell was sealed under vacuum after introducing a small amount of condensed Rb through distillation. Three different cells were used in the experiments with typical grain sizes of 10, 50, and 100 μ m. The actual statistical distribution of pore dimensions in our samples is yet unknown. We assume throughout this work that the typical pore dimensions are comparable to the corresponding typical grain size. Additional details on the cell fabrications are provided in Refs. [8,16]. During the experiments the cells were placed inside an oven for atomic density control by temperature variation.

We used two independent extended cavity diode lasers: a pumping laser operating around the D_2 lines of Rb (780 nm) and a coupling laser operating around the $5P_{3/2} \rightarrow 5D_{5/2}$ transition (776 nm). A frequency reference for the pumping laser was obtained from a saturation absorption setup. The

coupling laser frequency was measured with a wavemeter with a resolution of ± 25 MHz.

The pump and coupling laser powers were 15 and 10 mW, respectively. The laser beams were directed to the flat end of the sample glass tube. Due to losses at the grain surfaces and leakage from the sample border, a strong decrease of the light intensity occurs as the light penetrates the porous medium.

Detection is achieved using a lens that produces the image of a portion of the sample lateral surface on a photomultiplier tube. The selected surface is separated from the flat end of the tube by several millimeters to ensure that the collected light had a diffusive propagation while traveling inside the sample. A blue transmitting dielectric bandpass filter (10-nm bandwidth) was placed at the entrance of the photomultiplier tube to select the 420-nm emission and reject laser light.

The excitation spectra were recorded by tuning one laser while keeping the second laser frequency constant. In addition, we studied the transient decay of the emission at 420 nm arising when both lasers are tuned to resonance. For this the light from one laser was suddenly turned off with the help of an optical fiber Mach-Zehnder modulator (switching time $\lesssim 10 \text{ ns}$).

III. EXCITATION SPECTRA

Figure 2 shows the two-photon excitation spectra obtained scanning either the pump or the coupling laser for different detunings of the fixed frequency laser. In these plots the zero of the detuning axis corresponds to the position where the maximum signal is observed after freely varying both lasers frequencies. These line centers are located approximately at the maximum of the Doppler broadened absorption line of the corresponding transition (including the unresolved hyperfine structure). Figures 2(a) and 2(b) correspond to spectra taken at low atomic density ($T \approx 40\,^{\circ}\text{C}$) while Figs. 2(c)–2(e) correspond to large atomic density ($T \approx 120\,^{\circ}\text{C}$).

One noticeable property of the spectra in Fig. 2 is their symmetry with respect to zero detuning (a minor asymmetry can be attributed to the unresolved hyperfine structures). This fact is strikingly different from what occurs in ordinary vapor cells where, in general (depending on the angle between laser beams), the spectra are asymmetric with respect to the atomic resonance frequency and present maxima whose positions vary according to the detuning of the coupling field (see, for instance, [21]). Another remarkable feature in the spectra, visible in Figs. 2(a)–2(c) and 2(e), is the occurrence of flat-top line shapes whose width is approximately given by twice the absolute value of the detuning of the coupling laser.

We interpret these two properties as the consequence of the field randomization inside the porous material. A simplified description of two-photon excitation identifies two different excitation channels [22]: a stepwise excitation in which the atom is first promoted to the intermediate state from which it is excited to the final state and a direct excitation in which the atom is directly promoted from the ground level to the final level via the absorption of a photon from each field whose total energy equals the energy separation between initial and final levels. While the coherence between fields is not required for the stepwise process, it is an essential condition for the direct mechanism that requires the induction

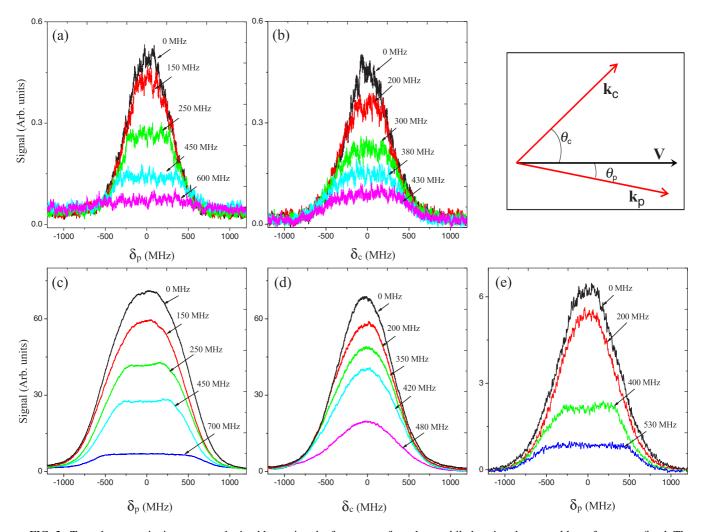


FIG. 2. Two-photon excitation spectra obtained by tuning the frequency of one laser while keeping the second laser frequency fixed. The detuning of the fixed frequency laser is indicated for each plot. (a)–(d) Cell with a 100- μ m typical pore size and (e) cell with a 10- μ m typical pore size at (a) and (b) $T \approx 40$ °C and (c)–(e) $T \approx 120$ °C. The inset shows the atomic velocity and two randomly oriented pump and coupling photons wave vectors.

of atomic coherence between $5S_{1/2}$ and $5D_{5/2}$ levels. Field randomization is responsible for the rapid variation of the field's relative phase during the light-atom interaction process. Relative phase variations occur at the time scale of $\lambda/\bar{v}\approx 3$ ns (where λ is the optical wavelength and \bar{v} is the most probable atomic velocity modulus), while the atomic coherence between $5S_{1/2}$ and $5D_{5/2}$ evolves at a time scale of the order of the lifetime of the excited state of a few hundred nanoseconds. This results in strong inhibition of the direct excitation channel.

Neglecting the homogeneous linewidth of the atomic transitions, for an atom moving with velocity \mathbf{v} in the presence of two fields with wave vectors \mathbf{k}_p and \mathbf{k}_c , the resonance conditions for the stepwise process are

$$\delta_p \simeq \mathbf{k}_p \cdot \mathbf{v} = k_p v \cos(\theta_p), \tag{1a}$$

$$\delta_c \simeq \mathbf{k}_c \cdot \mathbf{v} = k_c v \cos(\theta_c),$$
 (1b)

where the detunings δ_p and δ_c are defined in Fig. 1 and θ_p and θ_c refer to the angles between the atom velocity and the

corresponding wave vector (see the inset in Fig. 2). For the direct process the resonance condition is

$$\delta_p + \delta_c \simeq (\mathbf{k_p} + \mathbf{k_c}) \cdot \mathbf{v}.$$
 (2)

If the detuning δ_c is fixed, in the stepwise process the atomic velocity is selected though the condition (1b). For a selected velocity, the values of δ_p that satisfy the condition (1a) have an even distribution around $\delta_p = 0$ as a consequence of the isotropic random orientation of the wave vector \mathbf{k}_p in the speckle field. On the other hand, for the direct process (2) the wave-vector randomization leads to a distribution of δ_p centered around $-\delta_c$. Analogous arguments apply if the roles of the pump and coupling fields are reversed.

The fact that the observed spectra are centered on the atomic resonance transition and there is no observable peak opposite to the detuning of the fixed-frequency laser is a strong indication that the direct process is inhibited inside the porous medium. A simple qualitative explanation can be given as follows for the plateaulike spectra observed in Figs. 2(a)-2(c) and 2(e) [23]. Considering δ_c as a fixed detuning, $|\delta_c|/k_c$ determines the minimum velocity for the verification of Eq. (1b). For

velocities above this minimum, for any value of $|\delta_p|$ smaller than $k_p |\delta_c|/k_c$, Eq. (1a) can be fulfilled for some angle θ_p . The plateau originates from the uniform distribution probability for $\cos(\theta_p)$. The plateau ends when $|\delta_p| = k_p |\delta_c|/k_c$. For larger values of $|\delta_p|$, Eq. (1a) determines the minimum required atomic velocity thus reducing the number of atoms participating in the process as $|\delta_p|$ is increased.

For the two-photon stepwise excitation process, the excitation probability $S_0(\nu_p,\nu_c)$ for an atom traveling with velocity ${\bf v}$ in the presence of laser fields with wave vectors ${\bf k}_p$ and ${\bf k}_c$ is given by

$$S_0(\nu_p, \nu_c) \propto F_p \left(\nu_p - \frac{v}{\lambda_p} \cos \theta_p\right) F_c \left(\nu_c - \frac{v}{\lambda_c} \cos \theta_c\right),$$
 (3)

where $v_{p(c)}$, $\lambda_{p(c)}$, and $F_{p(c)}(v)$ represent, respectively, the frequency, wavelength, and normalized absorption profile in the atomic reference frame for the field and transition corresponding to the pump (coupling) field. In vapor cell spectroscopy the functions $F_{p(c)}(v)$ are usually considered to be homogeneous over the atomic ensemble. However, one has to keep in mind that for atoms confined in small volumes these functions could depend on the atomic velocity and position. Initially neglecting such dependences, the excitation spectrum profile can be obtained by summation over all possible atomic velocities and all orientations of vectors \mathbf{k}_p and \mathbf{k}_c ,

$$S(\nu_p, \nu_c)$$

$$\propto \int_0^{\pi} \sin \theta_p d\theta_p \int_0^{\pi} \sin \theta_c d\theta_c \int_0^{\infty} \mathcal{V}(v) S_0(\nu_p, \nu_c) dv, \quad (4)$$

where V(v) is the probability distribution of the atomic velocity modulus

An equation similar to Eq. (4) was previously encountered in the context of radiation trapping and near-resonance frequency redistribution in an atomic vapor [24]. In that context, v_p and v_c refer to the frequencies of the absorbed and reemitted photons, respectively. Similarly to our case where photons with random polarization arrive from random directions, radiated photons are emitted in a random direction (provided that polarization is not considered). The two problems are thus intimately connected. However, in the case of radiation redistribution, Eq. (3) is replaced by

$$S_0(\nu_p, \nu_c) \propto F_p \left(\nu_p - \frac{v}{\lambda_p} \cos \theta_p \right)$$

$$\times p \left(\nu_c - \frac{v}{\lambda_c} \cos \theta_c, \nu_p - \frac{v}{\lambda_p} \cos \theta_p \right), \quad (5)$$

where $p(\nu, \nu')$ is the probability for emission of a photon of frequency ν after absorption of a photon of frequency ν' in the atomic rest frame.

Equation (5) reduces to the form of Eq. (3) in two particular cases: (a) an infinitely narrow transition and perfectly elastic light scattering $[F_p(\nu) = \delta(\nu - \nu_0), p(\nu, \nu') = \delta(\nu - \nu')]$ and (b) uncorrelated frequencies in the atomic reference frame for emitted and absorbed photons. These two cases are discussed in Ref. [24] and for case (a) an analytical expression for $S(\nu_p, \nu_c)$ is given.

The spectrum profiles calculated using Eq. (4) are shown in Fig. 3. In this figure the laser detunings are expressed in

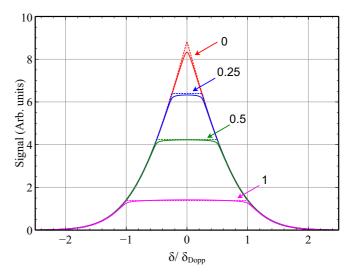


FIG. 3. Calculated excitation spectra as a function of the scanned laser detuning calculated using Eq. (4) for different values of the fixed-frequency laser detuning. Both detunings are expressed in units of the corresponding Doppler width $\delta_{\text{Dopp}} \equiv \sqrt{2k_BT/m}/\lambda$. Dashed lines show the negligible absorption width and solid lines the Lorentzian absorption line shapes with linewidth determined by the $5P_{3/2}$ radiative decay rate (6 MHz).

units of the corresponding Doppler detuning $\delta_{\text{Dopp}} \equiv \bar{v}/\lambda$, where $\bar{v} \equiv \sqrt{2k_BT/m}$ ($\bar{v} \approx 240$ m/s at room temperature corresponding to $\delta_{\text{Dopp}} \approx 310$ MHz for $\lambda = 780$ nm). The dotted lines correspond to the assumption of infinitely narrow absorption profiles for the lower and upper atomic transitions. Note the perfectly flat top of the spectra and the singularities in the spectral function derivative occurring for $|\delta_p|\lambda_p = |\delta_c|\lambda_c$. A better approximation to the experimentally observed line shapes is obtained when the width of the atomic absorption line is considered. The plots shown in Fig. 3 (solid lines) assume Lorentzian absorption line shapes with width determined by the intermediate level $(5P_{3/2})$ radiative decay rate (6 MHz). The flat tops of the spectral lines are now slightly rounded and the singularity in the derivative is eliminated. Keeping in mind that the unresolved hyperfine structure introduces additional broadening in the experimental spectra, satisfactory agreement with the theoretical simulations is observed.

As already mentioned, the assumption of homogeneous atomic absorption spectral profiles can be questioned for atoms under confinement. We have numerically evaluated the excitation spectra considering the transient atomic response of the atoms starting when the atom leaves a pore wall and ending when it collides with another wall. Such transient evolution introduces a velocity and position dependence of the atomic response. Our computation was based on assumptions about the statistical distribution of atomic trajectories inside the pores. However, for all reasonable assumptions consistent with the estimated pore sizes, the effect of the transient evolutions on the excitation line shape appears to be minor and is not presented here.

It is worth mentioning that in the context of the theory of radiation trapping the curves plotted in Fig. 3 represent an idealized process corresponding to a single absorption-radiation cycle [23]. Experimental verification of these

predictions is elusive or indirect since in actual radiation trapping experiments multiple absorption-radiation cycles occur and significantly modify the spectrum. Our result can be seen as an experimental test of the predictions corresponding to the single absorption-radiation cycle.

Figures 2(a) and 2(b) correspond to relatively low atomic density ($T \sim 40$ °C). Under these conditions the excitation spectra obtained by exchanging the fixed and scanning frequency lasers show similar features including the flat-top spectra. Notice, however, that the spectra obtained when the coupling laser is scanned [Fig. 2(b)] are not as neatly flat. This asymmetry under exchange of the roles of the two laser fields is not compatible with Eq. (4). The asymmetry becomes more evident as the density of the sample is increased. Figures 2(c) and 2(d) were taken at a temperature $T \sim 120$ °C. The two sets of spectra are now clearly different. Flat-top spectra are obtained when the pump laser is scanned and an overall broadening is observed. On the other hand, bell-shaped lines with no noticeable dependence on the pump frequency position are observed when the coupling laser is scanned. We interpret this asymmetric behavior as the consequence of the onset of photon trapping.

Photon trapping around the resonant $5S_{1/2}(F=2) \rightarrow 5P_{3/2}$ transition is known to occur in our samples when the atomic density is sufficiently large [16]. On the other hand, negligible photon trapping is expected to occur around the $5P_{3/2} \rightarrow 5D_{5/2}$ transition due to the small population in the $5P_{3/2}$ level.

When photon trapping occurs around the lower transition, an additional path for two-photon excitation is possible involving one-photon reemitted around the $5S_{1/2} \rightarrow 5P_{3/2}$ transition and one photon from the coupling laser. If the pump laser frequency is not too far detuned from the Doppler broadened atomic absorption line and for large enough atomic densities the spectrum of the trapped photons closely approaches the absorption profile with little dependence on the pump laser detuning [24]. In consequence, when the pump laser frequency is scanned the contribution to the spectrum of the two photon-excitation mechanism involving reemitted photons remains approximately constant until the pump field detuning is sufficiently large ($|\delta_p| \gtrsim 2\delta_{\text{Dopp}}$ [24]). We attribute the spectral broadening observed in all spectra in Fig. 2(c) to the contribution of trapped photons to the excitation of level $5D_{5/2}$. Conversely, when the coupling laser is scanned, the excitation mechanism involving trapped photons results in a contribution to the spectrum that roughly follows the spectral density of the trapped photons, which is essentially independent from the pump field detuning [Fig. 2(d)].

The features appearing in the excitation spectra described above show variations over a typical scale of the order of ~ 100 MHz. On the other hand, the frequency scale associated with the atomic flight between pore walls is of the order of \bar{v}/L , where L is the characteristic pore size. For our samples with typical pore sizes in the 10– $100~\mu m$ range, the frequency scale associated with confinement corresponds to 2–20 MHz. In consequence, the effect of the transient atomic evolution due to confinement is expected to have a small influence on the excitation spectra. This expectation is experimentally supported by the similarities between the spectra taken with the 100- μm pores cell [Fig. 2(c)] and with the 10- μm pores

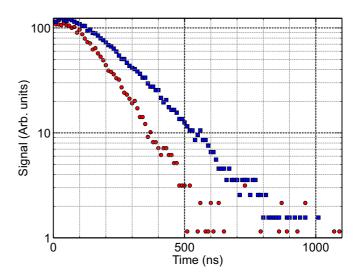


FIG. 4. Temporal evolution of the blue fluorescence after turn-off of the coupling laser. Blue squares represent light from unconfined vapor and red circles light form porous sample.

cell [Fig. 2(e)] when the pump laser is scanned. An overall narrowing of the spectra in Fig. 2(e) compared to Fig. 2(c) can be attributed to a reduced contribution of the two-photon excitation mechanism involving trapped photons [8].

IV. TRANSIENT SIGNAL DECAY

In order to detect the effect of spatial confinement on the atomic response, we study the temporal decay of the emitted blue radiation after a sudden switch-off of the coupling laser using a porous cell with typical pore size of 50 μ m. In these measurements the temperature of the cell is kept at $T=120\,^{\circ}\mathrm{C}$ and both lasers are tuned to line center ($\delta_p=\delta_c=0$). In the absence of any spatial confinement effect, sufficiently long after the turning off of the coupling laser, the blue fluorescence is expected to decay exponentially with a decay time determined by the $5D_{5/2}$ level lifetime (239 ns) [19].

We initially record the transient signal originating from the portion of the glass tube that is not occupied by the porous material (see Fig. 1). For long times we measure an exponential decay time $\tau_u = 180 \pm 10$ ns (Fig. 4). We attribute this reduced decay time to collisions with contaminants present in the Rb vapor.

We next measure the long-time decay time for the blue light originating from the porous medium. A shorter decay time $\tau_c=120\pm10$ ns is observed. Since the gas composition is expected to be the same inside and outside the porous medium, we attribute this additional shortening to the interruption of the emission process by the collisions of the atoms to the cell walls. From the two observed decay times we deduce a characteristic time $\tau_F\approx 360\pm100$ ns for the atomic time of flight between collisions with the pore walls $[\tau_F\equiv (\tau_c^{-1}-\tau_u^{-1})^{-1}]$. Considering the typical dimension of the pores $(\sim\!50~\mu\mathrm{m})$ the typical time of flight corresponds to a velocity $v_F\approx 140\pm40~\mathrm{m/s}$. This velocity is smaller than the mean velocity \bar{v} , which suggests that the two-photon excitation involving diffuse fields could favor slow atoms.

V. CONCLUSION

We have observed and studied the two-photon excitation of an alkali-metal vapor confined to the micrometer-size interstices of a porous glass. Due to the diffuse nature of the light fields, the two-photon excitation is essentially due to a stepwise process involving the excitation of the intermediate state. In consequence, the excitation spectra are centered around the atomic transitions. In addition, the field wave-vector randomization results in singular plateaulike line shapes similar to those predicted for the spectrum of the light emitted from a resonant atomic vapor in a single absorption-emission cycle. A significant reduction of the fluorescence decay time was measured as a consequence of the spatial confinement of atoms excited to a long-lived excited state. Further investigation is required to

plore velocity selection in two-photon excitation by diffuse fields.

The cells considered in this work have typical pore dimensions that are larger than the optical wavelength. The radiation spectra of atoms contained in the interstices of porous samples prepared with submicrometer pore sizes should reveal features corresponding to a regime in which the effects of confinement are dominant.

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- [1] D. S. Wiersma, Nat. Photon. 7, 188 (2013).
- [2] A. Ishimaru, Wave Propagation and Scattering in Random Media (Academic, New York, 1978), Vol. 2.
- [3] M. Segev, Y. Silberberg, and D. N. Christodoulides, Nat. Photon. 7, 197 (2013).
- [4] D. S. Wiersma, Nat. Phys. 4, 359 (2008).
- [5] T. Svensson, E. Adolfsson, M. Lewander, C. T. Xu, and S. Svanberg, Phys. Rev. Lett. 107, 143901 (2011).
- [6] B. Redding, S. F. Liew, R. Sarma, and H. Cao, Nat. Photon. 7, 746 (2013).
- [7] C. Liu, A. Di Falco, D. Molinari, Y. Khan, B. S. Ooi, T. F. Krauss, and A. Fratalocchi, Nat. Photon. 7, 473 (2013).
- [8] S. Villalba, H. Failache, A. Laliotis, L. Lenci, S. Barreiro, and A. Lezama, Opt. Lett. 38, 193 (2013).
- [9] S. Briaudeau, D. Bloch, and M. Ducloy, Europhys. Lett. 35, 337 (1996).
- [10] S. Briaudeau, D. Bloch, and M. Ducloy, Phys. Rev. A 59, 3723 (1999).
- [11] D. Sarkisyan, T. Varzhapetyan, A. Sarkisyan, Y. Malakyan, A. Papoyan, A. Lezama, D. Bloch, and M. Ducloy, Phys. Rev. A 69, 065802 (2004).
- [12] F. Benabid, F. Couny, J. Knight, T. Birks, and P. S. J. Russell, Nature (London) 434, 488 (2005).

- [13] W. Yang, D. B. Conkey, B. Wu, D. Yin, A. R. Hawkins, and H. Schmidt, Nat. Photon. 1, 331 (2007).
- [14] C. Perrella, P. S. Light, J. D. Anstie, T. M. Stace, F. Benabid, and A. N. Luiten, Phys. Rev. A 87, 013818 (2013).
- [15] P. Ballin, E. Moufarej, I. Maurin, A. Laliotis, and D. Bloch, Appl. Phys. Lett. 102, 231115 (2013).
- [16] S. Villalba, A. Laliotis, L. Lenci, D. Bloch, A. Lezama, and H. Failache, Phys. Rev. A 89, 023422 (2014).
- [17] S. Villalba, H. Failache, L. Lenci, and A. Lezama, Phys. Rev. A 90, 052518 (2014).
- [18] J. W. Goodman, Speckle Phenomena in Optics: Theory and Applications (Roberts, Englewood, 2007).
- [19] D. Sheng, A. P. Galván, and L. A. Orozco, Phys. Rev. A 78, 062506 (2008).
- [20] O. S. Heavens, J. Opt. Soc. Am. 51, 1058 (1961).
- [21] J. E. Bjorkholm and P. F. Liao, Phys. Rev. A 14, 751 (1976).
- [22] P. R. Berman and V. S. Malinovsky, *Principles of Laser Spectroscopy and Quantum Optics* (Princeton University Press, Princeton, 2010).
- [23] J. C. de A. Carvalho, M. Oriá, M. Chevrollier, H. L. D. de S. Cavalcante, and T. P. de Silans, Phys. Rev. A 91, 053846 (2015).
- [24] A. F. Molisch and B. P. Oehry, *Radiation Trapping in Atomic Vapours* (Clarendon, Oxford, 1999).