Storage and retrieval of microwave fields at the single-photon level in a spin ensemble

C. Grezes,¹ B. Julsgaard,² Y. Kubo,¹ W. L. Ma,^{3,4} M. Stern,¹ A. Bienfait,¹ K. Nakamura,⁵ J. Isoya,⁶ S. Onoda,⁷ T. Ohshima,⁷

V. Jacques, 8 D. Vion, ¹ D. Esteve, ¹ R. B. Liu, ³ K. Mølmer, ² and P. Bertet¹

¹*Quantronics Group, Service de Physique de l'Etat Condense, DSM/IRAMIS/SPEC, CNRS UMR 3680, ´*

CEA Saclay, 91191 Gif-sur-Yvette, France

²*Department of Physics and Astronomy, Aarhus University, Ny Munkegade 120, DK-8000 Aarhus C, Denmark*

³*Department of Physics, Centre for Quantum Coherence, and Institute of Theoretical Physics, The Chinese University of Hong Kong,*

Shatin, New Territories, Hong Kong, China

⁴*State Key Laboratory of Superlattices and Microstructures, Institute of Semiconductors, Chinese Academy of Sciences, Beijing 100083, China*

⁵*Energy System Research Institute, Fundamental Technology Department, Tokyo Gas Co., Ltd., Yokohama 230-0045, Japan*

⁶*Research Center for Knowledge Communities, University of Tsukuba, Tsukuba 305-8550, Japan*

⁷*Japan Atomic Energy Agency, Takasaki 370-1292, Japan*

⁸*Laboratoire Aime Cotton, CNRS, Universit ´ e Paris-Sud and ENS Cachan, 91405 Orsay, France ´*

(Received 8 April 2015; published 7 August 2015)

We report the storage of microwave pulses at the single-photon level in a spin-ensemble memory consisting of 1010 nitrogen-vacancy centers in a diamond crystal coupled to a superconducting *LC* resonator. The energy of the signal, retrieved 100 *μ*s later by spin-echo techniques, reaches 0*.*3% of the energy absorbed by the spins. This 0*.*3% storage efficiency is quantitatively accounted for by simulations. This figure of merit is sufficient to envision first implementations of a quantum memory for superconducting qubits.

DOI: [10.1103/PhysRevA.92.020301](http://dx.doi.org/10.1103/PhysRevA.92.020301) PACS number(s): 03*.*67*.*Lx*,* 42*.*50*.*Ct*,* 42*.*50*.*Pq*,* 85*.*25*.*Cp

Superconducting qubits are attractive candidates for solidstate implementations of quantum information processing, but suffer from coherence times shorter than ∼100 *μ*s [\[1–3\]](#page-3-0). To circumvent this issue, it has been proposed to use ensembles of spins in semiconductors $[4-9]$ $[4-9]$ as a multimode quantum memory, able to store multiple qubit states over longer periods of time, and to retrieve them on demand [\[10\]](#page-4-0). Inspired by research on optical quantum memories $[11-13]$, realistic protocols have been proposed recently [\[14,15\]](#page-4-0). The state of a superconducting qubit is first converted into the state of a microwave photon, propagating or trapped in a resonator. This photon is then resonantly and collectively absorbed by the spin ensemble, resulting in a transverse magnetization which, due to the spread of resonance frequency within the ensemble, decays in a time T_2^* called the free-induction decay time. The *write* step is later followed by the need to *read* the stored quantum state. Both protocols [\[14,15\]](#page-4-0) propose to apply sequences of π pulses to the spins, combined with dynamical tuning of the resonator frequency [\[16,17\]](#page-4-0) and quality factor [\[18,19\]](#page-4-0) in order to trigger the rephasing of the spins, resulting in the emission of an echo at a chosen time that faithfully reproduces the initial quantum state.

Whereas the transfer of a qubit state into a spin ensemble has been demonstrated experimentally [\[20–23\]](#page-4-0), implementing the *read* step remains the major obstacle to an operational microwave quantum memory. An intermediate goal consists in storing a classical microwave pulse with an ultralow power corresponding to an average of one photon in the resonator and to retrieve it as an echo after a refocusing pulse, as was achieved at optical frequencies [\[24,25\]](#page-4-0). First results in this direction were obtained using ensembles of negatively charged nitrogen-vacancy (NV) color centers in diamond [\[26,27\]](#page-4-0) and of rare-earth ions in a Y_2SiO_5 crystal [\[28\]](#page-4-0). The NV's electronic spin is a spin triplet $(S = 1)$ well suited for a quantum memory because of its long coherence times in pure crystals [\[29,30\]](#page-4-0) and the possibility of repumping it into its ground state $m_S = 0$

by optical irradiation at 532 nm $[31]$ (see Fig. [1\)](#page-1-0). In $[27]$, successive low-power microwave pulses were stored in an NV ensemble, and retrieved later as a series of echoes after a refocusing microwave pulse was applied. A key aspect in this experiment was an active reset of the NVs to increase the repetition rate of successive experimental sequences to obtain sufficient statistics; this was achieved by applying optical pumping laser pulses injected through an optical fiber introduced in the cryostat. The echo efficiency, defined as the ratio of the echo energy and the stored pulse energy, was, however, not sufficient in [\[27\]](#page-4-0) to observe an echo below 100 photons on average in the resonator.

Here, using a sample with a longer coherence time and an improved optical pumping scheme, we increase the echo efficiency and the storage time by one order of magnitude. This allows us to observe an echo with an initial pulse power corresponding to on average only one photon in the resonator. The diamond single crystal was synthesized by the temperature gradient method at high pressure and high temperature using 99*.*97% 12C-enriched pyrolytic carbon prepared from 12Cenriched methane as a carbon source [\[32\]](#page-4-0), resulting in a nominal 300 ppm concentration of 13C nuclei. The original 1*.*4 ppm concentration of substitutional nitrogen impurities (so-called P1 centers) was partially converted into NV centers by 2 MeV electron irradiation at room temperature followed by annealing for 2 h at 1000 °C, yielding a final $[NV^-] = 0.4$ ppm and $[P1] = 0.6$ ppm. A scheme of the experimental setup is shown in Fig. $1(a)$. The diamond is glued onto the inductance of a superconducting planar lumped-element *LC* resonator patterned in a niobium thin film on a silicon substrate. Microwave pulses can be sent to the resonator input; the reflected signal is amplified at 4 K and its amplitude and phase are measured at room temperature by a homodyne detection setup. For resetting the spins, laser pulses at 532 nm can be sent onto the sample through direct optical access in the dilution cryostat.

FIG. 1. (Color online) (a) Experimental setup and principle of the experiment. An ensemble of $\sim 10^{10}$ spins is inductively coupled to a planar superconducting LC resonator of frequency ω_r (with a collective coupling constant *g*ens), cooled at 10 mK. The resonator is measured in reflection through an input coupling capacitance. Microwave pulses are produced by mixing a continuous microwave source with dc pulses generated by an arbitrary wave form generator (AWG). They drive the spins via the microwave current induced in the resonator inductance. The reflected microwave signal (including the emitted echo) is amplified at low temperature and demodulated at room temperature, yielding its amplitude $A(t)$ and phase $\phi(t)$. (b) The spins are nitrogen-vacancy color centers in diamond, which consist of a nitrogen impurity next to a vacancy of the diamond lattice. A dc magnetic field B_{NV} applied parallel to the chip along the [110] crystalline axis so that only NV centers whose axis are nonorthogonal to the field (shown in blue in the figure) are Zeeman shifted and contribute to the signal. Laser pulses can be sent onto the diamond via a direct optical access to the cryostat mixing chamber. (c) NV centers energy levels in a weak magnetic field. The electronic ground state is a spin triplet *S* = 1, with a zero-field splitting $D/2\pi$ = 2.88 GHz, coupled by hyperfine interaction to the ¹⁴N nuclear spin triplet $I = 1$. This splits each of the $|m_S = 0\rangle \rightarrow |m_S = +1\rangle$ transitions into a triplet of lines.

The resonator reflection coefficient $S_{11}(\omega)$, measured with a network analyzer, is shown in Fig. $2(a)$, yielding the resonance frequency $\omega_r/2\pi = 2.915$ GHz and quality factor $Q = 650$, fixed by the coupling to the measurement line through the input capacitor. NV centers are detected by their absorption of the microwave whenever their transition frequency matches ω_r . The energy levels of the NV centers are schematically shown in Fig. $1(c)$. The electronic spin is coupled by hyperfine interaction to the spin-triplet $(I = 1)$ nuclear spin of the ¹⁴N atom, resulting in a splitting of the $|m_S = 0\rangle \rightarrow |m_S =$ +1) transition into three resonances separated by 2.2 MHz corresponding to the three different m_I states of the ¹⁴N. A dc magnetic field B_{NV} is applied parallel to the chip, along the [110] crystalline axis of the diamond. Out of the four possible orientations of NV centers along [111] crystalline axes, two are perpendicular to the field and are therefore not Zeeman shifted, so that they do not contribute to the signal. The remaining two families are brought into resonance with ω_r at $B_{\text{NV}} \sim 1.8 \text{ mT}$, as shown in Fig. $2(b)$ where the hyperfine triplet is clearly seen as dips in $|S_{11}(\omega)|$ when they cross the resonance. A ∼200 kHz

FIG. 2. (Color online) (a) Phase *φ* of the resonator reflection coefficient $S_{11}(\omega)$ measured with a vector network analyzer (blue dots), yielding $\omega_r/2\pi = 2.915$ GHz and $Q = 650$ (red line is a fit to the data). (b) $S_{11}(\omega)$ as a function of B_{NV} around 1.8 mT, showing the NV centers as a triplet of absorption dips. The inset shows $|S_{11}|(B_{\text{NV}})$ at $\omega/2\pi = 2.915$ GHz; blue dots are data, and red line is a fit to a sum of three Lorentzians with linewidth 0*.*012 mT. (c) Measured spin polarization for a laser pulse of power $P_L = 280 \mu W$ as a function of its duration *TL*, renormalized to its maximal value. Dashed red and black lines indicate the laser pulse durations $T_L = 0.2$ and 0.1 s used in the experiments shown in Figs. [3](#page-2-0) and [4,](#page-3-0) corresponding to relative polarizations $p/p_{\text{max}} = 0.72$ and 0.62.

full width at half maximum (FWHM) linewidth is measured for each line of the triplet, much narrower than in previous work [\[20,27\]](#page-4-0), due to a lower P1 center concentration and to the isotopic enrichment in 12 C.

For optical pumping of the NV centers, the laser beam is focused to a 0*.*6 mm diameter at the sample level, with a power of 0*.*28 mW. In this geometry, it is straightforward to optimize the laser beam position on the sample in order to minimize the amount of power needed to reset the spins in their ground state. The efficiency of the optical pumping is measured as explained in [\[27\]](#page-4-0). The experimental sequence includes an initial strong microwave pulse that results in spin saturation, followed by a laser pulse of varying duration T_L . After a 300 *μ*s delay necessary for relaxation of the quasiparticles generated in the superconducting thin film and in the silicon substrate, the reflected amplitude of a few-photon microwave pulse reveals the spin polarization. The extracted polarization level $p(T_L)$ is shown in Fig. 2(c). It changes only slightly

FIG. 3. (Color online) (a) Hahn echo sequence. The spins are first reset in their ground state by a laser pulse of power 280 μ W and duration 0.2 s. A first 1 μ s microwave pulse θ at ω_r , of power −71 dBm, induces a transverse magnetization which decays within T_2^* . A 1- μ s-long microwave refocusing pulse (*R*) of power -20 dBm is applied at $\tau = 50 \mu s$, which rephases the spins at 2τ . The microwave amplitude (blue curve) shows both the reflection of the two microwave pulses driving the spins (with their amplitude trimmed by saturation of our detection chain, as indicated in red), as well as the echo emitted at 2τ upon rephasing of the spins. (b) Measured decay of the echo amplitude *A* as a function of 2*τ* (open circles). Calculated decay due to a bath of 213 ppm of 13C (dashed orange curve), 0*.*6 ppm of P1 centers causing spectral diffusion (dotted green line), 0*.*2 ppm of NV centers causing instantaneous diffusion (dash-dotted blue line), and the combination of the three contributions (solid red line). The theory curves have been scaled in amplitude according to the data. An exponential fit (black solid line) yields a coherence time $T_2 = 84 \mu s$.

above $T_L = 1$ s, indicating that the maximum NV polarization possible with irradiation at 532 nm ($p_{\text{max}} = 90\%$ according to [\[33\]](#page-4-0)) is reached. Compared to earlier work [\[27\]](#page-4-0) where the laser position could not be optimized, the maximum polarization can be reached with ∼20 times lower pulse energy. This makes it possible to perform the experiments at a faster repetition rate (0.2 Hz) and at a cryostat temperature $T = 100$ mK instead of 400 mK $[27]$, thus closely approaching the condition $kT \ll \hbar \omega_r$ required in order for thermal noise to be completely suppressed.

High-power Hahn echoes are measured at $B_{\text{NV}} = 1.74 \text{ mT}$, using microwave pulses at $\omega = \omega_r$ according to the sequence shown in Fig. $3(a)$. The sequence starts with a laser pulse of duration $T_L = 0.2$ s, resulting in a spin polarization $p =$ 0.72 $p_{\text{max}} = 0.65$. At $t = 0$, a first pulse generates a transverse magnetization in the ensemble, followed by a refocusing microwave pulse at $t = \tau$ which induces rephasing of the spins

at 2τ and emission of a spin echo into the measuring line, as seen in Fig. $3(a)$. Note that due to spatial inhomogeneity of the microwave field generated by the planar inductance, it is not possible to apply a well-defined Rabi angle to all the spins, which results in a reduced echo visibility. The echo amplitude is measured as a function of the delay 2*τ* between the first pulse and the echo, and is found to decay approximately exponentially with a time constant $T_2 = 84 \mu s$ [see Fig. 3(b)]. Decoherence occurs due to dipolar interactions with the bath of paramagnetic species present in the sample $(^{13}C$ nuclei, P1 centers, and NV centers), whose dynamical evolution causes a randomization of the phase acquired by NV centers during the two halves of the spin-echo sequence. The 13 C nuclei bath precesses at the Larmor frequency $\gamma_n B_{\text{NV}} = 2\pi \times 130 \text{ kHz}$ (γ_n being the ¹³C gyromagnetic ratio), giving rise to a characteristic oscillation pattern [\[34–36\]](#page-4-0) in the spin-echo amplitude, visible in the data of Fig. $3(b)$. The dynamics due to flip-flop events within the P1 center bath is responsible for a decoherence process known as spectral diffusion [\[37\]](#page-4-0). Finally, the bath consisting of NV centers at frequency ω_r (only half of the total NV concentration) unavoidably undergoes spin flips due to the refocusing pulse itself, which constitutes an efficient decoherence process called instantaneous diffusion [\[38\]](#page-4-0). The various contributions of each bath were calculated using the cluster-correlation expansion method [\[39,40\]](#page-4-0), with concentrations $[P1] = 0.6$ ppm, $[NV^-] = 0.4/2 = 0.2$ ppm, and $[{}^{13}C] = 213$ ppm, compatible with the sample parameters. Good agreement with the data is obtained [see Fig. 3(b)]. Overall, dipolar interactions between NV centers appear to be the dominant source of decoherence in our experiment.

Since the echo efficiency was limited by the finite spin coherence time in earlier work [\[27\]](#page-4-0), a significant improvement is expected with this new sample. The echo efficiency is first measured by performing a Hahn echo sequence with a lowpower microwave pulse. The experimental sequence, shown in Fig. [4,](#page-3-0) starts with a 0*.*2 s repumping laser pulse, followed after 300 *μ*s by a microwave pulse populating the resonator with on average 60 photons, and $\tau = 50 \mu s$ later, by a refocusing pulse. A spin echo is detected at $t = 2\tau$. The efficiency, defined as the energy recovered during the echo divided by the absorbed energy, reaches $E = 0.3\%$.

The whole spin-echo sequence was simulated by numerical integration of the coupled differential equations obtained after discretizing the resonance frequency and coupling constant distribution in the spin ensemble (see [\[14\]](#page-4-0)). A 130 kHz linewidth of each hyperfine peak and a collective coupling constant $g_{\text{ens}}/2\pi = 410$ kHz (when all spins are polarized), are compatible with the experimentally determined parameters and yield quantitative agreement with the shape of both the absorbed microwave pulse and the spin-echo amplitude. The discrepancy noted in [\[27\]](#page-4-0) is absent in the present experiment, probably because decoherence is negligible during the driven evolution. The finite T_2 and the imperfect π pulse due to the spread in Rabi frequencies are the main factors limiting *E*, while the finite cooperativity $C = 0.22$ [\[14\]](#page-4-0) limits both the absorption and the echo emission out of the cavity.

Owing to the larger value of *E*, it becomes possible to reach the level where a spin echo can be observed for an initial pulse populating the resonator with only a single microwave photon on average. This is shown in Fig. $4(b)$. Note that a shorter

FIG. 4. (Color online) Spin echo at the few-photon level. The experimental sequence is the same as in Fig. [3,](#page-2-0) but with an initial microwave pulse having a power corresponding to (a) 60 and (b) one photon inside the resonator. The signal was averaged over 3×10^4 (a) and 5×10^5 (b) sequences, with a repetition rate of 5 Hz (a) and 10 Hz (b), limited by the laser pulse duration. Blue solid lines are experimental data, and red dashed-dotted lines are the results of simulations as explained in the text. The signal-to-noise ratio, defined as the ratio between signal intensity integrated over the echo duration and the corresponding noise intensity, is 4 for the 60-photon pulse (a) and 1*.*5 in the one-photon pulse (b).

C. GREZES *et al.* PHYSICAL REVIEW A **92**, 020301(R) (2015)

repumping time of 0*.*1 s (with the same laser power) was used, in order to enable a larger number 5×10^5 of repetitions of the experiment. The shorter repumping step yields a lower spin polarization $p = 0.56$ as shown in Fig. [2](#page-1-0) and a lower cooperativity of 0*.*19, which results in a correspondingly lower echo efficiency than in Fig. $4(a)$. These results are again quantitatively reproduced by the simulations with the same parameters as mentioned earlier, using the experimentally determined repumping efficiency.

The coherence times demonstrated in this experiment match those requested in a realistic quantum memory protocol [\[14\]](#page-4-0), which suggests that a first implementation is within reach. The remaining challenges are the improvement of the refocusing pulse using adiabatic passage as demonstrated recently [\[41\]](#page-4-0), and the integration of dynamical tuning of the resonator frequency and quality factor with more elaborate spin-echo sequences. The latter is needed in particular to silence the echo emission $[11,12]$ in-between the two π pulses in the course of the *read* step of the protocol. The microwave currents needed to drive the spins during the refocusing pulses are much stronger than typical Josephson junction critical currents. This precludes the use of integrated superconducting quantum interference devices as in $[20,42]$, while a combination of coupled linear and tunable resonators [\[43\]](#page-4-0) may be employed as tuning elements in the resonator.

In conclusion we report the measurement of a spin echo with an initial microwave pulse at the single-photon level. The figures of merit reached are sufficient to envision first implementations of a spin-ensemble multimode quantum memory for superconducting qubits.

We acknowledge technical support from P. Sénat, D. Duet, J.-C. Tack, P. Pari, and P. Forget, as well as useful discussions within the Quantronics Goup and with A. Dréau, J.-F. Roch, T. Chanelière, and J. Morton. We acknowledge the support of the French National Research Agency (ANR) with the QINVC project from CHISTERA program, the European project SCALEQIT, the C'Nano IdF project QUANTRO-CRYO, JST, and JSPS KAKENHI (Grant No. 26246001). Y.K. acknowledges support from the JSPS, and B.J. and K.M. from the Villum Foundation.

- [1] C. Rigetti, J. M. Gambetta, S. Poletto, B. L. T. Plourde, J. M. Chow, A. D. Córcoles, J. A. Smolin, S. T. Merkel, J. R. Rozen, G. A. Keefe, M. B. Rothwell, M. B. Ketchen, and M. Steffen, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.86.100506) **[86](http://dx.doi.org/10.1103/PhysRevB.86.100506)**, [100506](http://dx.doi.org/10.1103/PhysRevB.86.100506) [\(2012\)](http://dx.doi.org/10.1103/PhysRevB.86.100506).
- [2] R. Barends, J. Kelly, A. Megrant, D. Sank, E. Jeffrey, Y. Chen, Y. Yin, B. Chiaro, J. Mutus, C. Neill, P. O'Malley, P. Roushan, [J. Wenner, T. C. White, A. N. Cleland, and J. M. Martinis,](http://dx.doi.org/10.1103/PhysRevLett.111.080502) Phys. Rev. Lett. **[111](http://dx.doi.org/10.1103/PhysRevLett.111.080502)**, [080502](http://dx.doi.org/10.1103/PhysRevLett.111.080502) [\(2013\)](http://dx.doi.org/10.1103/PhysRevLett.111.080502).
- [3] M. Stern, G. Catelani, Y. Kubo, C. Grezes, A. Bienfait, D. Vion, D. Esteve, and P. Bertet, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.113.123601) **[113](http://dx.doi.org/10.1103/PhysRevLett.113.123601)**, [123601](http://dx.doi.org/10.1103/PhysRevLett.113.123601) [\(2014\)](http://dx.doi.org/10.1103/PhysRevLett.113.123601).
- [4] Y. Kubo, F. R. Ong, P. Bertet, D. Vion, V. Jacques, D. Zheng, A. Dreau, J. F. Roch, A. Auffeves, F. Jelezko, J. Wrachtrup, M. F. Barthe, P. Bergonzo, and D. Esteve, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.105.140502) **[105](http://dx.doi.org/10.1103/PhysRevLett.105.140502)**, [140502](http://dx.doi.org/10.1103/PhysRevLett.105.140502) [\(2010\)](http://dx.doi.org/10.1103/PhysRevLett.105.140502).
- [5] D. I. Schuster, A. P. Sears, E. Ginossar, L. DiCarlo, L. Frunzio, J. J. L. Morton, H. Wu, G. A. D. Briggs, B. B. Buckley, D. D. Awschalom, and R. J. Schoelkopf, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.105.140501) **[105](http://dx.doi.org/10.1103/PhysRevLett.105.140501)**, [140501](http://dx.doi.org/10.1103/PhysRevLett.105.140501) [\(2010\)](http://dx.doi.org/10.1103/PhysRevLett.105.140501).
- [6] R. Amsüss, C. Koller, T. Nöbauer, S. Putz, S. Rotter, K. Sandner, S. Schneider, M. Schramböck, G. Steinhauser, H. Ritsch, J. Schmiedmayer, and J. Majer, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.107.060502) **[107](http://dx.doi.org/10.1103/PhysRevLett.107.060502)**, [060502](http://dx.doi.org/10.1103/PhysRevLett.107.060502) [\(2011\)](http://dx.doi.org/10.1103/PhysRevLett.107.060502).
- [7] V. Ranjan, G. de Lange, R. Schutjens, T. Debelhoir, J. P. Groen, D. Szombati, D. J. Thoen, T. M. Klapwijk, R. Hanson, and L. DiCarlo, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.110.067004) **[110](http://dx.doi.org/10.1103/PhysRevLett.110.067004)**, [067004](http://dx.doi.org/10.1103/PhysRevLett.110.067004) [\(2013\)](http://dx.doi.org/10.1103/PhysRevLett.110.067004).
- [8] S. Probst, H. Rotzinger, S. Wünsch, P. Jung, M. Jerger, M. Siegel, A. V. Ustinov, and P. A. Bushev, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.110.157001) **[110](http://dx.doi.org/10.1103/PhysRevLett.110.157001)**, [157001](http://dx.doi.org/10.1103/PhysRevLett.110.157001) [\(2013\)](http://dx.doi.org/10.1103/PhysRevLett.110.157001).

STORAGE AND RETRIEVAL OF MICROWAVE FIELDS AT . . . PHYSICAL REVIEW A **92**, 020301(R) (2015)

- [9] Y. Tabuchi, S. Ishino, T. Ishikawa, R. Yamazaki, K. Usami, and Y. Nakamura, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.113.083603) **[113](http://dx.doi.org/10.1103/PhysRevLett.113.083603)**, [083603](http://dx.doi.org/10.1103/PhysRevLett.113.083603) [\(2014\)](http://dx.doi.org/10.1103/PhysRevLett.113.083603).
- [10] G. Kurizki, P. Bertet, Y. Kubo, K. Mølmer, D. Petrosyan, P. Rabl, and J. Schmiedmayer, [Proc. Natl. Acad. Sci. USA](http://dx.doi.org/10.1073/pnas.1419326112) **[112](http://dx.doi.org/10.1073/pnas.1419326112)**, [3866](http://dx.doi.org/10.1073/pnas.1419326112) [\(2015\)](http://dx.doi.org/10.1073/pnas.1419326112).
- [11] V. Damon, M. Bonarota, A. Louchet-Chauvet, T. Chanelière, and J.-L. Le Gouët, [New J. Phys.](http://dx.doi.org/10.1088/1367-2630/13/9/093031) **[13](http://dx.doi.org/10.1088/1367-2630/13/9/093031)**, [093031](http://dx.doi.org/10.1088/1367-2630/13/9/093031) [\(2011\)](http://dx.doi.org/10.1088/1367-2630/13/9/093031).
- [12] D. L. McAuslan, P. M. Ledingham, W. R. Naylor, S. E. Beavan, M. P. Hedges, M. J. Sellars, and J. J. Longdell, [Phys. Rev. A](http://dx.doi.org/10.1103/PhysRevA.84.022309) **[84](http://dx.doi.org/10.1103/PhysRevA.84.022309)**, [022309](http://dx.doi.org/10.1103/PhysRevA.84.022309) [\(2011\)](http://dx.doi.org/10.1103/PhysRevA.84.022309).
- [13] D. Rieländer, K. Kutluer, P. M. Ledingham, M. Gündoğan, J. Fekete, M. Mazzera, and H. de Riedmatten, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.112.040504) **[112](http://dx.doi.org/10.1103/PhysRevLett.112.040504)**, [040504](http://dx.doi.org/10.1103/PhysRevLett.112.040504) [\(2014\)](http://dx.doi.org/10.1103/PhysRevLett.112.040504).
- [14] [B. Julsgaard, C. Grezes, P. Bertet, and K. Mølmer,](http://dx.doi.org/10.1103/PhysRevLett.110.250503) Phys. Rev. Lett. **[110](http://dx.doi.org/10.1103/PhysRevLett.110.250503)**, [250503](http://dx.doi.org/10.1103/PhysRevLett.110.250503) [\(2013\)](http://dx.doi.org/10.1103/PhysRevLett.110.250503).
- [15] M. Afzelius, N. Sangouard, G. Johansson, M. U. Staudt, and C. M. Wilson, [New J. Phys.](http://dx.doi.org/10.1088/1367-2630/15/6/065008) **[15](http://dx.doi.org/10.1088/1367-2630/15/6/065008)**, [065008](http://dx.doi.org/10.1088/1367-2630/15/6/065008) [\(2013\)](http://dx.doi.org/10.1088/1367-2630/15/6/065008).
- [16] A. Palacios-Laloy, F. Nguyen, F. Mallet, P. Bertet, D. Vion, and D. Esteve, [J. Low Temp. Phys.](http://dx.doi.org/10.1007/s10909-008-9774-x) **[151](http://dx.doi.org/10.1007/s10909-008-9774-x)**, [1034](http://dx.doi.org/10.1007/s10909-008-9774-x) [\(2008\)](http://dx.doi.org/10.1007/s10909-008-9774-x).
- [17] M. Sandberg, C. M. Wilson, F. Persson, T. Bauch, G. Johansson, V. Shumeiko, T. Duty, and P. Delsing, [Appl. Phys. Lett.](http://dx.doi.org/10.1063/1.2929367) **[92](http://dx.doi.org/10.1063/1.2929367)**, [203501](http://dx.doi.org/10.1063/1.2929367) [\(2008\)](http://dx.doi.org/10.1063/1.2929367).
- [18] Y. Yin, Y. Chen, D. Sank, P. J. J. O'Malley, T. C. White, R. Barends, J. Kelly, E. Lucero, M. Mariantoni, A. Megrant, C. Neill, A. Vainsencher, J. Wenner, A. N. Korotkov, A. N. Cleland, and J. M. Martinis, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.110.107001) **[110](http://dx.doi.org/10.1103/PhysRevLett.110.107001)**, [107001](http://dx.doi.org/10.1103/PhysRevLett.110.107001) [\(2013\)](http://dx.doi.org/10.1103/PhysRevLett.110.107001).
- [19] J. Wenner, Y. Yin, Y. Chen, R. Barends, B. Chiaro, E. Jeffrey, J. Kelly, A. Megrant, J. Y. Mutus, C. Neill, J. J. O'Malley, P. Roushan, D. Sank, A. Vainsencher, T. C. White, A. N. Korotkov, A. N. Cleland, and J. M. Martinis, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.112.210501) **[112](http://dx.doi.org/10.1103/PhysRevLett.112.210501)**, [210501](http://dx.doi.org/10.1103/PhysRevLett.112.210501) [\(2014\)](http://dx.doi.org/10.1103/PhysRevLett.112.210501).
- [20] Y. Kubo, C. Grezes, A. Dewes, T. Umeda, J. Isoya, H. Sumiya, N. Morishita, H. Abe, S. Onoda, T. Ohshima, V. Jacques, A. Dréau, J.-F. Roch, I. Diniz, A. Auffeves, D. Vion, D. Esteve, and P. Bertet, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.107.220501) **[107](http://dx.doi.org/10.1103/PhysRevLett.107.220501)**, [220501](http://dx.doi.org/10.1103/PhysRevLett.107.220501) [\(2011\)](http://dx.doi.org/10.1103/PhysRevLett.107.220501).
- [21] X. Zhu, S. Saito, A. Kemp, K. Kakuyanagi, S.-i. Karimoto, H. Nakano, W. J. Munro, Y. Tokura, M. S. Everitt, K. Nemoto, M. Kasu, N. Mizuochi, and K. Semba, [Nature \(London\)](http://dx.doi.org/10.1038/nature10462) **[478](http://dx.doi.org/10.1038/nature10462)**, [221](http://dx.doi.org/10.1038/nature10462) [\(2011\)](http://dx.doi.org/10.1038/nature10462).
- [22] S. Saito, X. Zhu, R. Amsüss, Y. Matsuzaki, K. Kakuyanagi, T. Shimo-Oka, N. Mizuochi, K. Nemoto, W. J. Munro, and K. Semba, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.111.107008) **[111](http://dx.doi.org/10.1103/PhysRevLett.111.107008)**, [107008](http://dx.doi.org/10.1103/PhysRevLett.111.107008) [\(2013\)](http://dx.doi.org/10.1103/PhysRevLett.111.107008).
- [23] Y. Tabuchi, S. Ishino, A. Noguchi, T. Ishikawa, R. Yamazaki, K. Usami, and Y. Nakamura, [Science](http://dx.doi.org/10.1126/science.aaa3693) **[349](http://dx.doi.org/10.1126/science.aaa3693)**, [405](http://dx.doi.org/10.1126/science.aaa3693) [\(2015\)](http://dx.doi.org/10.1126/science.aaa3693).
- [24] H. De Riedmatten, M. Afzelius, M. U. Staudt, C. Simon, and N. Gisin, [Nature \(London\)](http://dx.doi.org/10.1038/nature07607) **[456](http://dx.doi.org/10.1038/nature07607)**, [773](http://dx.doi.org/10.1038/nature07607) [\(2008\)](http://dx.doi.org/10.1038/nature07607).
- [25] P. Jobez, C. Laplane, N. Timoney, N. Gisin, A. Ferrier, P. Godlner, and M. Afzelius, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.114.230502) **[114](http://dx.doi.org/10.1103/PhysRevLett.114.230502)**, [230502](http://dx.doi.org/10.1103/PhysRevLett.114.230502) [\(2015\)](http://dx.doi.org/10.1103/PhysRevLett.114.230502).
- [26] A. Gruber, A. Dräbenstedt, C. Tietz, L. Fleury, J. Wrachtrup, and C. Von Borczyskowski, [Science](http://dx.doi.org/10.1126/science.276.5321.2012) **[276](http://dx.doi.org/10.1126/science.276.5321.2012)**, [2012](http://dx.doi.org/10.1126/science.276.5321.2012) [\(1997\)](http://dx.doi.org/10.1126/science.276.5321.2012).
- [27] C. Grezes, B. Julsgaard, Y. Kubo, M. Stern, T. Umeda, J. Isoya, H. Sumiya, H. Abe, S. Onoda, T. Ohshima, V. Jacques, J. Esteve, D. Vion, D. Esteve, K. Mølmer, and P. Bertet, [Phys. Rev. X](http://dx.doi.org/10.1103/PhysRevX.4.021049) **[4](http://dx.doi.org/10.1103/PhysRevX.4.021049)**, [021049](http://dx.doi.org/10.1103/PhysRevX.4.021049) [\(2014\)](http://dx.doi.org/10.1103/PhysRevX.4.021049).
- [28] [S. Probst, H. Rotzinger, A. Ustinov, and P. Bushev,](http://dx.doi.org/10.1103/PhysRevB.92.014421) *Phys. Rev.* B **[92](http://dx.doi.org/10.1103/PhysRevB.92.014421)**, [014421](http://dx.doi.org/10.1103/PhysRevB.92.014421) [\(2015\)](http://dx.doi.org/10.1103/PhysRevB.92.014421).
- [29] G. Balasubramian, P. Neumann, D. Twitchen, M. Markham, R. Koselov, N. Mizuochi, J. Isoya, J. Achard, J. Beck, J. Tissler, V. Jacques, P. Hemmer, F. Jelezko, and J. Wrachtrup, [Nat. Mater.](http://dx.doi.org/10.1038/nmat2420) **[8](http://dx.doi.org/10.1038/nmat2420)**, [383](http://dx.doi.org/10.1038/nmat2420) [\(2009\)](http://dx.doi.org/10.1038/nmat2420).
- [30] N. Bar-Gill, L. Pham, A. Jarmola, D. Budker, and R. Walsworth, [Nat. Commun.](http://dx.doi.org/10.1038/ncomms2771) **[4](http://dx.doi.org/10.1038/ncomms2771)**, [1743](http://dx.doi.org/10.1038/ncomms2771) [\(2013\)](http://dx.doi.org/10.1038/ncomms2771).
- [31] N. B. Manson, J. P. Harrison, and M. J. Sellars, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.74.104303) **[74](http://dx.doi.org/10.1103/PhysRevB.74.104303)**, [104303](http://dx.doi.org/10.1103/PhysRevB.74.104303) [\(2006\)](http://dx.doi.org/10.1103/PhysRevB.74.104303).
- [32] K. Nakamura, S. Yamashita, T. Tojo, M. Mitsuishi, K. Kataoka, and M. Yoshimoto, [Diam. Relat. Mater.](http://dx.doi.org/10.1016/j.diamond.2007.07.001) **[16](http://dx.doi.org/10.1016/j.diamond.2007.07.001)**, [1765](http://dx.doi.org/10.1016/j.diamond.2007.07.001) [\(2007\)](http://dx.doi.org/10.1016/j.diamond.2007.07.001).
- [33] L. Robledo, L. Childress, H. Bernien, B. Hensen, P. Alkemade, and R. Hanson, [Nature \(London\)](http://dx.doi.org/10.1038/nature10401) **[477](http://dx.doi.org/10.1038/nature10401)**, [574](http://dx.doi.org/10.1038/nature10401) [\(2011\)](http://dx.doi.org/10.1038/nature10401).
- [34] J. R. Maze, J. M. Taylor, and M. D. Lukin, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.78.094303) **[78](http://dx.doi.org/10.1103/PhysRevB.78.094303)**, [094303](http://dx.doi.org/10.1103/PhysRevB.78.094303) [\(2008\)](http://dx.doi.org/10.1103/PhysRevB.78.094303).
- [35] P. L. Stanwix, L. M. Pham, J. R. Maze, D. Le Sage, T. K. Yeung, P. Cappellaro, P. R. Hemmer, A. Yacoby, M. D. Lukin, and R. L. Walsworth, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.82.201201) **[82](http://dx.doi.org/10.1103/PhysRevB.82.201201)**, [201201](http://dx.doi.org/10.1103/PhysRevB.82.201201) [\(2010\)](http://dx.doi.org/10.1103/PhysRevB.82.201201).
- [36] N. Zhao, S.-W. Ho, and R.-B. Liu, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.85.115303) **[85](http://dx.doi.org/10.1103/PhysRevB.85.115303)**, [115303](http://dx.doi.org/10.1103/PhysRevB.85.115303) [\(2012\)](http://dx.doi.org/10.1103/PhysRevB.85.115303).
- [37] G. de Lange, Z. H. Wang, D. Rist, V. V. Dobrovitski, and R. Hanson, [Science](http://dx.doi.org/10.1126/science.1192739) **[330](http://dx.doi.org/10.1126/science.1192739)**, [60](http://dx.doi.org/10.1126/science.1192739) [\(2010\)](http://dx.doi.org/10.1126/science.1192739).
- [38] A. Tyryshkin, S. Tojo, J. Morton, H. Riemann, N. Abrosimov, P. Becker, H.-J. Pohl, T. Schenkel, M. Thewalt, K. Itoh, and S. Lyon, [Nat. Mater.](http://dx.doi.org/10.1038/nmat3182) **[11](http://dx.doi.org/10.1038/nmat3182)**, [143](http://dx.doi.org/10.1038/nmat3182) [\(2012\)](http://dx.doi.org/10.1038/nmat3182).
- [39] W. Yang and R.-B. Liu, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.78.085315) **[78](http://dx.doi.org/10.1103/PhysRevB.78.085315)**, [085315](http://dx.doi.org/10.1103/PhysRevB.78.085315) [\(2008\)](http://dx.doi.org/10.1103/PhysRevB.78.085315).
- [40] W. Yang and R.-B. Liu, [Phys. Rev. B](http://dx.doi.org/10.1103/PhysRevB.79.115320) **[79](http://dx.doi.org/10.1103/PhysRevB.79.115320)**, [115320](http://dx.doi.org/10.1103/PhysRevB.79.115320) [\(2009\)](http://dx.doi.org/10.1103/PhysRevB.79.115320).
- [41] A. J. Sigillito, H. Malissa, A. M. Tyryshkin, H. Riemann, N. V. Abrosimov, P. Becker, H.-J. Pohl, M. L. W. Thewalt, K. M. Itoh, J. J. L. Morton, A. A. Houck, D. I. Schuster, and S. A. Lyon, [Appl. Phys. Lett.](http://dx.doi.org/10.1063/1.4881613) **[104](http://dx.doi.org/10.1063/1.4881613)**, [222407](http://dx.doi.org/10.1063/1.4881613) [\(2014\)](http://dx.doi.org/10.1063/1.4881613).
- [42] Y. Kubo, I. Diniz, A. Dewes, V. Jacques, A. Dréau, J.-F. Roch, A. Auffeves, D. Vion, D. Esteve, and P. Bertet, [Phys. Rev. A](http://dx.doi.org/10.1103/PhysRevA.85.012333) **[85](http://dx.doi.org/10.1103/PhysRevA.85.012333)**, [012333](http://dx.doi.org/10.1103/PhysRevA.85.012333) [\(2012\)](http://dx.doi.org/10.1103/PhysRevA.85.012333).
- [43] C. Grezes, Ph.D. thesis, Université Pierre-et-Marie-Curie, 2014.