

Photonic crystals with topological defects

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We introduce topological defects to a square lattice of elliptical cylinders. Despite the broken translational symmetry, the long-range positional order of the cylinders leads to a residual photonic band gap in the local density of optical states. However, the band-edge modes are strongly modified by the spatial variation of the ellipse orientation. The Γ - X band-edge mode splits into four regions of high intensity and the output flux becomes asymmetric due to the formation of crystalline domains with different orientation. The Γ - M band-edge mode has the energy flux circulating around the topological defect center, creating an optical vortex. By removing the elliptical cylinders at the center, we create localized defect states, which are dominated by either clockwise or counterclockwise circulating waves. The flow direction can be switched by changing the ellipse orientation. The deterministic aperiodic variation of the unit cell orientation adds another dimension to the control of light in photonic crystals, enabling the creation of a diversified field pattern and energy flow landscape.

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I. INTRODUCTION

Topological defects have been extensively studied in condensed matter physics. One notable example is screw and edge dislocations in liquid crystals [1]. It has been shown that the topological defects in liquid crystals can strongly influence the light-matter interaction [2–10]. On one hand, the nematic disclinations may induce singularities in the light fields, generating optical beams with orbital angular momenta. On the other hand, strong light fields can imprint topological defects in liquid crystals, producing matter vortices [5,8,11,12]. Such interactions, however, are not sufficient to confine light at the defects and create optical resonances, due to small refractive index variation in the liquid crystals.

One efficient method of controlling light-matter interaction is to introduce a periodic modulation of the refractive index on the length scale of optical wavelength to make a photonic crystal [13–16]. By introducing structural defects to the photonic crystals, light may be tightly confined and form resonances with a high quality factor [17]. Such defect cavities have also been used to manipulate light transport and generate optical vortices [18,19]. In addition, plasmonic nanostructures have been designed to mold the electromagnetic energy flow on the nanoscale via the formation and interaction of vortex nanogears [20]. These studies illustrate different ways of producing diversified optical flow patterns for integrated photonic circuits.

In this paper, we introduce topological defects to photonic crystals (PhC). The unit cells are anisotropic and their orientations vary spatially to create topological defects in the orientational order. Compared to the liquid crystal, the interaction of light with the topological defect is greatly enhanced, as the unit cell is much larger than the liquid crystal molecule and the refractive index contrast is much higher. Instead of introducing disorder to the structural factor as the regular photonic crystal defects, we create disorder in the form factor. Despite that the topological defect breaks the translational symmetry of the photonic crystal, the local

density of optical states at the center of the topological defect structure is strongly suppressed in the frequency range that corresponds to the photonic band gap. The band-edge states are dramatically modified in terms of spatial field profile and power flow pattern, e.g., the energy flux may circulate around the topological defect instead of flowing outwards. To further enhance optical confinement, we create the photonic crystal defect modes in these structures, and show that they are distinct from the regular defect modes, e.g. they may generate power flow vortices. Such characteristic features originate from the spatial variation of unit cell orientation.

II. TWO-DIMENSIONAL SQUARE LATTICE WITH TOPOLOGICAL DEFECT

We start with a two-dimensional (2D) square lattice of air cylinders in a dielectric host. The lattice constant is d . The air cylinders have circular cross section of radius r . The refractive index of the dielectric host is n . We calculate the photonic bands using the plane-wave expansion method [21]. Figure 2(a) plots the first two bands of the transverse-electric (TE) polarization (electric field perpendicular to the cylinder axis) for $r/d = 0.3$ and $n = 2.83$. The photonic band gaps (PBGs) are seen in the Γ - X and Γ - M directions, but they do not overlap to form a full (isotropic) gap at this filling fraction of dielectric material.

Next we make the unit cell anisotropic by deforming the cross section of each cylinder to an ellipse [Fig. 1(a)]. The major axis of the ellipse is a and the minor axis is b . As the aspect ratio a/b is varied, the cross-sectional area of the ellipse is kept constant and the structure has the same filling fraction of dielectric with the PhC of circular unit cell. The photonic bands are modified, as seen in Fig. 2(a) for $a/b = 1.4$. The bands in the Γ - X_1 direction (parallel to the major axis of ellipse) are blue shifted, whereas the bands in the Γ - X_2 direction (parallel to the minor axis of ellipse) are red shifted. This can be understood from the shrinking (or expanding) of the dielectric region between two adjacent air cylinders in the Γ - X_1 (or Γ - X_2) direction, resulting in a decrease (or increase) of the effective refractive index for light propagating in the Γ - X_1 (or Γ - X_2) direction. Hence, the frequency degeneracy

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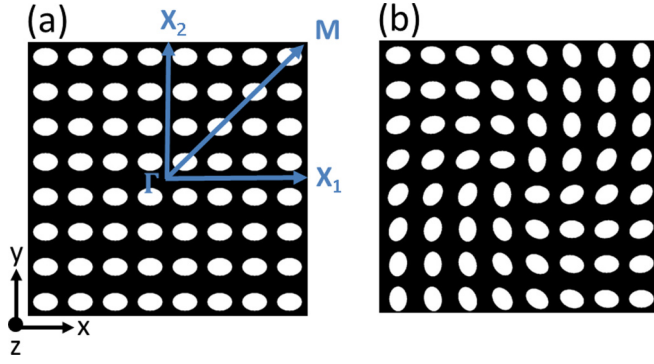


FIG. 1. (Color online) Introducing a topological defect to a photonic crystal with anisotropic unit cell. (a) A square-lattice of air cylinders with elliptical cross section embedded in a dielectric host. The major axis of the ellipses is parallel to the Γ - X_1 direction. (b) To introduce the topological defect, the major axis of each ellipse is rotated to an angle $\phi = k\theta + c$ from the x axis. θ is the polar angle of the center position of the ellipse. $k = 1$ and $c = \pi/4$. Away from the center, the ellipses in each of the four quadrant are aligned in the same direction, forming crystalline domains that rotate 90° from one quadrant to the next.

between the Γ - X_1 and Γ - X_2 band-edge modes is lifted by the deformation of the unit cell. The magnitude of their frequency splitting depends on the aspect ratio of the ellipses. The Γ - X_1 band-edge modes have electric field polarized in the y direction (E_y), and the Γ - X_2 band-edge modes in the x direction (E_x). Such a square-lattice photonic crystal with elliptical-shaped scattering units has been used to generate polarized optical beams from photonic crystal surface emitting lasers [22] and as a polarization beam splitter [23].

Finally, we introduce the topological defect by rotating individual ellipses on the square lattice to different directions. Following the configurations of wedge disclinations in liquid crystals, the angle between the major axis of an ellipse to the x axis is set to $\phi = k\theta + c$, where θ denotes the polar angle of the center position of the ellipse, k is a half integer or an integer that represents the topological charge, and c is a constant. Figure 1(b) shows such a structure with $k = 1$ and $c = \pi/4$, which forms a structural vortex at the center. Note that the center of the topological defect, which coincides with the origin of the 2D coordinates, is chosen to be in the middle of four adjacent cylinders. Moving away from the center, the ellipses in each of the four quadrants are aligned in the same direction, albeit their direction rotates by 90° from one quadrant to the next. This structure is clearly nonperiodic and does not possess any translational symmetry due to spatially varying orientation of the anisotropic unit cell. Nevertheless, a residual photonic band gap can be seen in the local density of optical states (LDOS) at the center of the structure in Fig. 2(b). The LDOS, $g(\mathbf{r}, \omega) = (2\omega/\pi c^2)\text{Im}[G(\mathbf{r}, \mathbf{r}, \omega)]$, where $G(\mathbf{r}, \mathbf{r}', \omega)$ is the Green's function for the propagation of the magnetic field H_z from point \mathbf{r} to \mathbf{r}' , is calculated numerically with a commercial program COMSOL [24]. The LDOS of the 32×32 pattern displays the same amount of reduction as that of the 48×48 pattern [Fig. 2(b)], indicating it becomes independent of the structure size once the size is sufficiently large. The frequency range in which the LDOS

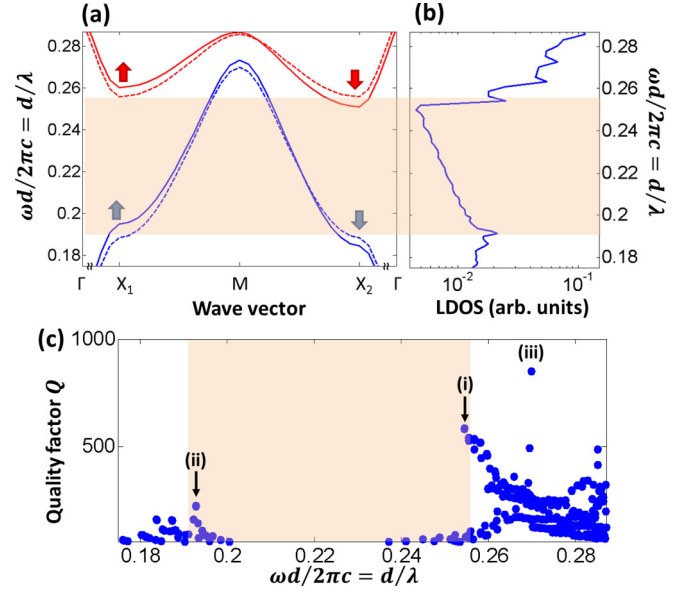


FIG. 2. (Color online) Residual photonic band gap (PBG) in the topological structure. (a) Dispersion relation of the first and second photonic bands with TE polarization in the square lattice of circular cylinders (dashed line) and elliptical cylinders (solid line). The refractive index of the cylinder is 1.0 and that of the dielectric host is 2.83. The circular cylinders have the radius $r = 0.3d$, where d is the lattice constant. The elliptical cylinders occupy the same fraction of area, with aspect ratio $a/b = 1.4$. PBGs exist in the Γ - X and Γ - M directions, but the frequency degeneracies of the Γ - X_1 and Γ - X_2 bands are lifted once the cylinder cross section deviates from circle. (b) Calculated local optical density of states (LDOS) at the center of the topological defect structures of 32×32 (blue curve) and 48×48 (black curve) sizes. For comparison, the red curve is the LDOS of the 32×32 square lattice of non-rotating ellipses. The LDOS exhibits the same amount of suppression in the frequency range that corresponds to the photonic band gap in the Γ - X direction (shaded region). The residual PBG effect results from the long-range order in the elliptical cylinder position. (c) Quality factor (Q) of TE-polarized modes in the topological defect structure with 32×32 cylinders. High- Q modes, e.g., the ones labeled (i)–(iii), are found close to the band-edges of the corresponding periodic structure.

is suppressed overlaps with the PBG in the Γ - X direction [Fig. 2(a)]. The suppression of LDOS at the center of a 32×32 square lattice of nonrotating elliptical cylinders coincides with that of the topological defect structure [Fig. 2(b)]. These results confirm the existence of a residual photonic band gap in the LDOS of the topological defect structure, which results from the long-range positional order of the cylinders in the structure.

III. OPTICAL RESONANCES IN PHOTONIC TOPOLOGICAL DEFECT STRUCTURE

In this section we calculate the optical resonances with high-quality (Q) factor in the photonic topological defect structure of finite size. The structure consists of $N = 1024$ air cylinders, forming a 32×32 square lattice. Such a pattern can be fabricated into a dielectric membrane and the light escaping through the boundary of the pattern will propagate in the surrounding dielectric membrane away from the pattern.

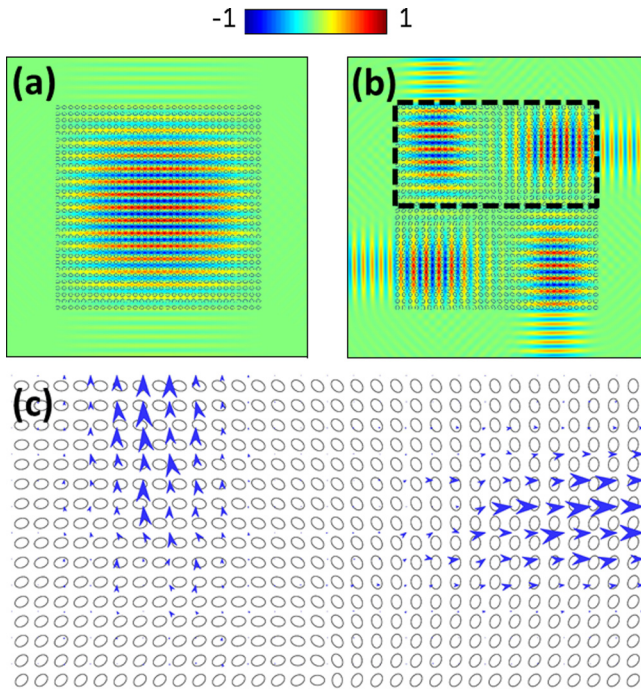


FIG. 3. (Color online) Modification of Γ - X_2 air band-edge mode by topological defect. (a) Spatial distribution of the magnetic field ($\text{Re}\{H_z\}$) for the TE-polarized air band-edge mode in the Γ - X_2 direction of a square-lattice with elliptical cylinders shown in Fig. 1(a). The structural parameters are the same as those in Fig. 2(a). Light propagates in the y -direction and escapes from the top and bottom boundaries of the lattice. (b) The spatial distribution of magnetic field of a high- Q mode, labeled (i) in Fig. 2(c), in the topological defect structure. The mode is split into four regions of high intensity, each of them resembling the field pattern in (a) except a possible rotation. (c) The spatial map of the Poynting vector in the top half region highlighted in (b). Each arrow points in the direction of local energy flux, and its length is proportional to the amplitude of the flux. In each of the four domains, light escapes only in one direction, as the emission in the opposite direction is blocked by the adjacent domain due to local PBG effect.

In our simulation, the array of air cylinders is surrounded by a homogeneous dielectric medium, which is about $7d$ thick and terminated by a perfectly matched layer (PML). The light leaking out of the array will propagate for some distance before being absorbed by the PML to avoid any reflection back to the array. We calculate the TE polarized resonances using the finite-difference frequency-domain method [24]. Due to light leakage, the resonant modes have complex frequencies $\omega = \omega_r - i\omega_i$, and the quality factor is $Q = \omega_r/2\omega_i$. Figure 2(c) plots the Q factor versus the normalized frequency $\omega d/2\pi c = d/\lambda$ of resonances in the vicinity of the residual PBG shown in Fig. 2(b). High- Q modes, e.g., the ones labeled (i)–(iii) in Fig. 2(c), correspond to the band-edge modes in the Γ - X and Γ - M directions of the square-lattice PhC. However, they are strongly modified by the topological defect, as will be seen below.

In Figs. 3(a), 3(b) we compare the spatial field profiles of mode (i) in the topological defect structure and the corresponding band-edge mode in the PhC with elliptical cylinders [Fig. 1(a)]. The band-edge mode [Fig. 3(a)], located

at the high-frequency edge of the PBG in the Γ - X_2 direction, has maximum electric field intensity within the air cylinders, thus called an air band-edge mode. This mode is formed via distributed Bragg reflection of light propagating in the y direction (parallel to the minor axis of the ellipse) by layers of air ellipses parallel to the x axis, with the electric field polarized in the x direction (parallel to the ellipse major axis). In the presence of topological defects, mode (i) is split into four parts, each occupying one quadrant [Fig. 3(b)]. The field profile in every quadrant resembles that of the air band-edge mode in Fig. 3(a), which rotates by 90° from one quadrant to the next. As mentioned earlier, the ellipses in each quadrant, especially the ones far from the center, are aligned in the same direction, thus forming crystalline domains that support PBG locally. Since the crystalline orientation rotates 90° from one quadrant to the next, the band-edge mode reorient their spatial profiles. For the Γ - X_2 air band-edge mode, the direction of light propagation switches between x axis and y axis.

Due to the rotation of crystalline domains, light escapes from the topological defect structure asymmetrically. To visualize the energy flow, we calculate the Poynting vector averaged over one optical cycle, $\vec{S}(x,y) = \frac{1}{2}\text{Re}[\vec{E}(x,y) \times \vec{H}^*(x,y)]$. Figure 3(c) is a spatial map of the Poynting vector in the top half of the structure [highlighted in Fig. 3(b)]. Each arrow in the map points in the direction of local energy flux, and its length is proportional to the amplitude of the flux. In the top right quadrant the energy flows rightward, while in the top left quadrant the energy flows upward. The change in the flow direction follows the switch in the crystalline orientation. In each quadrant the energy flow is not symmetric, e.g., in the top right quadrant light escapes to the right but not to the left. This is because the crystalline domain on the left, which is rotated by 90° , blocks the light. Once leaving the top right domain and entering the top left one, the emission from the Γ - X_2 air band-edge mode begins propagating in the Γ - X_1 direction. Since Γ - X_1 air band edge has higher frequency than the Γ - X_2 air band edge, the Γ - X_2 air band-edge mode falls into the PBG in the Γ - X_1 direction, and its output is reflected by the left domain.

In contrast, the Γ - X_1 air band-edge mode in each domain can leak to the adjacent one, because its frequency falls outside the PBG in the Γ - X_2 . Consequently, its Q factor is much lower. Similar behavior is expected for the Γ - X_2 dielectric band-edge mode in the topological defect structure whose frequency is beyond the PBG of Γ - X_1 . However, the Γ - X_1 dielectric band-edge mode is different because its frequency falls into the PBG of Γ - X_2 , and it contributes to the high- Q mode (ii) in Fig. 2(c). In the PhC with elliptical cylinders, the Γ - X_1 dielectric band-edge mode propagates in the x direction (parallel to the major axis of the ellipse), with the electric field polarized in the y direction (parallel to the minor axis of the ellipse) [Fig. 4(a)]. Since the Γ - X_1 dielectric band edge has higher frequency than the Γ - X_2 dielectric band edge, the Γ - X_1 dielectric band-edge mode in each domain of the topological structure cannot penetrate into the adjacent domain, which is rotated by 90° [Fig. 4(b)]. Consequently, the energy flows only outwards, as shown in Fig. 4(c). Moreover, the topological defect introduces structural disorder in each domain, especially close to the center, hence the Γ - X_1 dielectric band-edge mode becomes coupled to nearby low- Q resonance, causing a distortion of its spatial field profile.

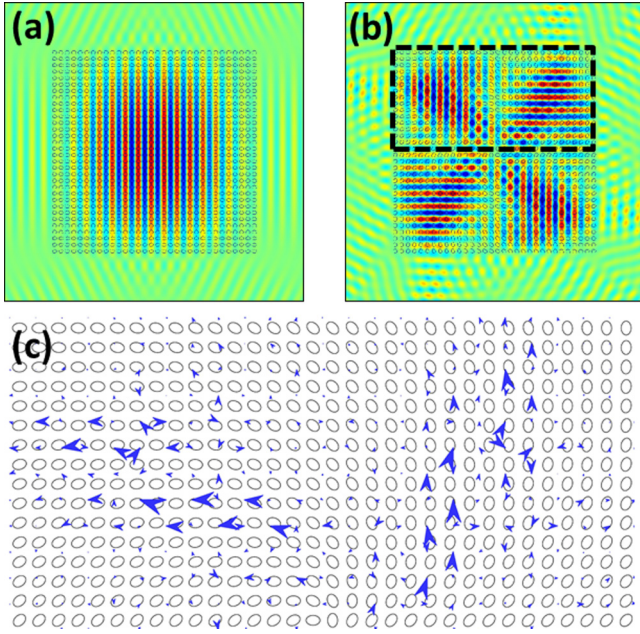


FIG. 4. (Color online) Modification of Γ - X_1 dielectric band-edge mode by topological defect. (a) Spatial distribution of the magnetic field ($\text{Re}\{H_z\}$) for the TE-polarized dielectric band-edge mode in the Γ - X_1 direction of a square-lattice with elliptical cylinders shown in Fig. 1(a). Light propagates in the x direction and escapes from the left and right edges of the lattice. (b) The spatial distribution of magnetic field of a high- Q mode, labeled (ii) in Fig. 2(c), in the topological defect structure. The mode is split into four regions of high intensity, each of them resembles the field pattern in (a) except a possible rotation. (c) The spatial map of the Poynting vector in the top half region of (b). Each arrow points in the direction of local energy flux, and its length is proportional to the amplitude of the flux. In each of the four domains, light escapes only in one direction, as the emission in the opposite direction is blocked by the adjacent domain due to local PBG effect.

In addition to the Γ - X band-edge modes, we also observe high- Q modes near the Γ - M band edges. One example is mode (iii) in Fig. 2(c), which is located close to the dielectric band edge. A comparison of its field profile to that of the Γ - M band-edge mode in the square-lattice PhC reveals a strong effect from the topological defect [Figs. 5(a), 5(b)]. Mode (iii) is split into five regions of high intensity, in addition to the four quadrants there is an additional one at the structure center. This is different from modes (i) and (ii), which have diminishing intensity at the center. Zooming into the field profile at the center, the dielectric band-edge mode in Fig. 5(c) displays a checkerboard pattern with the wave vector in the Γ - M direction. The continuous rotation of ellipses around the center of the topological defect structure causes a significant distortion of the field pattern, as seen in Fig. 5(d). In Fig. 5(e), the spatial map of the Poynting vector in the square-lattice PhC shows that the energy flowing out of the structure in all four directions. In the topological defect structure, however, the energy flux circulates inside, forming an optical vortex around the defect center [Fig. 5(f)]. Besides the counterclockwise (CCW) circulating flow at the center, there are additional clockwise (CW) circulating flows in the four quadrants. They

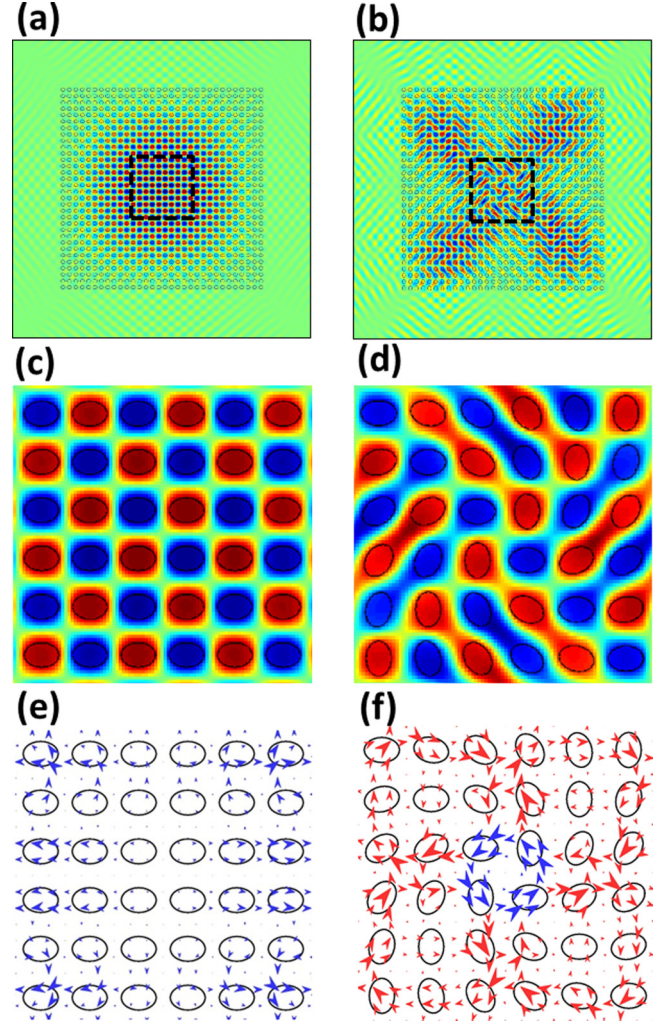


FIG. 5. (Color online) Modification of Γ - M dielectric band-edge mode by topological defect. (a) Spatial distribution of the magnetic field ($\text{Re}\{H_z\}$) for the TE-polarized dielectric band-edge mode in the Γ - M direction of a PhC with elliptical cylinders shown in Fig. 1(a). The structural parameters are the same as those in Fig. 2 (a). (b) The spatial distribution of magnetic field of a high- Q mode, labeled (iii) in Fig. 2(c), in the topological defect structure. The mode becomes distorted, forming a cross pattern. (c), (d) Zooming into the central region of the field patterns in (a), (b), revealing the distortion caused by the topological defect. (e), (f) The spatial map of the Poynting vector for the modes shown in (a), (b). Each arrow points in the direction of local energy flux, and its length is proportional to the amplitude of the flux. In the PhC with elliptical cylinders, the energy flows outward to the boundary. In the topological defect structure, the energy flux circulates around the defect center (colored in blue), forming an optical vortex. There are an additional four circulating flows in the four quadrants.

result from the spatial variation of the ellipse orientation, namely, the spatial inhomogeneity of the form factor.

IV. STRONGLY CONFINED DEFECT STATES

In the previous section, we have shown that by introducing topological defect into a square lattice of elliptical cylinders, the band-edge modes are significantly modified. Although

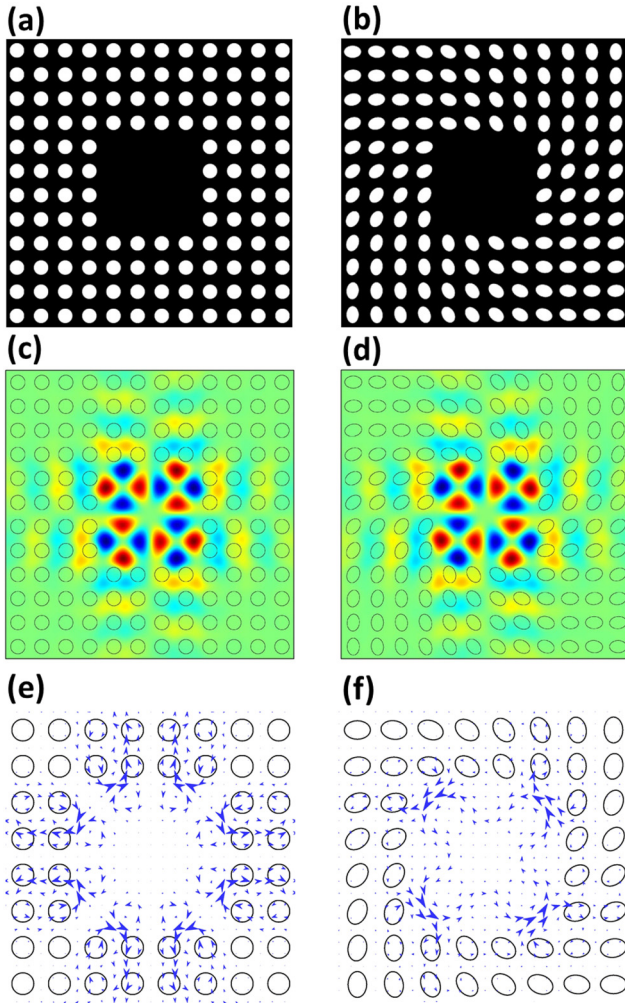


FIG. 6. (Color online) Localized defect state in the topological defect structure, in comparison to the PhC defect state. (a) Removing 4×4 cylinders from the center of a square lattice of circular cylinders to create photonic defect states. (b) Removing 4×4 cylinders from the center of the topological defect structure. The structural parameters remains the same as in previous figures. (c), (d) The spatial distribution of the magnetic field for the highest- Q defect state in (a), (b). The field profile is nearly unchanged by the topological defect. (e), (f) The spatial map of the Poynting vector for the defect states in (c), (d). Each arrow points in the direction of local energy flux, and its length is proportional to the amplitude of the flux. In (e), the energy flows out of the central defect region in all four directions. In (f), the optical flux circulates counter clockwise (CCW) in the central region.

their Q factors are the highest among all the resonances, such modes remain spatially extended and light can easily escape through the boundaries. To tightly confine light within the topological defect structure, we remove 4×4 ellipses from the center to create localized states similar to the photonic defect states of a regular PhC [Figs. 6(a), 6(b)]. Among all the defect states that are generated within the residual PBG, the one shown in Fig. 6(d) has the highest Q of 1.27×10^4 , which is more than one order of magnitude higher than the rest. Its field profile, presented in Fig. 6(d), resembles that of a regular photonic crystal defect state shown in Fig. 6(c).

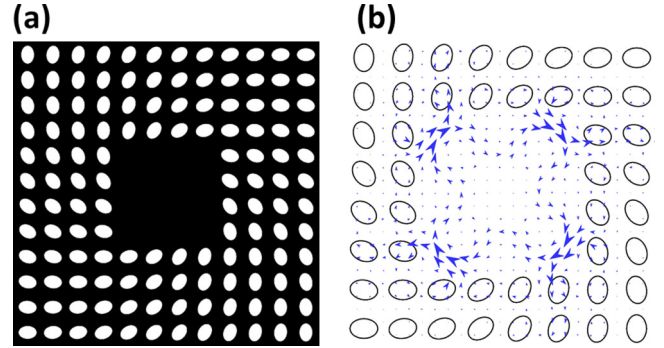


FIG. 7. (Color online) Switching the direction of energy flow in the defect state in Fig. 6. (a) The topological defect structure with the major and minor axes of the ellipse exchanged, which is equivalent to rotate all the ellipses in the structure shown in Fig. 6(b) by 90° . (b) The spatial map of the Poynting vector for the defect state in (a), showing the power circulation flips the direction from CCW to CW.

However, the energy flow pattern becomes notably different, as seen in Figs. 6(e), 6(f). For the regular photonic crystal defect state, the energy flows out of the central defect region [Fig. 6(e)]. In the presence of topological defect, the optical flux circulates CCW in the central region [Fig. 6(f)].

The drastic change in the energy flow can be attributed to the spatial variation of the ellipse orientation in the topological defect structure as shown Fig. 1(a). Light leaking out of the central defect cavity must propagate in the surrounding lattice to reach the boundary of the structure in order to escape. Therefore the leakage relies on the coupling between the defect state and the propagating modes in the surrounding lattice. As shown in Fig. 2(a), the PBG only exists in the Γ - X direction, the defect state can couple to one of the extended states propagating close to the Γ - M direction and eventually escapes the structure. In Fig. 6(a), with circular cylinders, the out-coupling of CW and CCW waves in the defect region is the same because the structure is symmetric. In Fig. 6(b), the rotation of the ellipses in the surrounding lattice breaks the balance in the out-coupling of CW and CCW waves in the defect region. For the high- Q defect state shown in Fig. 6(d), its CW wave component experiences more out-coupling than the CCW, thus the net energy flow inside the defect region is CCW. To confirm this mechanism, we switch the major and minor axes of the ellipse, which is equivalent to rotate all the ellipses by 90° [Fig. 7 (a)]. In this structure, the CCW wave experiences more out-coupling than the CW wave, thus the high- Q defect state is dominated by the CW wave, as confirmed from the flux pattern in Fig. 7(b).

V. CONCLUSION

In summary, we introduce topological defect into a square lattice of elliptical cylinders. Although the translational symmetry is broken, the residual photonic band-gap effect is evident from the suppressed density of optical states, which results from the long-range positional order of the ellipses. The band-edge modes are strongly modified by the spatial variation of the ellipse orientation, both the field profile and energy flow are altered. For example, the high- Q mode located at the edge

of Γ - X band gap splits into four regions of high intensity and the output flux becomes asymmetric due to spatially separated and rotated crystalline domains. The Γ - M band-edge mode is also modified significantly and the energy flux circulates around the topological defect center.

To enhance the optical confinement, we remove the elliptical cylinders at the center to create localized states, in analogy to the photonic crystal defect states. Such states are dominated by either CW or CCW circulating waves, due to unbalanced scattering loss from the elliptical cylinders at the boundary of the defect region. The flow direction can be switched by changing the ellipse orientation. The intrinsic optical vortices may be useful for modifying the motion of small particles or enhancing the interaction with chiral molecules for sensing applications.

Although this study is focused on a specific type of topological defect, we believe the photonic crystals with

various types of topological defects can support diversified resonances with distinct characteristic. For example, a simple mapping such as $\phi = k\theta + c$ can modify the resonances in a numerous ways by tuning the values of c and k . Therefore, a tremendous parameter space remains to be explored. The deterministic aperiodic variation of the unit cell orientation adds another dimension to the control of light in a photonic crystal, enabling creation of a desired field pattern and energy flow landscape.

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