Ferromagnetism in a repulsive atomic Fermi gas with correlated disorder

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We investigate the zero-temperature ferromagnetic behavior of a two-component repulsive Fermi gas in the presence of a correlated random field that represents an optical speckle pattern. The density is tuned so that the (noninteracting) Fermi energy is close to the mobility edge of the Anderson localization transition. We employ quantum Monte Carlo simulations to determine various ground-state properties, including the equation of state, the magnetic susceptibility, and the energy of an impurity immersed in a polarized Fermi gas (repulsive polaron). In the weakly interacting limit, the magnetic susceptibility is found to be suppressed by disorder. However, it rapidly increases with the interaction strength, and it diverges at a much weaker interaction strength compared to the clean gas. Both the transition from the paramagnetic phase to the partially ferromagnetic phase, and the one from the partially to the fully ferromagnetic phase, are strongly favored by disorder, indicating a case of order induced by disorder.

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Understanding the phenomena induced by the interactions in fermionic systems exposed to strong enough disorder to cause the Anderson localization of the single-particle states [1] (a regime which has been referred to as Fermi glass [2,3]) is one of the most relevant problems in condensed matter physics [4-6]. Following the first observations of the And erson localization of matter waves [7-10], the experiments performed with ultracold atoms exposed to optical speckle patterns have emerged as the ideal platform to explore the intricate interplay between disorder and interactions in a controllable setup [11–16]. Not only can experimentalists tune the interaction strength [17], but they can also control the disorder amplitude and manipulate its spatial correlations [18]. Some recent theoretical and computational advancements have allowed scientists to precisely determine the mobility edge (namely, the energy threshold separating the localized single-particle orbitals from the extended ones) using realistic models of the speckle pattern [19-21], thus paving the way to a quantitative comparison with accurate experimental measurements [22]. While these previous theoretical studies have addressed systems of noninteracting particles, in this Rapid Communication we employ quantum Monte Carlo simulations within the fixed-node approximation to investigate the zero-temperature properties of disordered and interacting Fermi gases. In particular, we consider a two-component mixture with short-range repulsive interspecies interactions which is exposed to a blue-detuned isotropic optical speckle pattern [23,24]. We model this system using a realistic continuous-space Hamiltonian that takes into account the spatial correlations of the speckles.

Our main interest is to inspect what impact the disorder has on the so-called Stoner instability [25], namely, the ferromagnetic transition which is supposed to occur in clean Fermi gases when the interatomic repulsion becomes sufficiently strong. The Stoner instability is one of the standard paradigms in the theory of quantum magnetism. It was proposed as the minimal model to explain itinerant ferromagnetism in certain transition metals. Being a strong-interaction phenomenon, its nature and even its subsistence are still controversial. So far, in solid-state systems it has not been possible to unambiguously identify the Stoner mechanism. Instead, the results of a very recent cold-atom experiment [26] (in which the problems related to the three-body recombinations [27–29] have been circumvented by preparing a configuration with fully separated components [30]) are consistent with the spin fluctuations expected in the vicinity of the Stoner instability [31] and with the quantum Monte Carlo predictions for the critical repulsion strength in clean systems [32–34].

In this Rapid Communication, we analyze the zerotemperature ferromagnetic behavior of the disordered repulsive Fermi gas, determining the critical interaction strength of the Stoner instability in the presence of disorder. We address both the transition from the paramagnetic phase to the partially ferromagnetic phase, and the one from the partially ferromagnetic to the fully ferromagnetic phase. The gas density and the disorder amplitude are tuned so that the Fermi energy of the noninteracting (balanced) gas is approximately close to the mobility edge. This (somewhat arbitrary) choice is motivated by the fact that close to the mobility edge the single-particle orbitals display multifractal properties, a feature which is expected to enhance the interaction effects [35]. In order to figure out the ferromagnetic behavior, we compute the zero-temperature equation of state as a function of the interaction strength and of the population imbalance, we extract the spin susceptibility, and we determine the energy of a single impurity immersed in a single-component Fermi gas. We find that in the presence of disorder these quantities vary with the interaction strength quite differently compared to the clean gas. More specifically, the magnetic susceptibility is suppressed by the disorder if the repulsion is weak, but it increases with the interaction strength much more rapidly than in the clean gas. The critical interaction strength where it diverges-which signals the instability towards the partially ferromagnetic phase—is much smaller than in the absence of disorder. The polaron energy is also strongly influenced by disorder, and the critical interaction strength at which it exceeds the chemical potential of the majority component which signals the transition to the fully ferromagnetic phaseis significantly weaker than in the clean gas. These results indicate that disorder strongly favors the onset of ferromagnetic behavior.

The disordered Fermi gas we consider is described by the following Hamiltonian:

$$H = \sum_{\sigma=\uparrow,\downarrow} \sum_{i_{\sigma}=1}^{N_{\sigma}} \left[-\Lambda \nabla_{i_{\sigma}}^{2} + V(\mathbf{r}_{i_{\sigma}}) \right] + \sum_{i_{\uparrow},i_{\downarrow}} v(r_{i_{\uparrow}i_{\downarrow}}) , \quad (1)$$

where *m* is the atomic mass, \hbar is the reduced Planck constant, and we introduced $\Lambda = \hbar^2/2m$. The indices i_{\uparrow} and i_{\downarrow} label atoms of the two species, hereafter referred to as spin-up and spin-down particles. The distance between unlike fermions is $r_{i_{\uparrow}i_{\downarrow}} = |\mathbf{r}_{i_{\uparrow}} - \mathbf{r}_{i_{\downarrow}}|$. The total number of fermions is $N = N_{\uparrow} + N_{\uparrow}$ N_{\downarrow} , and the polarization is defined as $P = (N_{\uparrow} - N_{\downarrow})/N$. The system is enclosed in a cubic box of size L with periodic boundary conditions. v(r) is a model potential that describes the short-range (interspecies) interactions. In a sufficiently dilute and cold gas, the interaction strength is parametrized just by the s-wave scattering length a (this parameter can be tuned experimentally using Feshbach resonances [17]), while the other details of the interatomic potential, such as, e.g., the effective range $r_{\rm eff}$ and the *p*-wave scattering length a_p , are irrelevant. We choose the hard-sphere model: $v(r) = +\infty$ if $r < R_0$ and zero otherwise; in this case, one has a = $R_0, r_{\rm eff} = 2a/3$, and $a_p = a$. The possible nonuniversal effects due to the details beyond a have been thoroughly analyzed in Refs. [33,34,36–38] using different models for the interatomic interactions, including the zero-range pseudopotential. While these works considered homogeneous Fermi gases, in Ref. [39] the universality has been studied in the presence of periodic optical lattices, which induce pronounced spatial inhomogeneities of the density, as the speckle disorder does. Both in the homogeneous and in the nonhomogeneous case, it was found that the equation of state (and, hence, the critical interaction strength for the Stoner instability) is affected by about 10% in the strong-interaction regime $k_F a \gtrsim 1$, where $k_F = (3\pi^2 n)^{1/3}$ is the Fermi wave vector defined with the average density $n = N/L^3$, and that these nonuniversal effects rapidly vanish for weaker interactions. In this Rapid Communication, we consider the disordered Fermi gas in the moderate interaction regime $k_F a \leq 1$, where we expect the nonuniversal effects not to play a significant role.

 $V(\mathbf{r})$ is an external random field representing a blue-detuned isotropic optical speckle pattern; such a random optical field can be experimentally realized by shining lasers through a diffusive plate [11,12]. In the case of a blue-detuned optical field, the atoms experience a repulsive potential with the exponential local-intensity distribution: $P_{bd}(V) = \exp(-V/V_{dis})/V_{dis}$, if the local intensity is $V \ge 0$, and $P_{bd}(V) = 0$ otherwise [23]. The parameter $V_{\rm dis} \ge 0$ fixes both the spatial average of the random field $V_{\rm dis} = \langle V(\mathbf{r}) \rangle$ and its standard deviation, so that $V_{\rm dis}^2 = \langle V(\mathbf{r})^2 \rangle - \langle V(\mathbf{r}) \rangle^2$; therefore, $V_{\rm dis}$ is the parameter that characterizes the global disorder amplitude. The two-point spatial correlations of the speckle field depend on the profile of the illumination on the diffusive plate and on the details of the optical setup. We consider the idealized case where the spatial correlations are isotropic, being described by the following correlation function [19]: $\Gamma(r = |\mathbf{r}|) = \langle V(\mathbf{r}' +$ $\mathbf{r} V(\mathbf{r}') / V_{\text{dis}}^2 - 1 = [\sin(r/\sigma)/(r/\sigma)]^2$ (here we assume averaging over the position of the first point \mathbf{r}'). The function $\Gamma(r)$ rapidly decreases with the distance r; it vanishes at $r = \pi \sigma$, which corresponds to the typical speckle size and,

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thus, to the disorder correlation length; for larger distances $\Gamma(r)$ displays small oscillations. To favor comparison with previous literature, we will express length scales in units of the correlation length $\pi\sigma$ and the energy scales in units of the correlation energy $e_{\sigma} = \hbar^2/(m\sigma^2)$. In our simulations, the isotropic speckle pattern is generated following the numerical recipe described in Ref. [20]; it satisfies the periodic boundary conditions. See also Refs. [19,40,41].

To determine the ground-state properties of the Hamiltonian (1) we employ quantum Monte Carlo simulations based on the fixed-node diffusion Monte Carlo (DMC) algorithm [42]. The DMC algorithm is designed to sample the lowest-energy wave function by stochastically evolving the Schrödinger equation in imaginary time. The fixed-node constraint, which consists in imposing that the nodal surface of the many-body wave function is the same as that of a trial wave function ψ_T , is introduced in order to circumvent the sign problem, which would otherwise hinder fermionic Monte Carlo simulations. If the nodal surface of ψ_T is exact, this variational method provides unbiased estimates of the ground-state energy. In general, the predicted energies are rigorous upper bounds, which have been found to be very close to the exact groundstate energy if the nodes of ψ_T are good approximations of the ground-state nodal surface (see, e.g., [43]). We adopt a trial wave function of the Jastrow-Slater type, which is known to describe quite accurately the normal (nonsuperfluid) phases of interacting fermions; for a review on this issue, see Refs. [43] and [44]. It is defined as

$$\psi_T(\mathbf{R}) = D_{\uparrow}(N_{\uparrow}) D_{\downarrow}(N_{\downarrow}) \prod_{i_{\uparrow}, i_{\downarrow}} f(r_{i_{\uparrow}i_{\downarrow}}) , \qquad (2)$$

where $\mathbf{R} = (\mathbf{r}_1, ..., \mathbf{r}_N)$ is the spatial configuration vector and $D_{\uparrow(\downarrow)}$ denotes the Slater determinant of single-particle orbitals of the particles with up (down) spin. In this study, the Jastrow correlation term f(r) is taken to be the solution of the s-wave radial Schrödinger equation describing the scattering of two hard-sphere particles in free space, as in Refs. [33] and [39]. Since f(r) > 0, the nodal surface is fixed by the antisymmetry of the Slater determinants only. This, in turn, is fixed by the choice for the single-particle orbitals. We employ the N_{\uparrow} (N_{\downarrow}) lowest-energy single-particle eigenstates $\phi_j(\mathbf{r})$ (with $j = 0, \dots, N_{\uparrow(\downarrow)} - 1$) of the disordered potential $V(\mathbf{r})$ for the spin-up (spin-down) particles. These eigenstates satisfy the equation $[-\Lambda \nabla^2 + V(\mathbf{r})]\phi_i(\mathbf{r}) = e_i\phi_i(\mathbf{r})$, with the eigenvalues e_i . We determine them via exact numerical diagonalization of the finite matrix obtained after introducing a discretization in the continuous space and approximating the Laplacian using high-order finite-difference formulas. We carefully analyze how the discretization error affects both the single-particle eigenvalues and the many-body groundstate energy obtained from the DMC simulations, ensuring that the discretization error is negligible compared to the statistical uncertainty of the Monte Carlo predictions. Three representative single-particle orbitals are visualized in Fig. 1. The first is the ground state (j = 0), which is localized in a restricted region of space due to the Anderson localization phenomenon. The second has an energy near the mobility edge e_c ; it has an intermediate character between extended and localized. The third orbital corresponds to an eigenvalue well

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FIG. 1. (a) Speckle pattern intensity $V(x,0,0)/e_{\sigma}$ along a onedimensional cross section. $e_{\sigma} = \hbar^2/(m\sigma^2)$ is the disorder correlation energy. The length unit is the disorder correlation length $\pi\sigma$. The dashed (green) line indicates the average intensity $V_{\text{dis}} = 1.5e_{\sigma}$. (b, c, d) Particle density distribution for three representative single-particle eigenstates $\phi_j(\mathbf{r})$ of a speckle pattern: (b) ground state (j = 0); (c) state at the Fermi energy $e_j = e_F \simeq 0.84e_{\sigma}$ corresponding to the density $n = N/L^3 \cong 0.185(\pi\sigma)^{-3}$ (notice that the mobility edge is $e_c = 0.80(3)e_{\sigma}$); (d) state at the energy $e_j \simeq 1.2e_{\sigma}$. The particle density is proportional to the probability density $|\phi_j(\mathbf{r})|^2$, with the normalization set so that max $(|\phi_j(\mathbf{r})|^2) = 1$; the color scale indicates the probability density.

above the mobility edge (and the Fermi energy). We mention that the energy on a noninteracting disordered gas with N_{\uparrow} (N_{\downarrow}) spin-up (spin-down) particles particles can be computed as $E(N_{\uparrow}, N_{\downarrow}) = \sum_{j=0}^{N_{\uparrow}-1} e_j + \sum_{j=0}^{N_{\downarrow}-1} e_j$. While, in principle, the fixed-node constraint might intro-

duce a systematic bias, in the case of weakly and moderately repulsive Fermi gases, the results based on the Jastrow-Slater trial wave function described above have been confirmed by comparison with different techniques. For weakly interacting atoms in deep optical lattices, which can also be described with the single-band (discrete) Hubbard model, the predictions provided by continuous-space DMC simulations [39] (obtained by fixing the nodes using the single-particle eigenstates, as we do here) have been found to precisely agree with accurate Hubbard model simulations performed using the auxiliaryfield quantum Monte Carlo method [45], which represents the state of the art in the simulation of strongly correlated fermions [46]. For moderately repulsive homogeneous Fermi gases, more elaborated trial wave functions including backflow correlations have been employed in Ref. [34], finding essentially negligible effects in the interaction regime of interest.

In this Rapid Communication, we first determine the zero-temperature equation of state of a population balanced Fermi gas with $N_{\uparrow} = N_{\downarrow}$ (P = 0). We consider a blue-detuned

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FIG. 2. Main panel: Single-particle (noninteracting) density of states (in arbitrary units) as a function of the energy e/e_{σ} (brown solid curve). The vertical dashed (green) line indicates the disorder amplitude $V_{\text{dis}}/e_{\sigma} = 1.5$, the vertical (gray) bar the mobility edge e_c/e_{σ} , and the vertical dot-dashed (red) line the Fermi energy ϵ_F at the density $n \cong 0.185(\pi\sigma)^{-3}$. Inset: Many-body ground-state energy per particle E/N versus the particle number N; the density is $n \cong 0.185(\pi\sigma)^{-3}$; the interaction parameter is $k_F a = 0.7$, corresponding to $a \cong 0.397\pi\sigma$.

isotropic speckle field with average intensity $V_{\rm dis} = 1.5e_{\sigma}$. The density of states of the noninteracting problem at this disorder strength is shown in Fig. 2 (main panel). The mobility edge e_c , namely, the energy threshold that separates the localized single-particle orbitals with energies $e_i < e_c$ from the extended orbitals with energies $e_i > e_c$, is $e_c = 0.80(3)e_{\sigma}$. This value is obtained from the statistical analysis of the spacings between energy levels [47], exploiting the universal value of the critical adjacent level-spacings ratio, following the procedure of Refs. [20] and [21]. This result agrees within statistical error with the prediction $e_{\rm c} = 0.787(9)e_{\sigma}$ obtained in Ref. [19] using the transfer matrix method. We consider a gas with fixed average density $n \cong 0.185(\pi\sigma)^{-3}$, for which the (noninteracting) Fermi energy is found to be $e_F \simeq 0.84 e_{\sigma}$, just above the mobility edge. With this choice, a significative part of the atoms are Anderson localized in the noninteracting limit.

In Fig. 3 we plot the energy per particle E/N, computed using the DMC algorithm described above, for increasing values of the *s*-wave scattering length *a*. We stress that in this study the adimensional density parameter $n(\pi\sigma)^3$ is fixed, while the ratio $a/(\pi\sigma)$ increases. The interaction parameter can also be cast in the form k_Fa , familiar from the theory of clean Fermi gases, defining the Fermi wave vector using the average density *n*. These results have been obtained by averaging over 15 to 25 realizations of the speckle field, using systems sizes from N = 40 to N = 80.

The analysis of the finite-size effects (shown in the inset of Fig. 2) suggests that the systems we simulate are sufficiently large to predict the ground-state energies corresponding to the thermodynamic limit, within the statistical uncertainties. It is worth emphasizing that while the simulations of finite clean Fermi systems are affected by strong shell effects (which can be largely alleviated, e.g., using twisted-averaged boundary conditions [48]), in the presence of disorder the degeneracies



FIG. 3. Energy per particle E/N at polarization P = 0 as a function of the scattering length $a/(\pi\sigma)$ for the clean gas (red circles, right vertical axis) and for the disordered gas (blue squares, left vertical axis) with disorder amplitude $V_{\text{dis}} = 1.5e_{\sigma}$. The interaction strength can be expressed also as $k_F a$, where the Fermi wave vector $k_F = (3\pi^2 n)^{1/3}$ is defined with the average density $n \cong 0.185(\pi\sigma)^{-3}$. The solid (red) curve is a fourth-order fit to the DMC data, the dashed (blue) line is a linear fit (see text). The horizontal dashed segments indicate the corresponding energies of the fully imbalanced gases. $3/5e_F^0$ is the energy per particle of a clean noninteracting Fermi gas.

between single-particle energies are suppressed, thus strongly reducing the shell effects (at the cost of having to average over disorder realizations).

The ground-state energy E/N displays a different dependence on the interaction strength with respect to the clean gas (also shown in Fig. 3, data from Ref. [33]). In the latter case, the equation of state is well described by the polynomial $E/N = e_u \sum_{i=0,...,4} c_i (k_F a)^i$, where $c_0 = 1, c_1 \cong 0.353$ 6, and $c_2 \cong 0.185$ 5 are provided by the second-order perturbation theory [49,50], while $c_3 = 0.307(7)$ and $c_4 = -0.115(8)$ are fitting parameters [51], and the energy unit is $e_u = 3/5e_F^0$, namely, the energy per particle of the clean noninteracting Fermi gas [being $e_F^0 = (\hbar k_F)^2/(2m)$ the corresponding Fermi energy].

In the disordered gas, a simple linear form (with $c_0 = 0.724(2)$, $c_1 = 0.162(5)$, $e_u = e_\sigma$, and $c_i = 0$ for i = 2,3,4) appears to accurately fit the data. It is surprising to observe this simple behavior emerging in such a complex quantum system.

We observe that in the disordered gas the energy of the balanced (P = 0) gas exceeds the energy of the fully imbalanced gas with P = 1 (which is indicated with a horizontal segment in Fig. 3) at weaker interaction strength than in the absence of disorder. This is a sufficient—though not necessary condition for the occurrence of ferromagnetic behavior [34]. A more precise characterization of the ferromagnetic properties can be obtained by analyzing the spin susceptibility and the polaron energy, as described below.

The transition from the paramagnetic phase to the partially ferromagnetic phase can be identified from the divergence of the spin susceptibility $\chi = n(\frac{\partial^2(E/N)}{\partial P^2})^{-1}$. This criterion is associated to a second-order phase transition, consistent with the argument of Ref. [52]. We determine χ by performing DMC simulations with imbalanced populations with $N_{\uparrow} > N_{\downarrow}$ ($0 \leq P \leq 1$), keeping the total particle number *N* fixed, for



FIG. 4. Inverse magnetic susceptibility χ_0/χ for the clean gas (red circles) and for the disordered gas (blue squares). $\chi_0 = 3n/(2e_F)$ is the result corresponding to the clean noninteracting Fermi gas. The solid (red) curve is a cubic fit to the DMC data, the dashed (blue) line is a linear fit (see text).

individual disorder realizations. For sufficiently small values of the population imbalance P, the energy per particle is found to vary with P according to the quadratic function: $E(P)/N = E(P = 0)/N + nP^2/(2\chi)$, where E(P = 0) and χ are fitting parameters. In Fig. 4 we show the inverse susceptibility χ^{-1} as a function of the interaction strength, obtained after averaging over 5 to 10 disorder realizations. We notice that in the weakly interacting limit, χ^{-1} is larger than in the clean gas (data from Ref. [51]), meaning that the disorder alone (i.e., in the absence of interactions) suppresses the spin fluctuations. However, χ^{-1} quickly drops to zero as the interaction parameter increases, indicating a strong interplay between disorder and interactions. Already at the interaction strength $k_F a \simeq 0.2$, the inverse susceptibility is smaller in the disordered gas than in the clean gas. In the disordered case, the critical point where χ^{-1} vanishes, which signals the transition to the partially ferromagnetic phase, is $k_F a \simeq 0.38$, considerably smaller than in the clean gas $k_F a \simeq 0.80$ [51]. We point out that while our data support the scenario of a second-order phase transition, our numerics cannot rule out an extremely weakly first-order transition [53] or an infinite-order transition [54]. Furthermore, in the case of clean systems, more exotic magnetic phases with spin-textured magnetization have been predicted to occur in the close vicinity of the ferromagnetic transition [32]; we do not consider these spin-textured phases. We also notice that while in the clean gas the inverse susceptibility is well described by the cubic fitting function $\chi_0/\chi = \sum_{i=0,\dots,3} d_i (k_F a)^i$, where $d_0 = 1, d_1 \cong -0.637$, and $d_2 \cong -0.291$ are provided by perturbation theory [31], and $d_3 = -0.56(1)$ is a fitting parameter, in the disordered case the simple linear fitting function [with $d_0 = 1.60(1), d_1 \cong -4.2(1), \text{ and } d_i = 0 \text{ for } i = 2,3$] precisely reproduces the trend of the data.

The transition from the partially ferromagnetic phase to the fully ferromagnetic phase can be located by determining the chemical potential at zero concentration of the repulsive polaron, defined as $A = E(N_{\uparrow}, 1) - E(N_{\uparrow}, 0)$, where $E(N_{\uparrow}, 1)$ is the energy of a gas with N_{\uparrow} spin-up particles plus a spindown impurity ($N_{\downarrow} = 1$). For sufficiently strong repulsion, *A* exceeds the chemical potential of the majority component



FIG. 5. Chemical potential at zero concentration of the repulsive polaron in the clean gas (red circles, right axis) and in the disordered gas (blue squares, left axis). $e_{F\uparrow}^0 = (\hbar k_{F\uparrow})^2/2m$ is the Fermi energy of the clean fully imbalanced noninteracting Fermi gas. The interaction parameter $a/(\pi\sigma)$ can be cast in the form $k_{F\uparrow}a$ using the Fermi wave vector $k_{F\uparrow} = (6\pi^2 n_{\uparrow})^{1/3}$ defined with the average spin-up density $n_{\uparrow} = N_{\uparrow}/L^3 \cong 0.185(\pi\sigma)^{-3}$. The horizontal dashed segments indicate the chemical potential of the majority component. The solid curves through DMC data are guides to the eye.

[which we compute as $e_{F\uparrow} = E(N_{\uparrow} + 1,0) - E(N_{\uparrow},0)$]. At this point, the fully ferromagnetic phase becomes energetically favorable [33,55]. The data shown in Fig. 5 (obtained by averaging 10 to 20 disorder realizations) indicate that in the

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presence of disorder this transition takes place at $k_{F\uparrow}a \simeq 0.82$ [where $k_{F\uparrow} = (6\pi^2 n_{\uparrow})^{1/3}$ is the majority-component Fermi wave vector, defined with the corresponding average density $n_{\uparrow} = N_{\uparrow}/L^3$], which is significantly smaller than in the clean gas: $k_{F\uparrow}a \simeq 1.22$. It is worth noticing that while in the absence of disorder the partially ferromagnetic phase is stable in the window $0.80 < k_Fa < 0.97$ [33,51], in the presence of disorder this window is shifted to weaker interactions, and it is enlarged: $0.38 < k_Fa < 0.65$ (we used the conversion $k_F = k_{F\uparrow}/2^{1/3}$).

In conclusion, we employed continuous-space quantum Monte Carlo simulations to investigate the zero-temperature properties of interacting Fermi gases exposed to correlated speckle disorder, including the equation of state, the magnetic susceptibility, and the polaron energy. We considered a fixed density and disorder amplitude—tuned so that the Fermi energy is in the rough vicinity of the mobility edge—and we observed that the ferromagnetic transition is shifted to significantly weaker interaction than in the clean gas. These results indicate an alternative route to observe quantum magnetism is cold-atom experiments, circumventing the molecule-formation problem that plagues the regime of strong interactions, and they constitute a useful benchmark for future theoretical studies on disordered interacting many-fermion systems.

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