# Cavity-output-field control via interference effects

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We show how interference effects are responsible for manipulating the output electromagnetic field of an optical microresonator in the good-cavity limit. The system of interest consists of a moderately strongly pumped two-level emitter embedded in the optical cavity. When an additional weaker laser of the same frequency is pumping the combined system through one of the resonator's mirrors then the output-cavity-electromagnetic field can be almost completely suppressed or enhanced. This is due to the interference among the scattered light by the strongly pumped atom into the cavity mode and the incident weaker laser field. The result applies to photonic crystal environments as well.

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# I. INTRODUCTION

Present and future quantum technologies require various tools allowing for complete or partial control of the quantummechanical interaction between light and matter. Therefore, quite a significant amount of papers is dedicated to this issue. Particularly, light interference is an widely investigated topic and, no doubt, its importance for various applications is enormous [1-5]. Due to quantum interference effects, for instance, elimination of spectral lines or complete cancellation of the spontaneous decay can occur. Spatial interference shows interesting features as well [2,4,5]. Furthermore, suppression of the resonance fluorescence in a lossless cavity was demonstrated in Ref. [6], whereas cavity-field-assisted atomic relaxation and suppression of resonance fluorescence at high intensities were shown in Ref. [7]. Inhibition of fluorescence in a squeezed vacuum was demonstrated in Ref. [8], whereas suppression of Bragg scattering by collective interference of spatially ordered atoms within a high-Q cavity mode was demonstrated, respectively, in Ref. [9]. On the other hand, cavity-enhanced single-atom spontaneous emission was observed in Ref. [10], whereas suppression of spontaneous decay at optical frequencies was shown in Ref. [11]. The control of the spontaneous decay as well as of the resonance fluorescence is of particular interest for quantum computation processes [12] where, in addition, highly correlated photons are required [13]. Combining few coherent driving sources one can achieve a further degree of control of the atom's quantum dynamics. Actually, the bichromatic driving of single atoms was intensively investigated recently emphasizing interesting interference phenomena. In particular, the resonance fluorescence of a two-level atom in a strong bichromatic field was analyzed in Ref. [14], and the response of a two-level system to two strong fields was experimentally studied in Ref. [15], correspondingly. The decay of a bichromatically driven atom in a cavity was investigated in Ref. [16]. Broadband high-resolution x-ray frequency combs were obtained via bichromatically pumping of three-level  $\Lambda$ -type atoms [17]. Moreover, bichromatic driving of a solid-state cavity quantum electrodynamics system was investigated in Ref. [18]. Finally,

a photonic crystal's influence on quantum dynamics of pumped few-level qubits was investigated in detail as well [19–21].

The above-mentioned papers may be of particular relevance in a quantum network [22,23], for instance. Related systems have already been proven to act as an optical diode [24,25]—an important ingredient in a quantum network. Since a precise control over system's properties is highly required in such a network, here, we investigate the feasibility of controlling the cavity-output-electromagnetic field in a system consisting of a moderately strongly pumped two-level emitter. If a second coherent driving is applied through one of the mirrors and perpendicular to the first laser beam, then the output-cavity field can be almost completely inhibited in the good-cavity limit. Notice that the lasers are in resonance with the cavity mode frequency. We have found that the interference between the second weaker light beam and the light scattered by the two-level emitter into the cavity mode due to stronger pumping is responsible for the suppression effect. The destructive interference can be turned into a constructive one (or vice versa) via varying the phase difference of the applied lasers. Furthermore, the inhibition requires the laser frequency to be out of atomic frequency resonance, whereas for photonic crystals' surroundings it can be even on resonance.

The article is organized as follows. In Sec. II we describe the analytical approach and the system of interest, whereas in Sec. III we analyze the obtained results. A summary is given in Sec. IV.

## II. QUANTUM DYNAMICS OF A PUMPED TWO-LEVEL ATOM INSIDE A DRIVEN MICROCAVITY

The Hamiltonian describing a two-level atomic system having the transition frequency  $\omega_0$  and interacting with a strong coherent source of frequency  $\omega_1$  while embedded in a pumped microcavity of frequency  $\omega_c$  in a frame rotating at  $\omega = \omega_1 = \omega_2$  (see Fig. 1), is as follows:

$$H = \hbar \Delta S_z + \hbar \delta a^{\dagger} a + \hbar g (a^{\dagger} S^{-} + a S^{+}) + \hbar \Omega (S^{+} e^{i\phi_1} + S^{-} e^{-i\phi_1}) + \hbar \epsilon (a^{\dagger} e^{i\phi_2} + a e^{-i\phi_2}), \quad (1)$$

where  $\Delta = \omega_0 - \omega$  and  $\delta = \omega_c - \omega$ . In the Hamiltonian (1) the components, in order of appearance, describe the atomic and the cavity free energies, the interaction of the two-level

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FIG. 1. (Color online) The schematic of the model: A two-level emitter possessing the transition frequency  $\omega_0$  embedded in a singlemode ( $\omega_c$ ) microcavity is pumped with an intense laser field of frequency  $\omega_1$ . A second coherent source of frequency  $\omega_2$  is driving the entire system through one of the mirrors.  $\gamma$  is the single-atom spontaneous decay rate, whereas  $\kappa$  describes the cavity photon leaking rate, respectively.

emitter with the microcavity mode, the atom's interaction with the first laser field with  $\Omega$  being the corresponding Rabi frequency, and the interaction of the second driving field with the cavity mode with  $\epsilon$  being proportional to the input laser field strength amplitude, respectively. The atomic bare-state operators  $S^+ = |e\rangle\langle g|$  and  $S^- = [S^+]^{\dagger}$  obey the commutation relations for SU(2) algebra, i.e.,  $[S^+, S^-] = 2S_z$  and  $[S_z, S^{\pm}] =$  $\pm S^{\pm}$ . Here,  $S_z = (|e\rangle\langle e| - |g\rangle\langle g|)/2$  is the bare-state inversion operator.  $|e\rangle$  and  $|g\rangle$  are the excited and ground states, respectively, of the atom, whereas  $a^{\dagger}$  and a are the creation and the annihilation operators of the electromagnetic field (EMF) in the resonator and satisfy the standard bosonic commutation relations, namely,  $[a, a^{\dagger}] = 1$  and  $[a, a] = [a^{\dagger}, a^{\dagger}] = 0$  [26,27].  $\{\phi_1, \phi_2\}$  are the corresponding phases of the coherent driving sources.

We will describe our system using the laser-qubit semiclassical dressed-state formalism defined as [4]

$$|+\rangle = \sin \theta |g\rangle + \cos \theta |e\rangle,$$
  
$$|-\rangle = \cos \theta |g\rangle - \sin \theta |e\rangle,$$
  
(2)

with tan  $2\theta = 2\Omega/\Delta$ . Applying this transformation to (1) one arrives then at the following dressed-state Hamiltonian:

$$H = H_0 + \hbar g (\cos^2 \theta R^- - \sin^2 \theta R^+) a^{\dagger} e^{-i\phi} + \hbar g (\cos^2 \theta R^+ - \sin^2 \theta R^-) a e^{i\phi}, \qquad (3)$$

with

$$H_0 = \hbar \bar{\Omega} R_z + \hbar \delta a^{\dagger} a + \hbar \epsilon (a^{\dagger} + a) + \hbar R_z (g_0^* a^{\dagger} + g_0 a).$$
(4)

Here,  $\bar{\Omega} = \sqrt{\Omega^2 + (\Delta/2)^2}$  whereas  $g_0 = (g/2) \sin 2\theta e^{i\phi}$ ,  $g_0^* = (g/2) \sin 2\theta e^{-i\phi}$ , and  $\phi = \phi_2 - \phi_1$ . We also employed  $S^{\pm} = \tilde{S}^{\pm} e^{\mp i\phi_1}$  and  $a^{\dagger} = \tilde{a}^{\dagger} e^{-i\phi_2}$  with  $a = [a^{\dagger}]^{\dagger}$  in the Hamiltonian (1) and dropped the tilde afterwards. The new quasispin operators, i.e.,  $R^+ = |+\rangle \langle -|, R^- = [R^+]^{\dagger}$ , and  $R_z = |+\rangle \langle +| - |-\rangle \langle -|$  are operating in the dressed-state picture. They obey the following commutation relations:  $[R^+, R^-] = R_z$  and  $[R_z, R^{\pm}] = \pm 2R^{\pm}$ .

Considering that  $\delta \ll \overline{\Omega}$  the last two terms in Eq. (3) can be ignored under the secular approximation. Therefore, the master equation describing the laser-dressed two-level atom inside a leaking pumped resonator and damped via the vacuum modes

of the surrounding EMF reservoir is as follows:

$$\frac{d}{dt}\rho(t) + \frac{i}{\hbar}[H_0,\rho] = -\kappa[a^{\dagger},a\rho] - \Gamma_0[R_z,R_z\rho] -\Gamma_+[R^+,R^-\rho] - \Gamma_-[R^-,R^+\rho] + \text{H.c.}$$
(5)

Here,

$$\Gamma_0 = (\gamma_0 \sin^2 2\theta + \gamma_d \cos^2 2\theta)/4,$$
  

$$\Gamma_+ = \gamma_+ \cos^4 \theta + (\gamma_d/4) \sin^2 2\theta,$$
  

$$\Gamma_- = \gamma_- \sin^4 \theta + (\gamma_d/4) \sin^2 2\theta.$$

 $\gamma_0 = \pi \sum_k g_k^2 \delta(\omega_k - \omega)$  and  $\gamma_{\pm} = \pi \sum_k g_k^2 \delta(\omega_k - \omega \mp 2\bar{\Omega})$ , respectively, are the single-atom spontaneous decay rates being dependent on the density of modes  $g_k$  at the dressedstate frequencies  $\{\omega, \omega \pm 2\bar{\Omega}\}$ , whereas  $\gamma_d$  signifies the pure dephasing rate. In free space one has that  $\gamma_0 = \gamma_{\pm} \equiv \gamma$ . Note that the master Eq. (5) was obtained either under the intense-field condition or under the far-off-detuned field, i.e., it is valid when  $\bar{\Omega} \equiv \sqrt{\Omega^2 + (\Delta/2)^2} \gg \{\delta, g, \epsilon, \Gamma_0, \Gamma_{\pm}\}$ .

The equations of motion for the variables of interest can be easily obtained from the master Eq. (5). Therefore, the quantum dynamics is described by the following system of linear differential equations:

$$\frac{d}{dt} \langle a^{\dagger}a \rangle = ig_{0} \langle R_{z}a \rangle + i\epsilon \langle a \rangle - ig_{0}^{*} \langle R_{z}a^{\dagger} \rangle 
-i\epsilon \langle a^{\dagger} \rangle - 2\kappa \langle a^{\dagger}a \rangle, 
\frac{d}{dt} \langle R_{z}a \rangle = -(\kappa + i\delta + 2\Gamma_{+} + 2\Gamma_{-}) \langle R_{z}a \rangle 
-2(\Gamma_{+} - \Gamma_{-}) \langle a \rangle - i\epsilon \langle R_{z} \rangle - ig_{0}^{*}, 
\frac{d}{dt} \langle R_{z}a^{\dagger} \rangle = -(\kappa - i\delta + 2\Gamma_{+} + 2\Gamma_{-}) \langle R_{z}a^{\dagger} \rangle 
-2(\Gamma_{+} - \Gamma_{-}) \langle a^{\dagger} \rangle + i\epsilon \langle R_{z} \rangle + ig_{0}, \quad (6) 
\frac{d}{dt} \langle a \rangle = -(\kappa + i\delta) \langle a \rangle - ig_{0}^{*} \langle R_{z} \rangle - i\epsilon, 
\frac{d}{dt} \langle a^{\dagger} \rangle = -(\kappa - i\delta) \langle a^{\dagger} \rangle + ig_{0} \langle R_{z} \rangle + i\epsilon, 
\frac{d}{dt} \langle R_{z} \rangle = -2(\Gamma_{-} + \Gamma_{+}) \langle R_{z} \rangle + 2(\Gamma_{-} - \Gamma_{+}).$$

In the system of Eqs. (7), we have used the trivial condition  $R_{\tau}^2 = 1$ , which is the case for a single-qubit system.

In the following section, we will discuss our results, i.e., the possibility of inhibiting the cavity-output field in the steady state via interference effects.

#### **III. OUTPUT-CAVITY-FIELD CONTROL**

One of the solutions of system (7) in the steady state represents the mean-photon number in the microcavity mode, namely,

$$\langle a^{\dagger}a\rangle_s = A\epsilon^2 + B\epsilon + C. \tag{7}$$

For  $\delta = 0$  and  $\gamma_0 = \gamma_{\pm} \equiv \gamma$ , the coefficients *A*, *B*, and *C* are given by the following expressions:

$$A = \frac{1}{\kappa^2},$$

$$B = -\frac{2g\gamma \Delta\Omega \cos \phi}{\kappa^2 [\gamma \Delta^2 + 2(\gamma + \gamma_d)\Omega^2]},$$

$$C = \frac{g^2 \Omega^2}{\kappa^2 [\gamma \Delta^2 + 2(\gamma + \gamma_d)\Omega^2]} \times \frac{\gamma(\kappa + 2\gamma)\Delta^2 + 2\kappa(\gamma + \gamma_d)\Omega^2}{(\kappa + 2\gamma)\Delta^2 + 4(\kappa + \gamma + \gamma_d)\Omega^2}.$$
(8)

Because of the quadratic dependence on  $\epsilon$ , the minimum value of the mean-photon number is as follows:

$$\langle a^{\dagger}a\rangle_{s}^{\min} = C - \frac{B^{2}}{4A}.$$
(9)

The above value is achieved at

1

$$\epsilon^{\min} = -B/(2A)$$

Based on Eqs. (8) and (9) it follows that  $\epsilon^{\min}$  is independent of  $\{\kappa, \delta\}$  and its value does not exceed  $\frac{g\sqrt{2}}{4}(1 + \gamma_d/\gamma)^{-1/2}$ . The cavity-output field, i.e., the number of photons escaping the cavity per second, can be evaluated via  $\kappa \langle a^{\dagger}a \rangle_s$ . Particularly, in Fig. 2 the minimum value of the steady-state mean-photon number is  $\langle a^{\dagger}a \rangle_s^{\min} \approx 0.06$  and is achieved when  $(\epsilon/\gamma)^{\min} \approx 0.54$ . An explanation of the steady-state behaviors shown in Fig. 2 can be found if one represents the mean-photon number given by (7) as follows:

$$\langle a^{\dagger}a\rangle_{s} = \frac{\epsilon}{\kappa^{2}} \{\epsilon + |g_{0}|\langle R_{z}\rangle_{s}\cos\phi\} + \frac{|g_{0}|}{\kappa(\kappa + 2\Gamma_{+} + 2\Gamma_{-})} \\ \times \{|g_{0}| + \epsilon\langle R_{z}\rangle_{s}\cos\phi - 2(\Gamma_{+} - \Gamma_{-}) \\ \times (|g_{0}|\langle R_{z}\rangle_{s} + \epsilon\cos\phi)/\kappa\},$$
(10)

where

$$\langle R_z \rangle_s = -(\Gamma_+ - \Gamma_-)/(\Gamma_+ + \Gamma_-).$$

From the above expression (10), one can see that for  $\delta = 0$  the mean-photon number due to weaker external pumping of the cavity mode is proportional to  $\epsilon^2$ , whereas that due to stronger driving of the two-level qubit is proportional to  $|g_0|^2$ ,



FIG. 2. (Color online) The steady-state dependence of the microcavity mean-photon number  $\langle a^{\dagger}a \rangle_s$  versus the variables  $\epsilon/\gamma$  and  $\delta/\gamma$ . Other parameters are as follows:  $\gamma_d/\gamma = 0.01$ ,  $\kappa/\gamma = 0.1$ ,  $g/\gamma = 2$ ,  $\Delta/\Omega = 3$ , and  $\phi = 0$ .

respectively. There is also a cross contribution proportional to  $\epsilon |g_0| \cos \phi$ . All these terms demonstrate interference effects among the contributions due to two pumping lasers and, hence, the minima's nature in Fig. 2. In particular, for  $\Gamma_+ \gg \Gamma_-$  one has from Eq. (10) that

$$\langle a^{\dagger}a\rangle_{s} \approx \frac{\epsilon^{2}}{\kappa^{2}} + \frac{|g_{0}|^{2}}{\kappa^{2}} - \frac{2\epsilon|g_{0}|}{\kappa^{2}}\cos\phi, \qquad (11)$$

whereas for  $\Gamma_{-} \gg \Gamma_{+}$  we have

$$\langle a^{\dagger}a\rangle_{s} \approx \frac{\epsilon^{2}}{\kappa^{2}} + \frac{|g_{0}|^{2}}{\kappa^{2}} + \frac{2\epsilon|g_{0}|}{\kappa^{2}}\cos\phi, \qquad (12)$$

respectively. Thus, indeed, the output field suppression (or enhancement) occurs because of the interference effect taking place among the fraction of light  $|g_0|^2/\kappa^2$  scattered by the atom into the cavity mode due to stronger pumping by the first laser beam and the photon field of the second weaker laser field characterized by  $\epsilon^2/\kappa^2$ , respectively (see also, Fig. 1). Furthermore, the nature of destructive or constructive interference can be understood as follows: In the dressed-state picture both lasers are simultaneously in resonance with the dressed-state transitions  $|+\rangle \leftrightarrow |+\rangle$  and  $|-\rangle \leftrightarrow |-\rangle$  and, hence, different signs in front of the last term in Eqs. (11)and (12). Actually, if  $\Gamma_+ \gg \Gamma_-$  the atom is located on the lower dressed state  $|-\rangle$ , whereas it resides on the higher dressed state  $|+\rangle$  when  $\Gamma_{-} \gg \Gamma_{+}$ . However, the destructive interference can be turned into a constructive one (or vice versa) via varying the phase difference  $\phi$  [see Eqs. (11) and (12)]. This allows a better control of the output-cavity field. Notice that on resonance, i.e.,  $\Delta = 0$ , the inhibition effects are absent when  $\gamma_{+} = \gamma_{-}$  because  $\Gamma_{+} = \Gamma_{-}$  resulting in  $\langle R_{z} \rangle_{s} = 0$  [see Eq. (10)]. Also, one can obtain small values for  $\langle a^{\dagger}a \rangle_s$  if  $\kappa > \gamma$ . However, in this case we are in the bad-cavity limit and, therefore, lower values for the mean-photon number or even zero are expected [13,26,28]. Thus, contrarily, the cavity-output-field suppression reported here occurs in the good-cavity limit, i.e., when  $\gamma > \kappa$  and  $g > {\kappa, \gamma}.$ 

Apart from the dependence of the expression (10) on the parameters  $\{\epsilon, \kappa, \phi, |g_0|\}$ , it also depends on the generalized dressed-state decay rates  $\Gamma_{\pm}$ . These decay rates can be modified either by varying the detuning  $\Delta$  in free space with  $\gamma_{+} = \gamma_{-}$  or via modification of the density of modes at the dressed-state frequencies  $\omega \pm 2\bar{\Omega}$  and, consequently,  $\gamma_+ \neq \gamma_-$ , which is a typical situation in photonic crystal environments [19-21], for instance. In particular, one can also have a situation when  $\gamma_+ \gg \gamma_-$  or  $\gamma_- \gg \gamma_+$ . Figure 3 shows the mean-photon numbers obtained with the help of the expression (10) when the two-level emitter is located inside a microscopic cavity engineered in a photonic crystal material. In this case, the output-cavity field can be suppressed even on atom-laser frequency resonance, i.e., when  $\Delta = 0$  (see the dotted curve) because  $\gamma_{+} \neq \gamma_{-}$  and the population will be distributed unequally among the dressed states, whereas

$$\langle R_z \rangle_s = rac{\gamma_- - \gamma_+}{\gamma_- + \gamma_+ + 2\gamma_d} \neq 0, \quad \text{if } \Delta = 0.$$

Negative values for the dressed-state inversion with  $\phi = 0$  lead to cavity-output-field suppression [see Fig. 3 and Eq. (11)]. For the sake of comparison, the solid curve stands for ordinary vacuum-cavity environments. Thus, finalizing, we have shown



FIG. 3. The steady-state dependences of the mean-photon number  $\langle a^{\dagger}a \rangle_s$  as a function of  $\epsilon/\gamma_*$ . The solid line is for  $\gamma_* \equiv \gamma_-$  and  $\gamma_+ \to 0$ . Furthermore, the short-dashed line is for  $\gamma_* = \gamma_-$  and  $\gamma_- \to 0$ , whereas the dotted curve corresponds to  $\Delta = \delta = 0$ . Other parameters are the same as in Fig. 2 with  $\Delta/\Omega = 1$  and  $\delta/\gamma_* = 0$ .

here how the output-cavity field can be minimized due to interference effects.

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## **IV. SUMMARY**

Summarizing, we have demonstrated the feasibility of cavity-output-field control via interference effects. The system of interest is formed from a strongly pumped two-level atom placed in an optical microresonator. A second weak laser being in resonance with the cavity mode frequency is probing the whole system through one of the cavity's mirrors. Consequently, interference effects occur among the light scattered in the cavity mode by the strongly pumped atom and the incident weaker laser field leading to output-cavity-field inhibition or enhancement. Furthermore, the destructive interference can be turned into a constructive one (or vice versa) via varying the phase difference of the applied lasers providing in this way a better control over the output electromagnetic field. The idea works for photonic crystal environments as well.

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