Superscattering pattern shaping for radially anisotropic nanowires

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We achieve efficient shaping of superscattering by radially anisotropic nanowires relying on resonant multipolar interferences. It is shown that the radial anisotropy of refractive index can be employed to resonantly overlap electric and magnetic multipoles of various orders, and as a result, effective superscattering with different engineered angular patterns can be obtained. We further demonstrate that such superscattering shaping relying on unusual radial anisotropy parameters can be directly realized with isotropic multilayered nanowires, which may shed new light on much fundamental research and various applications related to scattering particles.

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I. INTRODUCTION

Stimulated by the recent demonstrations of optically induced magnetic responses in various nanostructures incorporating high-refractive-index materials [1-3], the principle of multipolar interferences has been widely applied in many particle-scattering-related systems and metasurfaces, provoking lots of applications and fundamental mechanism investigations in both the linear and the nonlinear regimes [4,5]. Among all the multipolar interference effects, an outstanding and attractive example is the efficient shaping of the superscattering that is beyond the single-channel scattering limit [6–8]. This manipulation relies on the resonant overlapping and interferences of electric and magnetic resonances of various orders [1–5] and can play a vital role in many applications that require simultaneous strong scattering and designed angular scattering patterns.

Conventional methods to resonantly overlap different multipoles supported by an individual particle rely on (i) a flat dispersion band or multiple dispersion bands to overlap electric resonances of different orders [6–8] and (ii) metal-dielectric hybrid nanostructures [9–12] or homogeneous dielectric particles of irregular shapes that are neither spherical nor cylindrical [13,14] to overlap electric and magnetic resonances. Recently it was shown that for fundamental homogeneous spherical particles, effective radial index anisotropy can be applied to significantly tune the positions of the electric resonances of various orders [15,16]. This enables flexible overlapping of multipoles of different natures (electric or magnetic) and/or orders, which results in multipolar interference-induced superscattering of different angular scattering patterns, including the ultradirectional forward superscattering [15,16]).

In this work, we extend our investigations of radial anisotropy-induced superscattering pattern shaping from three-dimensional (3D) spherical particles [15,16] to two-dimensional (2D) cylindrical ones. Such an extension is by no means trivial, considering that, compared to its 3D counterparts, the scattering of 2D nanowires shows polarization dependence and, more importantly, the number of degenerate scattering channels is quite different from that of 3D spherical particles for each resonance [9,11,17]. Here in this work we have achieved simultaneously, within radially

II. NORMAL SCATTERING OF PLANE WAVES BY RADIALLY ANISOTROPIC NANOWIRES

The scattering configuration we study is shown schematically in Fig. 1(a): a plane wave is normally incident on a homogeneous nanowire (of radius *R*) with wave vector **k** along *x*. Considering that the radial anisotropy of the refractive index can only affect the TM modes (with the magnetic field along the nanowire axis direction *z*) [20,21], here in this study we fix the electric field of the incident wave on the plane along *y*. The refractive indexes of the nanowire are n_r and n_t along the radial and azimuthal directions, respectively. The anisotropy parameter is defined as $\eta = n_t/n_r$. In this case the scattering properties can be analytically calculated, with the normalized scattering limit $2\lambda/\pi$ [6], where λ is the wavelength in the background medium) expressed as [11,20-22]

$$N_{\rm sca} = \sum_{m=-\infty}^{\infty} |a_m|^2.$$
 (1)

Here a_m is the scattering coefficient (*m* is the mode order that characterizes the field distributions along the azimuthal direction), and for TM incident waves, a_0 corresponds to the magnetic dipole (MD; **M**), $a_{\pm 1}$ corresponds to the electric dipole (ED; **D**), $a_{\pm 2}$ corresponds to the electric quadrupole (EQ; **Q**), and so on. It is clear that except for the MD, with only one scattering channel, all the other electric resonances correspond to two scattering channels which are degenerate as

anisotropic nanowires, flexible tuning of resonance positions and superscattering with different engineered scattering patterns induced by the interferences of multipoles resonantly overlapped. It is further shown that such efficient superscattering pattern shaping replying on naturally inaccessible anisotropy parameters can be simply realized within isotropic multilayered nanowires. Such an approach based on refractive index anisotropy renders an extra dimension of freedom for resonance tuning and scattering pattern shaping, which might play a significant role in various investigations into light-matter interactions and plenty of applications associated with particle scattering, such as nanoantennas, optical sensing and detection, scattering-particle-assisted passive radiation cooling, and photovoltaic devices [18,19].

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FIG. 1. (a) Schematic of a normally incident plane wave scattered by a radially anisotropic nanowire of radius R. The incident wave is TM polarized, with the magnetic field along the z direction and wave vector \mathbf{k} along the x direction. The radial and azimuthal indexes of the nanowire are n_r and n_t , respectively. The anisotropy parameter is $\eta = n_t/n_r$ and the scattering polar angle is θ . (b) The scattering spectra (normalized scattering cross section N_{sca}) with respect to the normalized size parameter α for a homogeneous isotropic nanowire $(\eta = 1)$. Both the total scattering spectrum and, also, the partial spectra of solely the MD, ED, and EQ are shown. The central resonant positions of the first two MDs, EDs, and EQs are indicated by $\mathbf{M}_{01,02}$ ($\alpha = \beta_{01,02} = 0.67, 1.661$), $\mathbf{D}_{11,12}$ ($\alpha = \beta_{11,12} = 1.02, 1.994$), and $Q_{21,22}$ ($\alpha = \beta_{21,22} = 1.384$, 2.326), respectively. The near-field distributions at these points are shown in (d)-(i), where color plots correspond to \mathbf{H}_z , vector plots correspond to electric fields in the x-y plane, and dashed circles denote the particle boundaries. (c) The scattering spectra of MDs, EDs, and EQs with anisotropy parameters of $\eta = 1.3$ and $\eta = 0.7$. In (b) and (c) the azimuthal index is fixed at $n_t = 3.5$, as is also the case in Figs. 2–4.

required by the symmetry of the nanowire [11,20-22],

$$a_m = a_{-m} = \frac{n_t \mathbf{J}_{\tilde{m}}(n_t \alpha) \mathbf{J}'_m(\alpha) - \mathbf{J}_m(\alpha) \mathbf{J}'_{\tilde{m}}(n_t \alpha)}{n_t \mathbf{J}_{\tilde{m}}(n_t \alpha) \mathbf{H}'_m(\alpha) - \mathbf{H}_m(\alpha) \mathbf{J}'_{\tilde{m}}(n_t \alpha)}, \quad (2)$$

where **J** and **H** are, respectively, the first-kind Bessel and Hankel functions [17]; α is the normalized size parameter $\alpha = kR$; \tilde{m} is the radial anisotropy-revised function order $\tilde{m} = m\eta$; and the accompanying primes indicate their differentiation with respect to the entire argument. According to Eq. (2), a_0 is independent of η . This is because for the MD, there are only electric fields along the azimuthal direction, and as a result, the MD is not affected by the radial anisotropy if the azimuthal index is fixed [see also Figs. 1(d) and 1(e)]. By definition, the spectral center of each resonance is located at $\alpha = \beta_{mq}$, which satisfies Here q is the radial mode number, which corresponds to the number of the field maximum points along the radius [see also Figs. 1(d)-1(i)].

To further exemplify what has been discussed above, in Fig. 1(b) we show the scattering spectra (α dependence of the normalized scattering cross section) of a homogeneous isotropic $(\eta = 1)$ nanowire. The azimuthal index of the nanowire investigated is fixed at $n_t = 3.5$ throughout this work unless otherwise specified. The spectral centers of the first two MDs, EDs, and EQs are indicated by $\mathbf{M}_{01,02}$, $\mathbf{D}_{11,12}$, and $\mathbf{Q}_{21,22}$, respectively. The corresponding near-field distributions of those resonances at the points indicated are shown in Figs. 1(d)–1(i), where both the magnetic fields along z (**H**_z; color plots) and the on-plane electric fields (vector plots) are shown. We emphasize that, to show specifically the characteristic field distributions of each resonance, in Figs. 1(d)-1(i)we plot the fields associated with each individual resonance only, where the contributions of other resonances are neglected [e.g., at \mathbf{Q}_{22} the fields associated with the ED and MD are not included in Fig. 1(i)].

The influence of the radial anisotropy on the spectral resonance positions is shown in Fig. 1(c), where the results for $\eta = 1.3$ and $\eta = 0.7$ are summarized. It is clear that with the azimuthal index fixed, a larger (smaller) η will blue-shift (red-shift) the EDs and EQs, with the MD unaffected. It is natural to expect from Fig. 1(c) that the radial anisotropy can be employed to flexibly overlap resonances of different natures (electric or magnetic), different orders *m*, and/or different radial mode numbers *q*. This can result in efficient shaping of the superscattering pattern achieved through the resonant interferences of the multipoles coexcited.

III. SUPERSCATTERING PATTERN SHAPING FOR RADIALLY ANISOTROPIC NANOWIRES

A. Fundamental mechanism and parity of multipolar scattering

With all the scattering coefficients obtained [see Eq. (2)], we can directly calculate the angular scattering amplitude $\Gamma(\theta)$ as [11,17]

$$\Gamma(\theta) = \sqrt{2/\pi k} \left| a_0 + 2 \sum_{m=1}^{\infty} a_m \cos(m\theta) \right|, \tag{4}$$

where k is the angular wave number (amplitude of wave vector **k**) in the background medium and θ is the scattering polar angle with respect to **k** on the x - y plane [see Fig. 1(a)]. For the two scattering directions (θ and $180^{\circ} - \theta$) that are symmetric with respect to the y direction and thus on opposite sides (forward or backward) of the scattering circle, considering that $\cos(m\theta) = (-1)^m \cos[m(180^{\circ} - \theta)]$, the scattering amplitudes show odd (even) parity for odd (even)-order resonances. This means that when resonances of different orders are coexcited, there are different types of interferences (constructive or destructive) for scattering amplitudes along different directions, which provides opportunities for efficient superscattering pattern shaping.

B. Superscattering pattern shaping through resonantly overlapping MDs and EDs

For cylindrical scattering particles, the simultaneous superscattering and efficient scattering pattern shaping was



FIG. 2. Scattering spectra with (a) $\eta = 0.109$ and (c) $\eta = 2.651$. Both the total spectra (black curve) and the partial contributions from MDs (green curve), EDs (red curve), and EQs (blue curve) are shown (as is the case in Figs. 3 and 4). The corresponding scattering amplitudes at the overlapping superscattering points indicated are shown, respectively, by solid blue curves in (b) at $\alpha = 0.67$ with $\eta = 0.109$ and in (d) at $\alpha = 1.661$ with $\eta = 2.651$. Here we also show the ideal scattering patterns with solely overlapped EDs and MDs by red crosses in (b) and (d).

first achieved in metal-dielectric core-shell nanowires through resonantly overlapping MDs and EDs [10,11]. Since for 2D nanowires, the number of MD scattering channels is only half that of ED scattering channels [Eq. (4)], the scattering is suppressed at other angles ($\theta = 120^{\circ}$ and 240°) [11] rather than in the backward direction ($\theta = 180^{\circ}$) for 3D metal-dielectric core-shell spherical particles [9]. Here we show the resonant overlapping of EDs and MDs within a homogeneous radially anisotropic nanowire, and the results are summarized in Fig. 2. Figure 2(a) shows the scattering spectra (both total and partial contributions) for $\eta = 0.109$, where it is clear that the anisotropy-induced red shift of the first ED (\mathbf{D}_{11}) enables its overlapping with the spectrally fixed first MD (M_{01}), leading to effective superscattering beyond the single-channel scattering limit ($N_{sca} = 1$) [6]. The scattering amplitude at the overlapping superscattering point $(\alpha = 0.67)$ is shown in Fig. 2(b) by the solid curve. Similarly to what has been achieved for core-shell nanowires [11], the scattering is suppressed in the backward half-scattering circle but enhanced in the forward half-scattering circle. This is due to the fact that (i) the scatterings of the ED and MD exhibit different parities (odd and even, respectively), and (ii) in the forward direction the two resonantly overlapped multipoles are always in phase according to the optical theorem [17]. For comparison, we also show in Fig. 2(b) by crosses the ideal scattering pattern of resonant overlapping of the ED and MD only with all other multipoles neglected ($a_0 = a_{\pm 1} = 1$, $a_{|m|>1} = 0$: $\Gamma(\theta) \propto |1 + \cos(\theta)|$. It is clear in Fig. 2(b) that the results of the two scenarios agree perfectly well, as the other multipoles can be effectively neglected at $\alpha = 0.67$ for $\eta = 0.109$ [see Fig. 2(a)].



FIG. 3. Scattering spectra with (a) $\eta = 0.0173$ and (c) $\eta = 1.414$. The corresponding scattering amplitudes at the overlapping superscattering points indicated are shown, respectively, by solid blue curves in (b) at $\alpha = 0.67$ with $\eta = 0.0173$ and in (d) of $\alpha = 1.661$ with $\eta = 1.414$. Here we also show the ideal scattering patterns with solely overlapped EQs and MDs by red crosses in (b) and (d).

The ED can also be engineered to resonantly overlap with the MD with a larger anisotropy parameter $\eta = 2.651$, as shown in Fig. 2(c), where the first ED (**D**₁₁) coincides spectrally with the second MD (**M**₀₂) at $\alpha = 1.661$. The corresponding scattering amplitude is shown in Fig. 2(d) (solid curve), which is slightly different from the ideal case (crosses). This is due to the fact that at $\alpha = 1.661$, the contributions of EQ are noneligible [see Fig. 2(c)].

C. Superscattering pattern shaping through resonantly overlapping MDs and EQs

According to Fig. 1(c), similarly to EDs, the spectral positions of EQs are also sensitive to η and thus the radial anisotropy can be employed to resonantly overlap EQs with MDs too, resulting in effective superscattering also. This is shown in Fig. 3(a) with $\eta = 0.0173$ and Fig. 3(c) with $\eta = 1.414$. In the former case the first EQ (\mathbf{Q}_{21}) is tuned to overlap with the first MD (M_{01}), while in the latter case it is the first EQ overlapped with the second MD (M_{02}). The corresponding scattering amplitudes at the overlapping superscattering points are shown by solid curves in Fig. 3(b) $(\alpha = 0.67 \text{ with } \eta = 0.0173)$ and Fig. 3(d) $(\alpha = 1.661 \text{ with } \eta = 0.0173)$ $\eta = 1.414$) together with the ideal scattering patterns (crosses) with only resonantly overlapped EQ and MD: $\Gamma(\theta) \propto |1 +$ $\cos(2\theta)$. The discrepancy in Fig. 3(b) originates from the noneligible contributions of the ED [see Fig. 3(a)], while in Fig. 3(d) the two sets of results are perfectly matched, as effectively there are no other multipolar contributions at the overlapping superscattering point [see Fig. 3(c)]. In contrast to the scattering patterns of overlapped MDs and EDs shown in Figs. 2(b) and 2(d), the scattering amplitudes are symmetric in the forward and backward half-scattering circles, which is induced by the same even parity of the scatterings of the MD and EQ. The complete destructive interferences still



FIG. 4. Scattering spectra with (a) $\eta = 0.11$ and (c) $\eta = 3.21$. The corresponding scattering amplitudes at the overlapping superscattering points are shown, respectively, by solid blue curves in (b) at $\alpha = 1.585$ with $\eta = 0.11$ and in (d) at $\alpha = 2.944$ with $\eta = 3.21$. Here we also show the ideal scattering patterns with pure overlapped EQs and EDs by red crosses in (b) and (d).

significantly suppress [Fig. 3(b)] or fully eliminate [Fig. 3(d)] the scattering at $\theta = 60^{\circ}$, 120° , 240° , and 300° .

D. Superscattering pattern shaping through resonantly overlapping EDs and EQs

Up to now, we have managed to resonantly overlap spectrally η -sensitive electric multipoles with spectrally fixed MDs relying on radial anisotropy. Though both EDs and EQs will red-shift (blue-shift) with smaller (larger) η [see Fig. 1(c)], it is also possible to overlap them as shown in Fig. 4(a) $[\eta = 0.11;$ second EQ (\mathbf{Q}_{22}) with second ED (\mathbf{D}_{12})] and in Fig. 4(c) [$\eta = 3.21$; first EQ (Q_{21}) with second ED]. The scattering patterns at the overlapping superscattering points ($\alpha = 1.585$, 2.944) are shown in Figs. 4(b) and 4(d), respectively, by solid curves, where the ideal scattering amplitudes with pure resonantly overlapped ED and EQ $[\Gamma(\theta) \propto |\cos(\theta) + \cos(2\theta)|]$ are also shown by crosses. The discrepancies exist for both scenarios, as at both overlapping superscattering points the contributions from MDs cannot be neglected [see Figs. 4(b) and 4(d)]. Similar to what is shown in Figs. 2(b) and 2(d), the symmetry of the scattering amplitudes in the forward and backward half-scattering circles is also broken since the parities of the ED and EQ scattering are different (odd and even, respectively). It is clear that the interferences of ED and EQ can significantly suppress the backward reflection and also scattering at the other two angles in the forward half-scattering circle ($\theta = 60^{\circ}$ and 300°).

IV. SUPERSCATTERING PATTERN SHAPING FOR MULTILAYERED ISOTROPIC NANOWIRES WITH EFFECTIVE RADIAL ANISOTROPY

In the discussions above about homogeneous anisotropic nanowires, we have employed unusual anisotropy parameters that are inaccessible for natural materials. Nevertheless, the recent rapid development of the field of metamaterials has provided lots of opportunities to obtain extreme anisotropy parameters in various artificial structures [23,24]. For example, effectively large radial anisotropy parameters can be obtained in a multilayered nanowire that is shown schematically in Fig. 5(a) [2,20,21,24]. This core-shell structure is made of alternating isotropic layers of two refractive indexes, n_1 and n_2 . According to the effective medium theory, the whole multilayered isotropic structure can be viewed effectively as a homogeneous radially anisotropic nanowire, with radial and azimuthal indexes expressed, respectively, as [16,20,21]

$$n_{\rm r} = n_1 n_2 / \sqrt{(1-f)n_1^2 + f n_2^2},$$

$$n_{\rm t} = \sqrt{f n_1^2 + (1-f)n_2^2},$$
(5)

where *f* is the filling factor of the layer of index n_1 (the overall thickness of all the layers of index n_1 divided by the radius of the whole structure R_m).

First, we study a 30-layered nanowire made of alternating dielectric layers of $n_1 = 5.54$ (each layer width is $d_1 =$ $R_m/30$) and $n_2 = 1.12$ (each layer width is $d_2 = R_m/30$), and thus $f = d_1/(d_1 + d_2) = 0.5$. According to Eq. (5), the corresponding effective parameter is $\eta = 2.57$ and $n_t = 4$. The scattering spectra of this multilayered nanowire (which can be analytically calculated based on generalized Mie theory [17]) and of its corresponding homogeneous anisotropic nanowire are shown in Figs. 5(b) and 5(c), respectively. The two sets of spectra agree quite well (validating the effectiveness of the effective medium theory employed) and for both cases the first ED (\mathbf{D}_{11}) can be tuned to resonantly overlap with the second MD (M₀₂), at $\alpha = 1.408$ and $\alpha = 1.419$, respectively. The spectra of the anisotropic nanowire [Fig. 5(c)] is blue-shifted compared to those of the isotropic one [Fig. 5(b)], and such discrepancies can be fully eliminated by decreasing each consisting isotropic layer width, as is also the case for Figs. 5(e) and 5(f). The scattering amplitudes at the overlapping superscattering points are shown in Figs. 5(d) for both cases, which are almost the same as what is shown in Fig. 2(d).

We also study another similar 30-layered nanowire with $n_1 = 5.54$ ($d_1 = 2R_m/75$), $n_2 = 2.5$ ($d_2 = 3R_m/75$), and f = 0.4, which corresponds to effective parameters of $\eta = 1.322$ and $n_t = 4$. The scattering spectra for both isotropic and anisotropic nanowires are shown in Figs. 5(e) and 5(f), where it is clear that the first EQ (\mathbf{Q}_{21}) and the second MD (\mathbf{M}_{02}) are resonantly overlapped. The scattering amplitudes at the overlapping superscattering points (isotropic nanowire, $\alpha = 1.403$; anisotropic nanowire, $\alpha = 1.419$) are shown in Fig. 5(g), which are more or less the same as those shown in Fig. 3(d).

It is worth mentioning that here we have confined our studies to all-dielectric nanowires with $n_1 > 0$ and $n_2 > 0$, which according to Eq. (5) leads to $\eta = n_t/n_r > 1$. Nevertheless, when we go beyond the all-dielectric regime, such as incorporating metals into the multilayered configurations, $\eta < 1$ and even more exotic anisotropic parameters can be obtained [16,24]. As a result, it is expected that other superscattering features shown in Figs. 2–4 can be also observed within multilayered isotropic nanowires.



FIG. 5. (a) Schematic of a multilayered nanowire made of alternate isotropic layers of refractive indexes n_1 (each layer width d_1) and n_2 (each layer width d_2), and thus $f = d_1/(d_1 + d_2)$. The radius of the whole nanowire is R_m . Scattering spectra of the 30-layered nanowire are shown in (b) with $n_1 = 5.54$, $n_2 = 1.12$, $d_1 = d_2 = R_m/30$, f = 0.5 and in (e) with $n_1 = 5.54$, $n_2 = 2.5$, $d_1 = 2d_2/3 = 2R_m/75$, f = 0.4. The scattering spectra of the corresponding anisotropic homogeneous nanowires are shown, respectively, in (c) with $n_t = 4$ and $\eta = 2.57$ and in (f) with $n_t = 4$ and $\eta = 1.322$. The first ED (**D**₁₁) and the second MD (**M**₀₂) are resonantly overlapped in (b) at $\alpha = 1.408$ and in (c) at $\alpha = 1.419$. (d) The scattering amplitudes at these superscattering points indicated in (b) and (c). The first EQ (**Q**₂₁) and the second MD are resonantly overlapped in (e) at $\alpha = 1.403$ and in (f) at $\alpha = 1.419$. (g) The scattering amplitudes at these superscattering points indicated in (e) and (f).

V. CONCLUSIONS AND OUTLOOK

In conclusion, we investigate the scattering properties of radially anisotropic nanowires and have achieved superscattering with engineered angular distributions. The efficient shaping of the superscattering pattern achieved originates from the resonant overlapping and different sorts of interferences between the electric and the magnetic multipoles coexcited, which is made possible by incorporating the radial anisotropy of the refractive index into homogeneous nanowires. We further demonstrate that the large anisotropy parameters required that are inaccessible for natural materials can be realized in artificial multilayered isotropic core-shell nanowires, where multipolar interference-induced superscattering manipulation can also be obtained.

Here in this work, we confine our investigations to lower order resonances up to quadrupoles ($m \le 2$) with small radial mode numbers ($q \le 2$) and have discussed only the case of two overlapped resonances. Similar studies can certainly be extended to higher order modes with larger radial mode numbers and to the cases of more than two overlapped resonances [12], where we expect extra flexibilities for more efficient superscattering pattern shaping. Moreover, the principle we have revealed here can also be applied to particle clusters and periodic arrays [25–27], where the eigenmodes of the whole system can be tuned by the index anisotropy and this may render much more opportunities for superscattering pattern shaping replying on the extra dimension of freedom of interparticle interaction control. At the same time, other kinds of anisotropy such as magnetic anisotropy can also be employed [28]. We anticipate that the approach based on anisotropy to achieve simultaneous superscattering and efficient scattering angular distribution control could not only play a significant role in various applications replying on resonant particle scattering, but also bring new stimuli for the emerging fields of topological photonics and low-dimensional photonics, which involves novel two-dimensional and topological materials that show an intrinsically huge anisotropy.

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