Attosecond structures from the molecular cavity in fullerene photoemission time delay

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Photoelectron spectroscopy studies earlier probed oscillations in C_{60} valence emissions, producing a series of minima whose energy separation depends on the molecular cavity. We show here that the quantum phase at these cavity minima exhibits variations from strong electron correlations in C_{60} , causing rich structures in the emission time delay. Hence, these minima offer unique spectral zones to directly explore multielectron forces via attosecond RABITT interferometry not only in fullerenes, but also in clusters and nanostructures for which such minima are likely abundant.

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I. INTRODUCTION

Resolving electron dynamics in real-time offers access into a plethora of electron-correlation driven processes in atomic, molecular, and more complex systems. The advent in technology of producing isolated ultrashort laser pulses and pulse trains dovetails a new landscape of active and precision research of light-matter interactions on ultrafast time scales [\[1–4\]](#page-4-0). For instance, in pump-probe laser spectroscopy, a pump pulse initiates an electronic process while a subsequent probe pulse explores the electron's motion with a temporal resolution of a few femtoseconds to several attoseconds. This serves as a microcosm of a fundamental mechanism by which a laser-driven process can be viewed as generating dynamical electronic wave packets with evolving amplitudes, phases, and group delays.

The relative delay between 2*s* and 2*p* photoemissions in neon was measured in a pilot experiment by attosecond streaking metrology [\[5\]](#page-4-0). Also, for argon, the relative delay between 3*s* and 3*p* photoemissions at energies below the 3*s* Cooper minimum [\[6,7\]](#page-4-0) and the group delay in 3*p* photorecombination across the 3*p* Cooper minimum [\[8\]](#page-4-0) were accessed using attosecond interferometry, known as RABITT. For simple molecules like diatomic nitrogen, two-color photoionization, resolved in attoseconds, was the subject of a recent study [\[9\]](#page-4-0). Moving to the other extreme in the structure scale, the condensed-phase systems, recent activities include measurements of the relative delay between the emission from conduction and valence band states of monocrystalline magnesium [\[10\]](#page-4-0) and tungsten [\[11\]](#page-4-0). Further, theoretical studies to explore delays in photoelectrons from metal surfaces brought about important insights [\[12\]](#page-4-0).

Straddling the line between atoms and condensed matters are clusters and nanostructures that not only have hybrid properties of the two extremes, but also exhibit special behaviors with fundamental effects and technological applications. Time-resolved access into the photoemission processes in fullerenes can be singularly attractive due to their eminent symmetry and stability. Recent efforts were

made to predict the time delay in photoemissions from atoms endohedrally confined in C_{60} [\[13–15\]](#page-4-0). However, these studies did not address the direct response of C_{60} electrons, but instead focused on the effects of confinement. Only recently, an electron momentum imaging measurement was performed to study the photoelectron angular distribution of C_{60} , establishing an indirect connection to the emission time delay at the plasmon resonance [\[16\]](#page-4-0). Evidently, hardly anything has been done to temporally explore cluster systems. In this paper, we report an investigation of the time delay in photoemission from the two highest occupied molecular orbitals, HOMO and HOMO-1, of C_{60} which uncovers dramatic attosecond response at characteristic emission minima. Results carry signatures of the C_{60} cavity, opening a new approach for molecular imaging applications, and most importantly establish an attosecond route to probing a remarkable aspect of electron correlations.

II. ESSENTIAL DETAILS OF THE METHOD

Time-dependent local density approximation (TDLDA) is employed to simulate the dynamical response of C_{60} to incident photons [\[17\]](#page-4-0). The dipole interaction, *z*, with the light that is linearly polarized in the *z* direction induces a frequencydependent complex change in the electron density arising from dynamical electron correlations. This can be written, using the independent particle (IP) susceptibility χ_0 , as

$$
\delta \rho(\mathbf{r}; \omega) = \int \chi_0(\mathbf{r}, \mathbf{r}'; \omega) [z' + \delta V(\mathbf{r}'; \omega)] d\mathbf{r}', \qquad (1)
$$

in which

$$
\delta V(\mathbf{r};\omega) = \int \frac{\delta \rho(\mathbf{r}';\omega)}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + \left[\frac{\partial V_{\rm XC}}{\partial \rho}\right]_{\rho = \rho_0} \delta \rho(\mathbf{r};\omega), \quad (2)
$$

where the first and second terms on the right-hand side are, respectively, the induced change of the Coulomb and the exchange-correlation potentials. Obviously, *δV* includes the dynamical field produced by important electron correlations within the linear response regime.

The gradient-corrected Leeuwen and Baerends exchangecorrelation functional (LB94) [\[18\]](#page-4-0) is used for the accurate asymptotic behavior of the ground-state potential. The C_{60} molecule is modeled by smearing 60 $C⁴⁺$ ions into a spherical

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FIG. 1. (Color online) Oscillations in the ratio of HOMO to HOMO-1 photoemission cross sections of C_{60} calculated using TDLDA and LB94, and compared with the experimental ratio [\[23\]](#page-4-0). Similar to [\[23\]](#page-4-0), a smooth background, that roughly fits the total photoionization cross section of atomic carbon [\[24\]](#page-4-0), is added to TDLDA cross sections to approximately account for local scatterings from carbon atoms. Photoelectron momenta at the peaks are indicated to illustrate that the conjugate of the oscillation period relates to the C_{60} diameter.

jellium shell, fixed in space, with an experimentally known C_{60} mean radius ($R = 3.54$ Å) and a width ($\Delta = 1.3$ Å) determined *ab initio* [\[17\]](#page-4-0). Inclusion of molecular orientations will have minimal effect on the result due to the C_{60} symmetry [\[19\]](#page-4-0). The delocalized system of total 240 valence electrons from 60 carbon atoms constructs the ground state in the Kohn-Sham frame [\[17\]](#page-4-0) using LB94. This produced HOMO and HOMO-1 to be of $2h$ ($l = 5$) and $2g$ ($l = 4$) character, respectively, with each having a radial node—a result known from the quantum chemical calculation [\[20\]](#page-4-0) supported by direct and inverse photoemission spectra [\[21\]](#page-4-0), and from energy-resolved electron-momentum density measurements [\[22\]](#page-4-0). TDLDA predicted oscillatory photoemission cross sections of HOMO and HOMO-1 in C_{60} which agreed well with the experiment [\[23\]](#page-4-0) and with quantum chemical calculations [\[23,25\]](#page-4-0). Figure 1 shows very good agreement between measurements and TDLDA ratio of HOMO and HOMO-1 cross sections for the four low-energy oscillations. An extra peak at 175 eV for TDLDA, and a slight offset between the theory-experiment positions of two high-energy peaks, *plus* some mismatch between their widths, are likely limitations of the jellium core. These oscillations are due to the interference between emissions from C_{60} shell edges as was shown by Fourier transforming the above ratio [\[23,26\]](#page-4-0) and evident from the fact in Fig. 1 that the reciprocal, $2\pi/\Delta k$, of the average peak separation ($\Delta k \sim 0.5$ a.u.) in photoelectron momentum (*k*) roughly equals the fullerene diameter. The comparison gives us confidence in the use of LB94.

Similar geometry-based oscillations in high-harmonic spectra of icosahedral fullerenes have been predicted [\[19\]](#page-4-0). This points to a common spectral implication between photoionization and recombination matrix elements.

III. CAVITY MINIMA

Studies of ionization time delay at resonances and minima (antiresonances) are attractive, since electron correlations can directly influence the result. Of particular interest is a Cooper minimum which arises at the zero of the wave-function overlap in the matrix element when the bound wave contains at least one radial node [\[27\]](#page-4-0). Around this minimum, the ionization probability is diminished which allows couplings with other electrons to dominate, offering a unique spectral zone to probe the correlation. We show that the minima in the oscillation of C_{60} valence emissions also appear from zeros in the matrix element, and thus can be of great value in capturing timeresolved many-electron dynamics.

Choosing the photon polarization along the *z* axis, the photoionization dipole amplitude in the IP picture, which omits the electron correlation dynamics, is $d = \langle \Psi_{kl'} | z | \Phi_{nl} \rangle$ in which $\Phi_{nl} = \phi_{nl}(r) Y_{lm}(\Omega_r)$ is a HOMO or HOMO-1 wave function, and the continuum wave function with $l' = l \pm 1$ is

$$
\Psi_{kl'}(\mathbf{r}) = (8\pi)^{\frac{3}{2}} \sum_{m'} e^{i\eta_{l'}} \psi_{kl'}(r) Y_{l'm'}(\Omega_{\mathbf{r}}) Y_{l'm'}^*(\Omega_{\mathbf{k}}), \quad (3)
$$

where the phase $\eta_{l'}(k)$ includes contributions from the shortrange and Coulomb potentials, besides a constant $l'\pi/2$. Using Eq. (3) , the radial matrix element (in length gauge) embedded in *d* is $\langle r \rangle = \langle \psi_{kl'} | r | \phi_{nl} \rangle$. This matrix element can also be expressed in an equivalent *acceleration gauge* as $\langle \psi_{kl'}| dV/dr | \phi_{nl} \rangle$, which embodies the notion that an ionizing (recoil) force *dV /dr* is available to an electron in a potential $V(r)$. Both the C₆₀ radial ground-state potential and its derivative are shown in Fig. $2(a)$. The potential exhibits rapid variations at the inner (R_{in}) and outer (R_{out}) radii but has a flatter bottom. Consequently, the derivative peaks (or antipeaks) at the shell edges, allowing two dominant contributions in the integral so one can approximate the matrix element as [\[26\]](#page-4-0)

$$
\langle r \rangle \approx A(k)[a_{\rm in} \psi_{kl'}(R_{\rm in}) + a_{\rm out} \psi_{kl'}(R_{\rm out})],\tag{4}
$$

where a_{in} and a_{out} are the values of ϕ_{nl} at R_{in} and R_{out} , and *A*(*k*) is a decaying function of *k* similar to the one calculated semiclassically for metal clusters [\[28\]](#page-4-0). In essence, this means a strong cancellation effect in the matrix elements at the interior region of the potential due to overlaps between oscillating $\psi_{kl'}$ and radially symmetric ϕ_{nl} . This symmetry, not present in atoms (where electrons are localized toward the nucleus), is a character of nanosystems with delocalized electrons; see the HOMO and HOMO-1 wave functions in Fig. $2(a)$. In any case, each term in Eq. (4) oscillates in *k* and vanishes when a node of $\psi_{kl'}$ moves through R_{in} or R_{out} or, equivalently, when an integer number of half-periods of continuum oscillation fits within $R_{\rm in}$ or $R_{\rm out}$; decreasing period of continuum waves with increasing energy is illustrated in Fig. $2(a)$. For each term, the effect is analogous to a single spherical-slit diffraction. Since the combination (interference) of two oscillations is itself an oscillation, $\langle r \rangle$ must also contain zeros, as shown in Fig. [2\(b\)](#page-2-0) for HOMO $\rightarrow k(l+1)$. Evidently, unlike the zero of a Cooper minimum, which depends on the node in the bound wave function, these zeros arise from nodes in the continuum wave function and can be termed as the *cavity minima*.

FIG. 2. (Color online) (a) Ground-state radial potential and its gradient, radial wave functions of HOMO and HOMO-1, and the continuum wave of $(l + 1)$ angular momentum for a low and a high energy. (b) The real IP radial matrix element compares to the real and imaginary components of the complex TDLDA matrix element. Besides two scaling regions, the imaginary part is multiplied by an overall factor of 5.

IV. RESULTS AND DISCUSSION

Wigner-Smith time delay, the energy differential of the phase of the photoemission amplitude [\[29\]](#page-4-0), is accessible by "two-color" XUV-IR schemes like an attosecond streak camera and RABITT. This is because the extra delay introduced by the IR probe pulse, the Coulomb-laser coupling delay, can be independently calculated and deducted from the data [\[15,30,31\]](#page-4-0). Our results [\[32\]](#page-4-0) of Wigner-Smith delay using the current TDLDA-LB94 scheme showed excellent agreement with RABITT measurements $[6-8]$ for argon. The standard techniques to extract the IR-induced delay information from the Coulomb and the short-range potentials are well described within the IP frame [\[30\]](#page-4-0). Reference [\[31\]](#page-4-0) derives this Coulomblaser coupling delay from a universal phase brought by the absorption of the IR photon in the presence of the Coulomb potential with charge *Z*. Whether multielectron effects like configuration interactions from level compactness could modify this delay is only a question for future research. In fact, experimental efforts to measure the current predictions or those from Ref. [\[16\]](#page-4-0) can only verify the validity of this question.

The IP radial matrix element $\langle r \rangle$ is real, implying that the IP phase is directly η in Eq. [\(3\)](#page-1-0) and, hence, insensitive to the zeros in the matrix element. However, the phase becomes sensitive to the cavity minima when TDLDA includes correlations via an energy-dependent complex induced potential *δV* in

FIG. 3. (Color online) TDLDA phases as a function of the photon energy for ionization through dipole allowed channels for (a) HOMO and (b) HOMO-1 electrons. Calculated ionization total phases from these levels are also shown.

the amplitude: $D = \langle \Psi_{kl'} | z + \delta V(\mathbf{r}) | \Phi_{nl} \rangle$; see Ref. [\[17\]](#page-4-0) for details of the formalism. Hence, the many-body effects could be directly probed by the phase and group delay measurements at these minima. The TDLDA phase

$$
\gamma = \eta + \arctan\left[\frac{\text{Im}\langle r + \delta V \rangle}{\text{Re}\langle r + \delta V \rangle}\right] = \eta + \arctan\left[\frac{\text{Im}\langle \delta V \rangle}{\langle r \rangle + \text{Re}\langle \delta V \rangle}\right], \tag{5}
$$

since $\langle r \rangle$ is real. In Eq. (5), the new radial matrix element $\langle r + \delta V(r) \rangle$ being complex suffers a π phase shift as its real part moves through zero at a cavity minimum.

TDLDA quantum phases for two dipole channels from each of HOMO and HOMO-1 are presented in Figs. 3. Phase shifts of about π at all cavity minima are noted; for HOMO-1 the shifts are roughly synchronized between the two channels [Fig. $3(b)$]. The direction of a phase shift, upward or downward, depends on the details of the TDLDA matrix element. Equation (5) suggests that $\langle r \rangle$ is correlation-corrected by $\text{Re}\langle \delta V \rangle$, but this correction diminishes at higher energies as seen in Fig. $2(b)$. When Re $\langle r + \delta V \rangle$ sloshes through zero, a *π* shift occurs. But the direction of the shift depends on the sign of Im $\langle r + \delta V \rangle$ —a quantity *entirely* correlation-induced. The oscillations in the imaginary part $[Fig. 2(b)]$ arise from a multichannel coupling with a large number of C_{60} inner channels which are open at these energies. The amplitudes of these inner channels do not oscillate in phase and have diverse phase offsets in relation to HOMO and HOMO-1 oscillations [\[26\]](#page-4-0). Consequently, the position of zeros in Im $\langle r + \delta V \rangle$ is a function of correlations via this multichannel process. Indeed, while the real and imaginary components are seen to oscillate roughly out of phase, the zeros of one do not occur

FIG. 4. (Color online) Wigner-Smith time delays for (a) HOMO and (b) HOMO-1 calculated within TDLDA framework and its comparison with the delays determined by a finite-difference approach, where an 800 nm IR pulse is used for the energy differential (see the text).

systematically on a definite side of the zeros of the other, causing the phase change to follow a pattern that directly maps the correlation the valence emission experiences at a cavity minimum.

In the RABITT experiment, one measures the delay associated with a phase Γ which is not resolved in the photoemission direction Ω_k :

$$
\Gamma = \arg[\bar{\mathcal{D}}_{l+1} \exp(i\gamma_{l+1}) + \bar{\mathcal{D}}_{l-1} \exp(i\gamma_{l-1})],\tag{6}
$$

where $\bar{\mathcal{D}}_l = \int d\Omega_{\mathbf{k}} |D_l(\Omega_{\mathbf{k}})|$. Since for a channel $\sigma_l \sim$ where $D_l = \int d\Omega_k |D_l(\Omega_k)|^2$, we approximate Eq. (6) by replacing $\bar{\mathcal{D}}$ by the square root of the respective channel cross sections. Figure [3](#page-2-0) also presents these calculated total phases.

TDLDA Wigner-Smith time delays, energy differentials of total phases, are shown in Fig. 4. To obtain the delay from the phases, one can use arbitrarily small energy steps for the differential. Measurements based on RABITT metrology typically use an 800 nm ($\omega = 1.55$ eV) IR probe pulse that leads to the extraction of the delay from measured Γ by $[\Gamma(E + \omega)$ – $\Gamma(E - \omega)/2\omega$. The resulting "finite-difference" TDLDA delays for HOMO and HOMO-1 are also shown in Fig. 4. Structures, corresponding to negative or positive delays, at the cavity minima indicate striking variations in the photoelectron speed. The fast (slow) emissions are effects of dynamical antiscreening (screening) from the multichannel coupling based on the Fano scheme [\[33\]](#page-4-0). In this, the correlation $\langle \delta V(\mathbf{r}) \rangle$

for the emission from *nl* (HOMO or HOMO-1) reads as [\[17\]](#page-4-0)

$$
\langle \delta V \rangle_{nl} = \sum_{\lambda} \lim_{\delta \to 0} \int dE' \frac{\langle \tilde{\psi}_{\lambda}(E') | \frac{1}{|\mathbf{r}_{nl} - \vec{r}_{\lambda}|} | \tilde{\psi}_{nl}(E) \rangle}{E - E' + i\delta} d_{\lambda}(E'), \quad (7)
$$

where the sum is over all other open channels *λ*, and the two-body wave functions $\tilde{\psi}$ involve both bound and continuum states in an IP channel. $\langle \delta V \rangle$ can be large, since bound wave functions of delocalized electrons occupy similar regions in space enabling a large overlap in Eq. (7). We note that the details of the correlation here are pretty complex, because all the open channels (about 30 in a jellium frame), constituting 240 delocalized electrons, are coupled. A simple interpretation of the results may still be outlined. At an XUV energy of current interest, each molecular level can ionize in its uncoupled IP channel. However, the interchannel coupling in Eq. (7) may include another possibility: An inner electron can initially absorb the XUV photon and then transfer the energy via Coulomb interactions to HOMO or HOMO-1 to cause an outer emission. Thus, since this repulsive $1/r_{12}$ underpins the coupling landscape [Eq. (7)], and since the correlation must dominate near a minimum of a channel, either of the valence electrons feels a strong outward force, via interchannel couplings, from the host of inner electrons and hence ionize faster. This is seen in Fig. 4 in predominant negative-delay structures. The exception at 190 eV needs further investigation. The HOMO-1 level, being below HOMO, feels some blockade from the inward Coulomb push via its coupling with the outer HOMO, and therefore gets relatively slower overall and, in particular, shows a second positive delay at 150 eV.

Probing correlation forces by the attosecond spectroscopy is the main focus of this work. Even though the separation between HOMO and HOMO-1 is 1.3 eV, our results can be experimentally accessed, since the resolution of RABITT measurements is not limited to the spectral width of the attosecond pulse but to that of the individual harmonics (∼100 meV) of the resulting frequency comb. Further, by approximating ψ by the asymptotic form $\cos(kr - l'\pi/2)$ of the spherical Bessel function $[34]$, Eq. [\(4\)](#page-1-0) becomes sinusoidal in *k*. This results in oscillations in the momentum space with radii being the frequencies. Hence, the reciprocals $(\pi/\Delta k)$ of the separations (periods) Δk between the minima, or between the delay extrema, connect to C_{60} radii. Obviously, for larger (smaller) fullerenes the structures will compactify (spread out). Furthermore, this technique may apply to access time information in a spheroidal fullerene, a carbon nanotube, or nanostructures of partial symmetry by properly orienting the polarization of XUV photons to minimize nondipole effects from deformity [\[36\]](#page-4-0).

The utilization of plane waves, instead of the continuum solutions as Eq. (3) , should produce cavity minima in the cross section, since, as discussed above, the origins of these minima are the nodes in the photoelectron wave that plane waves have. But in this case, the minima will appear at spectral positions different from the present result. Furthermore, as plane waves omit the Coulomb and short-range phases of Eq. [\(3\)](#page-1-0), the phase and time-delay profiles will differ from the current prediction. The plane waves routinely form the basis of the strong field approximation. But since the correlation effects diminish in a strong field environment, the delay structure may considerably weaken or be altered directly by the field.

V. CONCLUSION

In summary, photoemission quantum phases and Wigner-Smith time delays for HOMO and HOMO-1 electrons of a C_{60} molecule are investigated. Results show structures at the cavity minima in the energy range above the plasmon resonances and below the carbon *K* edge which carry the direct imprint of the dynamical correlation and the molecular size. Even though a jellium description of the ion core omits the scattering from local carbon ions [17], the structures should still be observed, but may soften in strength. We also calculated the results

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with a different, but less accurate than the current (LB94), XC functional. Specifically, using a functional as in Ref. [35] has shown similar qualitative results. We plan to include the comparison in a future paper. Besides fullerenes, the detection of photoemission minima in metal clusters [37] suggests a possible universality of the phenomenon in cluster systems, or even quantum dots [36], that confine finite-sized electron gas. The work predicts a research direction that applies attosecond RABITT metrology in the world of gas-phase nanosystems.

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