

Cascading quantum light-matter interfaces with minimal interconnection losses

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The ability to interface multiple optical quantum devices is a key milestone towards the development of future quantum information processors and networks. One of the requirements for any of their constituent elements will be cascading, i.e., the ability to drive the input of a device using the output of another one. Here, we report the cascading of quantum light-matter interfaces by storing few-photon level pulses of light in warm vapor followed by the subsequent storage of the retrieved field onto a second ensemble. We demonstrate that by using built-in purification mechanisms in the sequential storage, the final signal-to-background ratio can remain greater than one for weak pulses containing eight input photons on average.

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I. INTRODUCTION

Any machine can be defined as a device composed of many constituents with their own specific functions but that when interfaced together are designed to carry out a much greater task. This same description would hold true for a quantum information processor. Given the recent success in the manipulation of individual quantum systems [1,2], the next step towards the realization of such a quantum machine is the interconnection between multiple quantum network components [3–6].

Ideally these networks will have quantum nodes producing outputs suited for driving (as inputs) succeeding quantum nodes. This is the concept of quantum cascading [7], and it is a necessary attribute to share and process entanglement in many quantum computer architectures and quantum communication protocols [8–13]. This concept has been widely implemented in setups based upon the interconnecting of quantum state sources and memories [14,15]. However, protocols or operations interconnecting sources and multiple devices (i.e., memories) in a sequential manner have been primarily unexplored, particularly due to the severe losses incurred to purify the output of the system after each process.

Of the existing multidevice protocols, many will be reliant on operational quantum memories [16] and furthermore on the functionality to have quantum memories that efficiently interface with the output of a preceding memory while incurring minimal propagation losses between systems. More specifically, cascading of quantum memories are necessary for certain one-way quantum computing schemes [17], the implementation of conditional controlled-Z (CZ) gates [18], and generating multimode quantum states [19]. Building on recent successes [20–23], we consider room-temperature atomic vapor memories as the elements that comprise a series of cascading devices that could form the foundation of a quantum network. Room-temperature systems are a promising direction, as they can offer a relatively inexpensive experimental overhead while also having strong light-matter interaction at the single-photon level [24–26].

Here we present the cascaded storage of weak optical pulses containing a few photons on average in two, independent room-temperature quantum light-matter interfaces in the conditions of electromagnetically induced transparency (EIT).

II. THEORETICAL BACKGROUND

In order to utilize EIT for optical storage, we require atomic systems exhibiting a Λ -energy level scheme. In a cascaded optical storage procedure, the Λ -level scheme of the first atomic ensemble can be characterized by the interaction with two laser fields, Ω_{p1} (probe) and Ω_{c1} (control), with one-photon detunings Δ_1 and Δ_2 respectively (see Fig. 1). The output of this system will be the input to the second ensemble characterized by the interaction with two laser fields, Ω_{p2} (retrieved probe coming from system 1) and Ω_{c2} (control). We assume the detunings of both systems to be identical.

This optical storage can be understood using the Hamiltonian which describes the atom-field coupling in a rotating frame. This is given by

$$\hat{H} = \Delta_1 \hat{\sigma}_{33} + (\Delta_1 - \Delta_2) \hat{\sigma}_{22} + \Omega_{p1} E_{p1}(z, t) \hat{\sigma}_{31} + \Omega_{c1}(t) \hat{\sigma}_{32} + \text{H.c.}, \quad (1)$$

where $\hat{\sigma}_{ij} = |i\rangle\langle j|$, $i, j = 1, 2, 3$ are the atomic raising and lowering operators for $i \neq j$ and the atomic energy-level population operators for $i = j$, and $E_{p1}(z, t)$ is the normalized electric field amplitude of the probe. The dynamics of the first storage event can be obtained numerically by solving the master equation for the atom-light system density operator together with the Maxwell-Bloch equation that contains the impact of the atomic polarization on the electromagnetic field for an atomic sample of finite-length L .

$$\dot{\hat{\rho}} = -i[\hat{H}, \hat{\rho}] + \sum_{m=1,2} \Gamma_{3m} (2\hat{\sigma}_{m3} \hat{\rho} \hat{\sigma}_{3m} - \hat{\sigma}_{33} \hat{\rho} - \hat{\rho} \hat{\sigma}_{33}) \quad (2)$$

$$\partial_z E_{p1}(z, t) = i \frac{\Omega_{p1} N}{c} \langle \hat{\sigma}_{31}(z, t) \rangle. \quad (3)$$

Here Γ_{31} and Γ_{32} are the decay rates of the excited level $|3\rangle$ to the ground states $|1\rangle$ and $|2\rangle$, respectively, c is the speed of light in vacuum, and N is the number of atoms participating in the ensemble. Using initial conditions of $\Omega_{c1}(t)$ and $E_p(0, t) = E_o(t)$ (the original probe pulse shape) allows us to solve this set of equations and calculate the expected retrieved pulse shape $E_{\text{OUT}}(t) = E_{p1}(L, t)$. Once we know $E_{\text{OUT}}(t)$, we can propagate this result to serve as the input of the second Λ system and similarly calculate the result of the cascaded storage procedure $E_{\text{OUT}2}(t)$.

In Fig. 1(b), we plot the simulation of the first storage and retrieval event using $\Omega_{c1}(t)$ [black dot-dashed line in Fig. 1(b)]

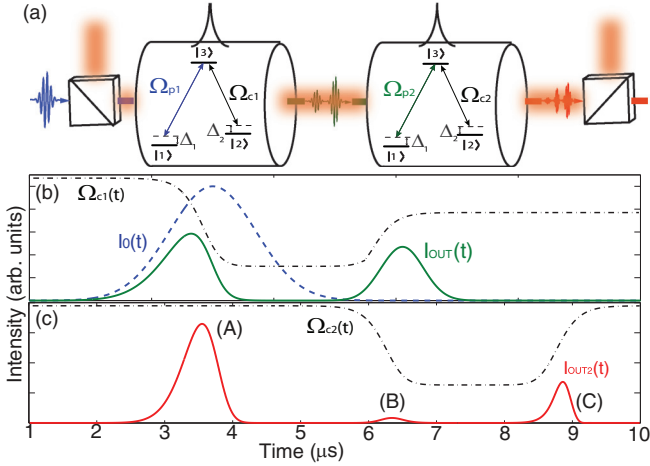


FIG. 1. (Color online) (a) Concept of the cascaded storage with two light-matter interfaces. (b) First storage: Input pulse (dashed line [blue online]), control field 1 time sequence (dot-dashed line [black online]), and retrieved light signal (solid line [green online]) as obtained by simulation. (c) Second storage: control field 2 time sequence (dot-dashed line [black online]), notice the time delay with respect to control field 1 and cascaded retrieved signal (solid line [red online]).

and $E_p(0,t) = E_o(t)$ [(dashed line [blue online]) in Fig. 1(b)] as the control and probe inputs respectively. The result for $E_{OUT}(t) = E_{p1}(L,t)$ [Fig. 1(b), in intensity, (solid line [green online]) light] contains a portion of the input pulse that is not stored and transmitted (left peak), followed by the retrieved signal due to the storage (right peak). Figure 1(c) shows the simulation of the second storage and retrieval event using $\Omega_{c2}(t)$ [dot-dashed black line in Fig. 1(c)] and $E_{OUT}(t)$ as the control and probe field inputs respectively.

The resultant cascaded stored signal contains three distinct peaks [Fig. 1(c) in intensity, (solid line [red online])], an initial probe leakage from the first storage procedure (A, leftmost peak), a second small leakage from the second procedure (B, middle peak), and a third peak whose timing matches that of

when the second control field is switch on again (C, rightmost peak). This final peak corresponds to a portion of the probe field that has been sequentially stored and retrieved in two independent light-matter interfaces. In our simulations we have used $\Gamma_{31} = \Gamma_{32} = 3.0\pi \times 10^6 \text{ s}^{-1}$, $N \sim 10^{10}$ atoms and $L = 7 \text{ cm}$.

III. EXPERIMENTAL SETUP

In order to implement the cascading procedure experimentally, we employed two external-cavity diode lasers as light sources, phase locked at 6.8 GHz to resonantly couple a Λ configuration. The probe field frequency is stabilized to the $5S_{1/2}F = 1 \rightarrow 5P_{1/2}F' = 1$ transition at a wavelength of 795 nm (red detuning $\Delta = 100 \text{ MHz}$) while the control field interacts with the $5S_{1/2}F = 2 \rightarrow 5P_{1/2}F' = 1$ transition [Fig. 2(a)].

Our setup is adapted from our prior dual-rail memory experiment [26], where each rail now serves as a distinct optical memory within a single vapor cell containing isotopically pure Rb 87. The temporal shaping of the probe and the control fields are independently controlled with acousto-optic modulators. A polarization beam displacer is used to create a dual-rail setup for the control field where each rail is mode matched to the respective probe via a Glan laser polarizer [see Fig. 2(b)]. An initial 100- μ W-peak input pulse of 1 μ s duration horizontally polarized is sent through the first rail (thin gray line [blue online] in Fig. 3). Using one of the control fields, the probe pulse is stored for a duration of 1 μ s. For the first storage, we apply a temporal modulation to the control field used for retrieval, which allows tuning of the instantaneous group velocity of the retrieved excitation and consequently the tailoring of its temporal shape. We use a near Gaussian temporal profile (see second peak of gray line [green online] in Fig. 3) to yield an efficiency (η_1) of $\sim 12\%$.

The retrieved pulse is transmitted through a polarizer followed by a beam displacer for recombination to a single beam path. After this step, a 90:10 beam splitter is used to send the majority of the retrieved photons back to the front of the vapor cell (see Fig. 2), where a pickoff mirror sends the signal

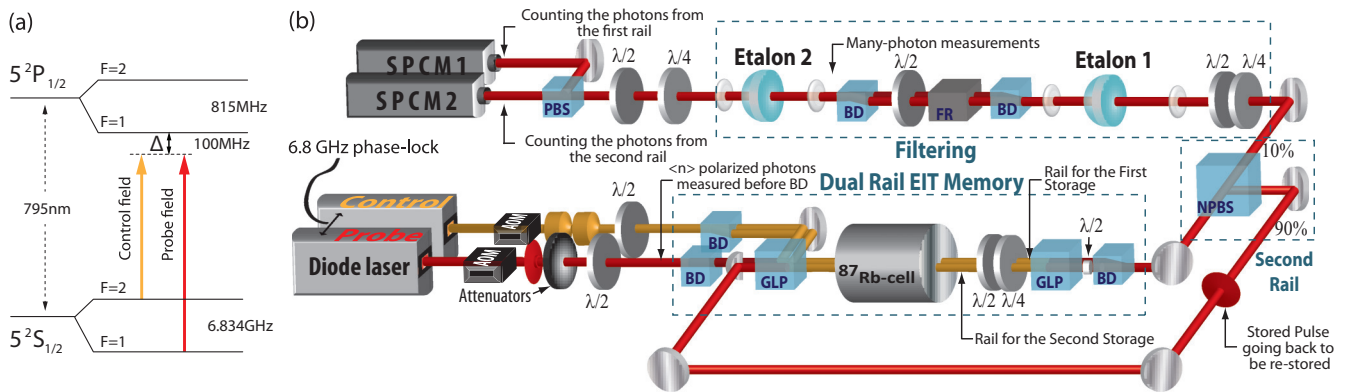


FIG. 2. (Color online) (a) Atomic level scheme and EIT configuration used in both memories. (b) Experimental setup for successive storage of pulses at the few-photon level, including the stages of control filtering. AOM, acousto-optic modulator; BD, beam displacer; GLP, Glan laser polarizer; FR, Faraday rotator; SPCM, single-photon-counting module; L, lens; M, mirror; NPBS, nonpolarizing beam splitter. Probe, gray beam paths [red online]; control, light gray beam paths [yellow online]. The NPBS transmits 10% of the first stored pulse through the filtering system to be characterized and sends 90% back to the second rail for a successive storage.

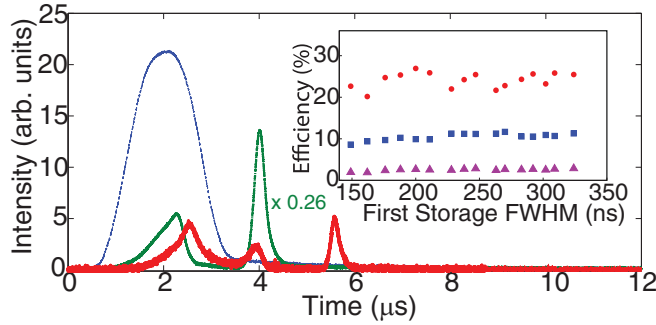


FIG. 3. (Color online) Successive storage of classical pulses. Thin gray line [blue online]: input pulse; gray line [green online]: rail 1 single storage signal; thick gray line [red online]: rail 2 cascaded storage signal. The gray line [green online] is scaled by a factor 0.26 to account for different propagation losses after the first and second rails. Inset: dependency of storage efficiencies on the full-width half maximum of the Gaussian shaped retrieved field for the first storage. Squares [blue online]: efficiency of the first storage η_1 ; circles [red online]: efficiency of the second storage η_2 ; and triangles [purple online]: overall efficiency of cascaded storage procedures η_T .

through the second rail. The timing of control field 2 is matched to the retrieval of the first memory for the second storage sequence. After the second beam displacer, the signals from the first and second rails are matched to the same beam path, albeit with orthogonal polarizations, which permits independent measurements. The signals transmitted through the 90 :10 beam splitter continue through a temperature-controlled etalon and a polarization-independent Faraday-isolator to remove the remnants of the control fields. At this point, the classical-level signals are detected in a photodetector (not shown in Fig. 2). The signals from the second rail (thin gray [blue online] and thick gray [red online] in Fig. 3) are 3.9 times smaller than those from the first (gray [green online] in Fig. 3) due to propagation losses and mismatched etalon coupling efficiencies. As shown in Fig. 3 (thick gray line [red online]), the resultant cascaded stored signal has three peaks as was predicted by our simulations.

To maximize the efficiency of the cascaded storage (η_T), we modify the duration of control field 1 which also affects the temporal length of the retrieved probe field. This has a significant effect on η_T , as the optimal bandwidth of the retrieved pulse resembles the EIT bandwidth exhibited by the vapor cell. A total storage efficiency of $\sim 3\%$ is obtained when the duration of the control field for the first retrieval is 300 ns. The efficiency of the second storage event is independently verified to be $\eta_2 \sim 25\%$. We emphasize that the increase in efficiency from η_1 to η_2 is a direct beneficial effect of the spectral shaping of the photons in the output of the first memory.

IV. FEW PHOTON LEVEL OPERATION

We now turn our attention to operating our system at the few-photon level. Specifically, we are interested in benchmarking the behavior of the complete optical storage network and determine the parameters needed to obtain a cascaded retrieved signal that is at the same level of the background produced by the experiment, i.e., signal-to-background ratio (SBR) of 1.

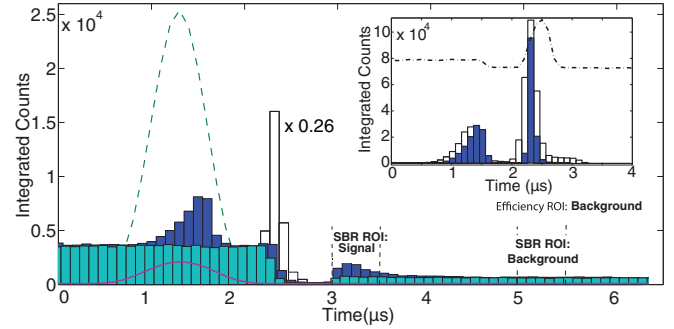


FIG. 4. (Color online) Cascaded optical storage for input pulses containing eight photons per pulse on average. Dashed line [green online]: input pulse (measured in SPCM 2); light gray line [purple online]: absorbed pulse (measured in SPCM 2); white bars histogram: retrieved pulse after first storage (measured in SPCM 1 scaled by a factor 0.26); gray bars histogram [blue online]: retrieved signal after cascaded storage procedure (with background, measured in SPCM 2); light gray bars histogram [blue online]: background-only measurement. Inset: The effect of reshaping the control field for the optical retrieval in the first rail. Storage using on-off modulation of control field 1 (grey bars histogram [blue online]) and storage counts obtained with a temporally modulated control field 1 (white bars histogram). The temporal shape of the control field 1 is indicated by the dotted black line.

A trace of the input state is shown in Fig. 4 (dashed line [green online], from 1 to 2 μ s) for an input mean photon number ~ 8 . In order to sufficiently extinguish the large number of photons coming from the control fields, we add a second filtering etalon to the setup of the previous measurement. Overall, the complete filtering setup achieves 154 dB of control field suppression, including the 90:10 beam splitter, while yielding a total probe field transmissions of 0.44% and 0.22% for the first and second rails, respectively, to generate an effective, control-probe suppression ratio of about 130 dB. As discussed before, the setup permits measurement of the storage in the first rail (see SPCM 1 in Fig. 2) or the cascaded storage from the second rail (see SPCM 2 in Figure 2).

To determine the total storage efficiency (η_1) in the first rail, we integrate the number of counts over the region of interest (ROI) corresponding to the retrieved pulse (from 2 to 2.5 μ s in the inset of Fig. 4) and subtract the number of counts from a signal-free measurement of the background over the same ROI. The magnified background shape of the control field is included (dashed black line in the inset of Fig. 4) as a guide to the eye. The storage efficiency is then calculated by comparing this difference in counts to the total counts of the probe pulse transmitted (in rail 1) through the filtering system without atomic interaction. The signal-to-background ratio is obtained using the counts integrated over the ROI in the storage histogram (signal+background) and the number of counts over a signal-free region in the same histogram (background). The SBR is then calculated as $[(\text{signal} + \text{background}) - (\text{background})] / (\text{background})$.

As shown in the inset of Fig. 4, there is a considerable effect on η_1 by using a temporal shaping of the control field for retrieval (white bars histogram), as compared to an experiment with an on-off control field (gray bars histogram [blue online]). We find a maximum signal-to-background ratio of 13 and an

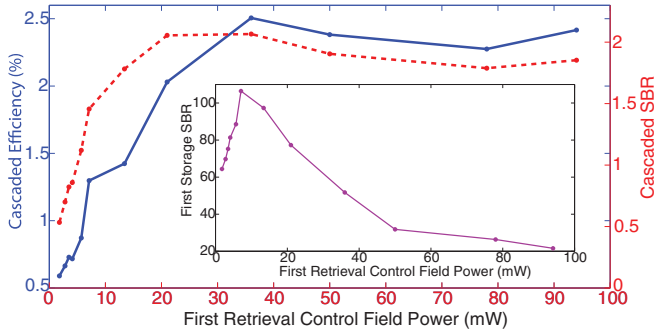


FIG. 5. (Color online) Total cascaded storage efficiency η_T (gray line [blue online]) and cascaded SBR (dashed gray line [red online]) vs optical power for first retrieval. Inset: SBR of first storage event vs optical power for first retrieval (purple online).

efficiency of 14.6% (see white bars histogram in Fig. 3). The majority of the photons retrieved from the first memory are sent to the second rail *together with any photons from the first control field* without passing through the filtering setup. This important step allows us to reduce the propagation losses by more than 90% by avoiding the use of additional purification optics in between the memories. We find that after propagation losses (including the routing beam splitter and interconnecting losses from the first to second rail of 53.4%), the mean photon number of the probe field at the input of the second memory is 0.6 photons compared to $\sim 10^8$ photons per pulse from the background. The probe photons are restored and then retrieved using the second control field (see gray bars histogram [blue online] in Fig. 4). For comparison, we also show the counts recorded when the input has been blocked (see light gray bars histogram [blue online] in Fig. 4).

The cascaded storage signal has a SBR of 1.2. Using a procedure similar to the one described previously, we measure the overall efficiency of the cascaded storage (using a ROI in the interval from 3 to 3.5 μs in Fig. 4) to be $\eta_T = 2.9\%$. The efficiency of the second memory η_2 was found to be 19.7%.

Finally we turn our attention to the noise characteristics of our cascaded storage system. Specifically, we are interested in the influence of the background noise photons generated from the first optical storage event on the final cascaded storage signal. We have measured the cascaded storage efficiency (η_T), the cascaded SBR, and the SBR of the first storage event vs control field 1 power. We used input states containing an average of 18 photons per pulse and an on-off modulation.

We can see that the total SBR after the cascading event (dashed gray line [red online] in Fig. 5) follows the behavior of the total storage efficiency η_T (gray line [blue online] in Fig. 5). By comparison, the SBR for the first storage event

(see inset in Fig. 5) does not follow the SBR of the cascaded procedure. This indicates that the second EIT storage ensemble simultaneously serves as a filter of the background generated in the first storage ensemble, implying that filtering schemes are only needed at the point of final measurement. Similar built-in filtering techniques have been implemented in light-matter interfaces with different purposes [27,28].

Creating a network of multiple devices that contain built-in filtering mechanisms will lead to a major decrease in both experimental overhead and overall loss in the endpoint read-out signal and becomes a fundamental consideration when constructing many-device machines.

V. SUMMARY

In summary, we have demonstrated a cascaded storage of few-photon-level pulses using two distinct atomic ensembles contained in the same vapor cell. Few-photon-level operation is made possible, even when using imperfect devices, by combining photon-shaping techniques and built-in filtering in the quantum light matter interfaces. We do mention that in our realization the few-photon *cascaded* efficiency is of the same magnitude as the *single-device* efficiency reported in recent implementations [29,30]. Our results demonstrate that with current room-temperature technology it is viable to interconnect several quantum light-matter interfaces in a sequential manner with minimal interconnection losses, a key attribute of a quantum optical network.

In our particular implementation it is not possible to use an original input at the single-photon level due to the nonunitary efficiencies of both systems and the inherent losses required by using a dual rail system. Significant improvement in efficiency and SBR are required in order to operate with single-photon carrying qubits. Some of these losses can be addressed by using separate vapor cells connected in series. Achieving this interconnection between quantum memories for input single photons carrying qubits could be a milestone towards building more sophisticated machines that interface even more quantum optical nodes. This in turn will pave the way for the creation of elementary one-way quantum information processors based on warm vapor ensembles.

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